

Workshop on **H**igh **E**nergy **P**hysics and **P**henomenology
WHEPP13

December 12-21, 2013 [Blue Lily Beach Resort](#) Puri, Odisha, India

Neutrino – Theory Status

Outline

- ▶ Neutrino mass operators and observables
- ▶ Neutrino and New Physics
- ▶ Neutrino and Higgs
- ▶ Neutrino and DM/BAU
- ▶ Neutrino and LHC

Neutrino mass operators & observables



Neutrino mass operators

- ▶ SM allows simple extensions for neutrino mass operators:

$$L \approx H_d (\approx \epsilon H_u^\dagger)$$

- ▶ Dirac operator – renormalizable, $U(1)_L$ conserving.

$$\mathcal{L}_D = y_{ij}^D L_i H_u N_j \Rightarrow m_{ij}^D = y_{ij}^D v_H / \sqrt{2}$$

- ▶ Majorana operator – effective, $U(1)_L$ violating.

$$\mathcal{L}_M = \frac{y_{ij}^M}{M_X} (L_i H_u)(L_j H_u) / (L_i L_j)(H_u H_u)$$

Weinberg 1979

$$\Rightarrow m_{ij}^M = y_{ij}^M \frac{v_H^2}{M_X}$$

- ▶ No reason to forbid them → observed!

Neutrino parameters

- ▶ Three masses, three angles, 1+2 phases:

$$|\nu_e\rangle = U_{e1}|\nu_1\rangle + U_{e2}|\nu_2\rangle + U_{e3}|\nu_3\rangle$$

$$|\nu_\mu\rangle = U_{\mu1}|\nu_1\rangle + U_{\mu2}|\nu_2\rangle + U_{\mu3}|\nu_3\rangle$$

$$|\nu_\tau\rangle = U_{\tau1}|\nu_1\rangle + U_{\tau2}|\nu_2\rangle + U_{\tau3}|\nu_3\rangle$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{\theta_{23}} & s_{\theta_{23}} \\ 0 & -s_{\theta_{23}} & c_{\theta_{23}} \end{pmatrix} \begin{pmatrix} c_{\theta_{13}} & 0 & s_{\theta_{13}} e^{i\delta} \\ 0 & 1 & 0 \\ -s_{\theta_{13}} e^{-i\delta} & 0 & c_{\theta_{13}} \end{pmatrix} \begin{pmatrix} c_{\theta_{12}} & s_{\theta_{12}} & 0 \\ -s_{\theta_{12}} & c_{\theta_{12}} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & e^{i\phi_3} \end{pmatrix}$$

atmospheric

reactor

solar

Majorana

$$\Delta m_{atm}^2 = |m_3^2 - m_1^2|$$

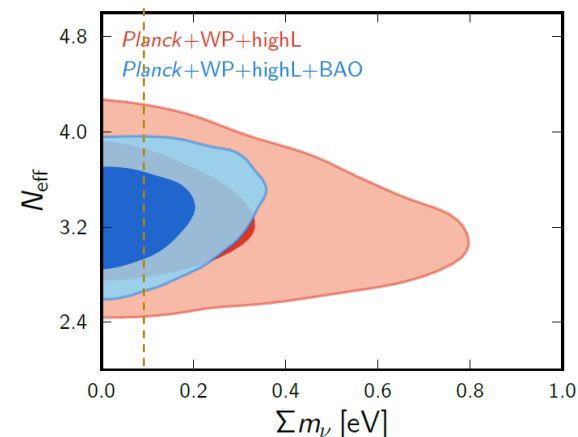
$$\Delta m_{sol}^2 = m_2 - m_1^2$$

- ▶ Two Δm^2 + three angles measured precisely by oscillation experiments.

Measurements: present & future

Parameter	best-fit ($\pm 1\sigma$)	3σ	Talks by Cheubey & Agarwala
Δm_{\odot}^2 [10^{-5} eV ²]	$7.58^{+0.22}_{-0.26}$	6.99 – 8.18	2002
$ \Delta m_A^2 $ [10^{-3} eV ²]	$2.35^{+0.12}_{-0.09}$	2.06 – 2.67	1998
$\sin^2 \theta_{12}$	0.306 (0.312) $^{+0.018}_{-0.015}$	0.259 (0.265) – 0.359 (0.364)	
$\sin^2 \theta_{23}$	$0.42^{+0.08}_{-0.03}$	0.34 – 0.64	
$\sin^2 \theta_{13}$ [140]	0.021 (0.025) $^{+0.007}_{-0.008}$	0.001 (0.005) – 0.044 (0.050)	2012
$\sin^2 \theta_{13}$ [142]	0.0251 ± 0.0034	0.015 – 0.036	

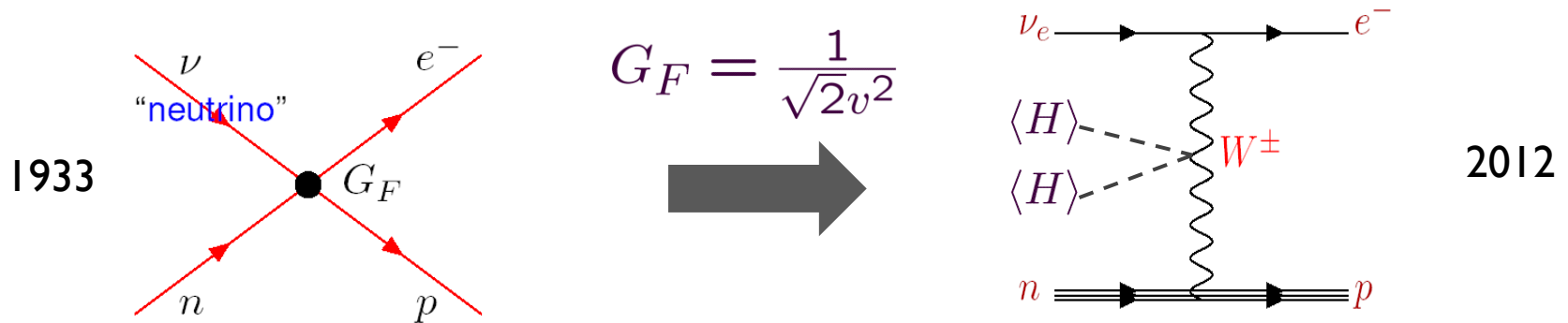
- ▶ Mass hierarchy: $m_3 > m_1$ or $m_1 > m_3$?
- ▶ CP violation?
- ▶ Majorana m_{ee} ?
- ▶ Sum[m_i] from cosmology?



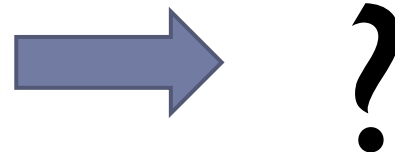
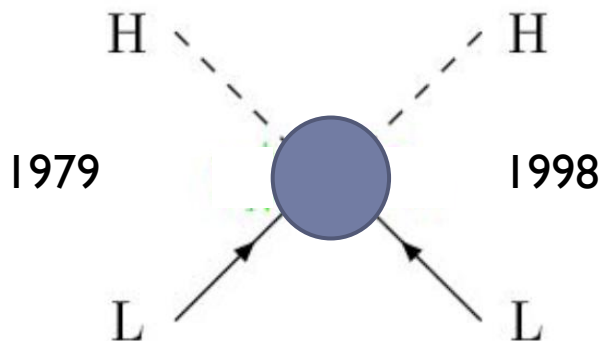
Neutrino & New Physics

UV theory of neutrino mass operators

► From Fermi to EBH.



► From Weinberg to ...



Dirac seesaw:

$$y^D \sim v/M_X \sim 10^{-13}$$

Dick, et.al., 9907462

EJC, Roy, 0803.1720

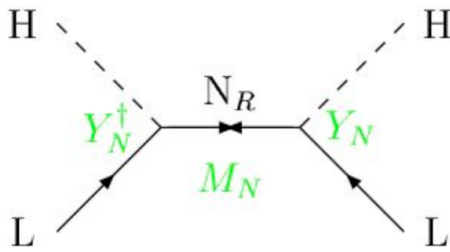
Majorana seesaw:

Arbitrary Yukawa with

$$M_X = \text{keV} - 10^{15} \text{ GeV}$$

Three Majorana Seesaws

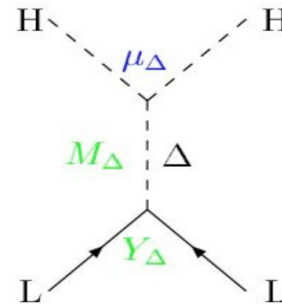
Fermion Singlet
(Type I)



$$m_\nu = Y_N^T \frac{1}{M_N} Y_N v^2$$

$$Y(N) = 0$$

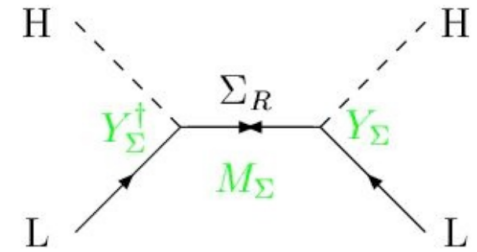
Scalar Triplet
(Type II)



$$m_\nu = Y_\Delta \frac{\mu_\Delta}{M_\Delta^2} v^2$$

$$Y(\Delta) = 1$$

Fermion Triplet
(Type III)



$$m_\nu = Y_\Sigma^T \frac{1}{M_\Sigma} Y_\Sigma v^2$$

$$Y(\Sigma) = 0$$

Type I/II in a gauge model

▶ LR:
$$W_L \begin{pmatrix} \nu \\ l \end{pmatrix} \Delta_L \Delta_R \begin{pmatrix} N \\ l^c \end{pmatrix} W_R$$

SU(2)_R breaking v_R giving heavy masses to N & W_R

▶ U(1)' : $c_1 U(1)_\chi + c_2 U(1)_\psi + c_3 U(1)_Y$

$$E_6 \rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_\chi \times U(1)_\psi$$

$$27 \rightarrow 10 + \bar{5} + \mathbf{1} + (5 + \bar{5}) + 1$$

U(1)' breaking v' giving heavy masses to N & Z'

$$\mathcal{L}_\nu = y_\nu H L N + \frac{1}{2} y_N S N N + h.c.$$

$$m_\nu = y_\nu \frac{v_H^2}{M_N} y_\nu^T$$

U(1)' models

Erler, et.al., I 103.2659

Q'	q	\bar{u}	e^+	\bar{d}	l	$\bar{\nu}$	\bar{D}	L	D	\bar{L}	S
$2Q_R$	0	-1	+1	+1	0	-1	0	-1	0	1	0
$2Q_d$	0	+1	-1	0	+1	0	-1	0	0	-1	1
$2Q_I$	0	0	0	-1	-1	+1	1	1	0	0	-1
$2\sqrt{3}Q_{L_1}$	+1	0	+2	0	-1	+2	0	-1	-2	-1	2
$2\sqrt{3}Q_{R_1}$	0	-1	+1	-1	-2	+1	2	1	0	1	-2
$2\sqrt{3}Q_{\nu}$	0	-1	+1	+2	+1	-2	-1	-2	0	1	1
$2\sqrt{3}Q_{\eta}$	0	+2	-2	-1	+1	+1	-1	1	0	-2	1
$2\sqrt{6}Q_{B-L}$	+1	-1	+3	-1	-3	+3	2	0	-2	0	0
$2\sqrt{6}Q_{ALR}$	+1	-1	+3	+2	0	0	-1	-3	-2	0	3
$2\sqrt{6}Q_{\psi}$	+1	+2	0	-1	0	+3	-1	0	-2	-3	3
$2\sqrt{6}Q_{\psi}$	+1	+1	+1	+1	+1	+1	-2	-2	-2	-2	4
$2\sqrt{10}Q_{\chi}$	-1	-1	-1	+3	+3	-5	-2	-2	2	2	0
$2\sqrt{10}Q_N$	+1	+1	+1	+2	+2	0	-3	-3	-2	-2	5
$2\sqrt{15}Q_{\eta}$	+2	+2	+2	-1	-1	+5	-1	-1	-4	-4	5
$2\sqrt{15}Q_Y$	+1	-4	+6	+2	-3	0	2	-3	-2	3	0
$4\sqrt{15}Q_S$	-1	-1	-1	+8	+8	-10	-7	-7	2	2	5

$SH_u H_d$
if $Q'(S) \neq 0$



Type II Seesaw

- ▶ SM + a triplet boson ($Y=1$):

$$\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$$

$$\mathcal{L}_\Delta = f_{\alpha\beta} L_\alpha^T C i\tau_2 \Delta L_\beta + \frac{1}{\sqrt{2}} \mu \Phi^T i\tau_2 \Delta \Phi + h.c. \Rightarrow v_\Delta = \mu \frac{v_\Phi^2}{M_\Delta^2}$$

- ▶ Triplet VEV generates neutrino mass matrix:

$$m_{\alpha\beta}^\nu = f_{\alpha\beta} v_\Delta \Rightarrow f_{\alpha\beta} \frac{v_\Delta}{v_\Phi} \sim 10^{-12}$$

- ▶ A peculiar signature of SS2L resonance from the doubly charged boson if $f \sim v_\Delta/v_\Phi$: $\Delta^{++} \xrightarrow{f_{\alpha\beta}} l_\alpha^+ l_\beta^+$
→ Determine the neutrino mass hierarchy at colliders!

EJC, Lee, Park, 0304069

Type II Yukawa after θ_{13}

- ▶ Neutrino oscillation data (assuming vanishing CP phases) determines the coupling $f = M^\nu/v_\Delta$:

$$M^\nu = \begin{matrix} & \text{NH} & & \text{IH} \\ \begin{pmatrix} 0.00403 & 0.00816 & 0.00259 \\ 0.00816 & 0.0264 & 0.0215 \\ 0.00259 & 0.0215 & 0.0286 \end{pmatrix} & & & \begin{pmatrix} 0.0479 & -0.00557 & -0.00573 \\ -0.00557 & 0.0239 & -0.0240 \\ -0.00573 & -0.0240 & 0.02693 \end{pmatrix} \end{matrix}$$

- ▶ $\text{Br}(\Delta^{++})$ for di-lepton channels (100% for $v_\Delta < 10^{-4}$ GeV):

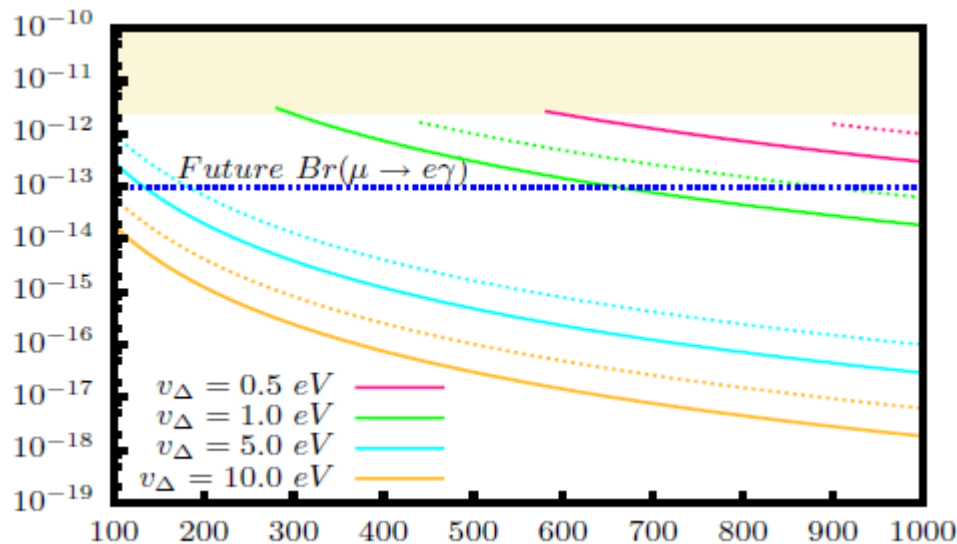
Br (%)	ee	$e\mu$	$e\tau$	$\mu\mu$	$\mu\tau$	$\tau\tau$
NH	0.62	5.11	0.51	26.8	35.6	31.4
IH1	47.1	1.27	1.35	11.7	23.7	14.9

Q) Revisit the CP phase effect?

► Correlations of LFV procedures in type II.

$$\text{Br}(\mu \rightarrow e\gamma) = \frac{27\alpha}{256\pi G_F^2 M_{H^{\pm\pm}}^4} \frac{|(m_\nu m_\nu^\dagger)_{e\mu}|^2}{v_\Delta^4} \text{Br}(\mu \rightarrow e\bar{\nu}\nu)$$

$$\text{Br}(\mu \rightarrow 3e) = \frac{1}{16G_F^2 M_{H^{\pm\pm}}^4} \frac{|(m_\nu)_{\mu e}|^2 |(m_\nu)_{ee}|^2}{v_\Delta^4} \text{Br}(\mu \rightarrow e\bar{\nu}\nu)$$



$$\frac{m_{ee} m_{e\mu}^*}{(m m^\dagger)_{e\mu}} < 0.025$$

$$\frac{1}{(m m^\dagger)_{e\mu}} < 1$$

EJC, Lee, Park, 0304069

Type III Seesaw

- ▶ SM + fermion triplets with $Y=0$:

$$\mathcal{L}_{\text{III}} = y_\nu L H_u \Sigma + \frac{1}{2} M \Sigma \Sigma \quad \Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$$

- ▶ Additional Dirac & Majorana masses for leptons:

$$\mathcal{L}_{\text{mass}} = m_D (l^- \Sigma^+ + \nu \Sigma^0) + M \Sigma^+ \Sigma^- + \frac{1}{2} M \Sigma^0 \Sigma^0$$

- ▶ Neutrino mass matrix by Seesaw ($m_D \ll M$):

$$M_\nu = m_D \frac{1}{M} m_D^T$$

- ▶ l - Σ^- / ν - Σ^0 mixing

→ L- Σ gauge vertices $\propto g m_D / M \sim 10^{-6}$

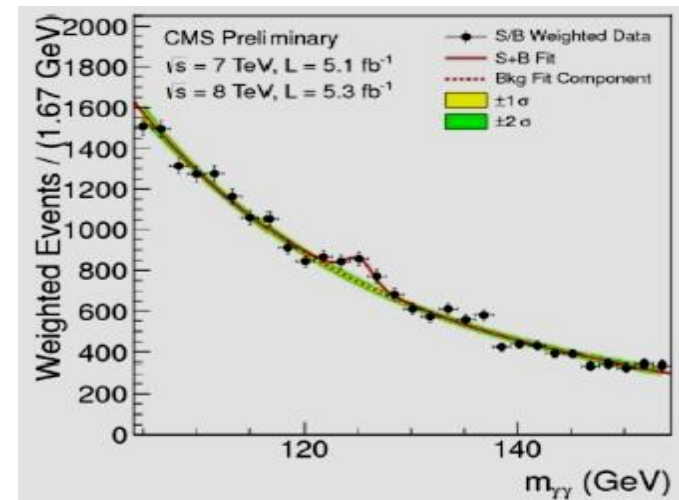
$$W^\pm l^\mp \Sigma^0, \quad W^\pm \nu \Sigma^\mp, \quad Z l^\pm \Sigma^\mp, \quad Z \nu \Sigma^0$$

Neutrino & Higgs

Natural Higgs mass?

- ▶ 125 GeV Higgs at LHC questions the usual argument for NP through the hierarchy problem:

$$\begin{aligned} \delta m_h^2 &= (-1)^F \frac{\lambda}{8\pi^2} \int^\Lambda \frac{d^4 p}{p^2 - m^2} \\ &= \frac{3}{8\pi^2 v^2} (4m_t^2 - 2m_W^2 - m_Z^2 - m_h^2) \Lambda^2 \\ &= m_h^2 \left(\frac{\Lambda}{500 \text{ GeV}} \right)^2 \end{aligned}$$



- ▶ Λ can be a physical mass scale of a UV theory, *i.e.*, $\Lambda = M_X$.
- ▶ Naturalness with Higgs coupling to seesaw particles.

Low-scale seesaw natural?

- ▶ Seesaw particle contribution to Higgs mass:

$$\delta m_h^2 \lesssim m_h^2 \times \Delta$$

Farina, Pappadopulo, Strumia, 1303.7244

- ▶ Type I:
$$\delta m^2 = \frac{4\lambda_N^2}{(4\pi)^2} M^2 \left(\ln \frac{M^2}{\bar{\mu}^2} - 1 \right) \quad \bar{\mu} \sim M_{\text{Pl}}$$

$$M \lesssim m_h \left(\Delta \frac{16\pi^2 m_h}{m_\nu} \right)^{1/3} \approx 0.7 \cdot 10^7 \text{ GeV} \times \sqrt[3]{\Delta}$$

- ▶ Type II:
$$\delta m^2 = -M^2 \frac{6g_2^4 + 3g_Y^4}{(4\pi)^4} \left(\frac{3}{2} \ln^2 \frac{M^2}{\bar{\mu}^2} + 2 \ln \frac{M^2}{\bar{\mu}^2} + \frac{7}{2} \right)$$

$$M \lesssim 200 \text{ GeV} \times \sqrt{\Delta}$$

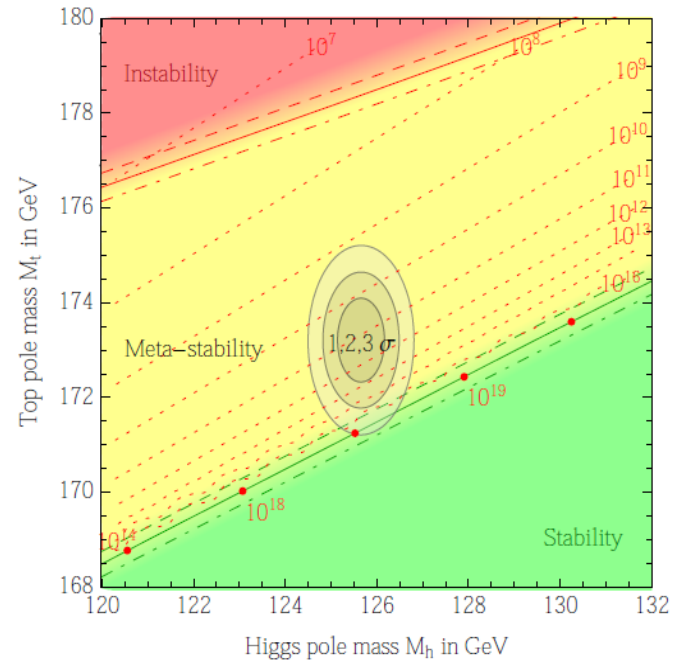
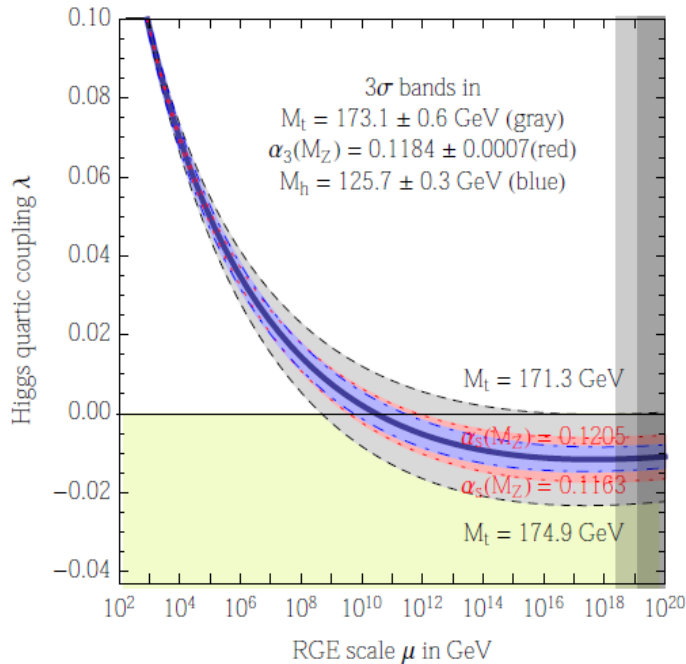
- ▶ Type III:
$$\delta m^2 = \frac{g_2^4}{(4\pi)^4} M^2 \left(36 \ln \frac{M^2}{\bar{\mu}^2} - 6 \right)$$

$$M \lesssim 0.94 \text{ TeV} \times \sqrt{\Delta}$$

Higgs instability

- ▶ Higgs quartic turns to negative due to large y_t :

$$32\pi^2 \frac{d\lambda_H}{dt} = 24\lambda_H^2 - (3g_Y^2 + 9g^2 - 24y_t^2)\lambda_H + \frac{3}{8}g_Y^4 + \frac{3}{4}g_Y^2g^2 + \frac{9}{8}g^4 - 24y_t^4 + \dots$$



Degrassi, et.al., 1307.3536

Higgs instability in type II

- ▶ Higgs potential of type II – coupling of doublet and triplet:

$$\begin{aligned} V(H, \Delta) = & m^2 H^\dagger H + M^2 \text{Tr}(\Delta^\dagger \Delta) \\ & + \lambda_1 (H^\dagger H)^2 + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + 2\lambda_3 \text{Det}(\Delta^\dagger \Delta) \\ & + \lambda_4 (H^\dagger H) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 (H^\dagger \tau_i H) \text{Tr}(\Delta^\dagger \tau_i \Delta) \\ & + \frac{1}{\sqrt{2}} \mu H^T i\tau_2 \Delta H + h.c. \end{aligned}$$

- ▶ Vacuum stability condition:
 - $\lambda_1 > 0$, Arhrib, et.al., 1105.1925
 - $\lambda_2 > 0$,
 - $\lambda_2 + \frac{1}{2}\lambda_3 > 0$
 - $\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda_1 \lambda_2} > 0$,
 - $\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda_1 (\lambda_2 + \frac{1}{2}\lambda_3)} > 0$.
- ▶ Perturbativity: $|\lambda_i| \leq \sqrt{4\pi}$.

Higgs instability in type II

► 1-loop RGE in type II:

Chao, Zhang, 0611323
Schmidt, 07053841

$$16\pi^2 \frac{d\lambda_1}{dt} = 24\lambda_1^2 + \lambda_1(-9g_2^2 - 3g'^2 + 12y_t^2) + \frac{3}{4}g_2^4 + \frac{3}{8}(g'^2 + g_2^2)^2 - 6y_t^4 + 3\lambda_4^2 + 2\lambda_5^2$$

$$16\pi^2 \frac{d\lambda_2}{dt} = \lambda_2(-12g'^2 - 24g_2^2) + 6g'^4 + 9g_2^4 + 12g'^2g_2^2 + 28\lambda_2^2 + 8\lambda_2\lambda_3 + 4\lambda_3^2 + 2\lambda_4^2 + 2\lambda_5^2$$

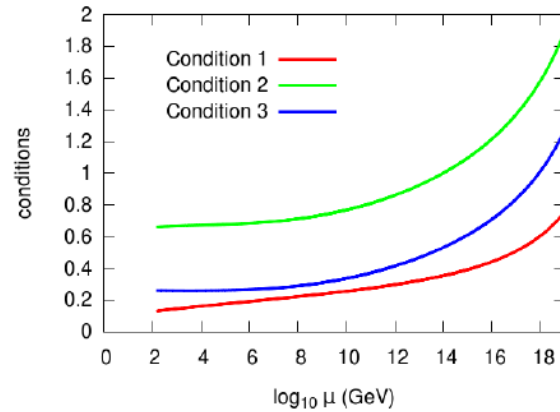
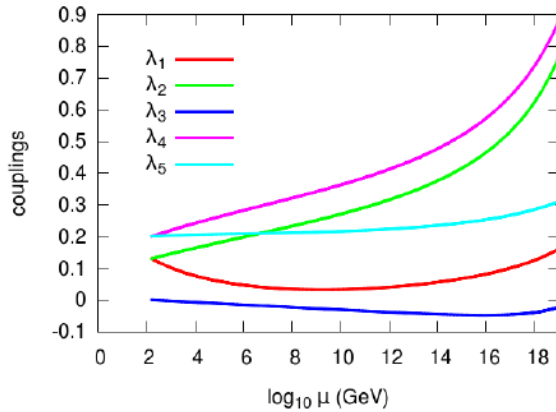
$$16\pi^2 \frac{d\lambda_3}{dt} = \lambda_3(-12g'^2 - 24g_2^2) + 6g_2^4 - 24g'^2g_2^2 + 6\lambda_3^2 + 24\lambda_2\lambda_3 - 4\lambda_5^2$$

$$16\pi^2 \frac{d\lambda_4}{dt} = \lambda_4\left(-\frac{15}{2}g'^2 - \frac{33}{2}g_2^2\right) + \frac{9}{5}g'^4 + 6g_2^4 + \lambda_4(12\lambda_1 + 16\lambda_2 + 4\lambda_3 + 4\lambda_4 + 6y_t^2) + 8\lambda_5^2$$

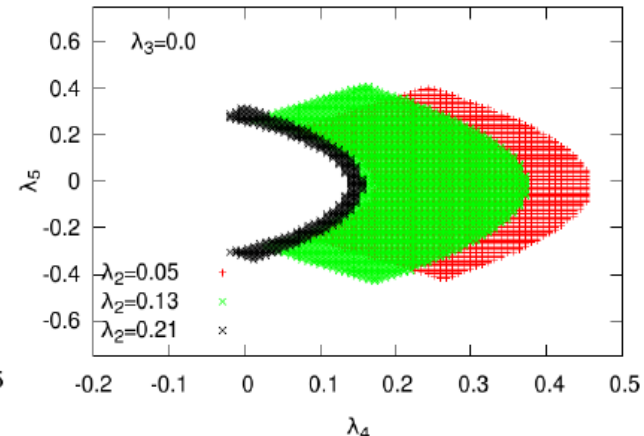
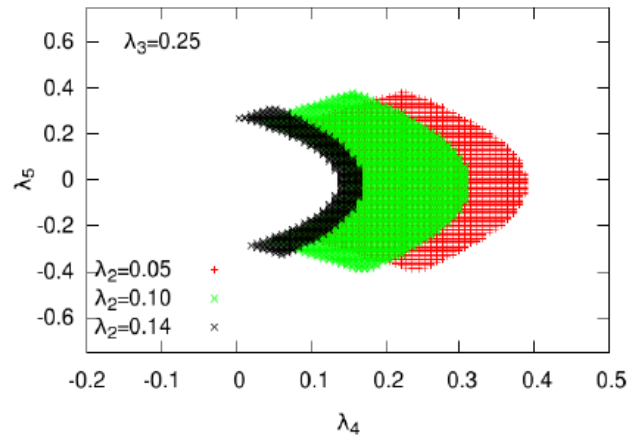
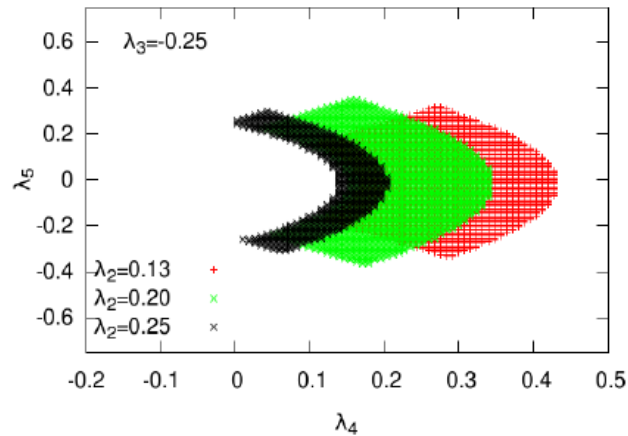
$$16\pi^2 \frac{d\lambda_5}{dt} = \lambda_4\left(-\frac{15}{2}g'^2 - \frac{33}{2}g_2^2\right) + 6g'^2g_2^2 + \lambda_5(4\lambda_1 + 4\lambda_2 - 4\lambda_3 + 8\lambda_4 + 6y_t^2),$$

Higgs stability & perturbativity in type II

EJC, Lee, Sharma, 1209.1303



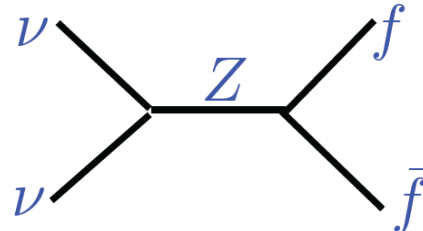
	10^{19} GeV
λ_2	(0, 0.25)
λ_3	(-0.55, 0.62)
λ_4	(0, 0.5)
λ_5	(-0.4, 0.4)



Neutrino & DM/BAU

Neutrino as DM

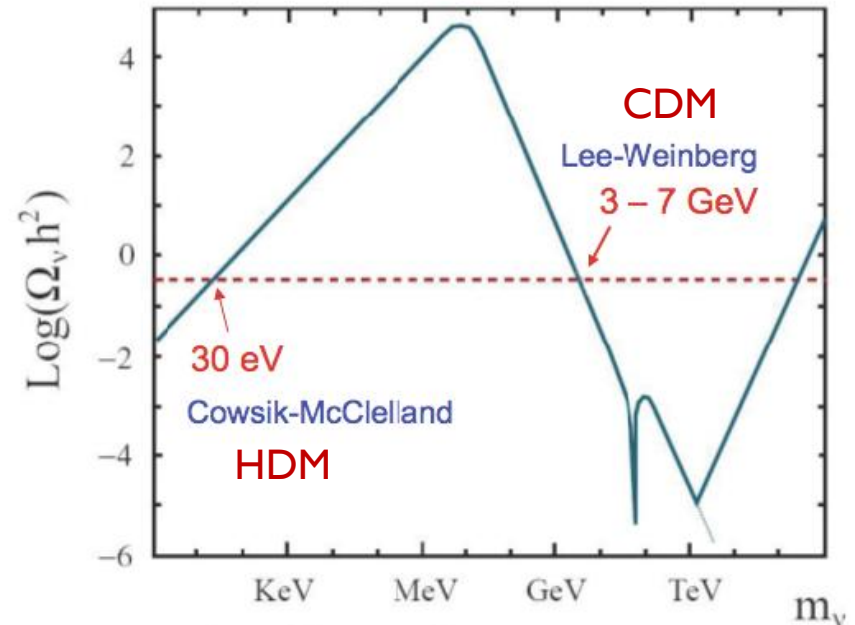
- ▶ The standard weak interaction can generate a right amount of CDM for a 10 GeV neutrino – WIMP.



A Feynman diagram illustrating the annihilation of two neutrinos (ν) into a fermion (f) and an antifermion (\bar{f}) through the exchange of a Z boson. The neutrinos enter from the left, meet at a vertex, and a Z boson is exchanged. The fermion and antifermion exit to the right from another vertex.

$$\langle \sigma_w v \rangle \sim \frac{\alpha_w^2 m_{\nu H}^2}{m_Z^4} \sim \frac{10^{-9}}{\text{GeV}^2}$$

Lee-Weinberg, 1977



Neutrino-DM connection?

Leptogenesis I

Type I/III seesaw :

$$\mathcal{L} = yLH_2N + \frac{1}{2}MNN \quad M_{ij}^\nu = y_{ik}y_{jk} \frac{\langle H_2 \rangle^2}{M_k}$$

L asymmetry from N decay: CP phase in Y_ν .

$$\epsilon_1 = \frac{\Gamma(N_1 \rightarrow LH_2) - \Gamma(N_1 \rightarrow \bar{L}\bar{H}_2)}{\Gamma(N_1 \rightarrow LH_2) + \Gamma(N_1 \rightarrow \bar{L}\bar{H}_2)} = \frac{3}{8\pi} \frac{\sum_i \text{Im}([(yy^\dagger)_{1i}]^2)}{(yy^\dagger)_{11}} \frac{M_1}{M_i}$$

$$\epsilon_1 \leq \frac{M_1 m_{\nu 3}}{\langle H_2 \rangle^2} \simeq 2 \times 10^{-7} \left(\frac{M_1}{10^9 \text{ GeV}} \right) \left(\frac{m_{\nu 3}}{0.05 \text{ eV}} \right)$$

Davidson-Ibarra

L asymmetry converted to B asymmetry by Γ_{sp}

$$Y_B \equiv c_{sp} \frac{n_L - n_{\bar{L}}}{s} = c_{sp} \frac{n_N^{eq}}{s} \epsilon \eta \approx 0.1 \frac{1}{g_*} \epsilon_1 \eta \sim 10^{-10}$$

$$g_* \sim 100, \eta < 1, \epsilon > 10^{-7}$$

$$M > 10^9 \text{ GeV}$$

nb) $m_\nu, \epsilon \propto y^2$

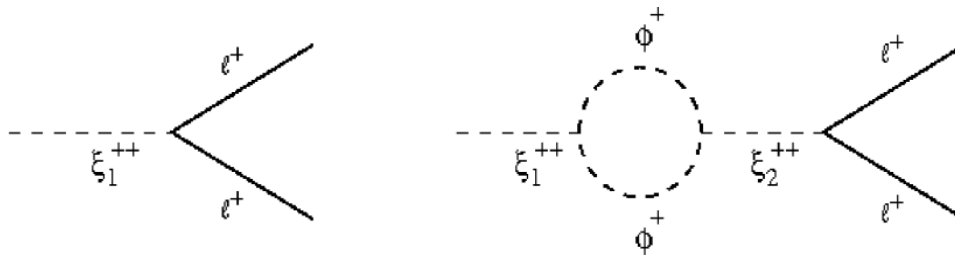
Leptogenesis II

Type II seesaw : $\mathcal{L} = f_{ij} L_i L_j \Delta + \mu H H \Delta + h.c.$

$$M_{ij}^\nu = f_{ij} v_\Delta = f_{ij} \mu \frac{v_H^2}{M_\Delta^2}$$

L asymmetry from $\Delta_{1,2}$ decay: CPV from mixing:

Ma-Sarkar



$$\delta_i \simeq \frac{\text{Im} \left[\mu_1 \mu_2^* \sum_{k,l} f_{1kl} f_{2kl}^* \right]}{8\pi^2 (M_1^2 - M_2^2)} \left[\frac{M_i}{\Gamma_i} \right]$$

$$\Gamma \sim f^2 + \mu^2 / M^2$$

Davidson-Ibarra bound persists.

Efficiency

Efficiency η and K factor: $K \equiv \frac{\Gamma_D}{H(T=M)}$

$K \gg 1 \rightarrow \eta \ll 1$ (strong wash-out regime) :

inverse-decay ($n_{\text{eq}}\Gamma_D$) decouples at $T < M$;
Boltzmann suppression.

$K \sim 1 \rightarrow \eta \sim 1$: out-of-equilibrium decay.

$K \ll 1 \rightarrow \eta \ll 1$ (weak wash-out regime) :

weak neutrino Yukawa interaction;
inefficient thermalization of N.

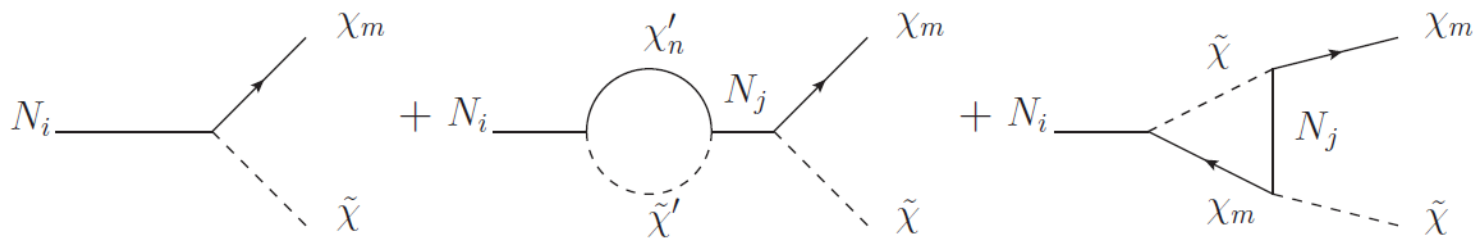
Gauge interaction reduces the efficiency.

TeV Leptogenesis

- ▶ Difficult to realize a low scale leptogenesis through CP asymmetry from neutrino Yukawas in type I (with $U(1)'$), II, III seesaw ($K \gg 1$ due to tiny $H \sim T^2 / M_p$, and large gauge interaction).
- ▶ A common exercise: add new states unrelated neutrino mass generation in type I.

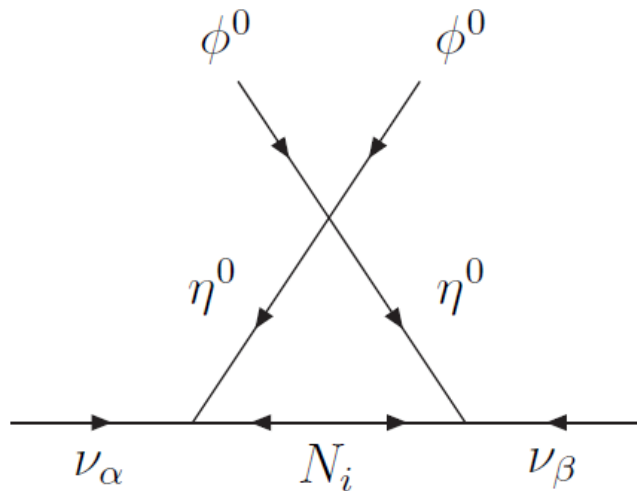
Fong, et.al., 1305.6312

$$- \mathcal{L}_{\tilde{\psi}} = \eta_{mi} \bar{\psi}_{Lm} N_i \tilde{\psi} + \sum_{\psi' \psi''} y_{mn} \bar{\psi}'_{Lm} \psi''_{Rn} \tilde{\psi} + \text{h.c.}$$



Radiative seesaw and inert doublet DM

- ▶ Inert doublet for neutrinos: $y_\nu \mathbf{L} \mathbf{H}' \mathbf{N}$. Ma, 0605180
- ▶ One-loop neutrino mass with $\lambda_5 (\mathbf{H}^\dagger \mathbf{H}')^2$.
- ▶ DM = \mathbf{H}'_R lighter than \mathbf{H}'_1 : correct thermal density + direct detection bound.
- ▶ Leptogenesis for $M_1 > 10^7$ GeV.



- ▶ No Higgs hierarchy problem.
- ▶ Seesaw/DM/BAU from sterile neutrinos.
- ▶ BAU from **GeV** $N_{2,3}$ through CP violating oscillations of sterile neutrinos ($Y_L = -Y_{L_s} \sim 10^{-10}$) at $T > T_{\text{sph}}$ if $\Delta M / M \sim 10^{-4 \sim -6}$.

$$\hat{H} = V(t) + U \frac{\hat{M}^2}{2k(t)} U^\dagger$$

Akhmedov, Rubakov, Smirnov, 9810255

- ▶ **keV** N_1 DM production through MSW conversion in thermal plasma if $Y_L > 8 \times 10^{-6}$ at $T \sim 100$ MeV.

Shi, Fuller, 9810076

$$V_x = \frac{\delta m^2}{2E} \sin 2\theta, \quad V_y = 0, \quad V_z = -\frac{\delta m^2}{2E} \cos 2\theta + V_\alpha^L + V_\alpha^T$$

$$V_\alpha^L \approx 0.35 G_F T^3 \left[L_0 + 2L_{\nu\alpha} + \sum_{\beta \neq \alpha} L_{\nu\beta} \right]$$

Q) Consistent M_ν & $0\nu 2\beta$?

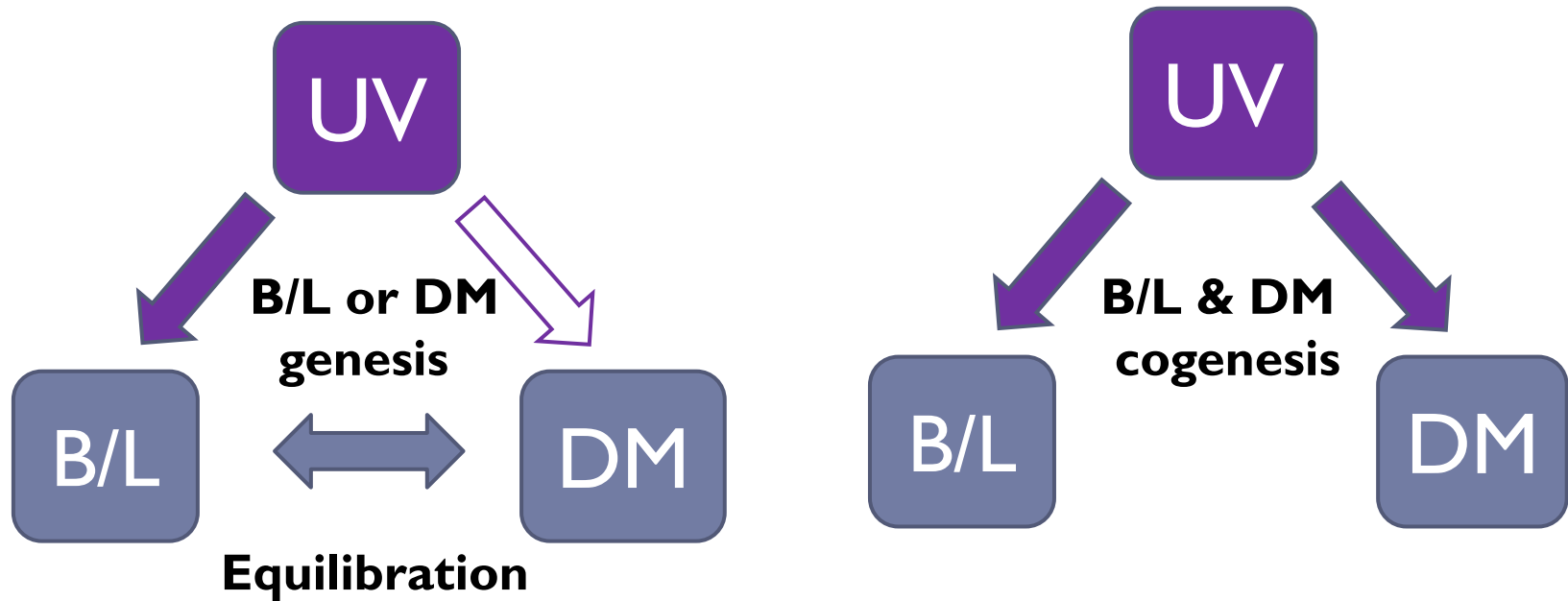
Asymmetric Dark Matter

- ▶ $\Omega_{\text{DM}}/\Omega_{\text{B}} = 5$: coincidence?
- ▶ Postulate the same origin for matter-antimatter asymmetry & dark matter population.

$$\Omega_{\text{DM}}/\Omega_{\text{B}} = m_{\text{DM}}Y_{\text{DM}}/m_{\text{B}}Y_{\text{B}}$$

- i) $Y_{\text{DM}} \sim Y_{\text{B}}$, $m_{\text{DM}} \sim 5 \text{ GeV}$ for COGENT/DAMA
- ii) $Y_{\text{DM}} \sim 0.05Y_{\text{B}}$, $m_{\text{DM}} \sim 100 \text{ GeV}$ for usual WIMP

Scenarios



Techni-Baryon Asymmetry

- ▶ Consider a GUT group containing both the baryon sector and the techni-baryon sector.
- ▶ Asymmetries in both sectors can be assumed to arise from a heavy GUT particle decay: $Y_B = Y_{TB}$.

$$\rho_B = Y_B m_B, \quad \rho_{TB} = Y_{TB} m_{TB} = \rho_{DM}$$

$$\Omega_{DM}/\Omega_B = m_{TB}/m_B = 5 \text{ if } \Lambda_{TB}/\Lambda_B = 5$$

Nussinov, PLB, 1985

Equilibration of B-L & DM

Kaplan, et.al., 0911.4117

- ▶ Assume an initial B-L (or DM) asymmetry
- ▶ Add an interaction which equilibrate the dark matter asymmetry and the initial B-L asymmetry
- ▶ A conserved quantum number: B-L+DM/2
e.g., $LH \leftrightarrow XX$

Equilibration interaction

$$W = \frac{1}{M} LH_u XX + m_X XX^c$$

Interaction rate > Expansion rate

$$\Gamma \sim \frac{T^3}{8\pi M^2} > H \sim \frac{3T^2}{M_P}$$

Chemical equilibrium relation

$$X = -\frac{11}{79}(B - L), \quad B = 0.3(B - L)$$

$$\frac{\Omega_{DM}}{\Omega_B} = \frac{m_X X}{m_B B} \Rightarrow m_X = 12\text{GeV}$$

Equilibration of B-L & DM

- ▶ **Require the suppression of the symmetric component.** →

Annihilation rate much larger than the standard value for the thermal freeze-out relic density.

Assume a “strong” interaction:

$$W = \lambda_X S X X^c + \lambda_H S H_u H_d + \lambda_S S^3$$

$$X \bar{X} \leftrightarrow H_u H_d$$

$$\Omega_{X+\bar{X}} h^2 \approx 0.1 \frac{3 \times 10^{-9} \text{GeV}^{-2}}{\langle \sigma_A v \rangle}$$

Type I seesaw & EWDM asymmetry

- ▶ A simple model relating the origins of tiny neutrino masses, the baryon asymmetry and the DM density.
- ▶ Realize asymmetric EWDM with sub-TeV mass.
- ▶ Naturally suppressed symmetric density. $\Omega_{\text{SDM}} h^2 \sim 0.1 \left(\frac{2\text{TeV}}{m_{DM}} \right)^2$
- ▶ Copious production at the LHC.
- ▶ Clean signals of disappearing charged tracks & stable charged tracks.

An, et.al., 0911.4463

EJC, 1009.0983

Falkowski, et.al., 1101.4936

Haba, et.al., 1101.5679

EJC, 1102.3455

A simple Model

- Introduce a vector-like $SU(2)_L$ multiplet:

EJC, 1102.3455

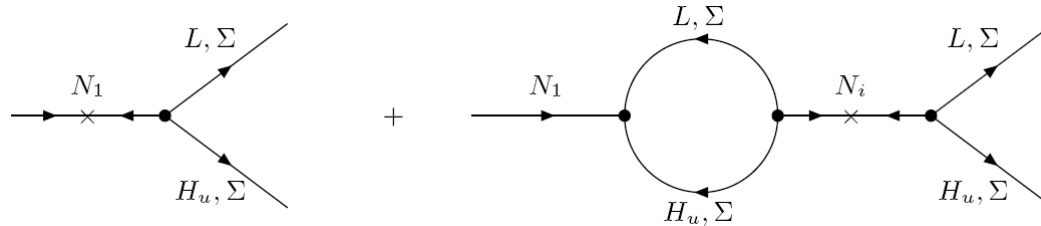
Σ, Σ^c with $Y = 0$ and $T = 1, 2, 3, \dots$

$$W = y_i N_i L H_u + \frac{1}{2} h_i N_i \Sigma \Sigma + m_\Sigma \Sigma \Sigma^c + \frac{1}{2} M_i N_i N_i$$

- “Extended B-L” broken by M:

superfields	L	N	Σ	Σ^c	M
$B - L$	-1	1	$-\frac{1}{2}$	$\frac{1}{2}$	-2

- Asymmetries from N decay:



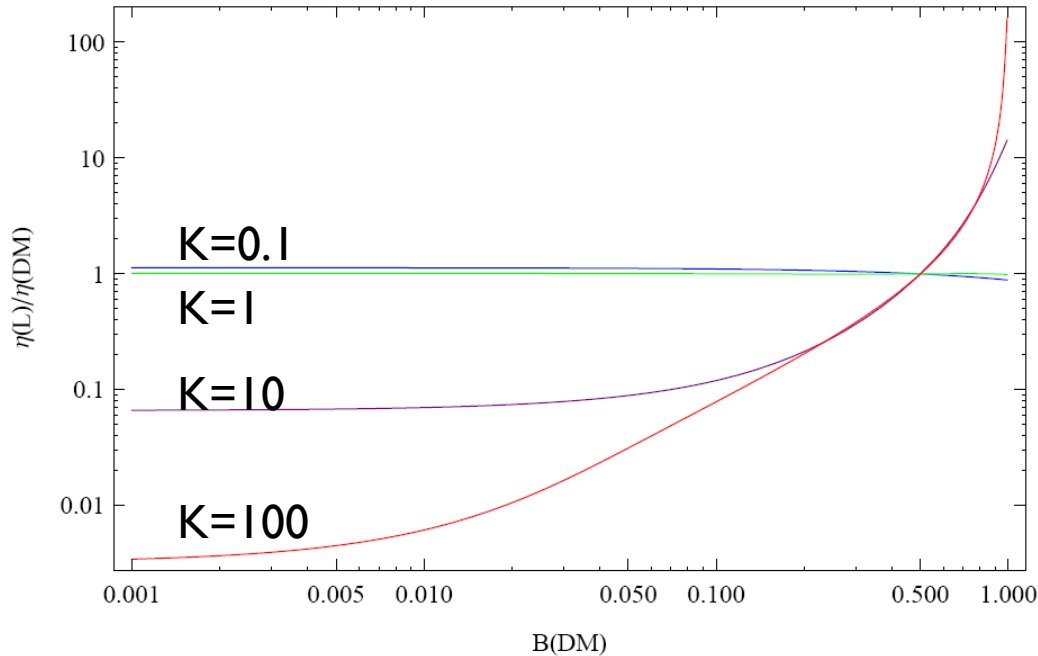
$$\varepsilon_L \approx \frac{1}{4\pi} \frac{\sum_i \text{Im}[y_i y_1^* (y_i y_1^* + h_i h_1^*)]}{|y_1|^2 + \frac{3}{4}|h_1|^2} \frac{M_1}{M_i},$$

$$\varepsilon_{DM} \approx \frac{2}{4\pi} \frac{\sum_i \text{Im}[h_i h_1^* (y_i y_1^* + h_i h_1^*)]}{|y_1|^2 + \frac{3}{4}|h_1|^2} \frac{M_1}{M_i},$$



$$Y_{L,DM} = \frac{315\zeta(3)}{4\pi^4 g_*} \varepsilon_{L,DM} \eta_{L,DM}$$

L/DM efficiency ratio



$$K = \frac{\Gamma_{N_1}}{H(T = M_{N_1})} \sim \frac{\tilde{m}_\nu}{10^{-3} \text{ eV}}$$

$$\frac{\varepsilon_{DM}}{\varepsilon_L} \approx 10^{-2} \frac{\eta_L}{\eta_{DM}} \frac{200 \text{ GeV}}{m_{DM}}$$

$$\frac{\Omega_{DM}}{\Omega_B} = \frac{m_{DM} Y_{DM}}{m_B Y_B} \approx \frac{31}{10} \frac{\varepsilon_{DM}}{\varepsilon_L} \frac{\eta_{DM}}{\eta_L} \frac{m_{DM}}{1 \text{ GeV}}$$

Mass spectra of DM multiplets ($T=1$)

- ▶ Fermion: (Σ^\pm, Σ^0)
Scalar: $(\tilde{\Sigma}_{1,2}^\pm, \tilde{\Sigma}_{1,2}^0)$

- ▶ Mass spectrum:

$$m_{\tilde{\Sigma}_1^0} > m_{\tilde{\Sigma}_1^\pm} > m_{\Sigma^\pm} > m_{\Sigma^0}$$



D-term splitting
 $\sim 1\text{ GeV}$



EW loop splitting
 $\sim 0.1\text{ GeV}$

LHC Signatures

- Effective interaction below M:

$$\mathcal{L}_{eff} = \xi \nu \Sigma^\pm \tilde{\Sigma}^\mp \Leftrightarrow W_{eff} = \frac{yh}{2M} LH_u \Sigma \Sigma$$

$$\xi = \frac{yh \langle H_u^0 \rangle}{2M} \sim \frac{m_\nu}{\langle H_u^0 \rangle} \sim 10^{-12} \text{ for } m_\nu = 0.1 \text{eV}$$

- Two kinds of long-lived charged particle tracks:

$$\tilde{\Sigma}^\pm \rightarrow \nu \Sigma^\pm \qquad \Sigma^\pm \rightarrow \pi^\pm \Sigma^0$$

$$\Gamma_{\tilde{\Sigma}^\pm} = \frac{\xi^2}{8\pi} m_{\tilde{\Sigma}^\pm} \qquad \Gamma_{\Sigma^\pm} = \frac{T(T+1)}{\pi} G_F^2 V_{ud}^2 \Delta m^3 f_\pi^3 \sqrt{1 - \frac{m_{\pi^\pm}^2}{\Delta m^2}}$$

$$\tau_{\tilde{\Sigma}^\pm} \sim 10^{-2} \text{sec} \qquad \tau_{\Sigma^\pm} \approx 106 \text{cm}$$

Stable charged track

Disappearing charged tracks

- Multiply charged tracks for T=3,2:

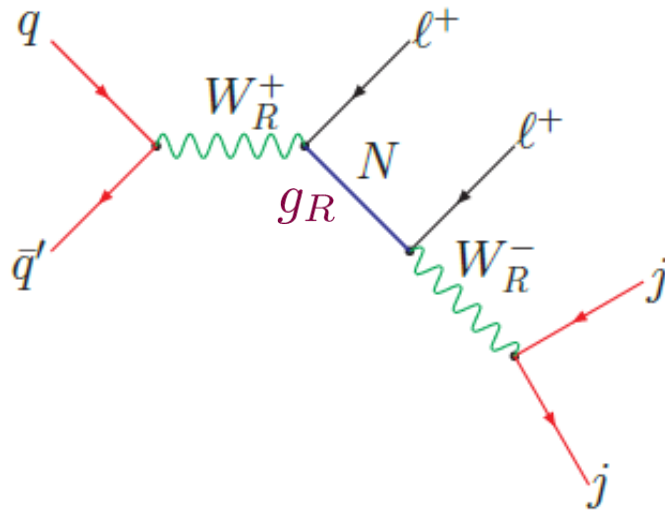
$$\tilde{\Sigma}^{\pm\pm\pm}, \tilde{\Sigma}^{\pm\pm} \qquad \Sigma^{\pm\pm\pm} \xrightarrow{35\text{cm}} \pi^\pm \Sigma^{\pm\pm} \xrightarrow{18\text{cm}} \pi^\pm \Sigma^\pm$$

Neutrino & LHC

LR & U(1)' at LHC

- ▶ Typical signatures: **SS2L+jj** probing Majorana nature of N.

Keung, Senjanovic, 1983



LR

$$q\bar{q} \rightarrow Z' \rightarrow NN$$

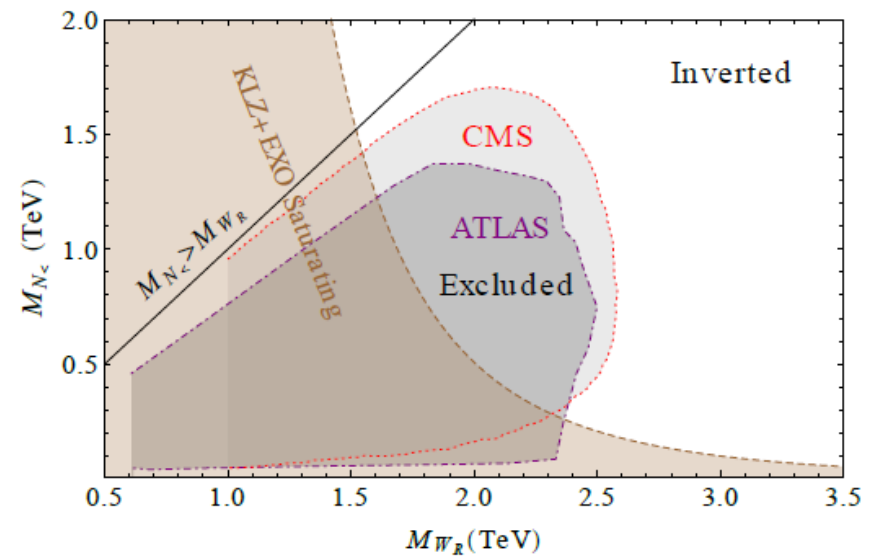
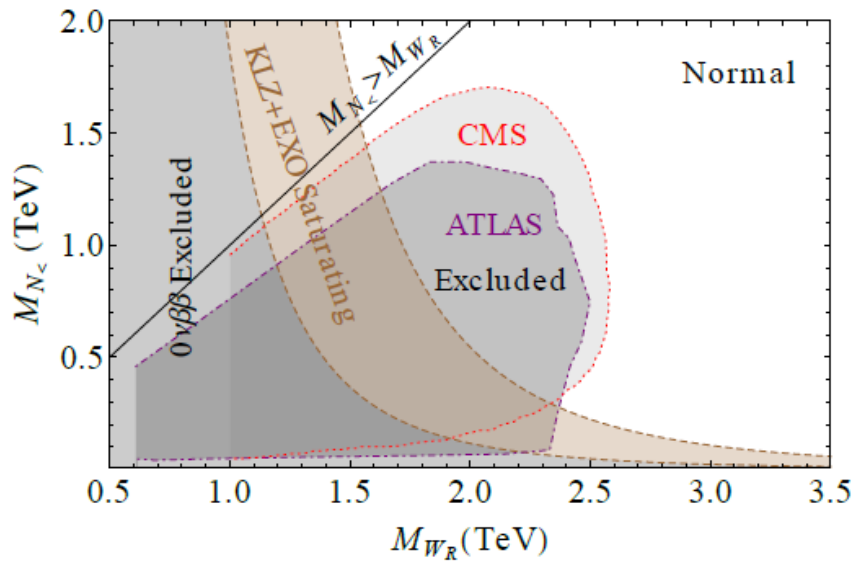
$$\rightarrow l^\pm l^\pm W^\mp W^\mp$$

$$\theta_{\nu N} \sim \sqrt{\frac{m_\nu}{M_N}}$$

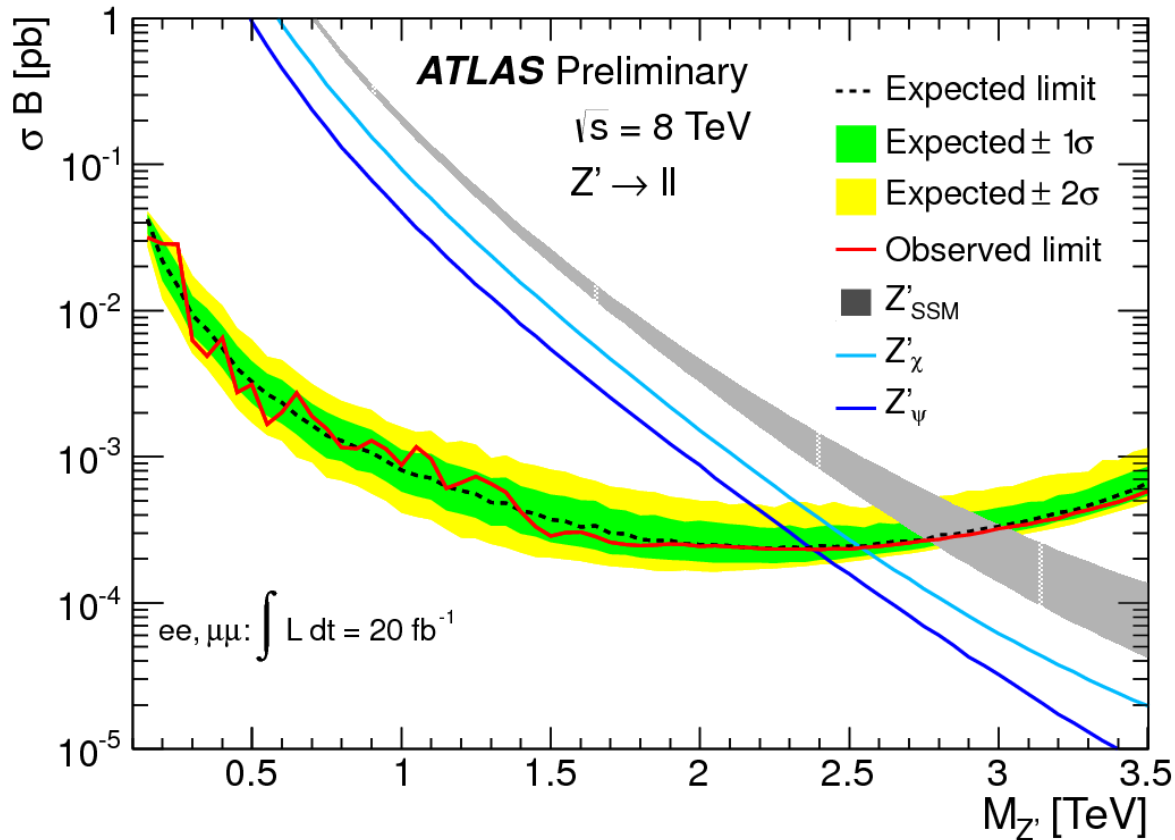
U(1)'

LHC+ $0\nu 2\beta$ search of LR model

Bhupal Dev, et.al., I305.0056
Type II dominance

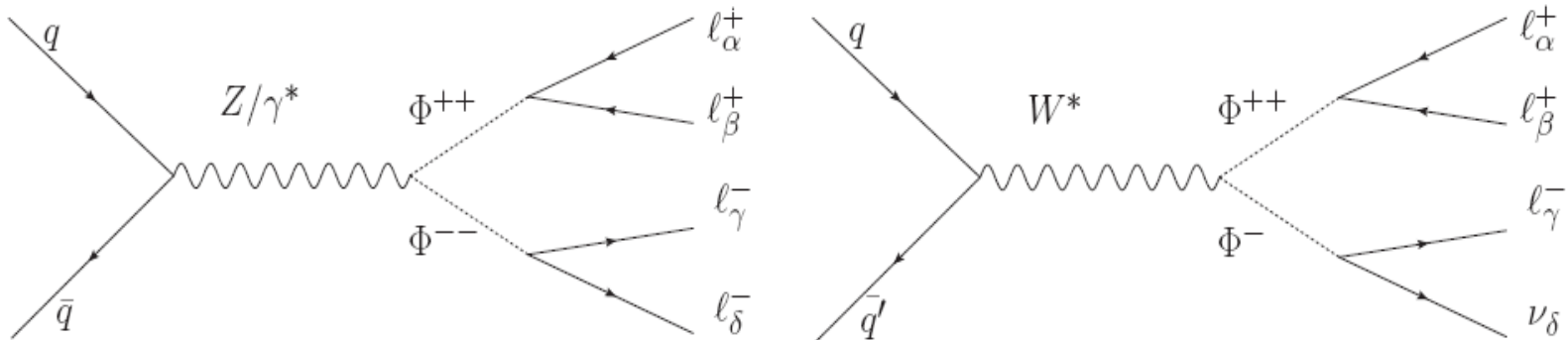


Z' search



Multi-lepton signals in type II

- ▶ 4l (2xSS2L) from $H^{++} H^{--}$ pair production.
- ▶ 3l from $H^{++} H^-$ associated production if $\Delta M \sim 0$.
- ▶ CMS looks for 4l or 3l events.
- ▶ ATLAS looks for SS2L resonances.

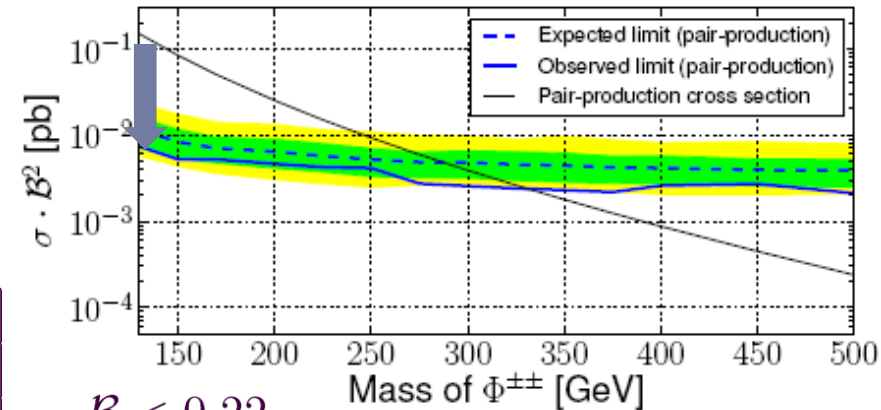


Benchmark point	Combined 95% CL limit [GeV]	95% CL limit for pair production only [GeV]
$\mathcal{B}(\Phi^{++} \rightarrow e^+e^+) = 100\%$	444	382
$\mathcal{B}(\Phi^{++} \rightarrow e^+\mu^+) = 100\%$	453	391
$\mathcal{B}(\Phi^{++} \rightarrow e^+\tau^+) = 100\%$	373	293
$\mathcal{B}(\Phi^{++} \rightarrow \mu^+\mu^+) = 100\%$	459	395
$\mathcal{B}(\Phi^{++} \rightarrow \mu^+\tau^+) = 100\%$	375	300
$\mathcal{B}(\Phi^{++} \rightarrow \tau^+\tau^+) = 100\%$	204	169
BP1	383	333
BP2	408	359
BP3	403	355
BP4	400	353

Benchmark point	ee	eμ	eτ	μμ	μτ	ττ
BP1	0	0.01	0.01	0.30	0.38	0.30
BP2	1/2	0	0	1/8	1/4	1/8
BP3	1/3	0	0	1/3	0	1/3
BP4	1/6	1/6	1/6	1/6	1/6	1/6

Cf.)

Br (%)	ee	eμ	eτ	μμ	μτ	ττ
NH	0.62	5.11	0.51	26.8	35.6	31.4
IH1	47.1	1.27	1.35	11.7	23.7	14.9



$$\mathcal{B} < 0.22$$

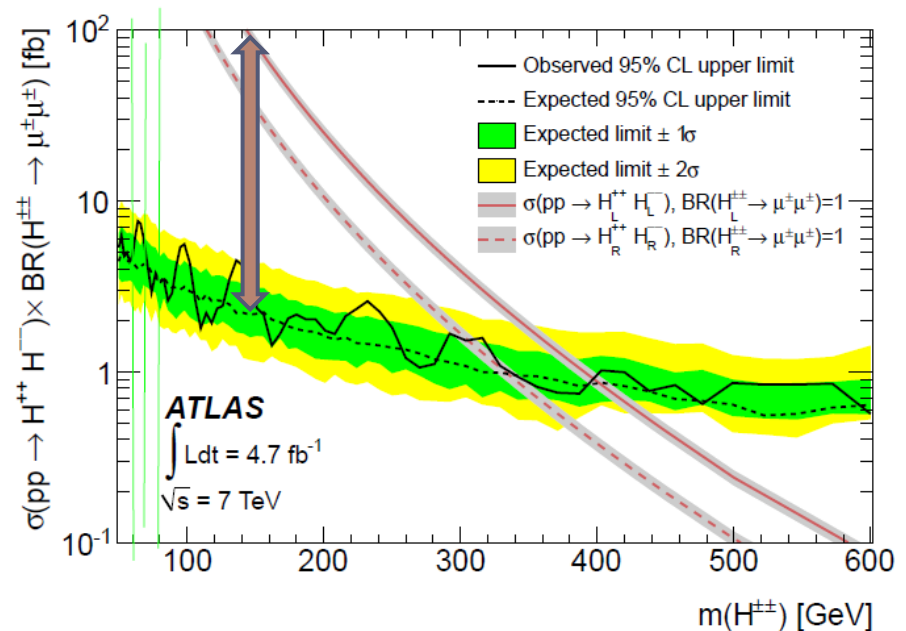
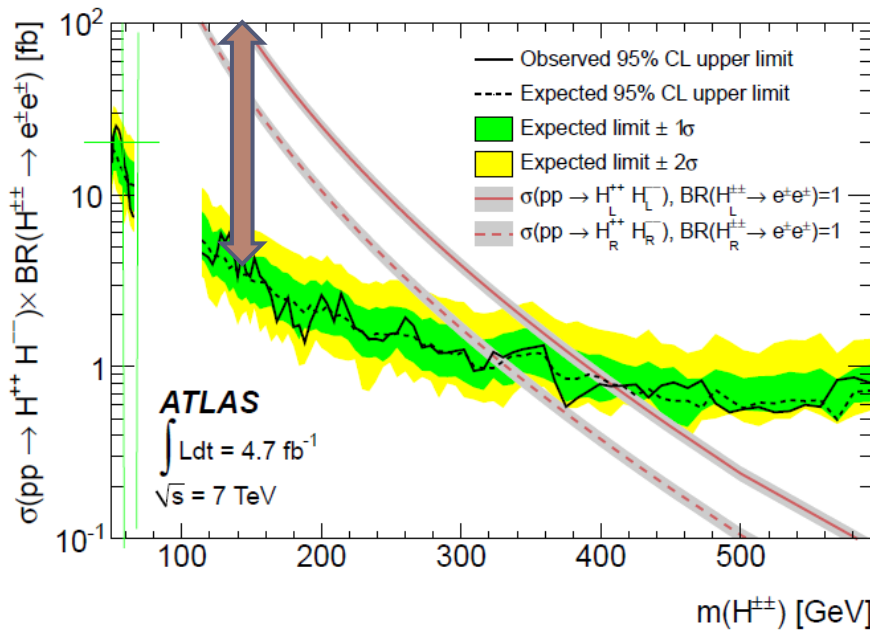
$$M_{H^{++}} < 100\text{GeV}$$

ATLAS search

ATLAS, 1210.5070

BR($H_L^{\pm\pm} \rightarrow \ell^\pm \ell'^\pm$)	95% CL lower limit on $m(H_L^{\pm\pm})$ [GeV]					
	$e^\pm e^\pm$		$\mu^\pm \mu^\pm$		$e^\pm \mu^\pm$	
	exp.	obs.	exp.	obs.	exp.	obs.
100%	407	409	401	398	392	375
33%	318	317	317	290	279	276
22%	274	258	282	282	250	253
11%	228	212	234	216	206	190

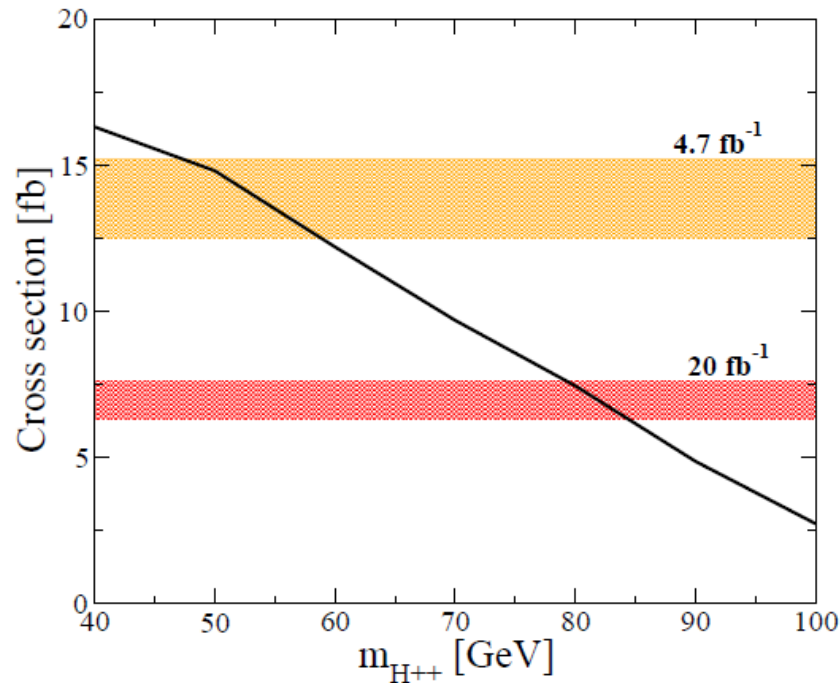
NH : BR($\mu\mu$) \approx 27%
IH : BR(ee) \approx 47%



$H^{++} \rightarrow W^+ W^+$ search

- ▶ $H^{++} \rightarrow l^+ l^+ + X$ from ATLAS SS2L data:

Kanemura, Yagyu, Yokoya, I 305.2383



Q) LEP limit from multi-jet final states?

Type III Seesaw

- ▶ SM + fermion triplets with $Y=0$:

$$\mathcal{L}_{\text{III}} = y_\nu L H_u \Sigma + \frac{1}{2} M \Sigma \Sigma \quad \Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$$

- ▶ Additional Dirac & Majorana masses for leptons:

$$\mathcal{L}_{\text{mass}} = m_D (l^- \Sigma^+ + \nu \Sigma^0) + M \Sigma^+ \Sigma^- + \frac{1}{2} M \Sigma^0 \Sigma^0$$

- ▶ Neutrino mass matrix by Seesaw ($m_D \ll M$):

$$M_\nu = m_D \frac{1}{M} m_D^T$$

- ▶ l - Σ^- / ν - Σ^0 mixing

→ L- Σ gauge vertices $\propto g m_D / M \sim 10^{-6}$

$$W^\pm l^\mp \Sigma^0, \quad W^\pm \nu \Sigma^\mp, \quad Z l^\pm \Sigma^\mp, \quad Z \nu \Sigma^0$$

LHC signatures

▶ Σ decay: $\Sigma^\pm \rightarrow l^\pm h, l^\pm Z, \nu W^\pm$

$$\Sigma^0 \rightarrow \nu h, \nu Z, l^\pm W^\mp$$

Franceschini, et.al.

0805.1613

▶ Σ production: $pp \rightarrow \Sigma^+ \Sigma^-, \Sigma^\pm \Sigma^0$

▶ Four lepton final states at ATLAS

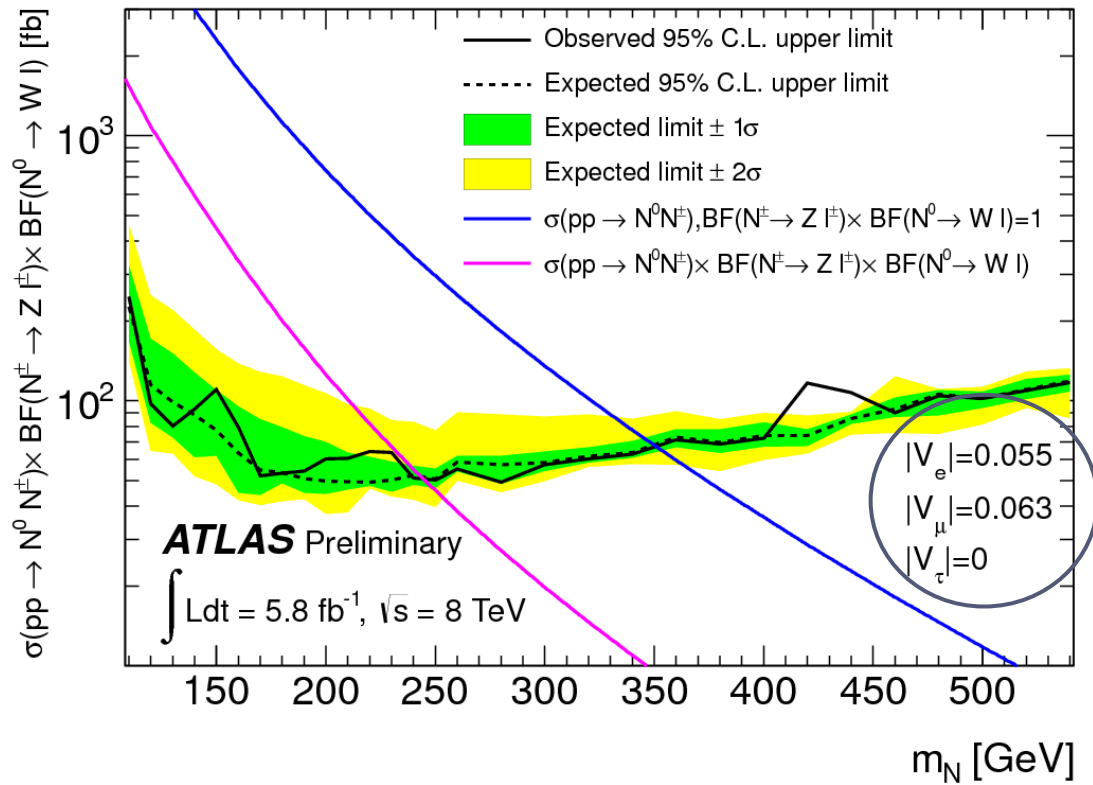
$$pp \rightarrow \Sigma^\pm \Sigma^0 \rightarrow l^\pm Z (l\bar{l}) l^\pm W^\mp (jj')$$

▶ Higgs production associated with charged leptons:

$$pp \rightarrow \Sigma^\pm \Sigma^0 \rightarrow l^\pm l^\pm h W^\mp$$

Bandyopadhyay, Choi, EJC, Kang, 1112.3080

ATLAS search



Conclusion

- ▶ Great achievements from oscillation observation during past 15 years.
- ▶ Further Quest for the nature of neutrino mass: Dirac/Majorana, absolute scale, hierarchy & CPV.
- ▶ Neutrino-DM/BAU connection: leptogenesis+ADM.
- ▶ Majorana mass models at TeV scale?
- ▶ LHC signatures of type I, II, III seesaws: SS2L, displacement, associated Higgs production.
- ▶ LHC13/14 continues to probe the neutrino signals.
- ▶ More for peculiar type II: SS2L resonance, SS4L, Higgs-to-diphoton.

Neutrino & LHC – More on Type II

▶ Same-sign tetra-leptons.

Triplet-antitriplet oscillation

EJC & Sharma, 1206.6278

▶ Higgs boson Phenomenology.

EWPD

Perturbativity & vacuum stability

Higgs-to-diphoton rate

EJC, Lee & Sharma, 1209.1303

▶ General study in $(v_{\Delta}, \Delta M)$.

EJC & Sharma, 1309.6888

Type II Seesaw

- ▶ SM + a triplet boson ($Y=1$):

$$\Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$$

$$\mathcal{L}_\Delta = f_{\alpha\beta} L_\alpha^T C i\tau_2 \Delta L_\beta + \frac{1}{\sqrt{2}} \mu \Phi^T i\tau_2 \Delta \Phi + h.c. \Rightarrow v_\Delta = \mu \frac{v_\Phi^2}{M_\Delta^2}$$

- ▶ Triplet VEV generates neutrino mass matrix:

$$m_{\alpha\beta}^\nu = f_{\alpha\beta} v_\Delta \Rightarrow f_{\alpha\beta} \frac{v_\Delta}{v_\Phi} \sim 10^{-12}$$

- ▶ A peculiar signature of SS2L resonance from the doubly charged boson if $f \sim v_\Delta/v_\Phi$: $\Delta^{++} \xrightarrow{f_{\alpha\beta}} l_\alpha^+ l_\beta^+$
→ Determine the neutrino mass hierarchy at colliders!

EJC, Lee, Park, 0304069

Type II Yukawa after θ_{13}

- ▶ Neutrino oscillation data (assuming vanishing CP phases) determines the coupling $f = M^\nu/v_\Delta$:

$$M^\nu = \begin{matrix} & \text{NH} & & \text{IH} \\ \begin{pmatrix} 0.00403 & 0.00816 & 0.00259 \\ 0.00816 & 0.0264 & 0.0215 \\ 0.00259 & 0.0215 & 0.0286 \end{pmatrix} & & & \begin{pmatrix} 0.0479 & -0.00557 & -0.00573 \\ -0.00557 & 0.0239 & -0.0240 \\ -0.00573 & -0.0240 & 0.02693 \end{pmatrix} \end{matrix}$$

- ▶ $\text{Br}(\Delta^{++})$ for di-lepton channels (100% for $v_\Delta < 10^{-4}$ GeV):

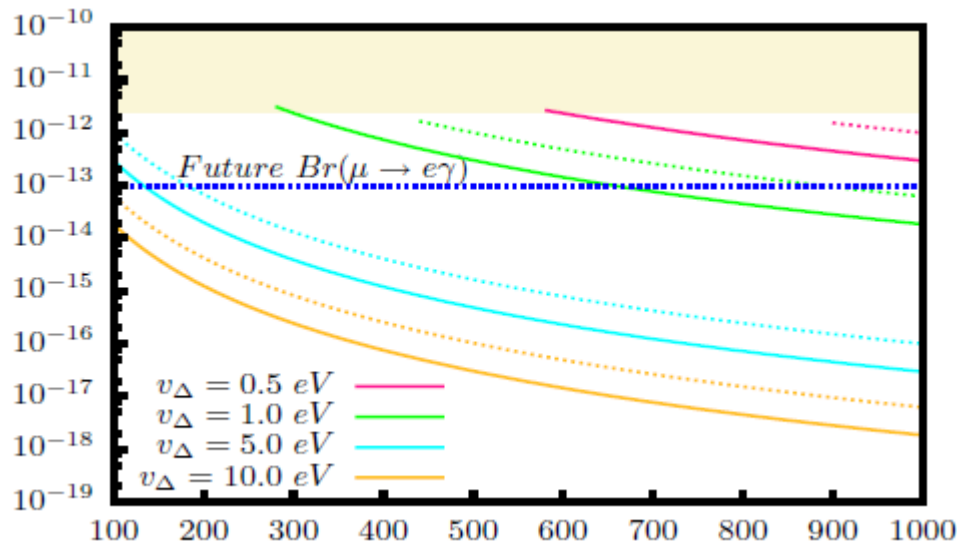
Br (%)	ee	$e\mu$	$e\tau$	$\mu\mu$	$\mu\tau$	$\tau\tau$
NH	0.62	5.11	0.51	26.8	35.6	31.4
IH1	47.1	1.27	1.35	11.7	23.7	14.9

Q) Revisit the CP phase effect at LHC?

► Correlations of LFV procedures in type II.

$$\text{Br}(\mu \rightarrow e\gamma) = \frac{27\alpha}{256\pi G_F^2 M_{H^{\pm\pm}}^4} \frac{|(m_\nu m_\nu^\dagger)_{e\mu}|^2}{v_\Delta^4} \text{Br}(\mu \rightarrow e\bar{\nu}\nu)$$

$$\text{Br}(\mu \rightarrow 3e) = \frac{1}{16G_F^2 M_{H^{\pm\pm}}^4} \frac{|(m_\nu)_{\mu e}|^2 |(m_\nu)_{ee}|^2}{v_\Delta^4} \text{Br}(\mu \rightarrow e\bar{\nu}\nu)$$



$$\frac{m_{ee} m_{e\mu}^*}{(m m^\dagger)_{e\mu}} < 0.025$$

$$\frac{1}{(m m^\dagger)_{e\mu}} < 1$$

EJC, Lee, Park, 0304069

Type II scalar sector

► Scalar potential of type II seesaw

$$\begin{aligned} V(\Phi, \Delta) = & m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) \\ & + \lambda_1 (\Phi^\dagger \Phi)^2 + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + 2\lambda_3 \text{Det}(\Delta^\dagger \Delta) \\ & + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 (\Phi^\dagger \tau_i \Phi) \text{Tr}(\Delta^\dagger \tau_i \Delta) \\ & + \frac{1}{\sqrt{2}} \mu \Phi^T i\tau_2 \Delta \Phi + h.c. \end{aligned}$$

► Five boson mass eigenstates

$$\begin{array}{c} \Delta^{++}, \Delta^+, \Delta^0 \\ \Phi^+, \Phi^0 \end{array} \Rightarrow h^0, H^0, A^0, H^+, H^{++}$$

Doublet-triplet mixing

- ▶ Doublet-triplet mixing controlled by $\xi = v_{\Delta}/v_{\Phi}$:

$$\begin{array}{lll} \phi_I^0 = G^0 - 2\xi A^0 & \phi^+ = G^+ + \sqrt{2}\xi H^+ & \phi_R^0 = h^0 - a\xi H^0 \\ \Delta_I^0 = A^0 + 2\xi G^0 & \Delta^+ = H^+ - \sqrt{2}\xi G^+ & \Delta_R^0 = H^0 + a\xi h^0 \end{array}$$

$$a = 2 + (4\lambda_1 - \lambda_4 - \lambda_5)v_{\Phi}^2/(M_{H^0}^2 - m_{h^0}^2)$$

- ▶ We will work in the limit: $\xi \ll 0.01$.
- ▶ (note) ρ parameter constraint:

$$\rho = (1+2\xi^2)/(1+4\xi^2) \rightarrow \xi < 0.03$$

Triplet scalar spectrum

- Mass gap among triplet components:

$$\begin{aligned} M_{H^{++}}^2 &= M^2 + 2\frac{\lambda_4 - \lambda_5}{g^2} M_W^2 \\ M_{H^\pm}^2 &= M_{H^{++}}^2 + 2\frac{\lambda_5}{g^2} M_W^2 \\ M_{H^0, A^0}^2 &= M_{H^\pm}^2 + 2\frac{\lambda_5}{g^2} M_W^2. \end{aligned}$$

$\Delta M = M_{H^+} - M_{H^{++}}$

$\Delta M \approx \frac{\lambda_5}{g^2} \frac{M_W^2}{M} < M_W$

- Two mass hierarchies:

$$M_{H^{++}} < M_{H^+} < M_{H^0/A^0} \quad \text{if } \lambda_5 > 0$$

$$M_{H^{++}} > M_{H^+} > M_{H^0/A^0} \quad \text{if } \lambda_5 < 0$$

Triplet decay channels

- ▶ Gauge decays for non-vanishing ΔM (λ_5):

$$\begin{aligned}
 H^0/A^0 &\rightarrow H^\pm W^* \rightarrow H^{\pm\pm} W^* W^* \\
 H^{++} &\rightarrow H^\pm W^* \rightarrow H^0/A^0 W^* W^*
 \end{aligned}
 \quad \leftarrow \Delta M(\lambda_5)$$

- ▶ Di-lepton (same-sign) decays through $f_{\alpha\beta}$:

$$H^{++} \rightarrow l_\alpha^+ l_\beta^+; \quad H^+ \rightarrow l_\alpha^+ \nu_\beta; \quad H^0/A^0 \rightarrow \nu_\alpha \nu_\beta \quad \leftarrow f_{\alpha\beta}$$

$$(*) f_\xi \sim 10^{-12}$$

- ▶ Di-quark/di-boson decays through ξ :

$$\begin{aligned}
 H^{++} &\rightarrow W^+ W^+; & H^+ &\rightarrow t\bar{b}; & H^0/A^0 &\rightarrow t\bar{t}, b\bar{b} \\
 & & &\rightarrow ZW, hW & &\rightarrow ZZ, hh/Zh
 \end{aligned}
 \quad \leftarrow \xi \equiv \frac{v_\Delta}{v_\Phi}$$

Δ - $\bar{\Delta}$ Oscillation

EJC & Sharma, I206.6278

- ▶ Triplet (lepton) number is conserved in the production:

$$pp \rightarrow \Delta \bar{\Delta}$$

- ▶ Triplet number breaking by doublet-triplet mixing:

$$\mathcal{L}_{\Delta} = \frac{1}{\sqrt{2}} \mu \Phi^T i\tau_2 \Delta^\dagger \Phi + h.c.$$

- ▶ It induces a tiny mass splitting between H^0 & A^0 :

$$\mathcal{L}_{\Delta} = \frac{1}{\sqrt{2}} \mu \Phi^T i\tau_2 \Delta^\dagger \Phi + h.c. \Rightarrow -\mu v_{\Phi} h^0 H^0$$

$$v_{\Delta} = \frac{\mu v_{\Phi}^2}{\sqrt{2} M_{H^0}^2}$$

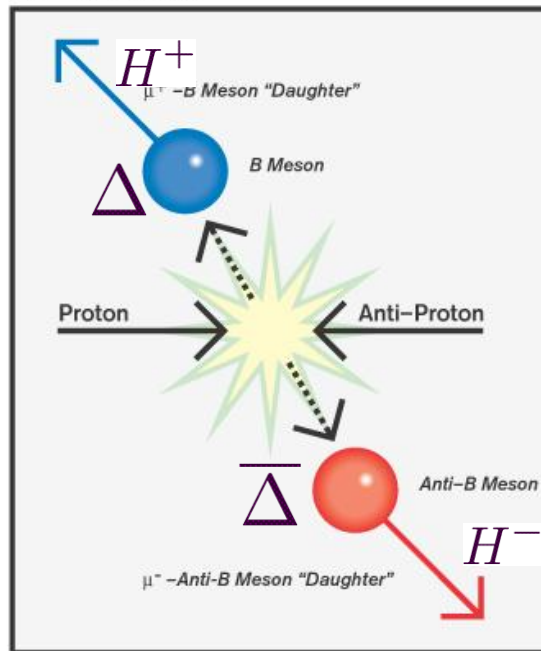
$$\delta M_{HA} \approx 2M_{H^0} \frac{v_{\Delta}^2}{v_0^2} \frac{M_{H^0}^2}{M_{H^0}^2 - m_{h^0}^2}$$

Δ - $\bar{\Delta}$ Oscillation



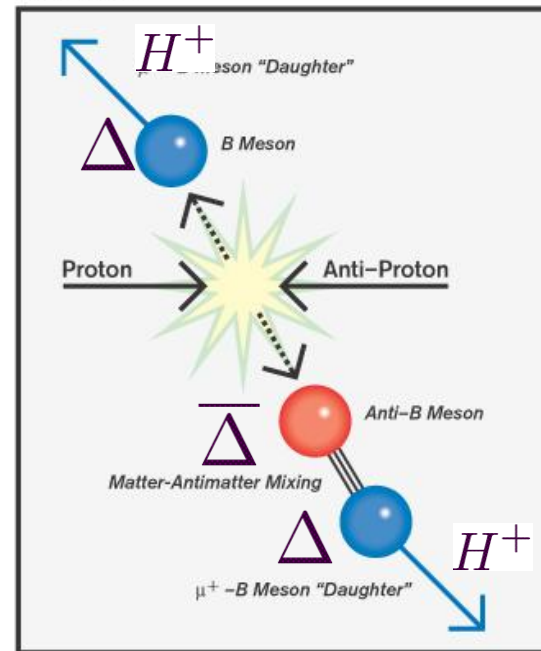
No Mixing

$$l^+l^+l^-l^-$$



Mixing

$$l^+l^+l^+l^+$$



Δ - $\bar{\Delta}$ Oscillation

- ▶ Initial $\Delta = H^0 + i A^0$ evolves as

$$|\Delta(t)\rangle = g_+(t)|\Delta\rangle + g_-(t)|\bar{\Delta}\rangle \quad [\Gamma = \Gamma_{H^0} = \Gamma_{A^0}]$$

$$g_{\pm}(t) = \frac{1}{2}e^{-\Gamma t/2} \left(e^{iM_{H^0}t} \pm e^{iM_{A^0}t} \right)$$

- ▶ Probabilities of Δ going to Δ or $\bar{\Delta}$ are

$$\chi_{\pm} \equiv \frac{\int_0^{\infty} dt |g_{\pm}(t)|^2}{\int_0^{\infty} dt |g_+(t)|^2 + \int_0^{\infty} dt |g_-(t)|^2}$$

$$\chi_{\pm} = \begin{cases} \frac{2+x^2}{2(1+x^2)} \\ \frac{x^2}{2(1+x^2)} \end{cases}$$

$$x \equiv \frac{\delta M}{\Gamma} = \frac{\tau_{dec}}{\tau_{osc}}$$

Same-Sign Tetra-Leptons

▶ Lepton number violating processes:

$$\begin{aligned}
 pp &\rightarrow \Delta^0 \bar{\Delta}^0 \Rightarrow \Delta^0 \Delta^0 \rightarrow H^+ H^+ 2W^- \rightarrow H^{++} H^{++} 4W^- \\
 &\Delta^+ \bar{\Delta}^0 \Rightarrow \Delta^+ \Delta^0 \rightarrow H^{++} H^+ 2W^- \rightarrow H^{++} H^{++} 3W^-
 \end{aligned}$$

▶ Production cross-section:

$$\begin{aligned}
 \sigma(4\ell^\pm + 3W^\mp) &= \sigma(pp \rightarrow H^\pm H^0 + H^\pm A^0) \left[\frac{x_{HA}^2}{1 + x_{HA}^2} \right] \text{BF}(H^0/A^0 \rightarrow H^\pm W^\mp) \\
 &\times [\text{BF}(H^\pm \rightarrow H^{\pm\pm} W^\mp)]^2 [\text{BF}(H^{\pm\pm} \rightarrow \ell^\pm \ell^\pm)]^2; \\
 \sigma(4\ell^\pm + 4W^\mp) &= \sigma(pp \rightarrow H^0 A^0) \left[\frac{2 + x_{HA}^2}{1 + x_{HA}^2} \frac{x_{HA}^2}{1 + x_{HA}^2} \right] \text{BF}(H^0 \rightarrow H^\pm W^\mp) \text{BF}(A^0 \rightarrow H^\pm W^\mp) \\
 &\times [\text{BF}(H^\pm \rightarrow H^{\pm\pm} W^\mp)]^2 [\text{BF}(H^{\pm\pm} \rightarrow \ell^\pm \ell^\pm)]^2.
 \end{aligned}$$

Same-Sign Tetra-Leptons

► Is this observable?

i) H^{++} is the lightest and $f_{\alpha\beta} > \xi$.

ii) ΔM sufficiently large to allow $\Delta^0 \rightarrow H^+ W^- \rightarrow H^{++} 2W^-$.

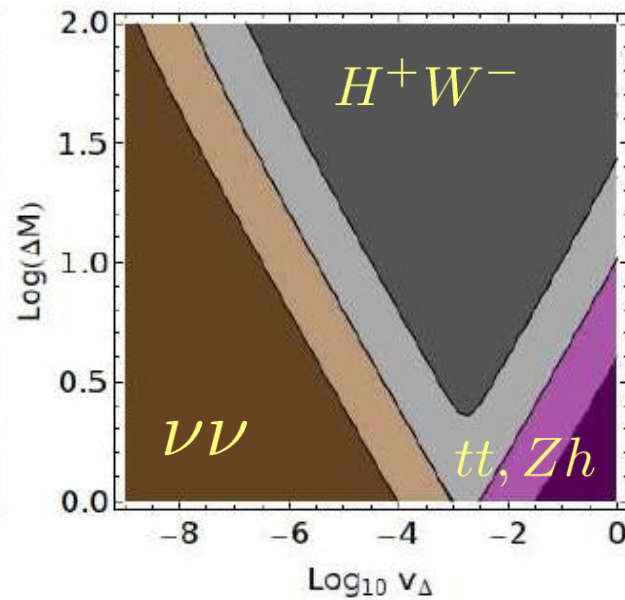
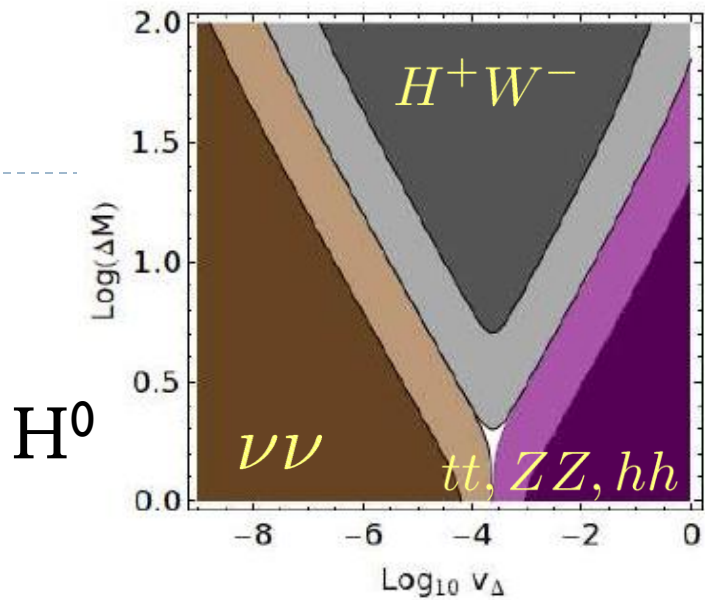
iii) Sizable oscillation parameter: $x \sim 1$.

$$\delta M_{HA} \sim 2 \frac{v_{\Delta}^2}{v_{\Phi}^2} M_{H^0} \quad \Gamma_{H^0/A^0} \sim \frac{G_F^2 \Delta M^5}{\pi^3}$$

$$v_{\Delta} \sim 10^{-4} \text{GeV}, \quad \Delta M \sim 2 \text{GeV} \quad \Rightarrow \quad \delta M_{HA} \sim \Gamma_{H^0/A^0} \sim 10^{-11} \text{GeV}$$

Triplet decay channels

H^0	A^0	H^+	H^{++}
$\rightarrow t\bar{t}$	$\rightarrow t\bar{t}$	$\rightarrow t\bar{b}$	$\rightarrow \ell^+\ell^+$
$\rightarrow b\bar{b}$	$\rightarrow b\bar{b}$	$\rightarrow \ell^+\nu$	$\rightarrow W^{+*}W^{+*}$
$\rightarrow \nu\bar{\nu}$	$\rightarrow \nu\bar{\nu}$	$\rightarrow W^+Z$	
$\rightarrow ZZ$	$\rightarrow Zh^0$	$\rightarrow W^+h^0$	
$\rightarrow h^0h^0$	$\rightarrow H^\pm W^\mp^*$	$\rightarrow H^{++}W^{-*}$	
$\rightarrow H^\pm W^\mp^*$			

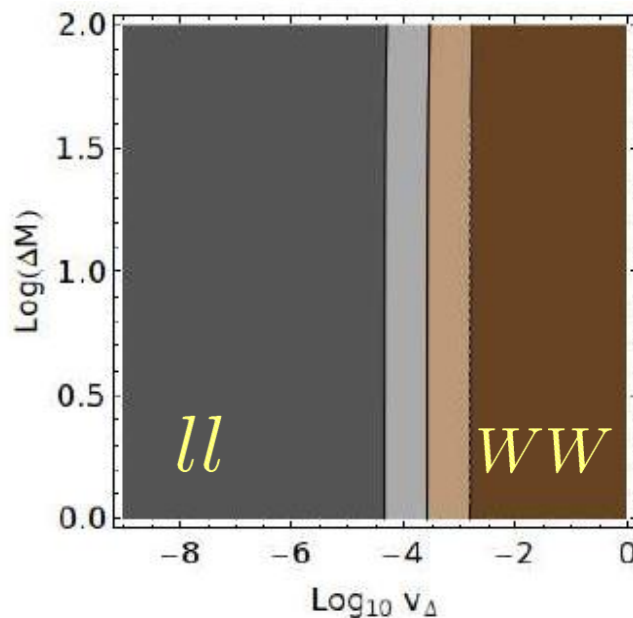
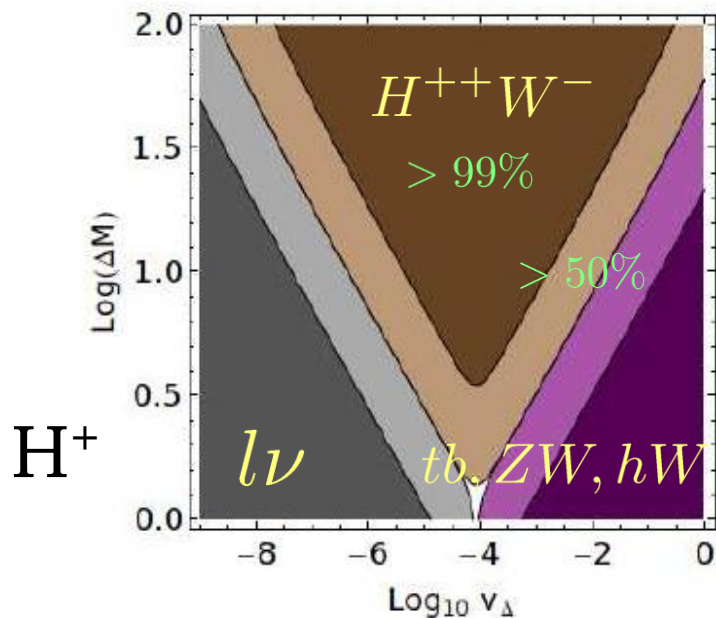


A^0

$M_{H^{++}} = 300\text{GeV}$

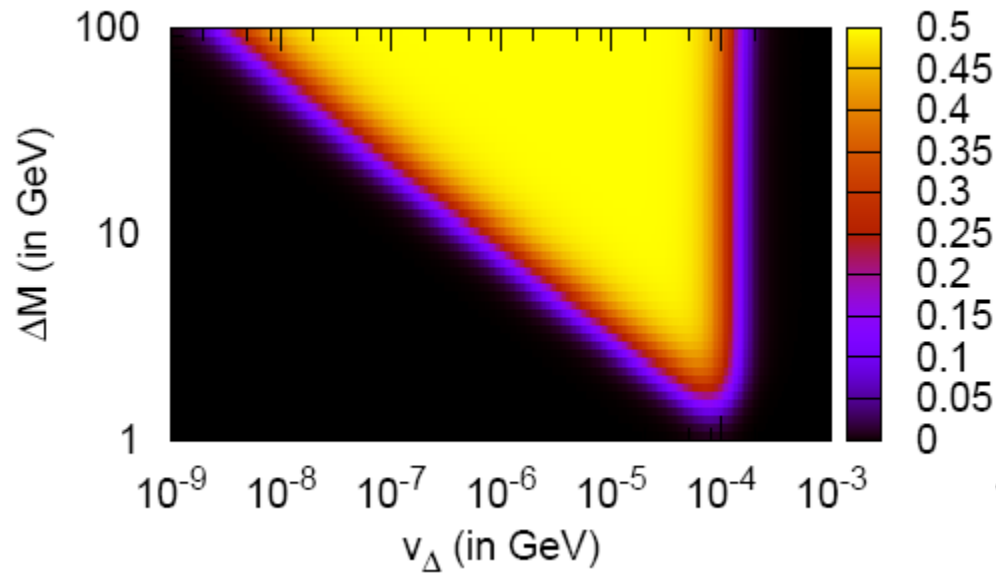
$< M_{H^+}$

$< M_{H^0/A^0}$

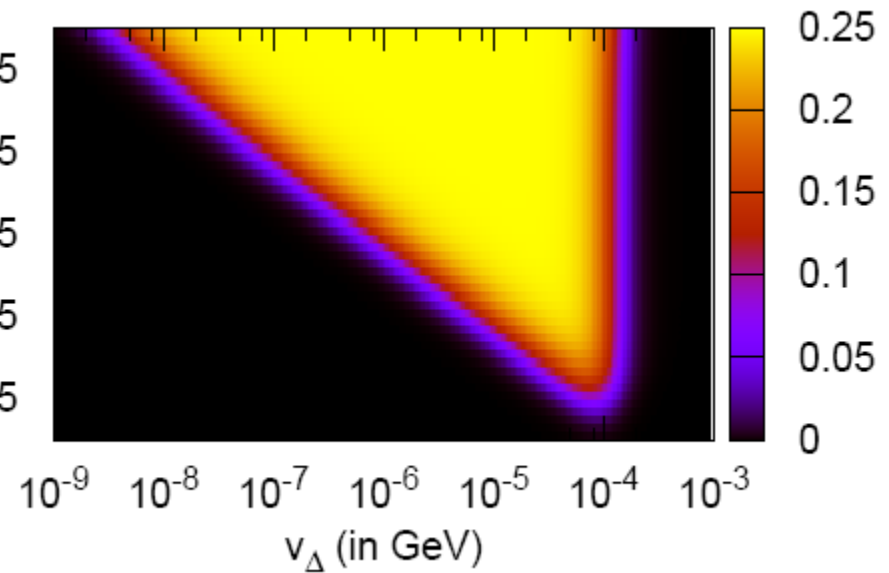


H^{++}

Maximizing the branching fraction



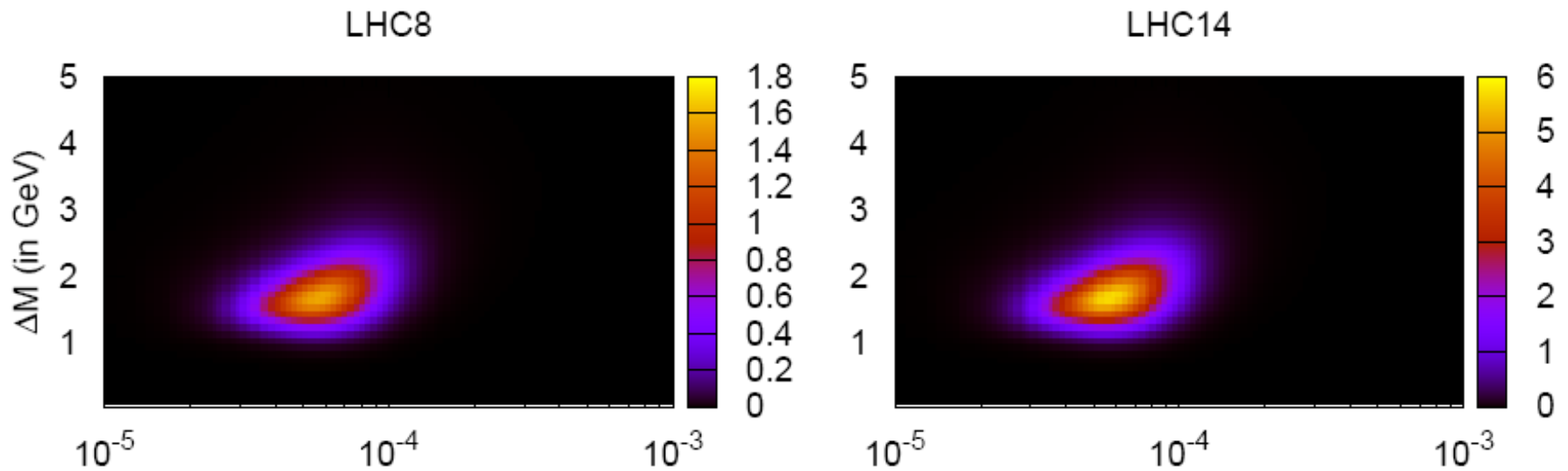
for $4l + 3W^*$



for $4l + 4W^*$

SS4L cross-section

- ▶ SS4L production including the oscillation factor:



$$M_{H^{\pm\pm}} = 400\text{GeV}$$

- ▶ Benchmark point:

$$v_{\Delta} = 7 \times 10^{-5} \text{ GeV}, \Delta M = 1.5 \text{ GeV}.$$

Event numbers

Final State	σ/fb (8 TeV)	σ/fb (14 TeV)
$H^+ H^0$	0.761	2.931
$H^+ A^0$	0.761	2.931
$H^- H^0$	0.275	1.209
$H^- A^0$	0.275	1.209
$H^0 A^0$	1.014	4.322

No background
Lepton selection cuts only

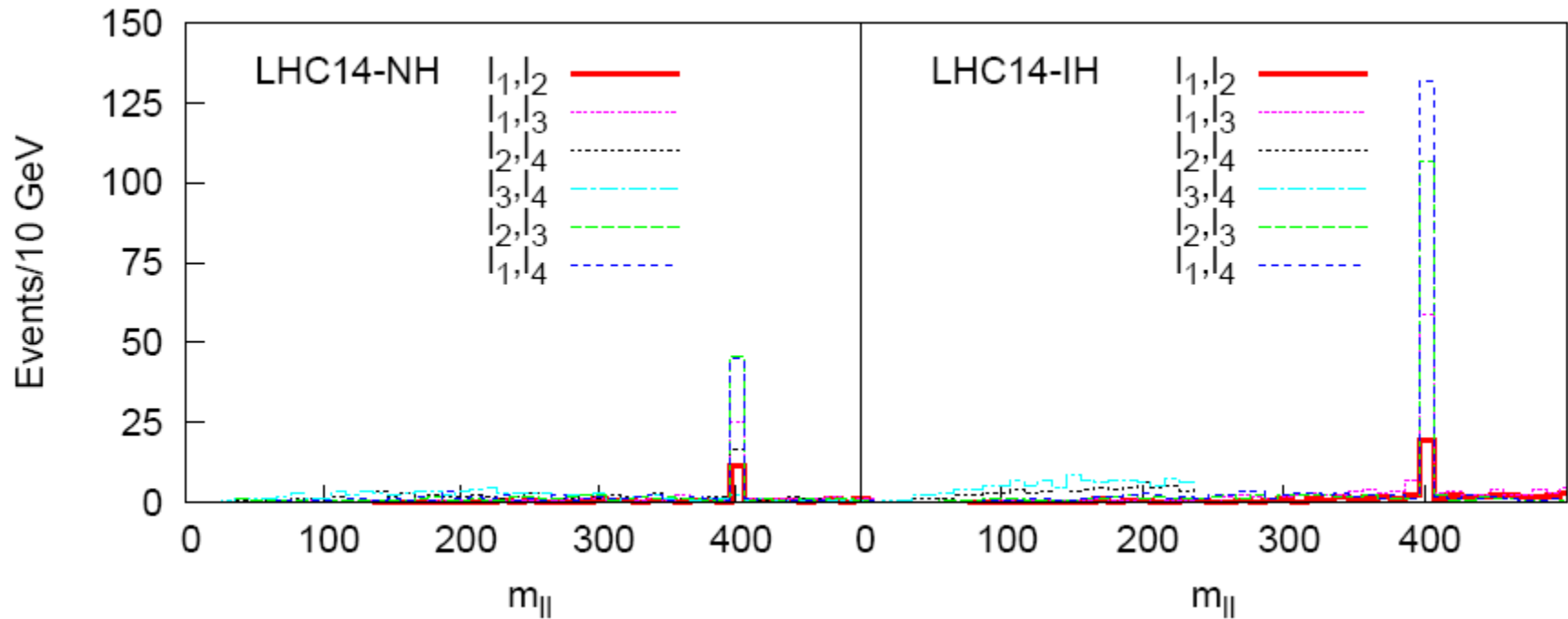
15 fb^{-1}

100 fb^{-1}

	Pre-selection	Selection
$l^\pm l^\pm l^\pm l^\pm$ (LHC8-NH)	4	3
$l^\pm l^\pm l^\pm l^\pm$ (LHC8-IH)	9	8
$l^\pm l^\pm l^\pm l^\pm$ (LHC14-NH)	110	94
$l^\pm l^\pm l^\pm l^\pm$ (LHC14-IH)	240	210



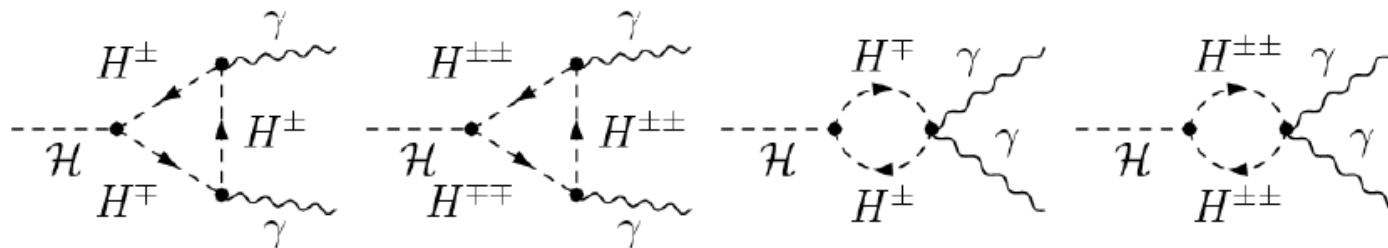
Mass reconstruction



Higgs-to-diphoton

EJC, Lee & Sharma, I209.I303

- ▶ 1-loop process sensitive to New Physics.
- ▶ Its precision data to constrain H^{++} & H^+ contribution.



$$\Gamma(h \rightarrow \gamma\gamma) = \frac{GF\alpha^2 m_h^3}{128\sqrt{2}\pi^3} \left| \sum_f N_c Q_f^2 g_{ff}^h A_{1/2}^h(x_f) + g_{WW}^h A_1^h(x_W) + g_{H^+H^-}^h A_0^h(x_{H^+}) + 4g_{H^{++}H^{--}}^h A_0^h(x_{H^{++}}) \right|^2$$

- $g_{H^+H^+}^h = \frac{\lambda_4}{2} \frac{v_0^2}{M_{H^+}^2},$
- $g_{H^{++}H^{++}}^h = \frac{\lambda_4 - \lambda_5}{2} \frac{v_0^2}{M_{H^{++}}^2},$

Arhrib, et.al., I112.5453
 Kanemura, Yagyu, I201.6287
 Akeryod, Moretti, I206.0535

EWPD

▶ Triplet contribution to S, T & U:

Lavoura, Li, 9309262

$$S = -\frac{1}{3\pi} \ln \frac{m_{+1}^2}{m_{-1}^2} - \frac{2}{\pi} \sum_{T_3=-1}^{+1} (T_3 - Qs_W^2)^2 \xi \left(\frac{m_{T_3}^2}{m_Z^2}, \frac{m_{T_3}^2}{m_Z^2} \right)$$
$$T = \frac{1}{16\pi c_W^2 s_W^2} \sum_{T_3=-1}^{+1} (2 - T_3(T_3 - 1)) \eta \left(\frac{m_{T_3}^2}{m_Z^2}, \frac{m_{T_3-1}^2}{m_Z^2} \right)$$
$$U = \frac{1}{6\pi} \ln \frac{m_0^4}{m_{+1}^2 m_{-1}^2} + \frac{1}{\pi} \sum_{T_3=-1}^{+1} \left[2(T_3 - Qs_W^2)^2 \xi \left(\frac{m_{T_3}^2}{m_Z^2}, \frac{m_{T_3}^2}{m_Z^2} \right) \right. \\ \left. - (2 - T_3(T_3 - 1)) \xi \left(\frac{m_{T_3}^2}{m_W^2}, \frac{m_{T_3}^2}{m_W^2} \right) \right]$$

$m_{+1,0,-1} = M_{H^{++}, H^+, H^0}$

▶ Tree-level contribution is neglected ($\mu \rightarrow 0$).

EWPD

► Most recent STU fit:

Baak, et.al., 1209.2716

$$S_{\text{best fit}} = 0.03, \quad \sigma_S = 0.10$$

$$T_{\text{best fit}} = 0.05, \quad \sigma_T = 0.12$$

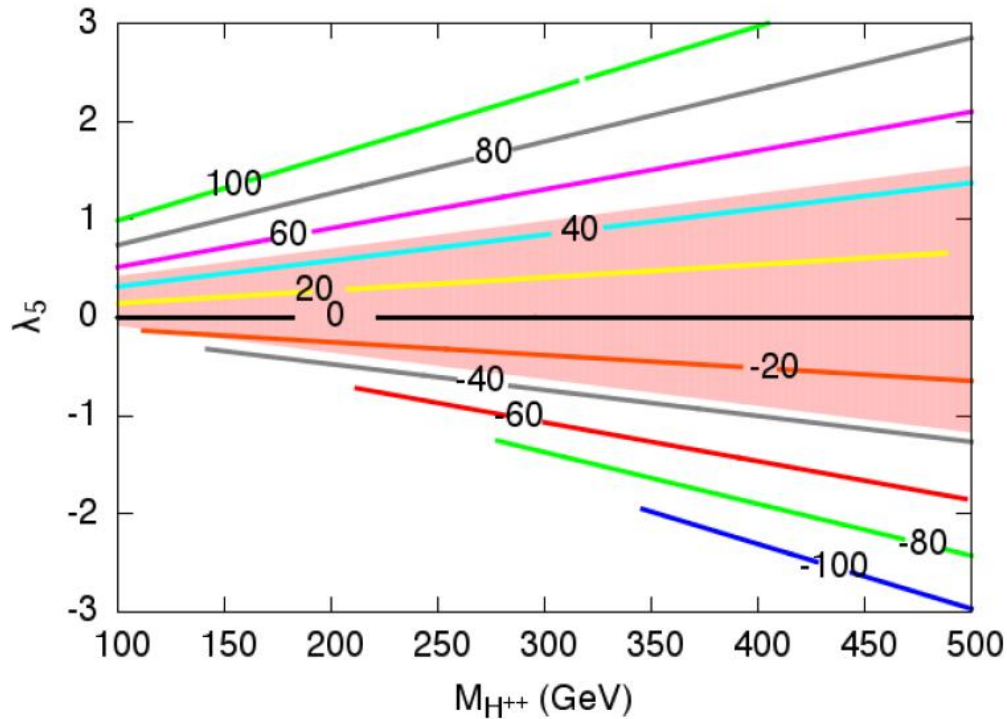
$$U_{\text{best fit}} = 0.03, \quad \sigma_U = 0.10$$

$$\rho_{ST} = 0.89, \quad \rho_{SU} = -0.54, \quad \rho_{TU} = -0.83$$

► It strongly constrains the mass splitting.

$$\begin{pmatrix} \Delta S \\ \Delta T \\ \Delta U \end{pmatrix}^T \begin{pmatrix} \sigma_S \sigma_S & \sigma_S \sigma_T \rho_{ST} & \sigma_S \sigma_U \rho_{SU} \\ \sigma_S \sigma_T \rho_{ST} & \sigma_T \sigma_T & \sigma_T \sigma_U \rho_{TU} \\ \sigma_U \sigma_S \rho_{US} & \sigma_U \sigma_T \rho_{TU} & \sigma_U \sigma_U \end{pmatrix}^{-1} \begin{pmatrix} \Delta S \\ \Delta T \\ \Delta U \end{pmatrix} < -2 \ln(1 - CL)$$

EWPD

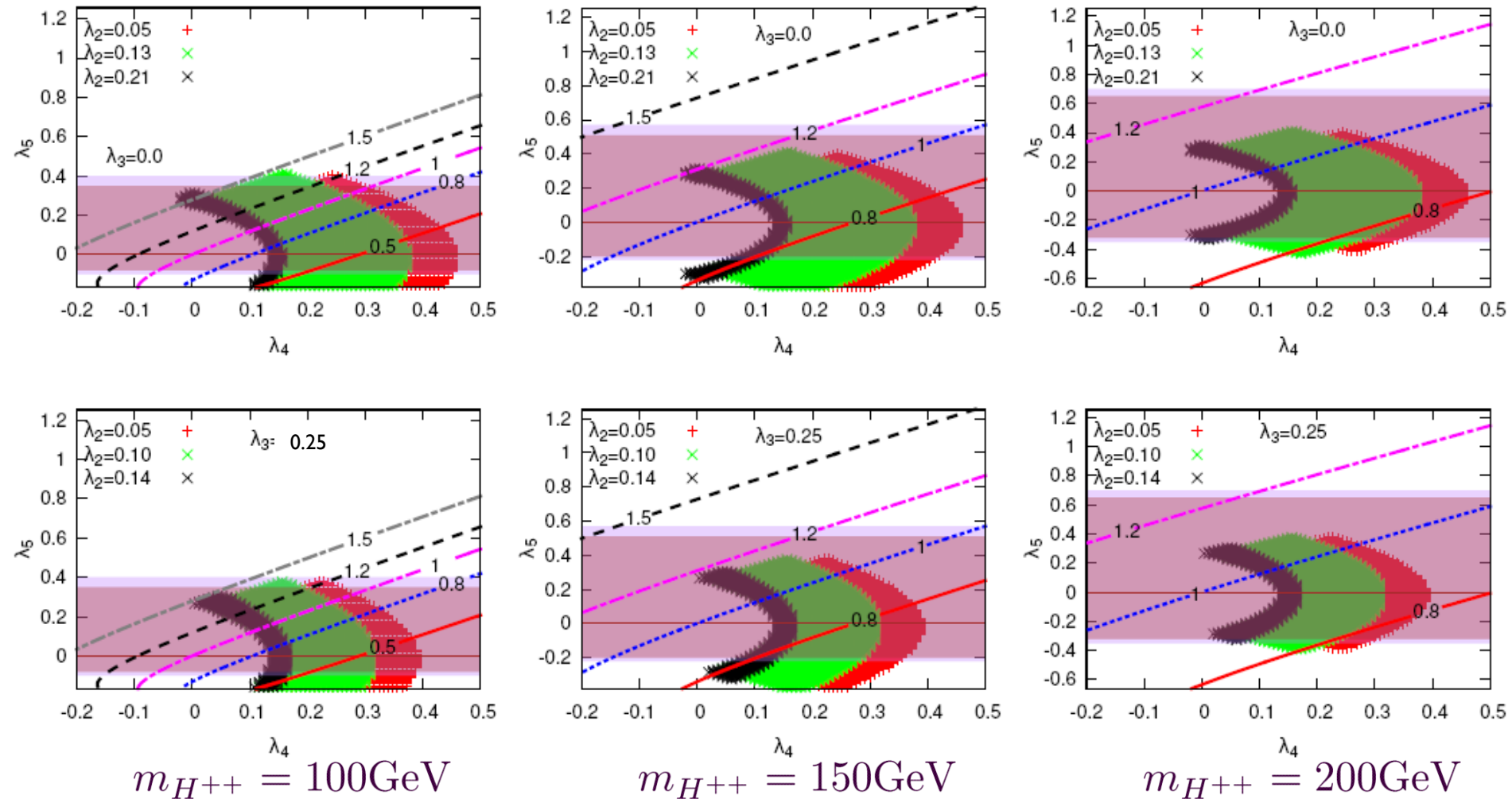


$$|\Delta M| < 40 \text{ GeV}$$

$$\lambda_5 = (-0.1, 0.4), \quad (-0.2, 0.6), \quad (-0.35, 0.7)$$

$$M_{H^{++}} = 100, 150, \text{ and } 200 \text{ GeV,}$$

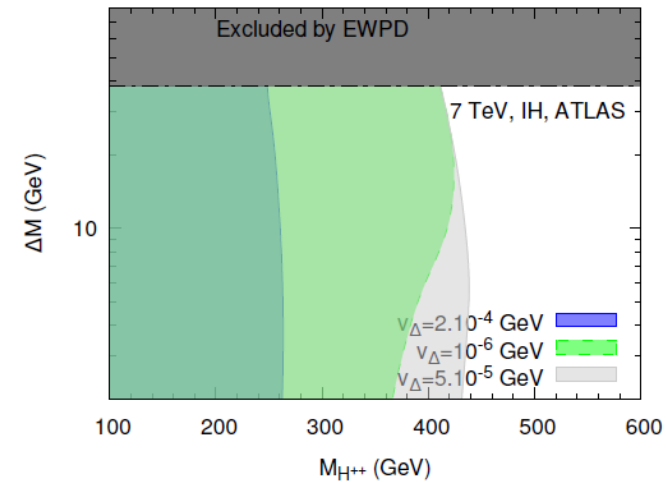
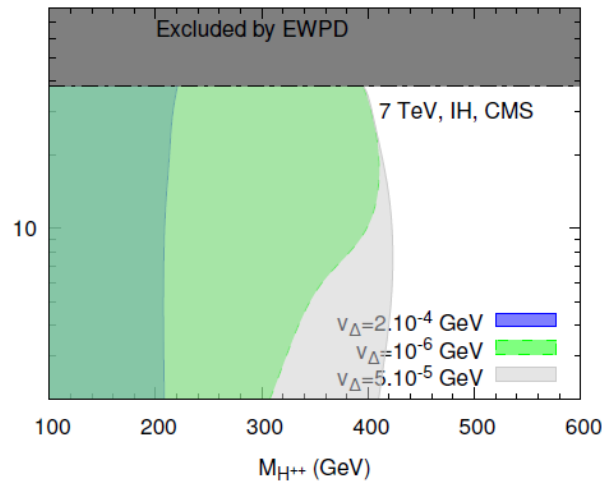
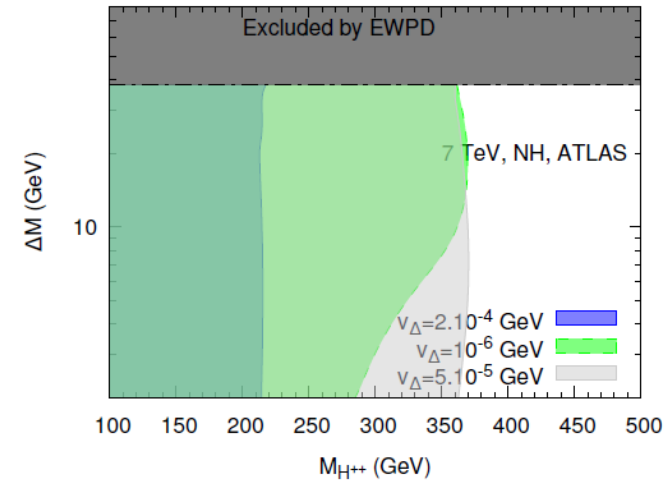
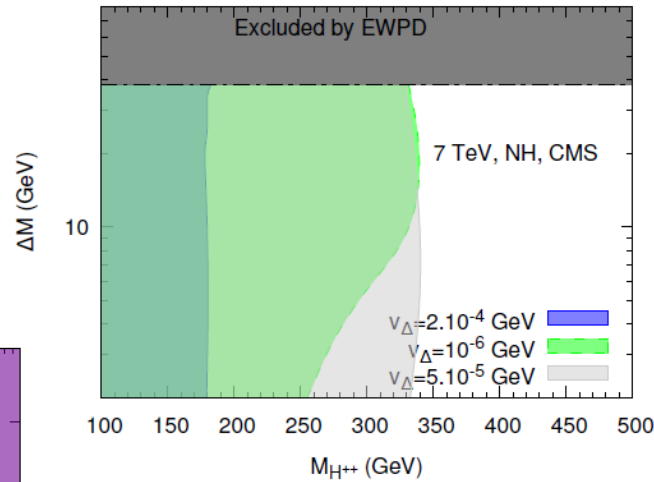
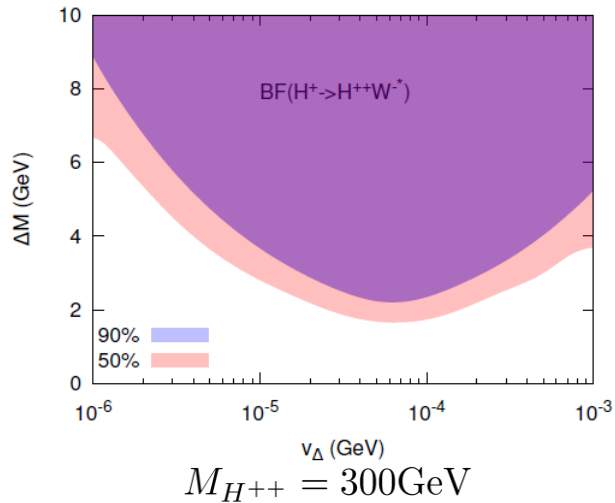
Combined results for 10^{19} GeV



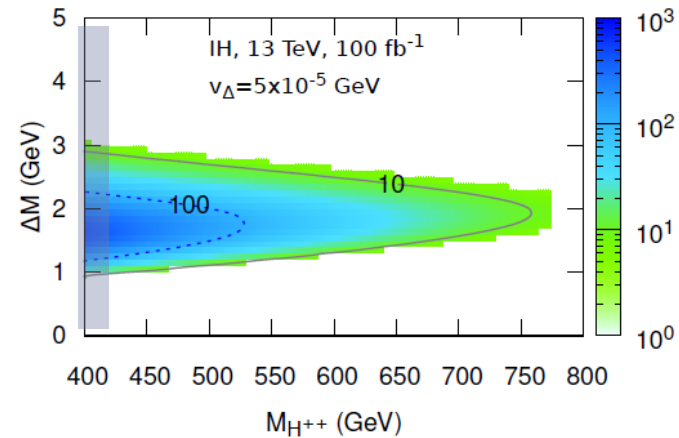
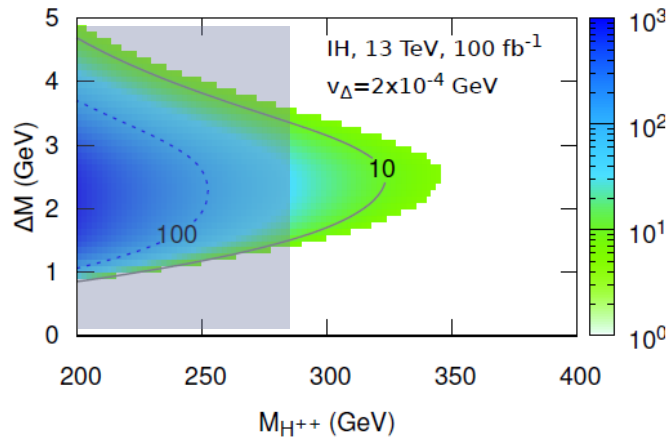
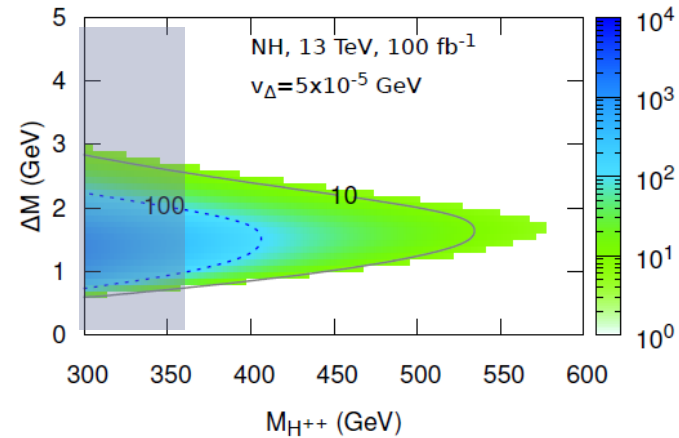
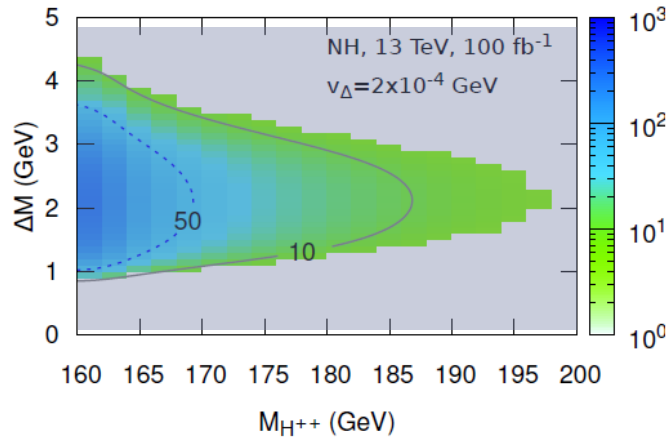
General $v_\Delta - \Delta M$ study

Melfo, et.al., I108.4416

EJC & Sharma, I309.6888



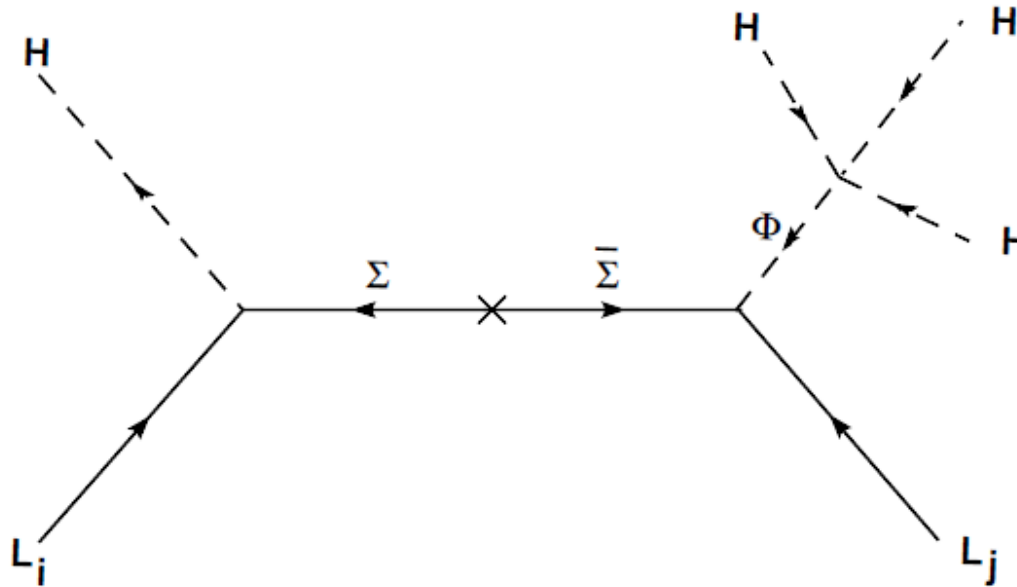
SS4L at LHC13



UV theories of $D > 5$ operators?

- ▶ 4-plet Model: $(\Phi^{+++}, \Phi^{++}, \Phi^+, \Phi^0)$.
- ▶ $\Phi^{+++} \rightarrow l^+ l^+ W^+, W^+ W^+ W^+$

Babu, et.al., 0905.2710
 Bambhaniya, et.al., 1305.2795



Q) SS5L study?

Conclusion

- ▶ Great achievements from oscillation observation during past 15 years.
- ▶ Further Quest for the nature of neutrino mass: Dirac/Majorana, absolute scale, hierarchy & CPV.
- ▶ Neutrino-DM/BAU connection: leptogenesis+ADM.
- ▶ Majorana mass models at TeV scale?
- ▶ LHC signatures of type I, II, III seesaws: SS2L, displacement, associated Higgs production.
- ▶ LHC13/14 continues to probe the neutrino signals.
- ▶ More for peculiar type II: SS2L resonance, SS4L, Higgs-to-diphoton.

Thank you