

# Intracellular Transport & Collective Force Generation by Motor Proteins

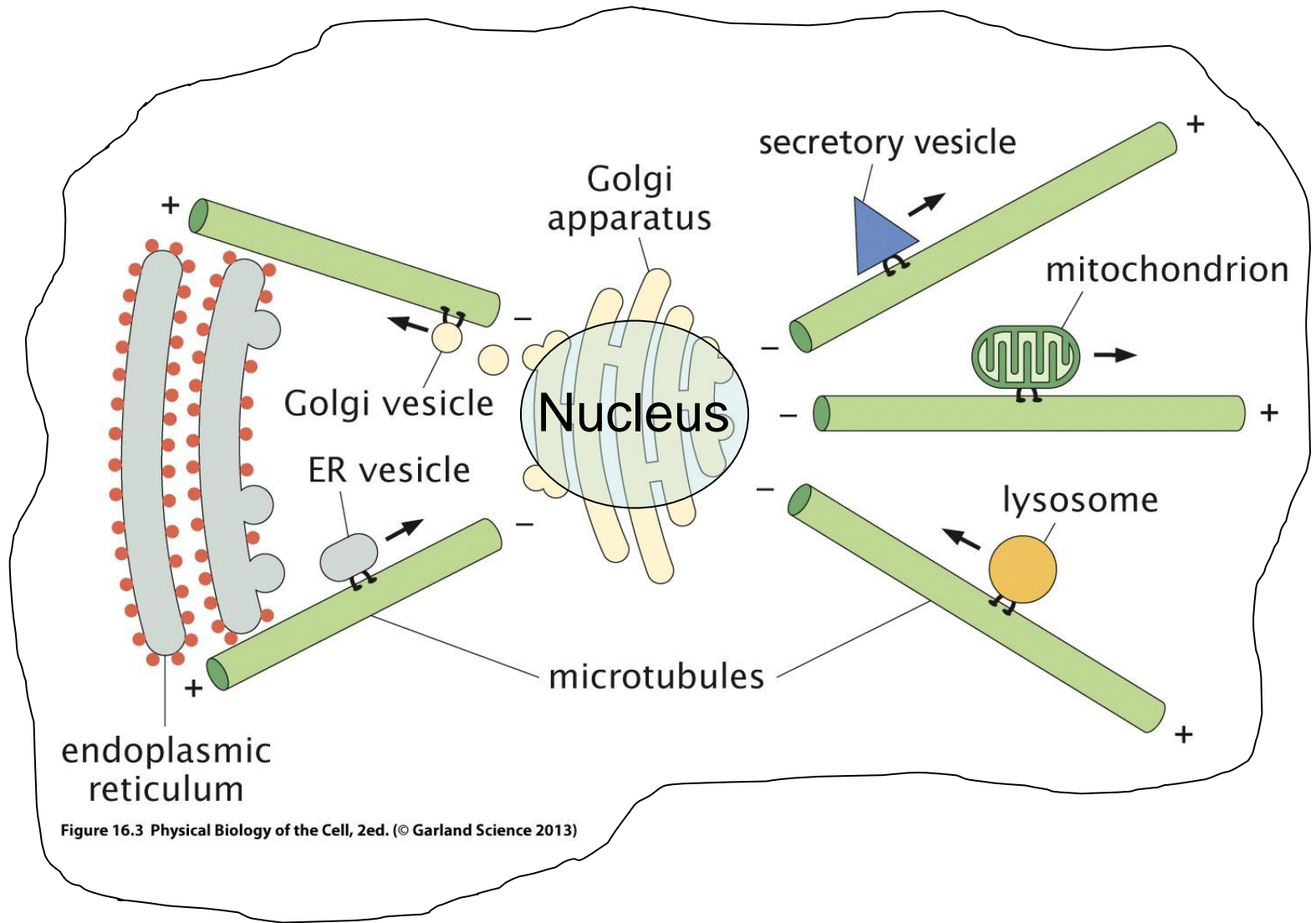
Roop Mallik

Department of Biological Sciences  
TIFR Mumbai

I. Background

II. Single Motors

III. Collections of Motors

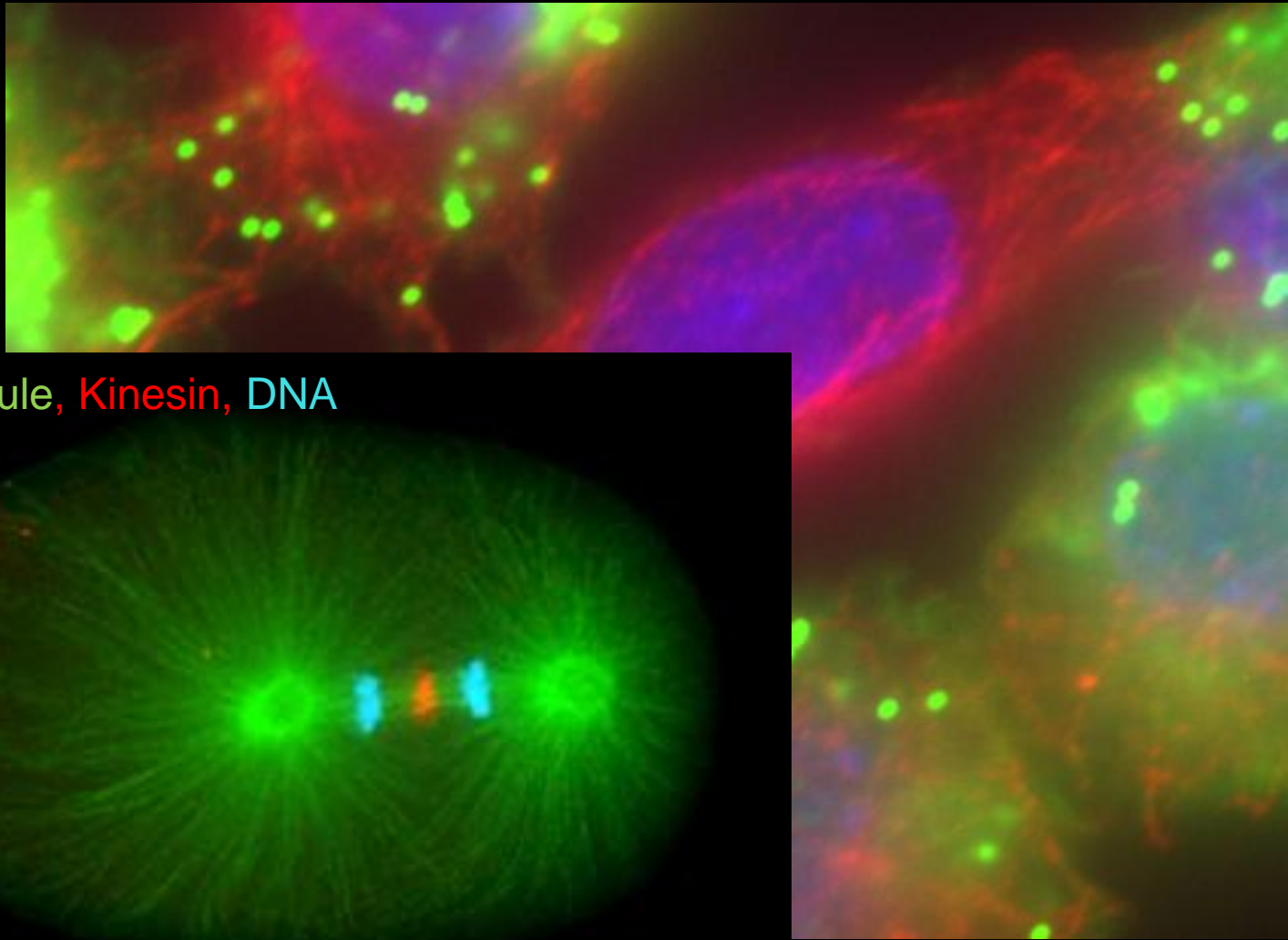


Pigment granules, Chromosomes, Bacteria, Virus, .....

Microtubules

Nucleus

Cargo



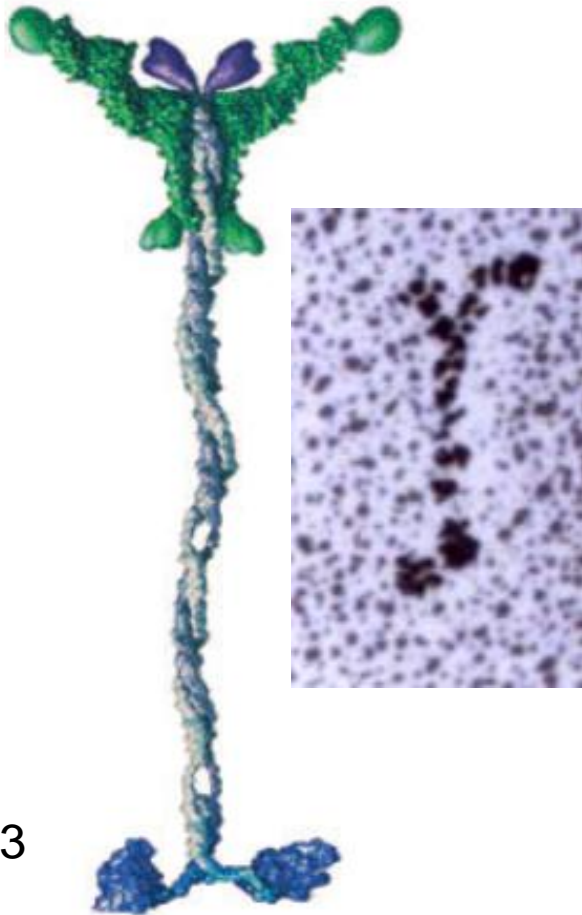
Microtubule, Kinesin, DNA



5 microns

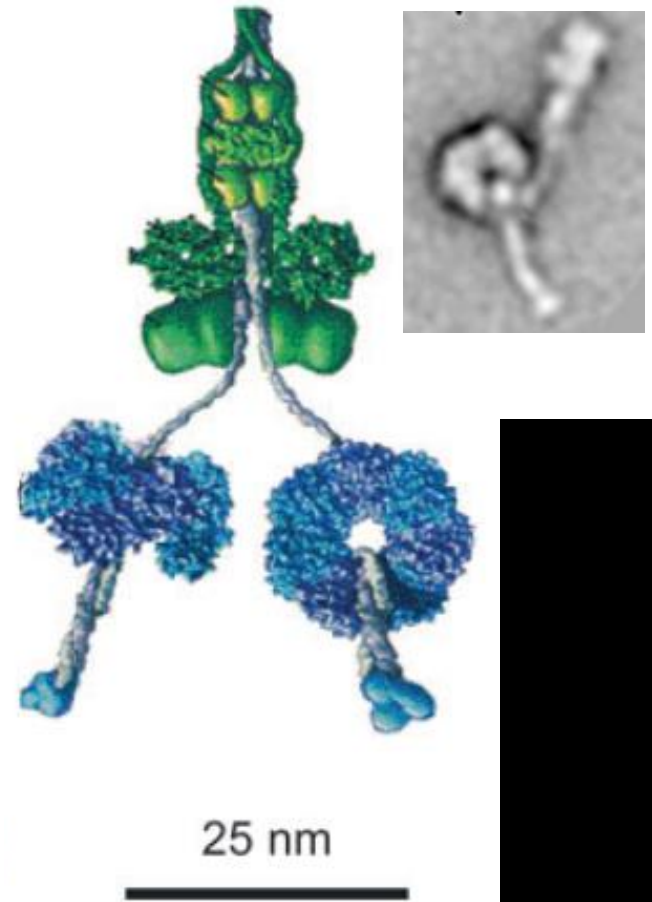
C. Elegans mitotic division, Canman Lab, Columbia

# Kinesin



Vale 2003

# Dynein



## Typical numbers

Dimension of cells  $\rightarrow$  10 Microns

Size of a Motor  $\rightarrow$  50-100 nm

Cargoes carried by Motors  $\rightarrow$  50nm – Few microns

Velocity of motion  $\rightarrow$  1-2 microns/sec

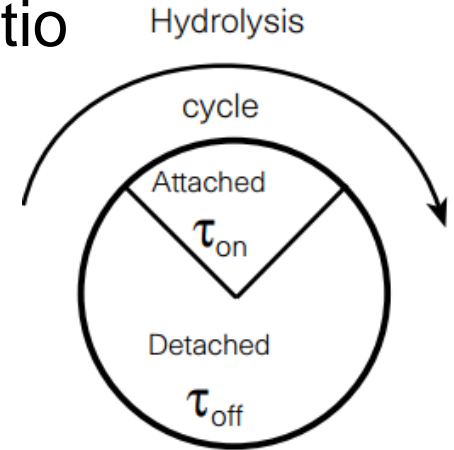
100 cycles completed in 1 second

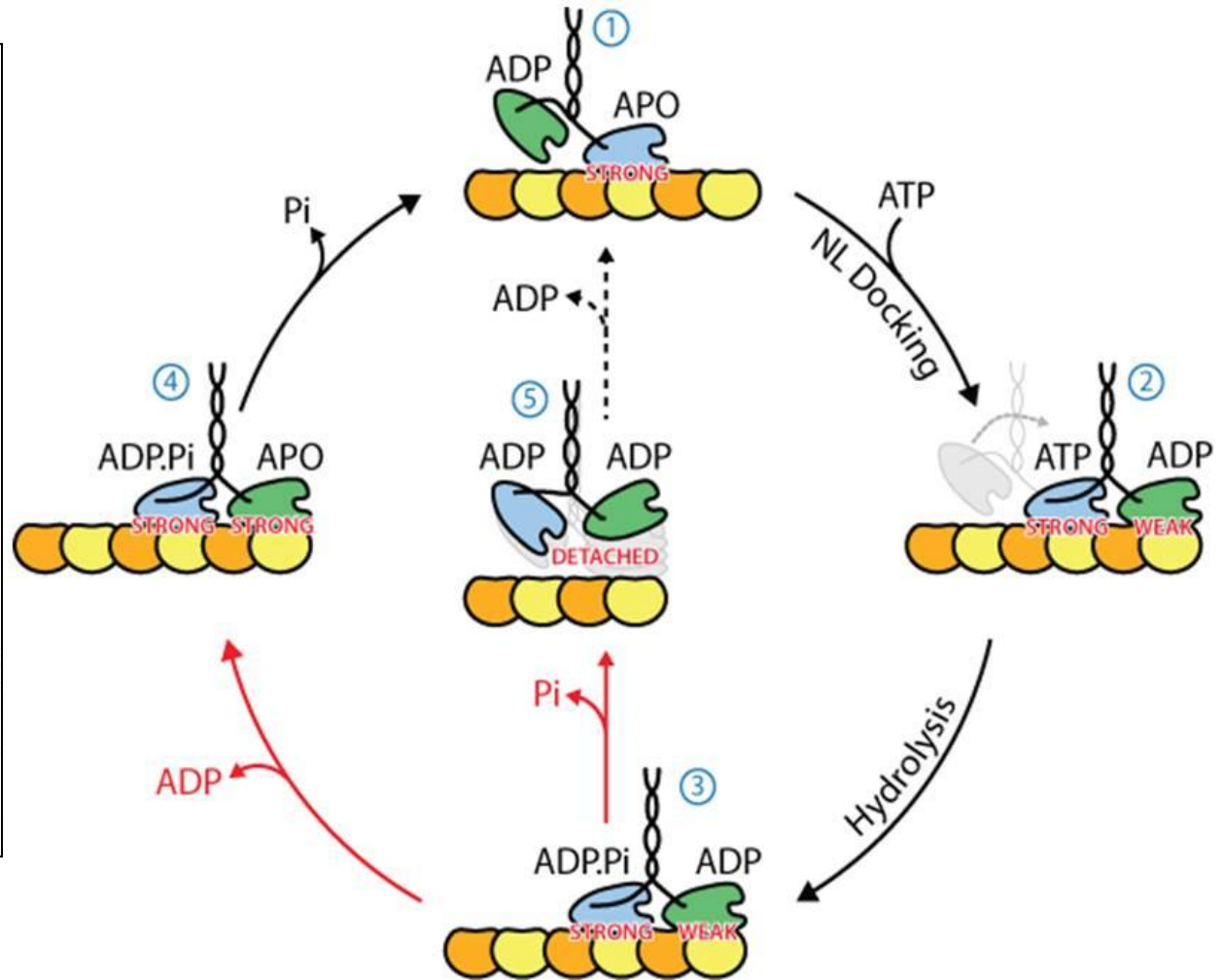
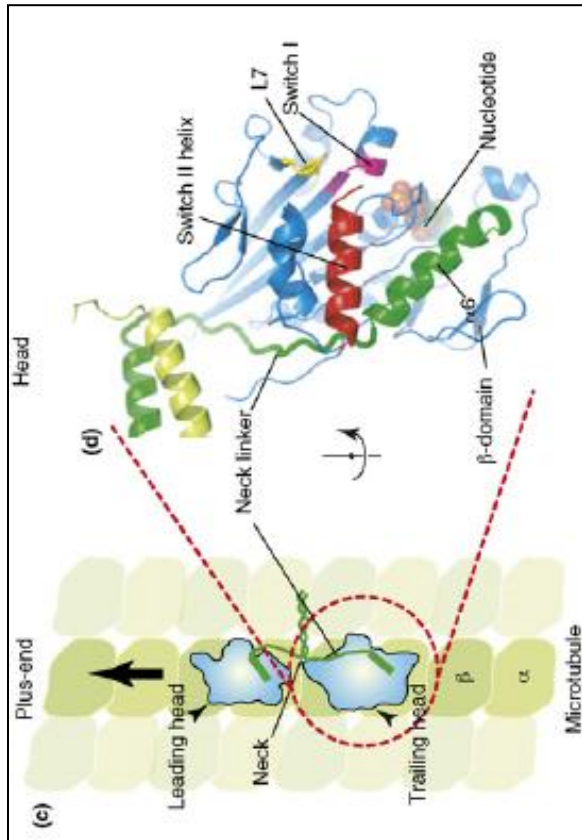
Energy available from 1 ATP =  $25 K_b T = 100$  pN-nm

Work done per cycle  $\sim$  50 pN-nm

Diffusion constant for 50nm object  $\sim$  1 micron<sup>2</sup>/sec

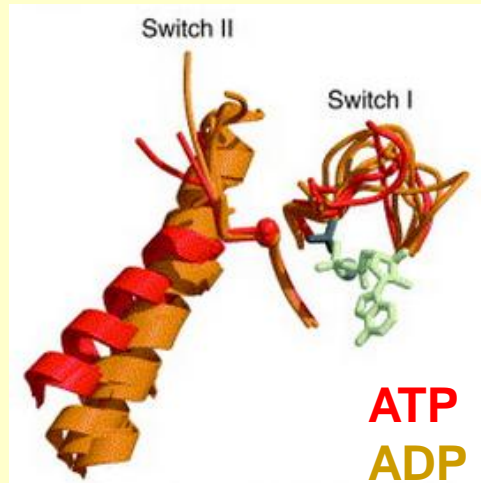
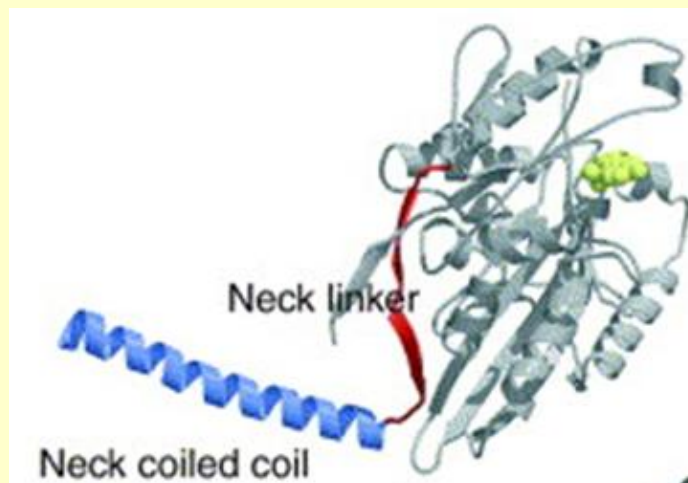
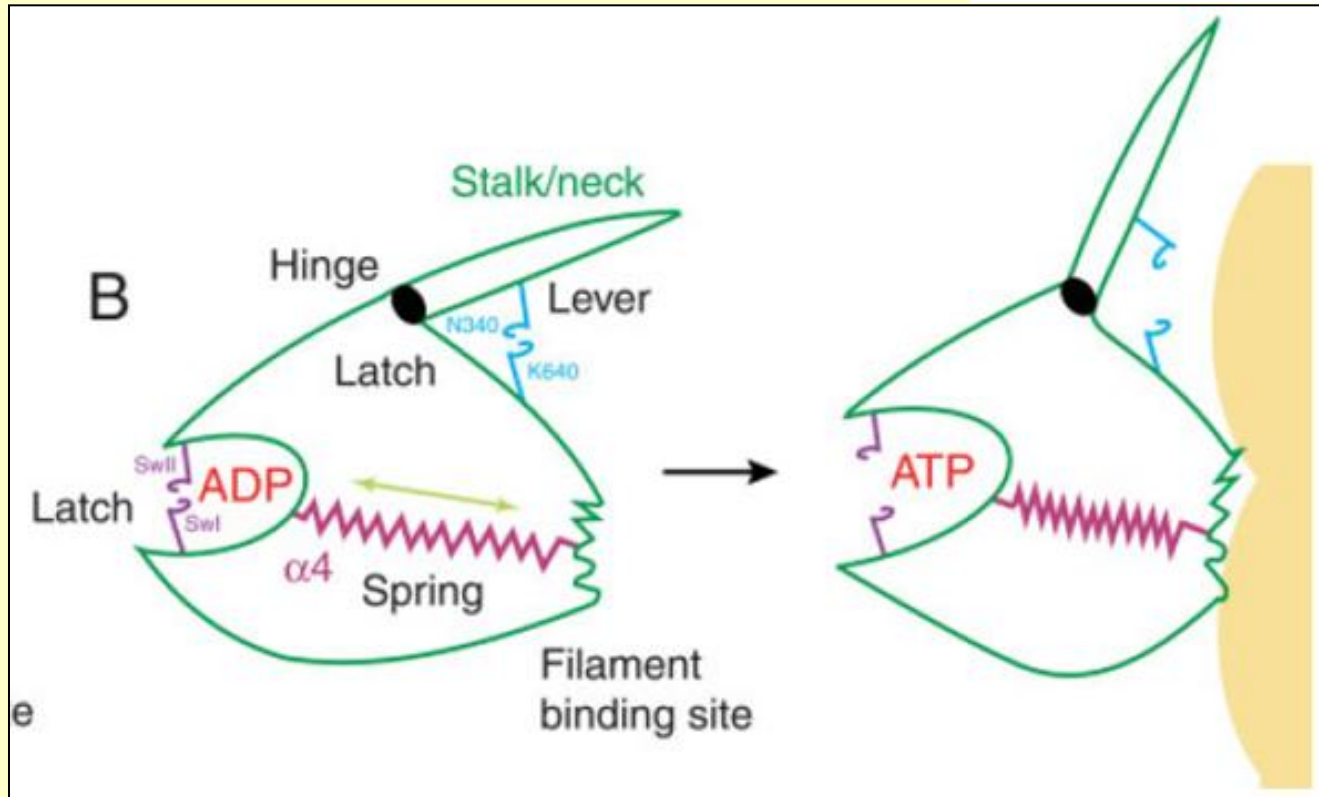
Duty Ratio



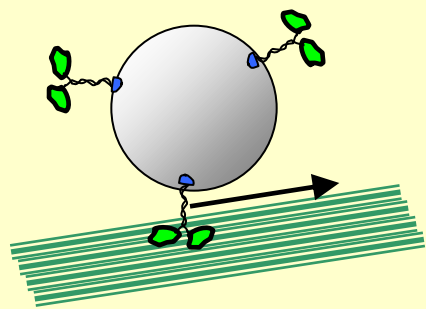


Weakly bound  
Strongly bound

ADP  
ATP, ADP-Pi and Nucleotide free (Apo)



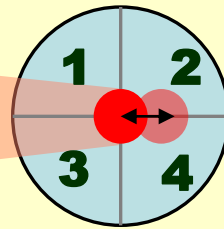
# I. Studying Single Motors ...



Kinesin



5 microns

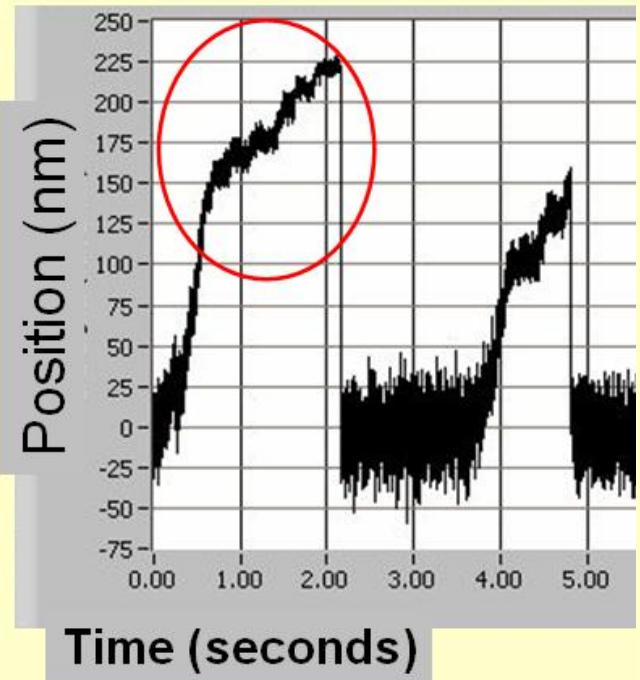


$F_{\text{Trap}}$

$F_{\text{motor}}$



Objective





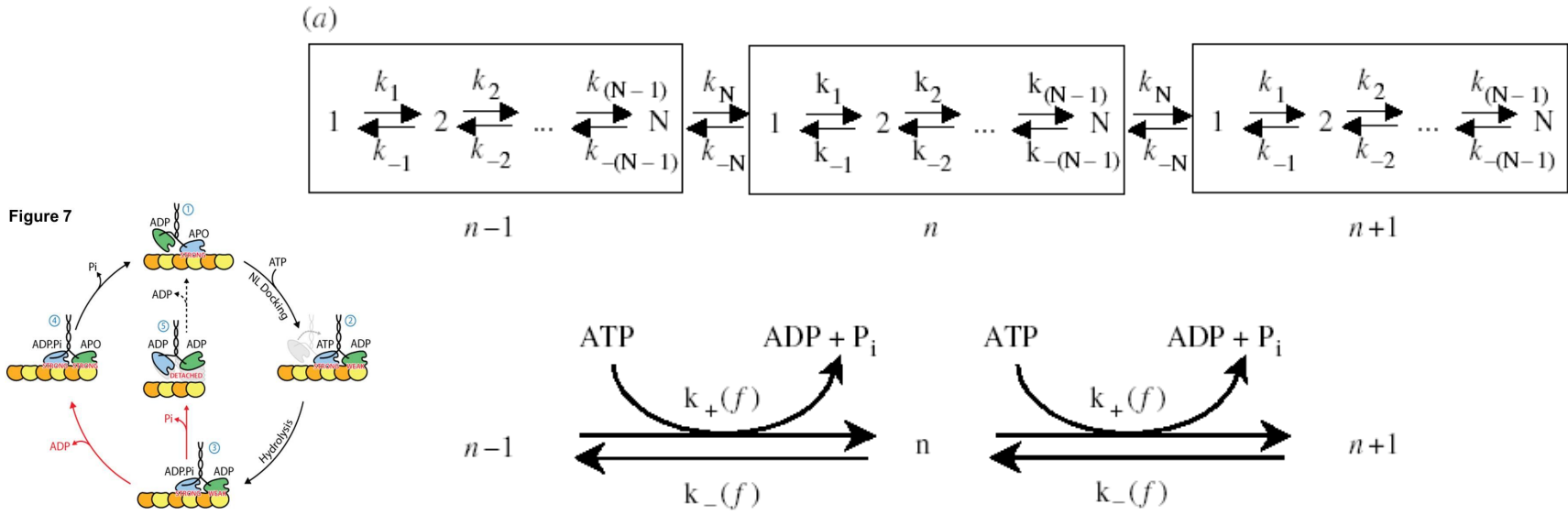


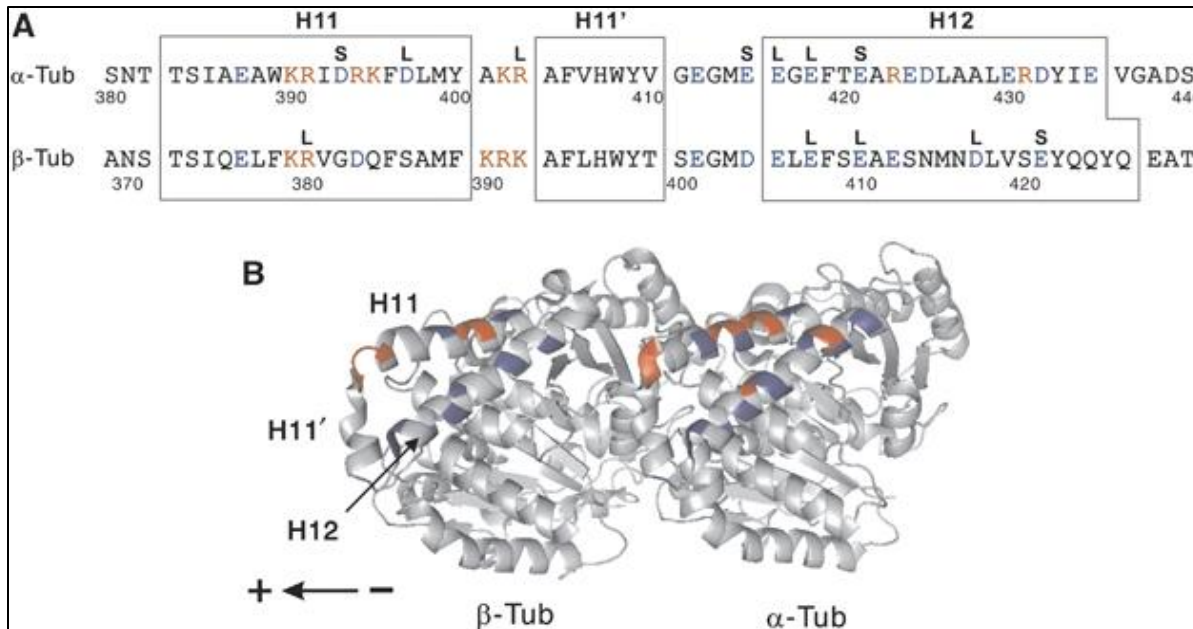
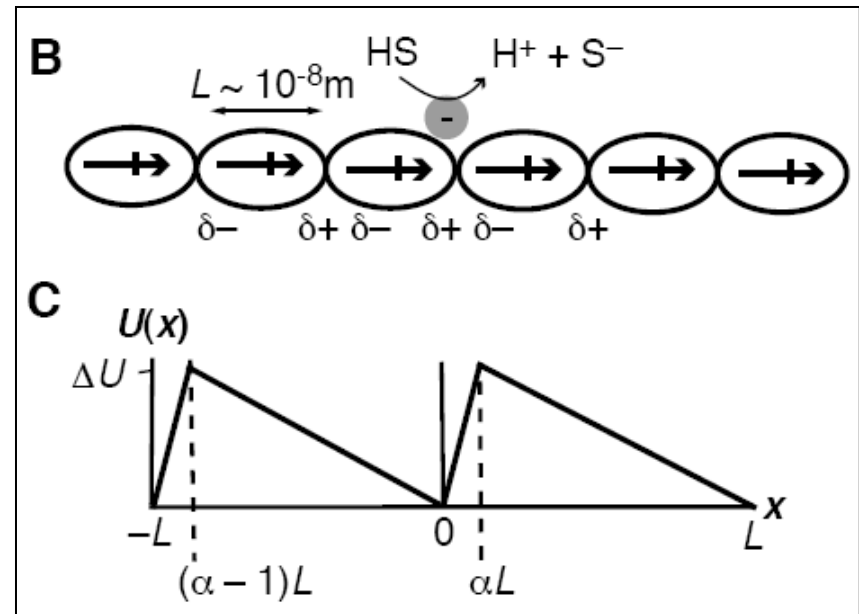
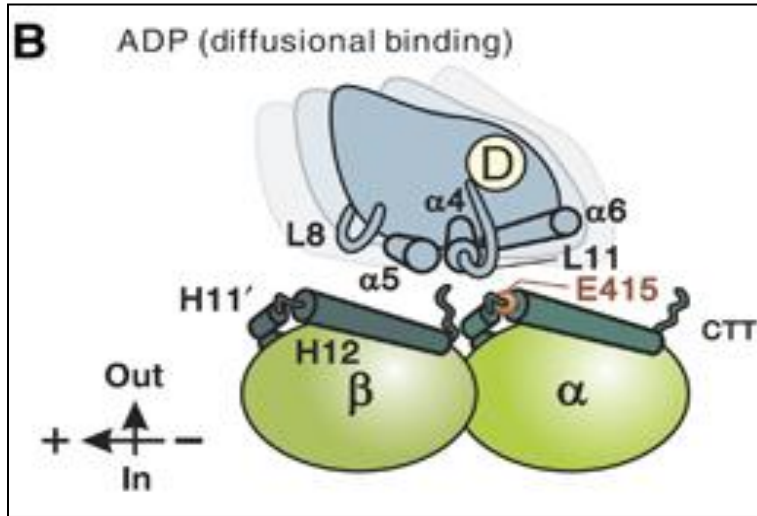
Figure 2. Kinetic schemes for a tightly coupled motor that hydrolyses one molecule of ATP in moving forwards from site  $n$  to  $n + 1$  while pulling against a constant load  $f$ . (a) A general  $N$ -state motor. (b) An idealized one-state motor.

$$Keq = \frac{[k_1(f)k_2(f)k_3(f), \dots, k_N(f)]}{[k_{-1}(f)k_{-2}(f)k_{-3}(f), \dots, k_{-N}(f)]} = A \exp(-\Delta G/kT). \quad (3.5)$$

Equation of motion (overdamped)

$$0 = -\gamma \frac{dx}{dt} - \frac{dV_\mu(x)}{dx} + F_{ext} + \xi(t),$$

Uchimura et al, 2010



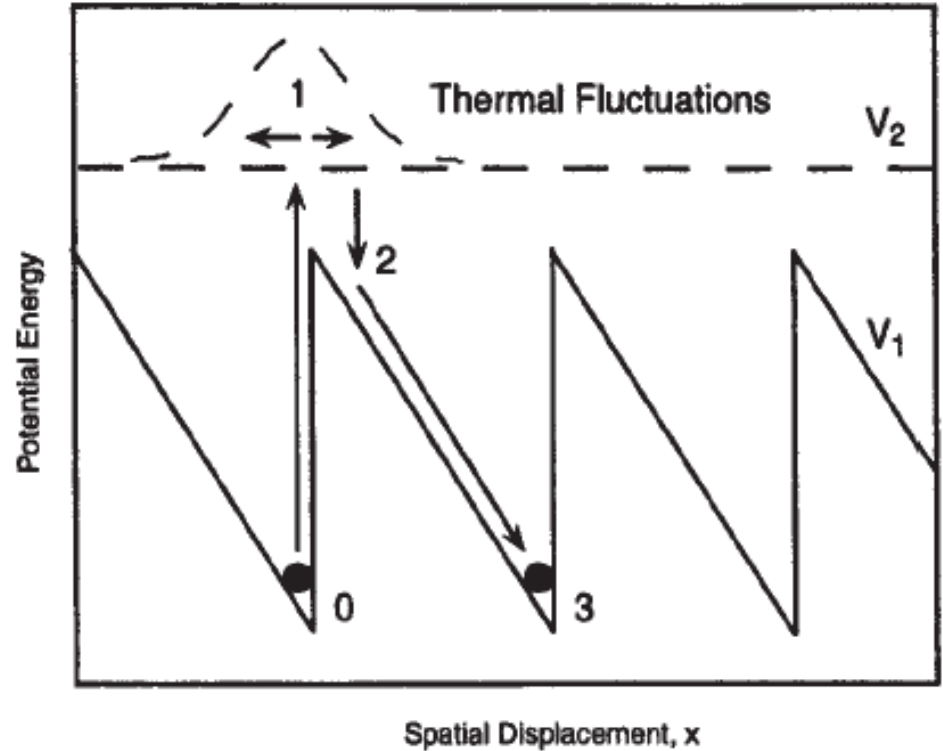
(B) Dipoles within units of a protein polymer  
(C) Anisotropic sawtooth potential

# Continuum Ratchets

Ajdari, A. and Prost, J. (1992)

## Flashing Ratchet..

Fig. 4. The mechanism of transport in a flashing ratchet. In the flat potential,  $V_2(x)$ , the probability distribution of the position of the particle is a Gaussian function with its mean located near a minimum of the asymmetric potential. Once the asymmetric potential is switched on,  $V_1(x)$ , half of the area of the Gaussian distribution is located on the slope leading to the right neighboring local minimum, and the other half is on the slope leading to the same local minimum at which the particle was located in the previous step. The movement of the particle is biased to the right.



Chowdhury, 2008

Chemical state evolves following the Discrete master equation

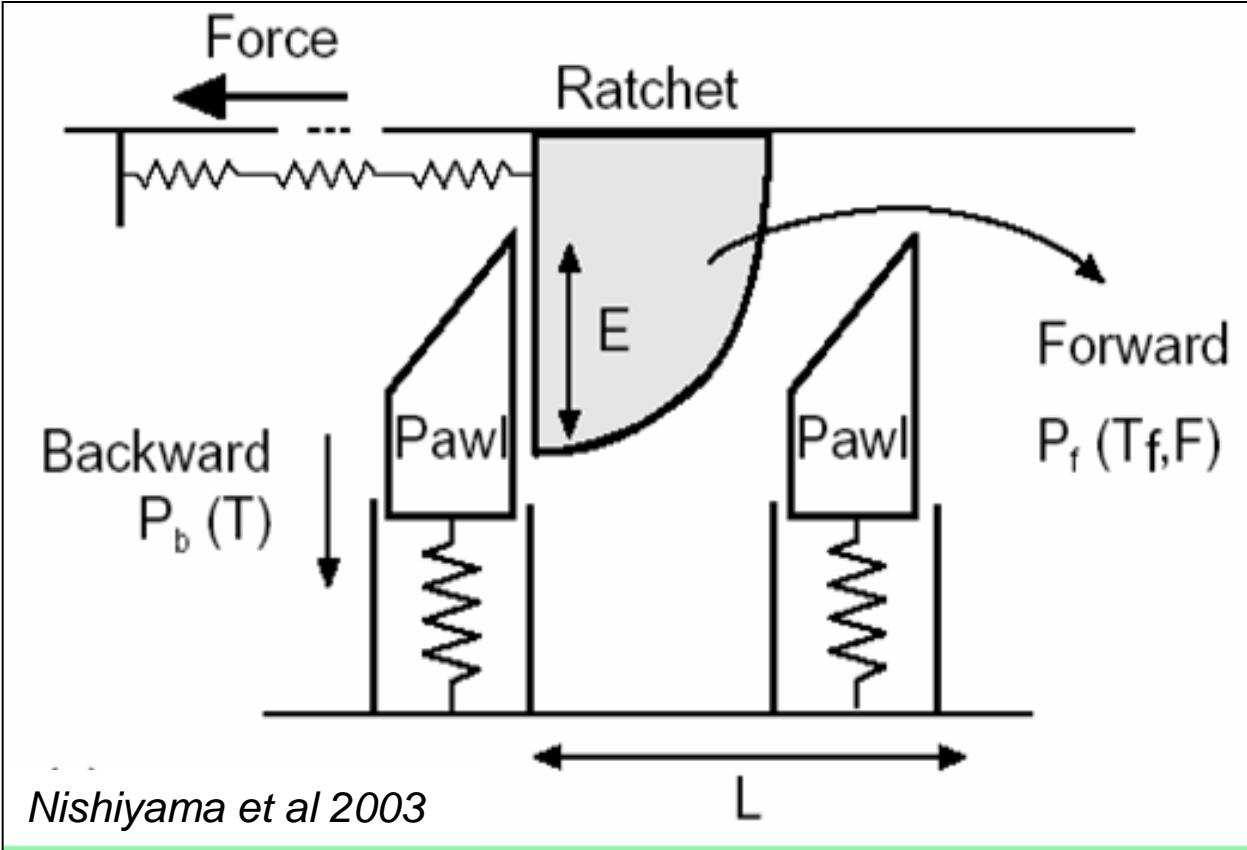
$$\frac{\partial P_{\mu}(x,t)}{\partial t} = \sum_{\mu'} P_{\mu'}(x,t) W_{\mu' \rightarrow \mu}(x) - \sum_{\mu'} P_{\mu}(x,t) W_{\mu \rightarrow \mu'}(x)$$

# Fokker Planck equation for motion

$$\frac{\partial P_\mu(x,t)}{\partial t} = \underbrace{\frac{1}{\eta} \frac{\partial}{\partial x} \left[ \left\{ V'_\mu(x) - F \right\} P_\mu(x,t) \right]}_{\text{Hydrodynamics}} + \underbrace{\left( \frac{k_B T}{\eta} \right) \frac{\partial^2 P_\mu(x,t)}{\partial x^2}}_{\text{Hydrodynamics}} + \sum_{\mu'} P_{\mu'}(x,t) W_{\mu' \rightarrow \mu}(x) - \sum_{\mu'} P_\mu(x,t) W_{\mu \rightarrow \mu'}(x).$$

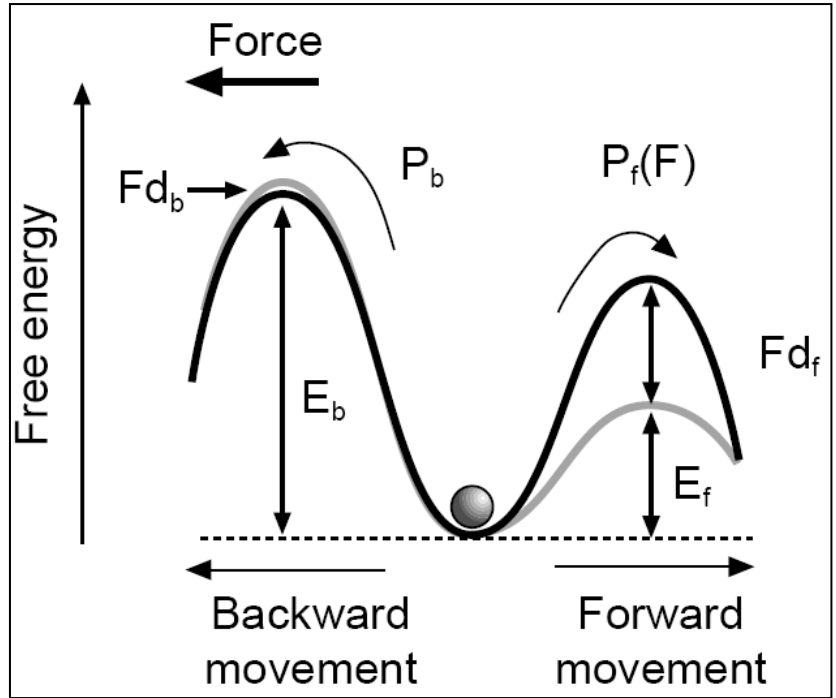
Hydrodynamics

Discrete Chemical transitions (Markov)



Nishiyama et al 2003

Nishiyama et al, 2003

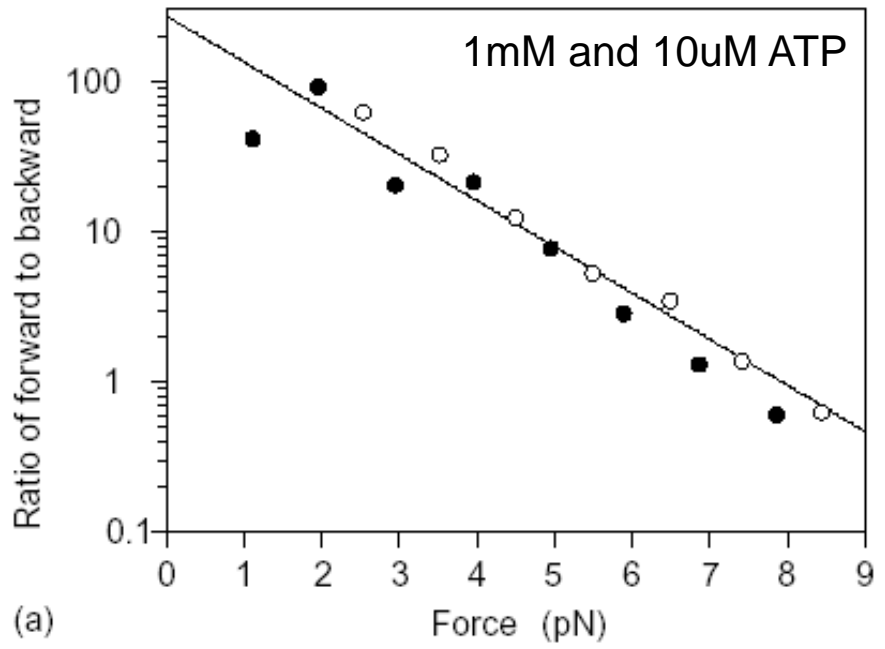


$$\frac{k_{3f}}{k_{3b}} = \exp\left[\frac{E_b - E_f}{k_B T}\right] \exp\left(-\frac{Fd}{k_B T}\right)$$

$$d (=d_f - d_b)$$

Number of movements in the forward direction relative to those in the backward direction

→ Can be obtained from exp data (a)



Our results show that the energy difference between the barrier heights in the forward and backward directions was  $5.4k_B T$  ( $T = 298$  K) at zero load, which is about one fourth of the free energy of the ATP hydrolysis ( $\sim 20k_B T$ ).

# II Collections of Motors -- Forces in the Cell

Molecular Forces

1-10 pN

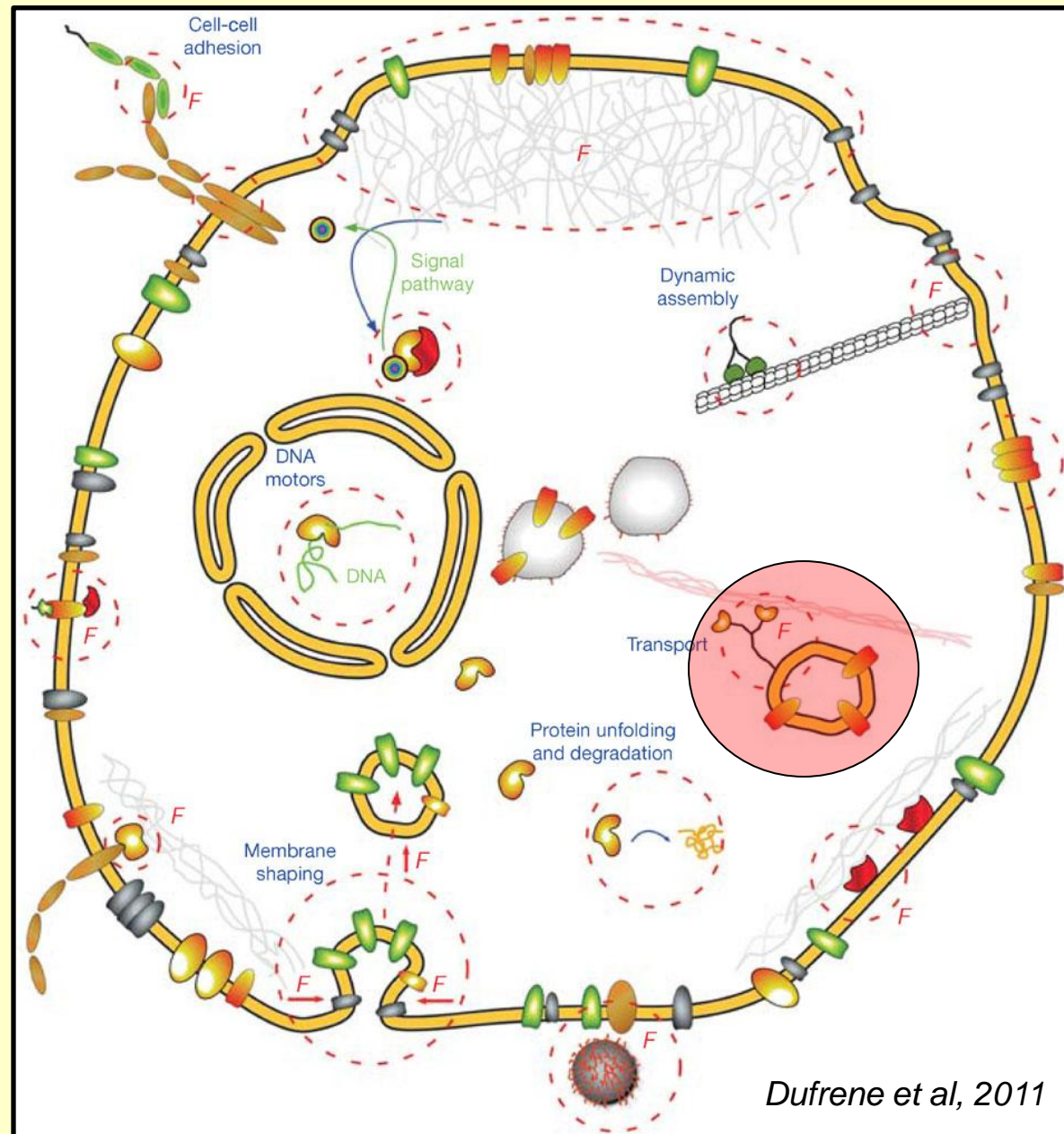
Cellular Forces

10 -1000 pN

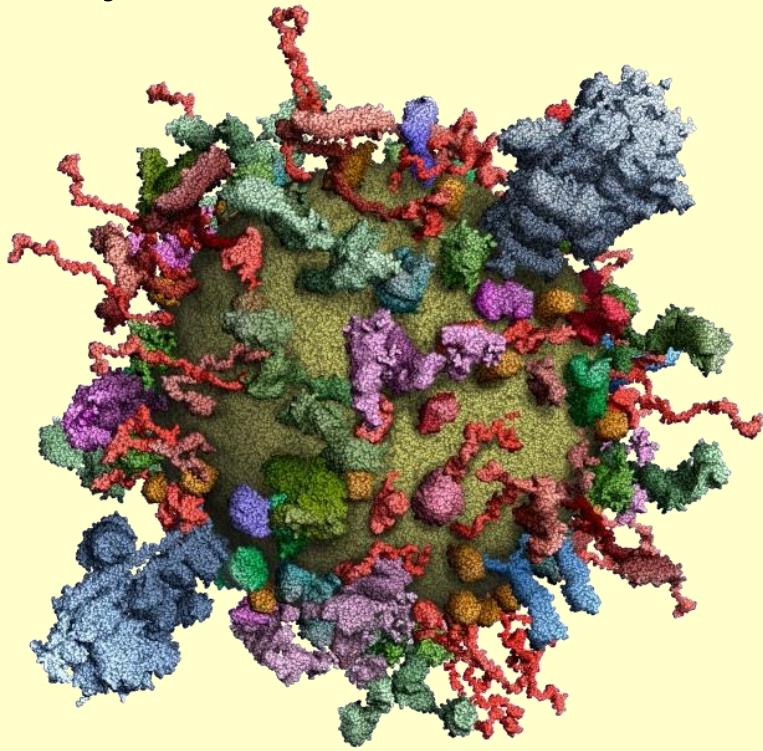
Heterogeneous, Difficult to measure

Contribution of individual molecules?

Reduced complexity:  
Look at Single cargoes in the cell



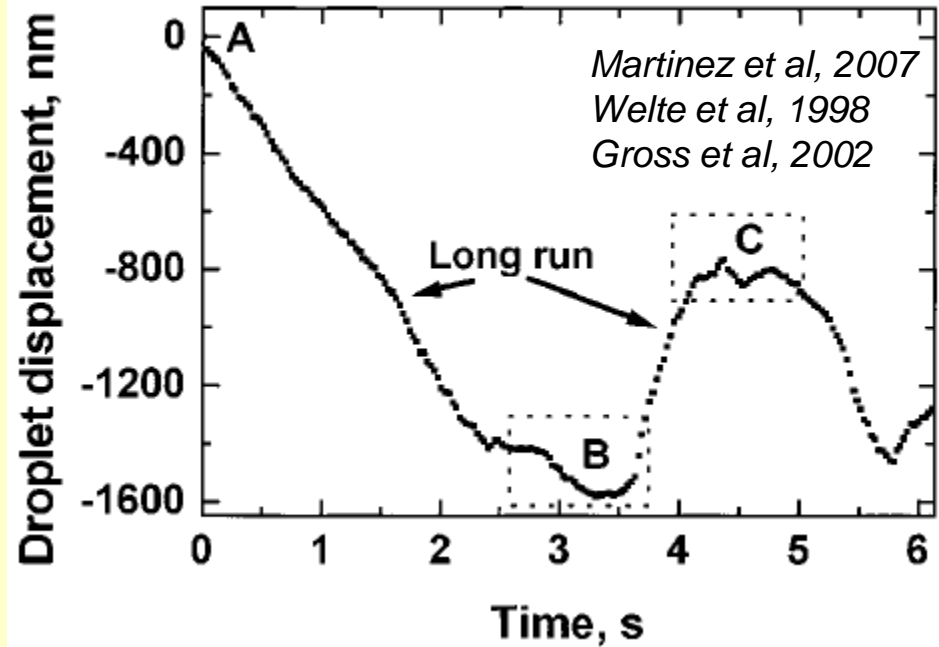
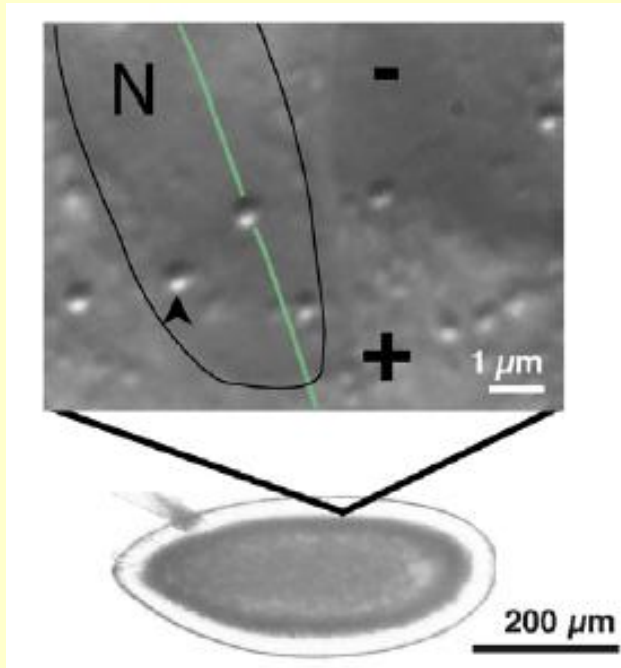
Reality ...



[www.biotechnologie.de](http://www.biotechnologie.de)



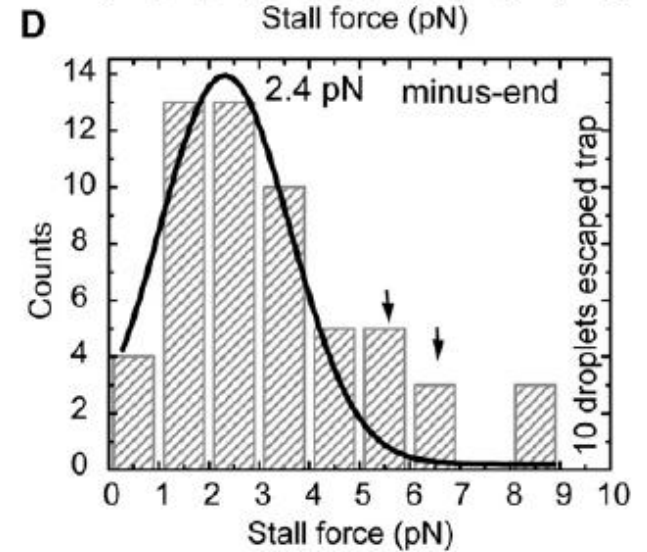
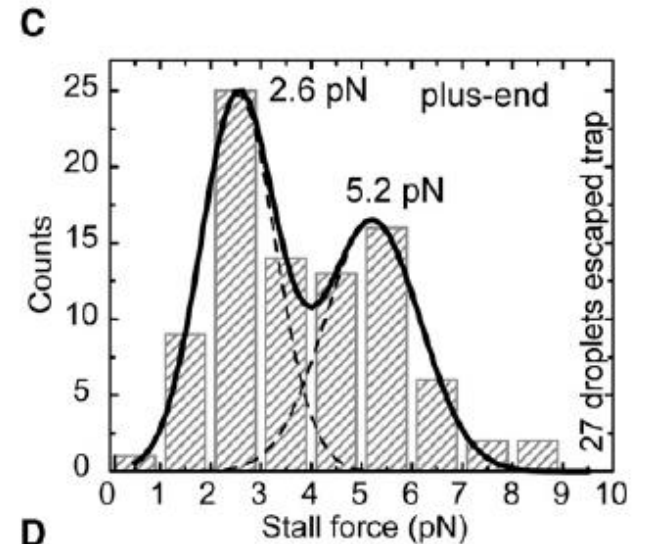
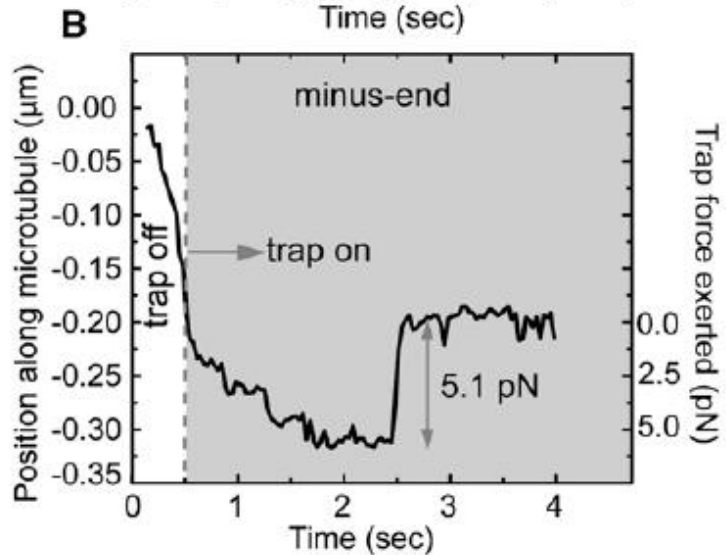
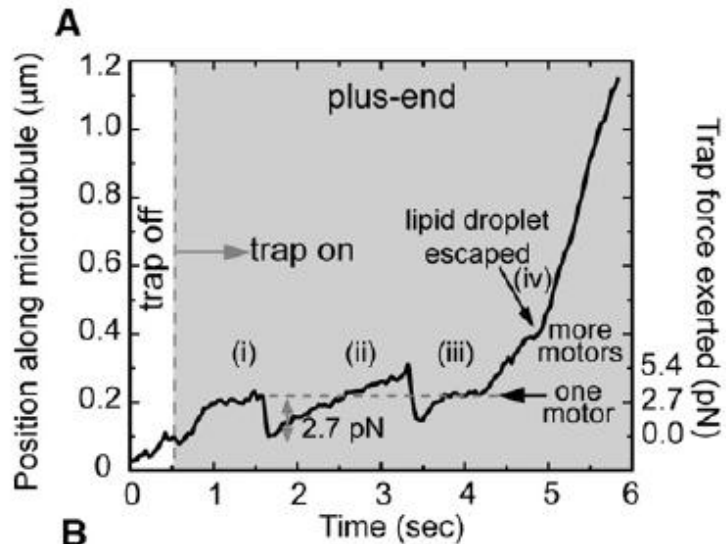
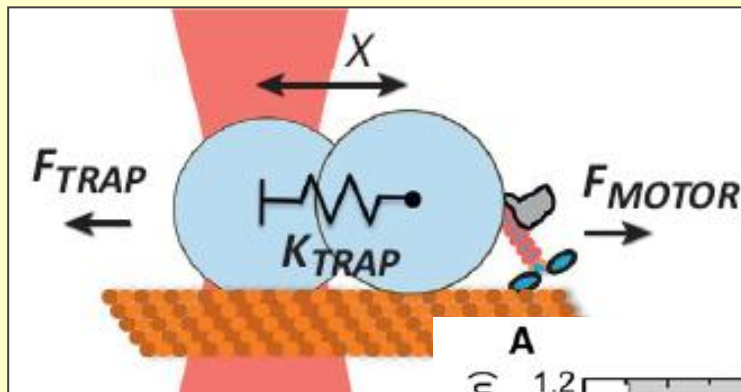
# Motion of Lipid droplets in *Drosophila* embryos



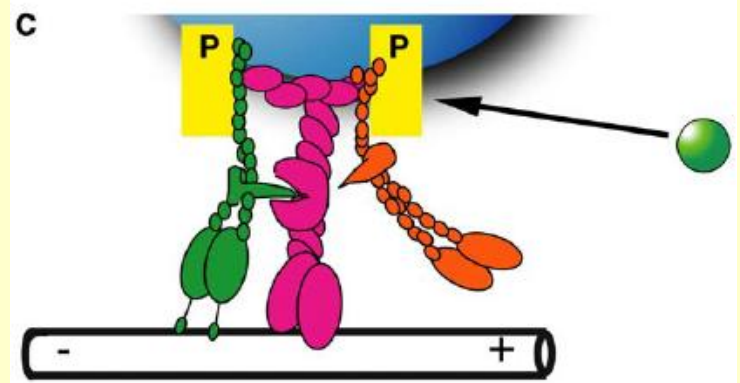
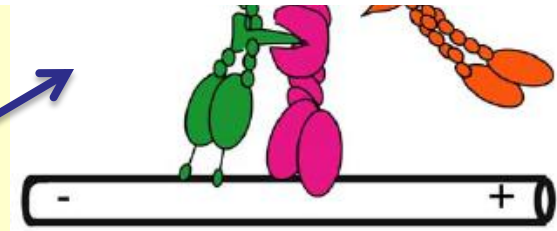
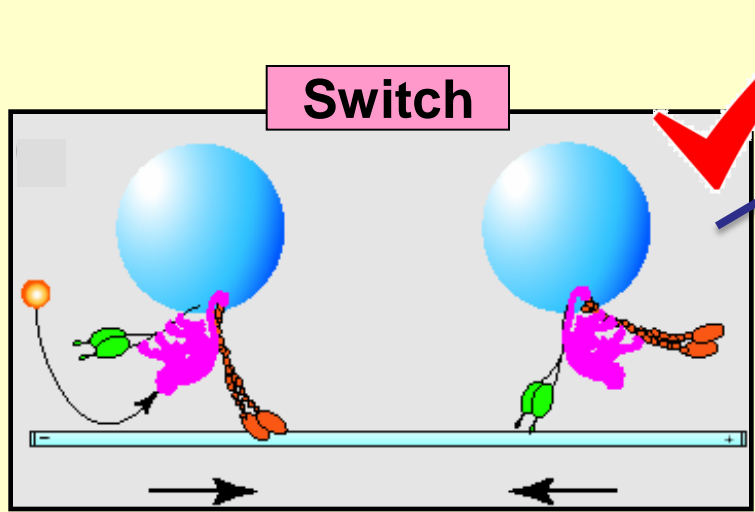


# Force measurements in embryos

Shubeita et al, 2008



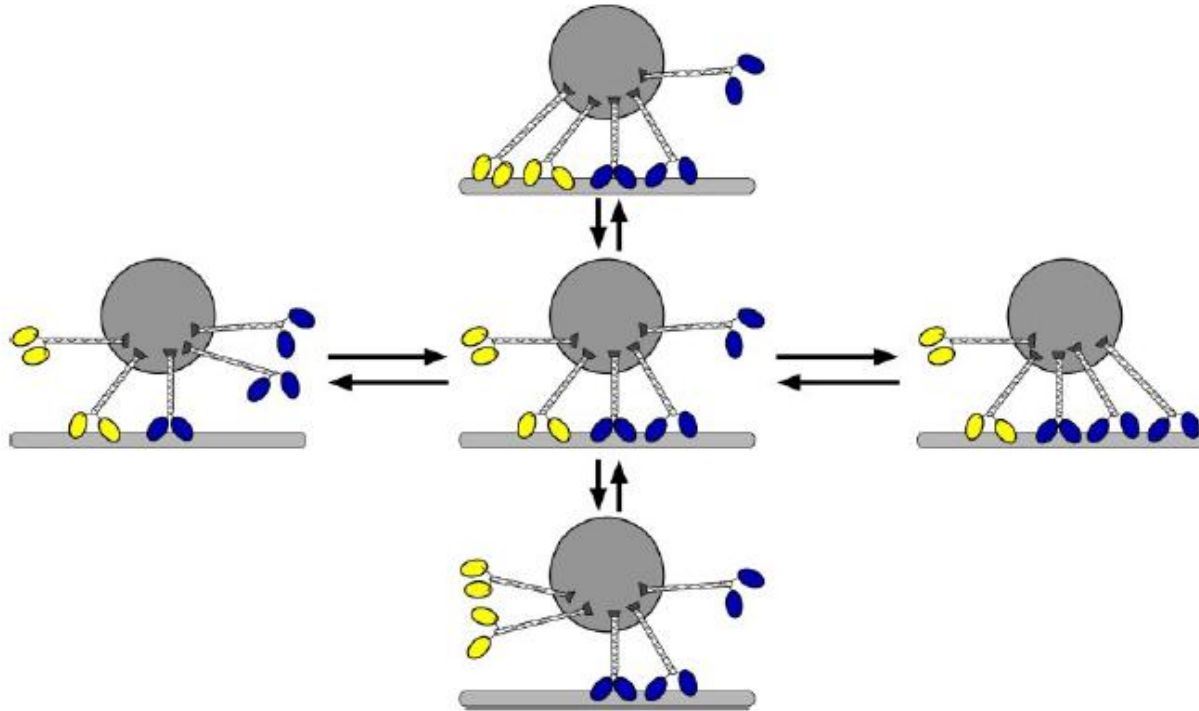
force should not affect plus-end travel. In all four instances we examined, this was not the case: minus-end mutations resulted in impairment of plus-end motion in an allele-specific manner. These observations are not consistent with the tug-of-war model. We conclude that in the wild-type, plus- and minus-end motors are coordinated, and postulate that the



# Tug-of-war as a cooperative mechanism for bidirectional cargo transport by molecular motors

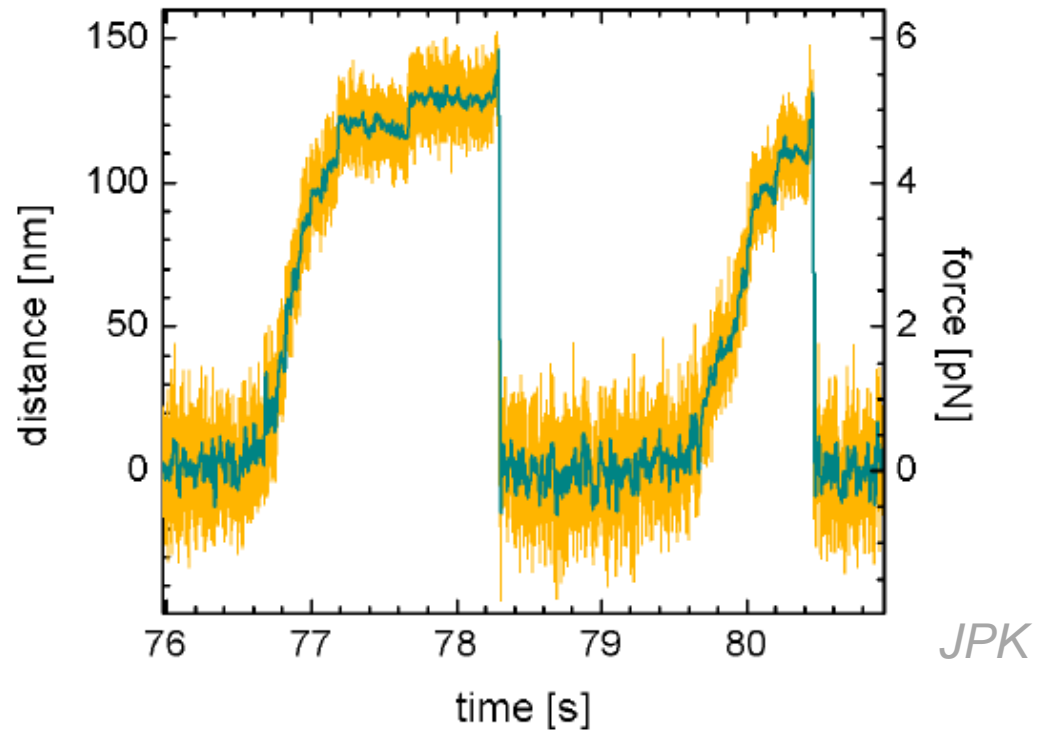
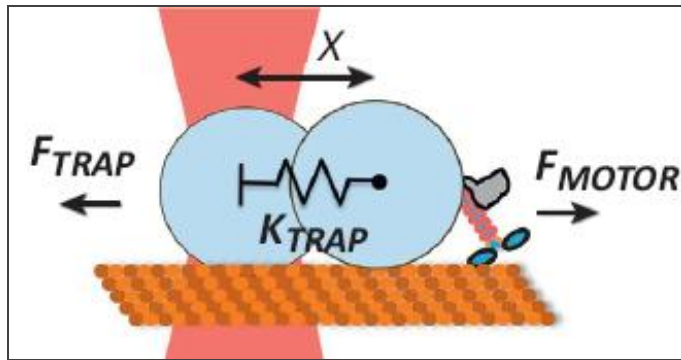
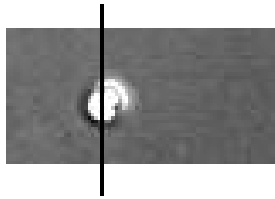
Melanie J. I. Müller\*, Stefan Klumpp†, and Reinhard Lipowsky\*\*

PNAS | March 25, 2008



- Stochastic transitions between two species of motor yields Bidirectional motion
- Tuning of single-motor parameters
- No need to invoke a third “coordination complex”

# To model the motion



Velocity 
$$v(F) = \begin{cases} v_F (1 - F/F_s) & \text{for } F \leq F_s \\ v_B (1 - F/F_s) & \text{for } F \geq F_s \end{cases}$$

Unbinding rate

$$\varepsilon(F) = \varepsilon_0 \exp[F/F_d],$$

Binding rate

$$\pi(F) = \pi_0$$

**Table 1. Values of the single-motor parameters for kinesin 1, cytoplasmic dynein, and an unknown plus motor (kin?) that transports *Drosophila* lipid droplets**

Parameter	Kinesin 1	Dynein
Stall force $F_s$ , pN	6 (29, 30)	1.1* (12, 27) 7 (31)
Detachment force $F_d$ , pN	3 (30)	0.75*
Unbinding rate $\varepsilon_0$ , $s^{-1}$	1 (30, 32)	0.27* (27, 33)
Binding rate $\pi_0$ , $s^{-1}$	5 (34)	1.6* (33, 35)
Forward velocity $v_F$ , $\mu\text{m/s}$	1 (32, 36)	0.65* (33, 37)
Back velocity $v_B$ , nm/s	6 (36)	72*

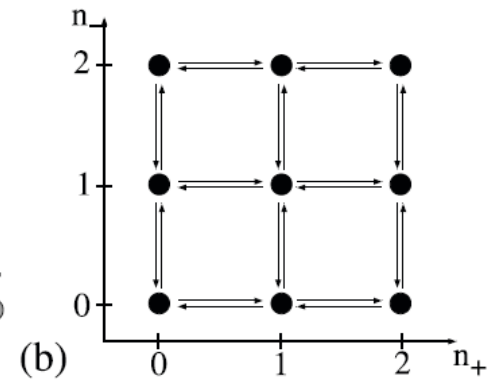
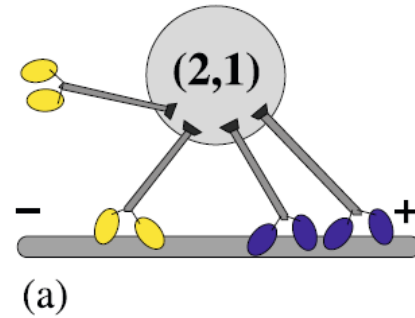
Unbinding rate  $\varepsilon$

Binding rate  $\pi$

Steady state solution to ...

$$\frac{\partial}{\partial t} p(n_+, n_-, t)$$

$$\begin{aligned} &= p(n_+ + 1, n_-, t) \varepsilon_+(n_+ + 1, n_-) + p(n_+, n_- + 1, t) \varepsilon_-(n_+, n_- + 1) \\ &+ p(n_+ - 1, n_-, t) \pi_+(n_+ - 1, n_-) + p(n_+, n_- - 1, t) \pi_-(n_+, n_- - 1) \\ &- p(n_+, n_-, t) [\pi_+(n_+, n_-) + \pi_-(n_+, n_-) + \varepsilon_+(n_+, n_-) + \varepsilon_-(n_+, n_-)]. \end{aligned}$$

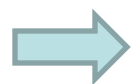


Force Balance

$$n_+ F_+ = -n_- F_- \equiv F_c(n_+, n_-),$$

Mean field

$$F_+ = F_c/n_+$$



$$\varepsilon_+(n_+, n_-) = n_+ \varepsilon_{0+} \exp[F_c(n_+, n_-)/(n_+ F_{d+})].$$

Velocity Balance

$$v_c(n_+, n_-) = v_+(F_+) = -v_-(-F_-).$$

The force and velocity balances as given by (6) and (9) lead to the cargo force

$$F_c(n_+, n_-) = \lambda(n_+, n_-) n_+ F_{s+} + [1 - \lambda(n_+, n_-)] n_- F_{s-}, \quad (10)$$

with

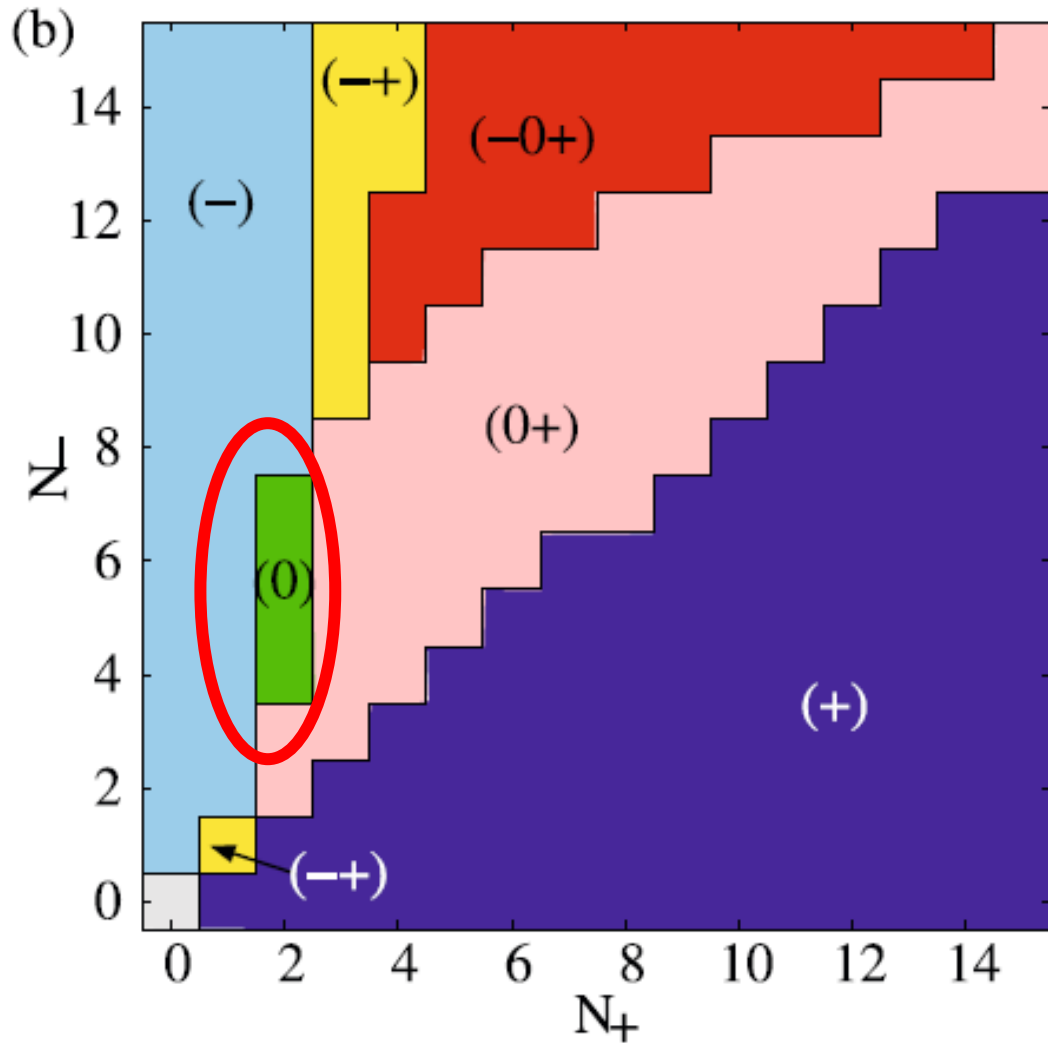
$$\lambda(n_+, n_-) = 1/[1 + (n_+ F_{s+} v_{0-})/(n_- F_{s-} v_{0+})], \quad (11)$$

and to the cargo velocity

$$v_c(n_+, n_-) = \frac{n_+ F_{s+} - n_- F_{s-}}{n_+ F_{s+}/v_{0+} + n_- F_{s-}/v_{0-}}. \quad (12)$$

We solve the Master equation (1) for the steady state by determining the eigenvector of the associated transition matrix with eigenvalue zero. In addition, we simulate individual cargo trajectories by using the Gillespie algorithm [10] for the binding/unbinding dynamics as given by (7) and (8) and let the cargo move with velocity  $v_c$  in the intervals between (un-)binding events.

# Phase diagram of Bidirectional motion



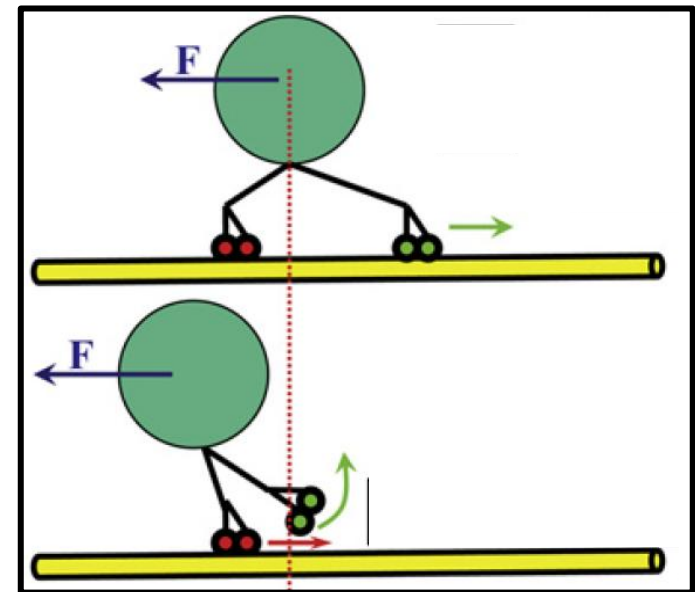
Muller et al, 2008

## Criticisms ...

Equal Load Sharing

Linear Force Velocity

Detachment under load





# Tug-of-war between dissimilar teams of microtubule motors regulates transport and fission of endosomes

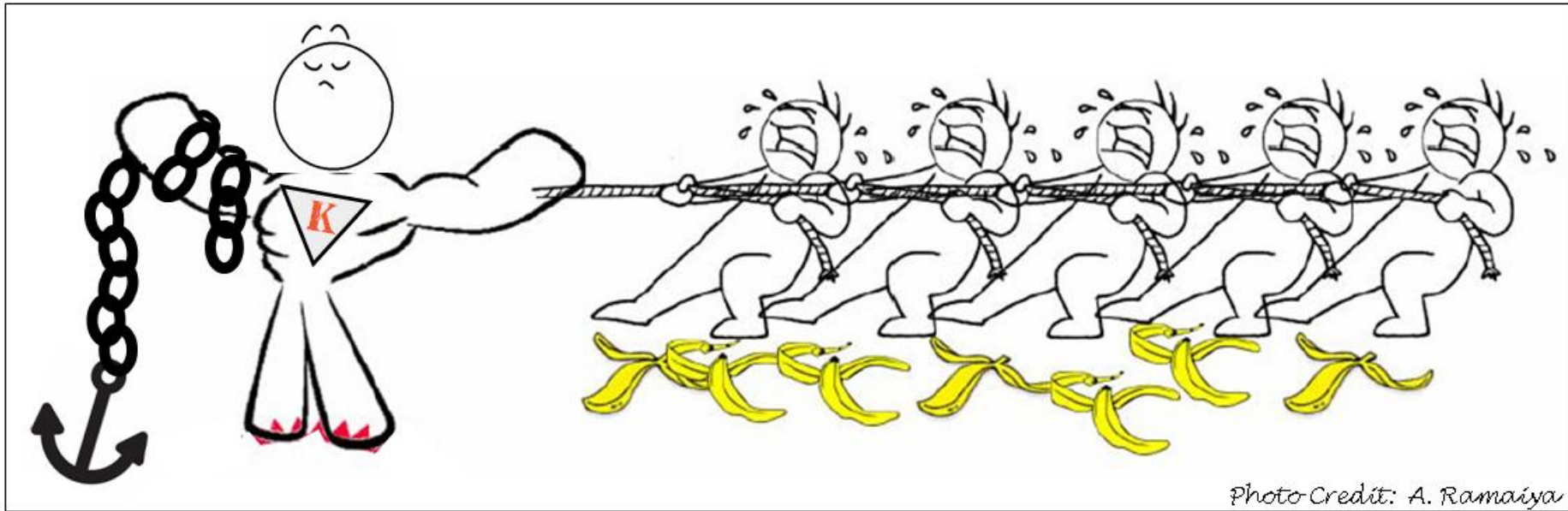


Virupakshi Soppina, Arpan Kumar Rai, Avin Jayesh Ramaiya, Pradeep Barak, and Roop Mallik<sup>1</sup>

Department of Biological Sciences, Tata Institute of Fundamental Research, Homi Bhabha Road, Colaba, Mumbai 400005, India

Edited by J. Richard McIntosh, University of Colorado, Boulder, CO, and approved September 14, 2009 (received for review June 12, 2009)

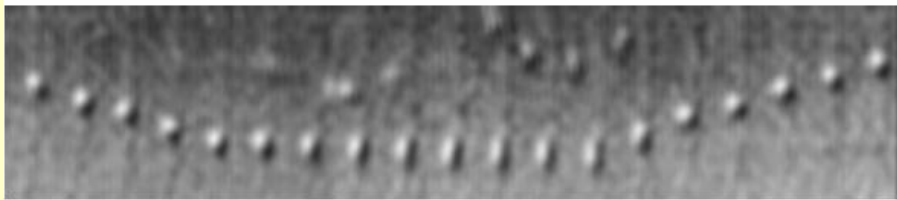
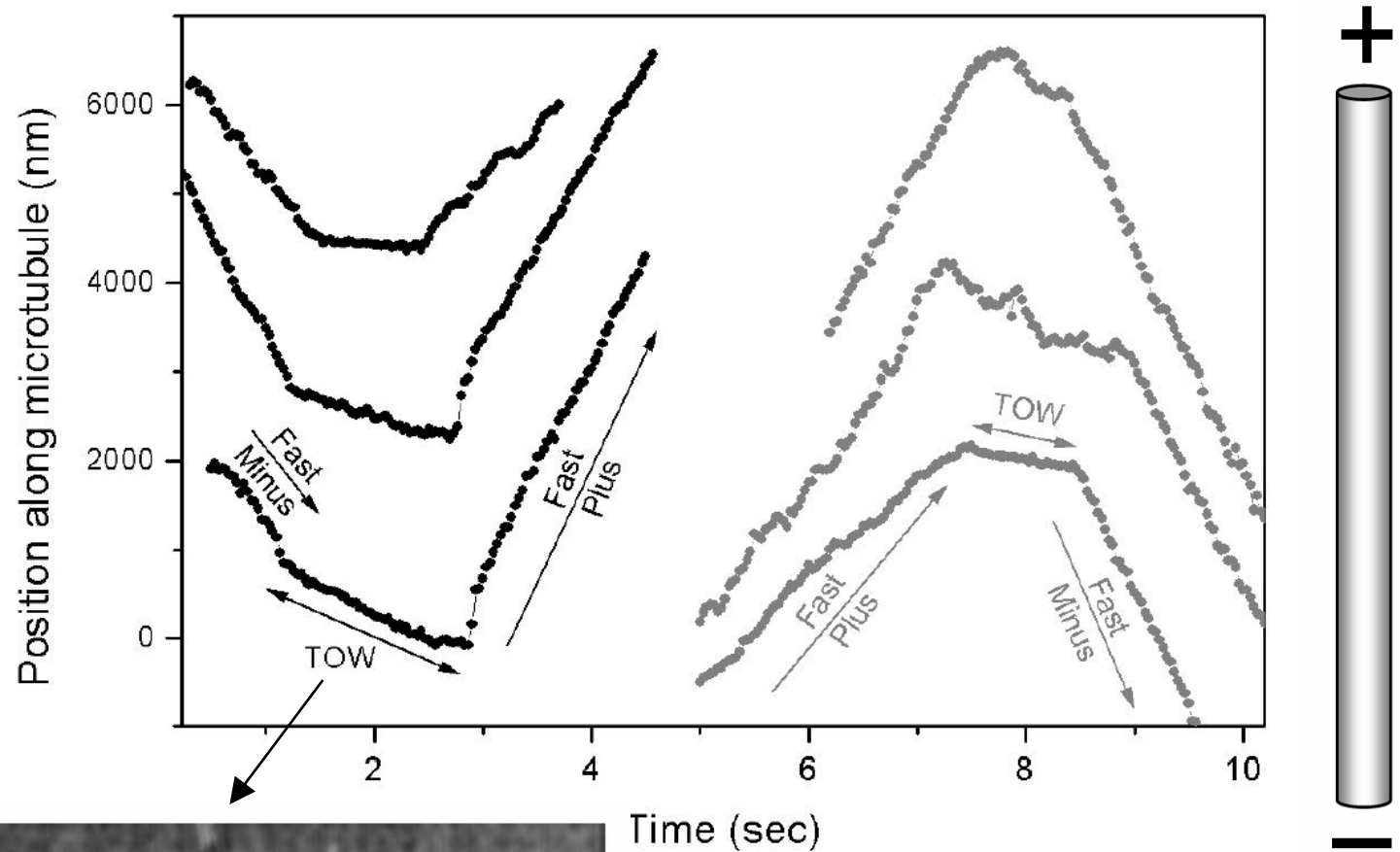
*PNAS*, 2009



5.5 pN

$1.1 \times 5 = 5.5 \text{ pN}$

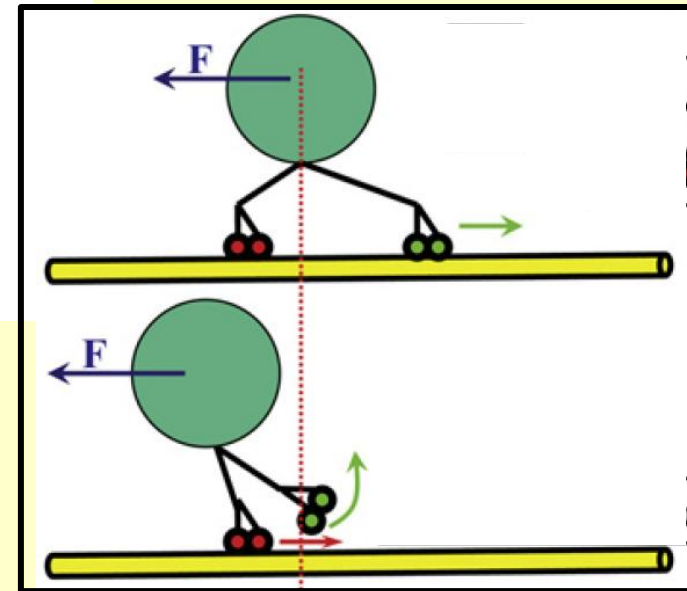
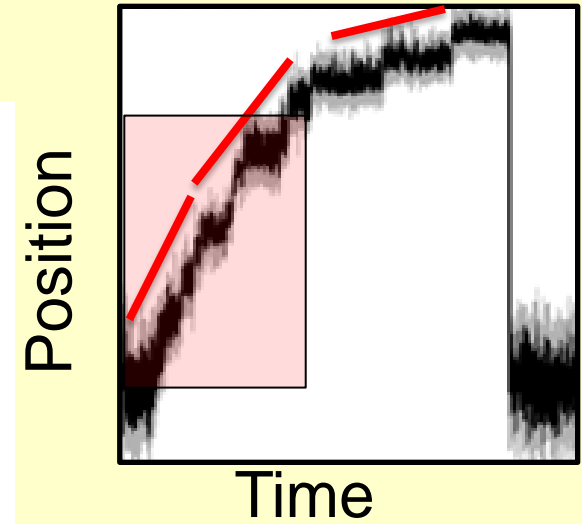
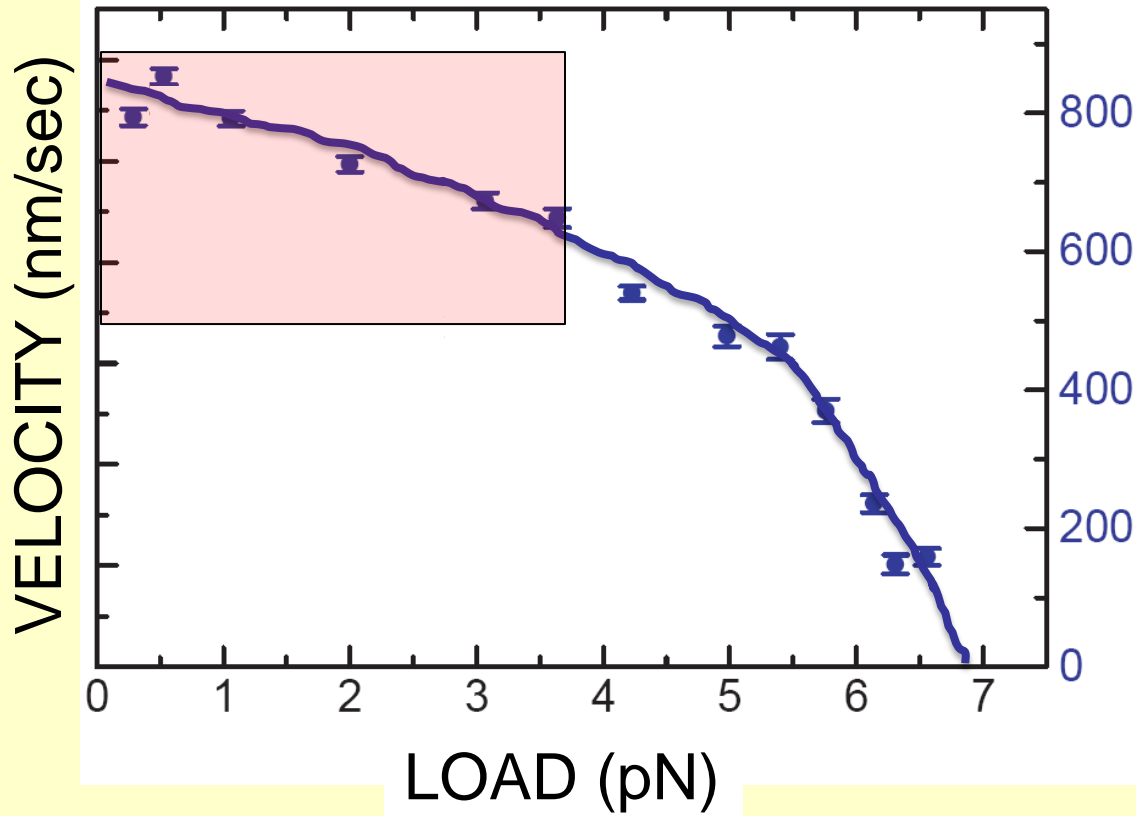
# Motion of Endosomes



5-8 Dyneins in Tug Of War against 1-2 Kinesins  
... In good agreement with Lipowsky (??)

# Kinesin's response to Load ...

F-V curve

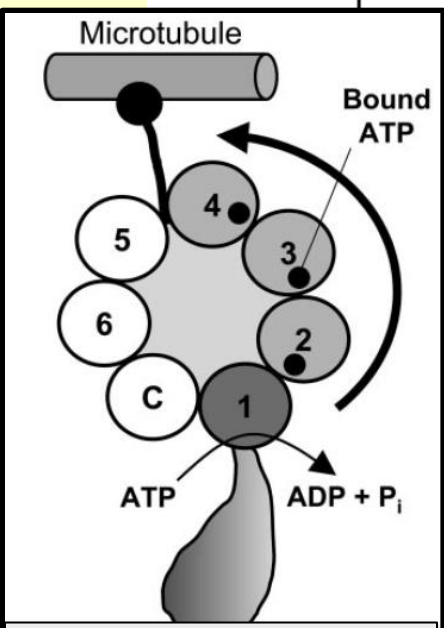
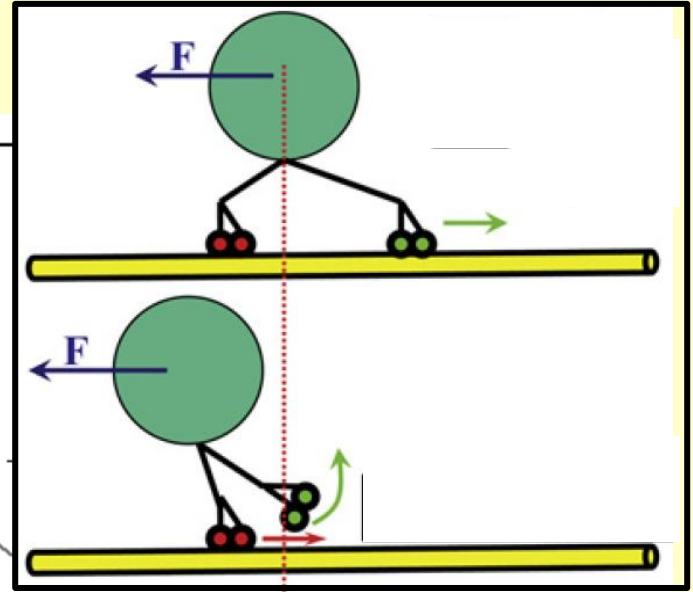
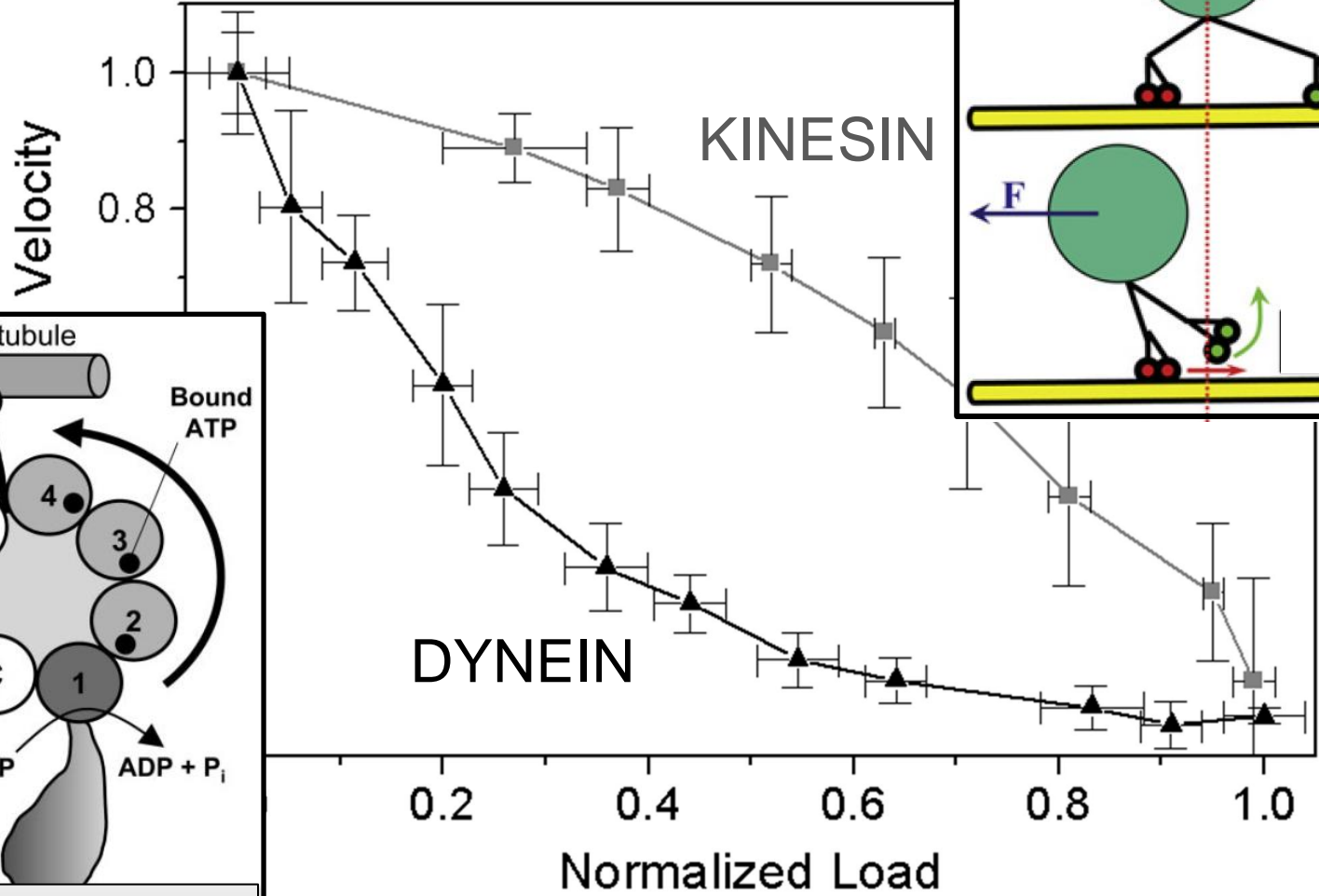


*Visscher et al, Nature 1999*

*Jamison et al 2010*  
*Driver et al 2011*  
*Kunwar et al 2008*

# Mechanism for Dynein's improved collective Function ?

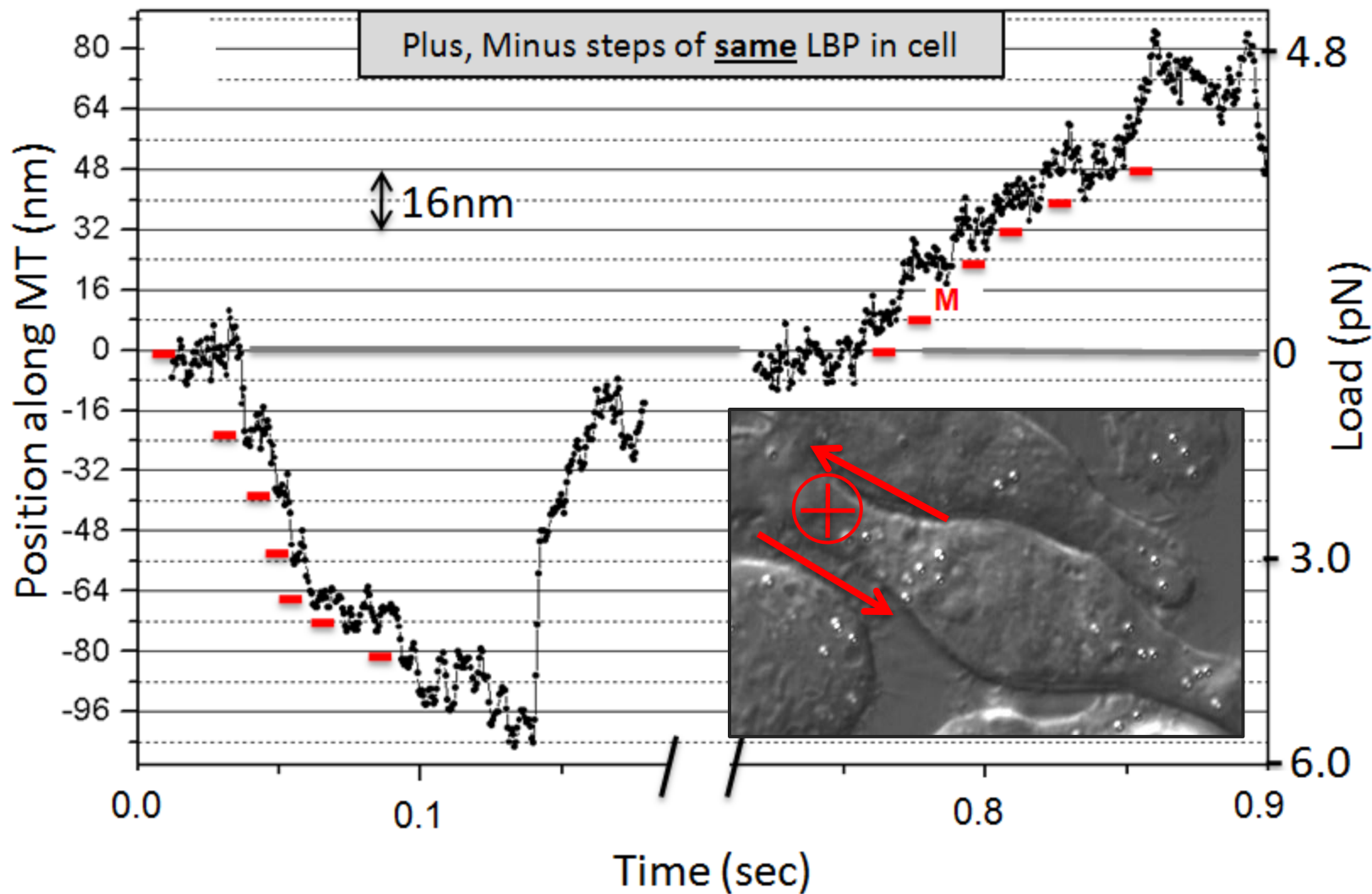
## MEASURED F-V CURVES



Dynein as a Gear  
*Mallik et al, Nature 2004*

Crucial input from MC  
 --- Singh et al , PNAS 2005

# LOAD-DEPENDENT STEP SIZE INSIDE CELLS



# Problem at high load (Bhat et al, 2012)

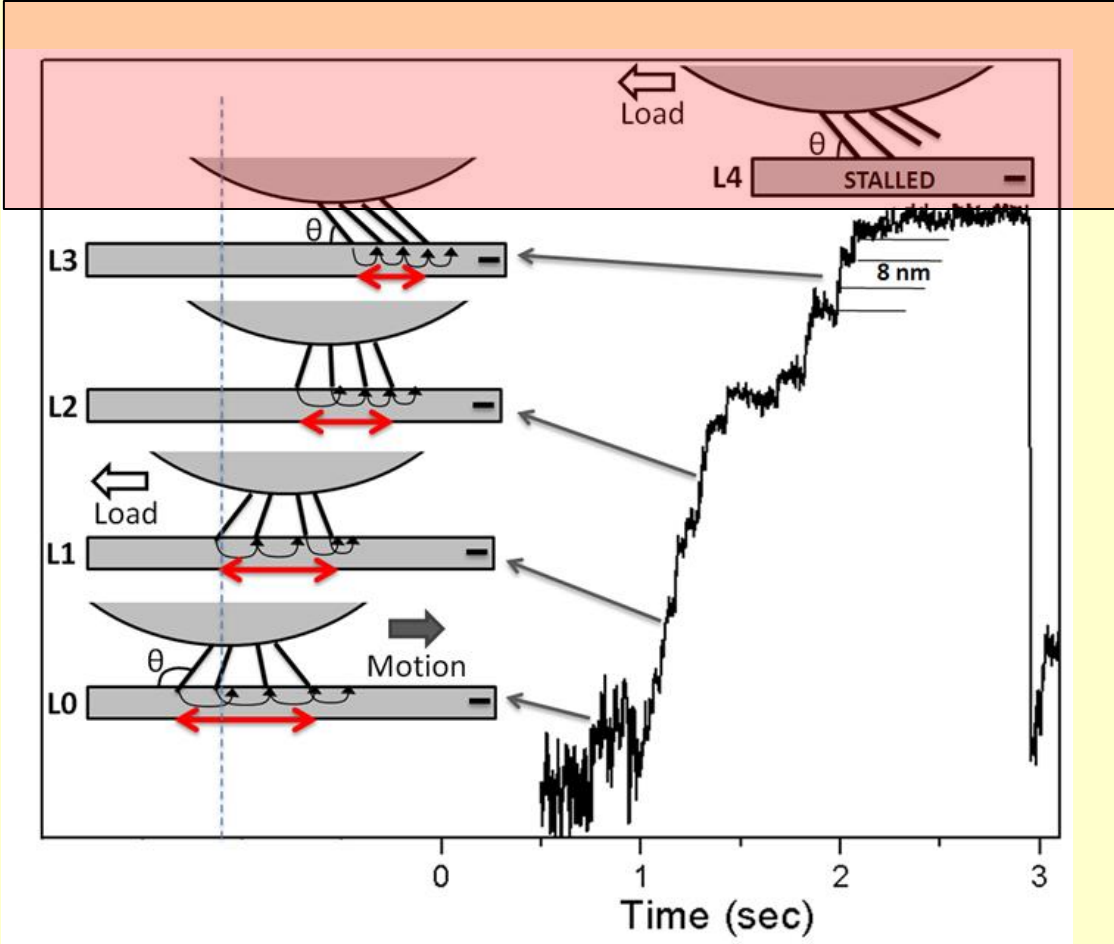
$$\epsilon(F) = \epsilon_0 \exp(|F|/F_d)$$

$$\epsilon_+(n_+, n_-) = n_+ \epsilon_{0+} \exp[F_c(n_+, n_-)/(n_+ F_{d+})].$$

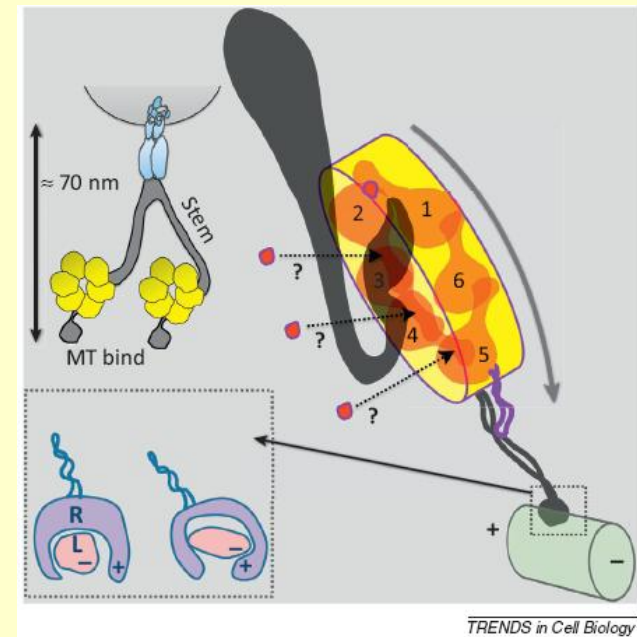
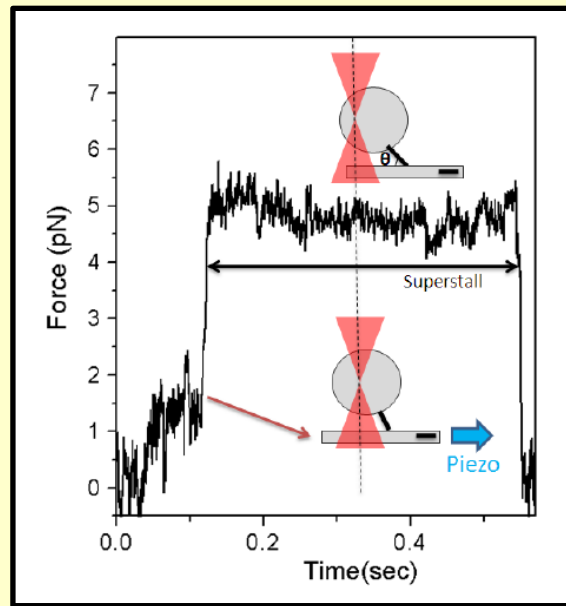


$F_s$

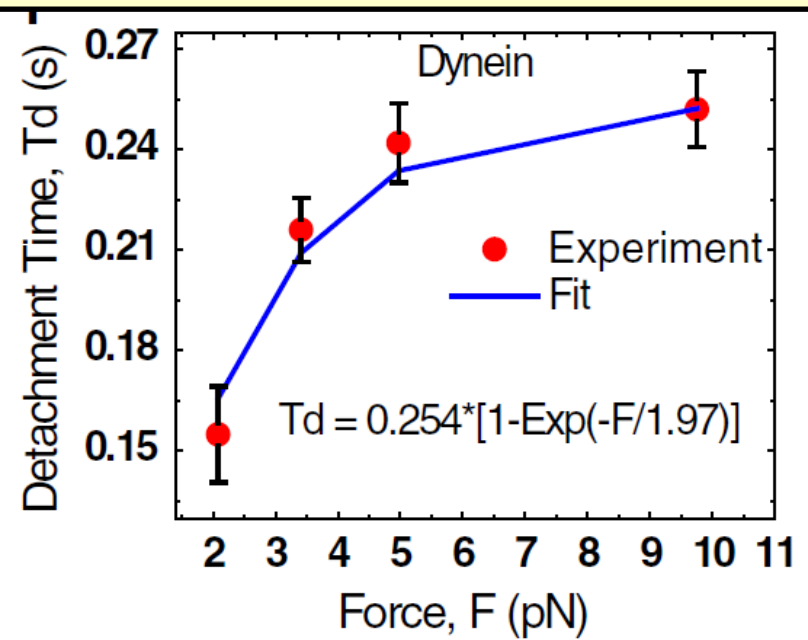
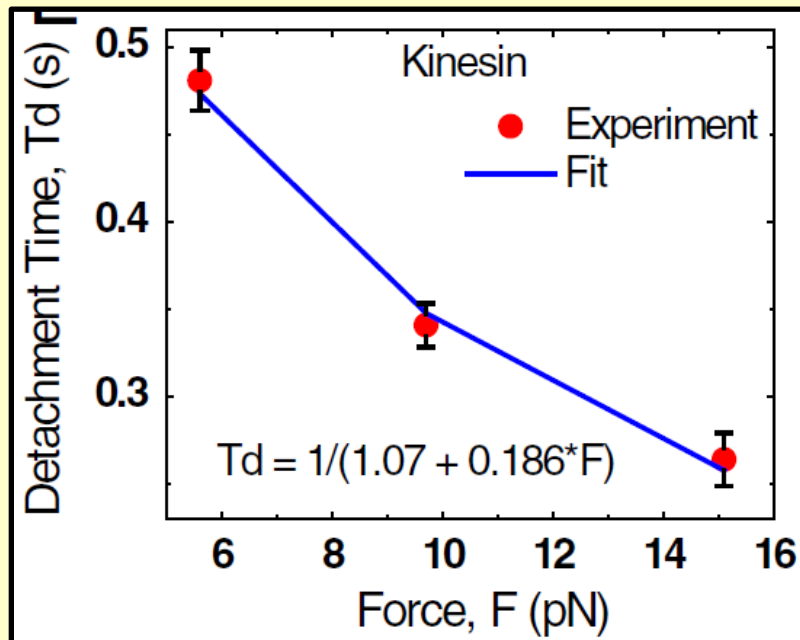
$$\epsilon(F) = \epsilon_0 \exp(|F|/F_d)$$



# Catch bond In Dynein



*Kunwar et al, PNAS 2011*



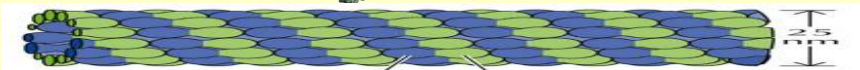
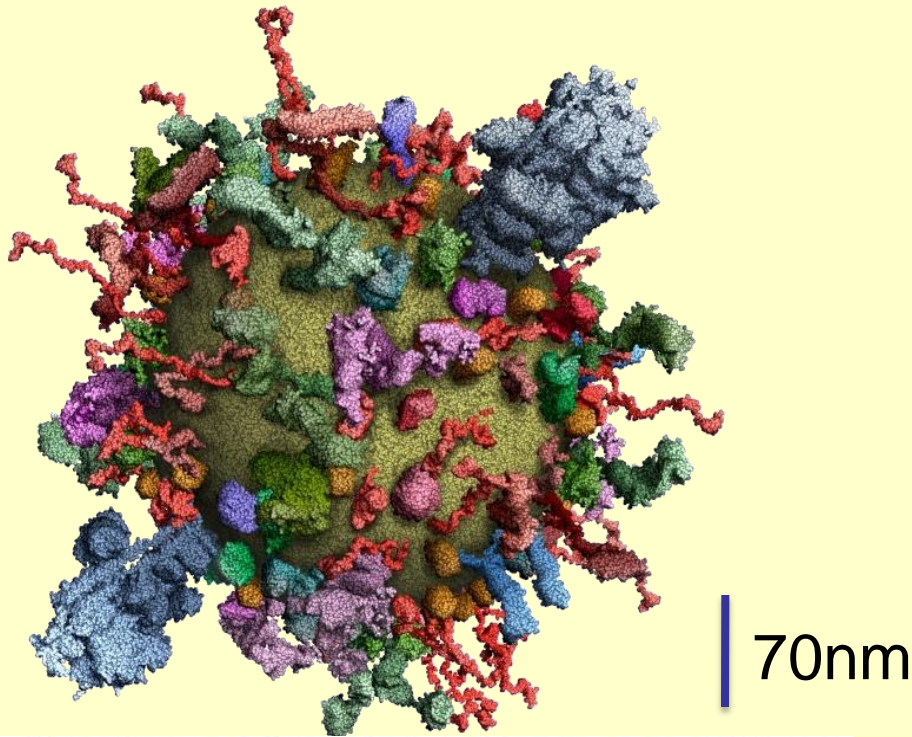


Rai *et al*,  
2013

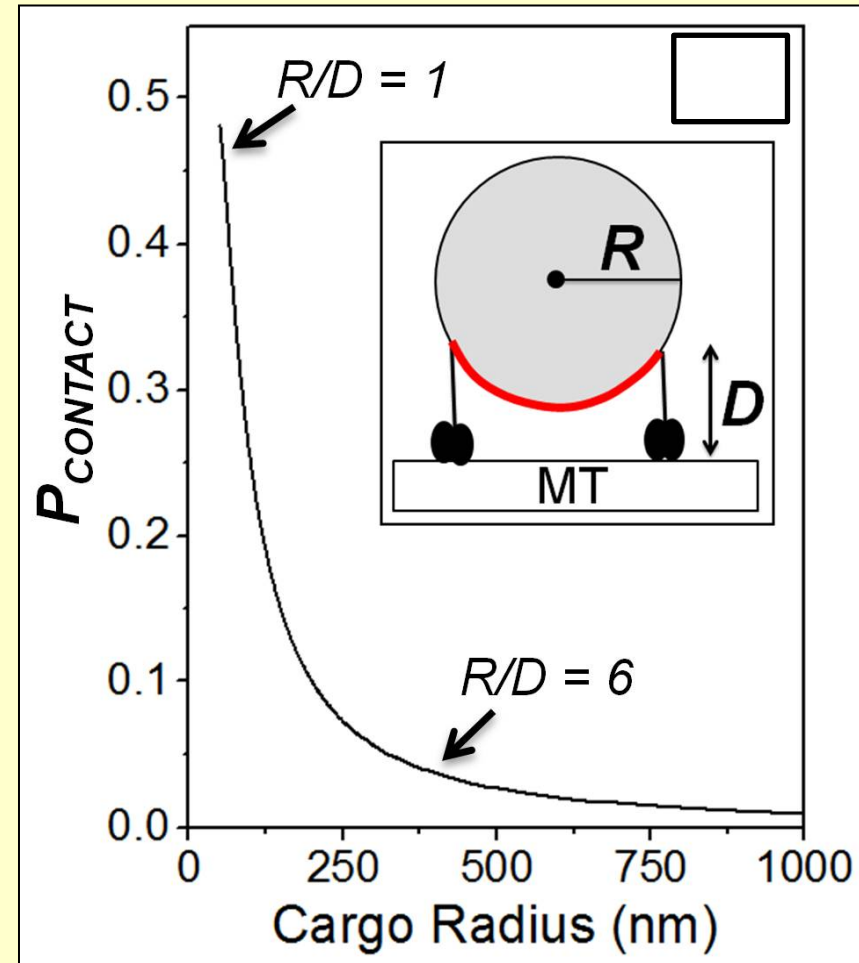
- Roles are reversed between Single and Collective behaviour
- Dyneins appears molecularly adapted to generate large collective forces → Gear, Catch-bond
- Possible to tune forces, and therefore processes with Dynein. Less so with Kinesin.
- 8 -12 Dyneins can generate force simultaneously.



# What next ? ... Geometry

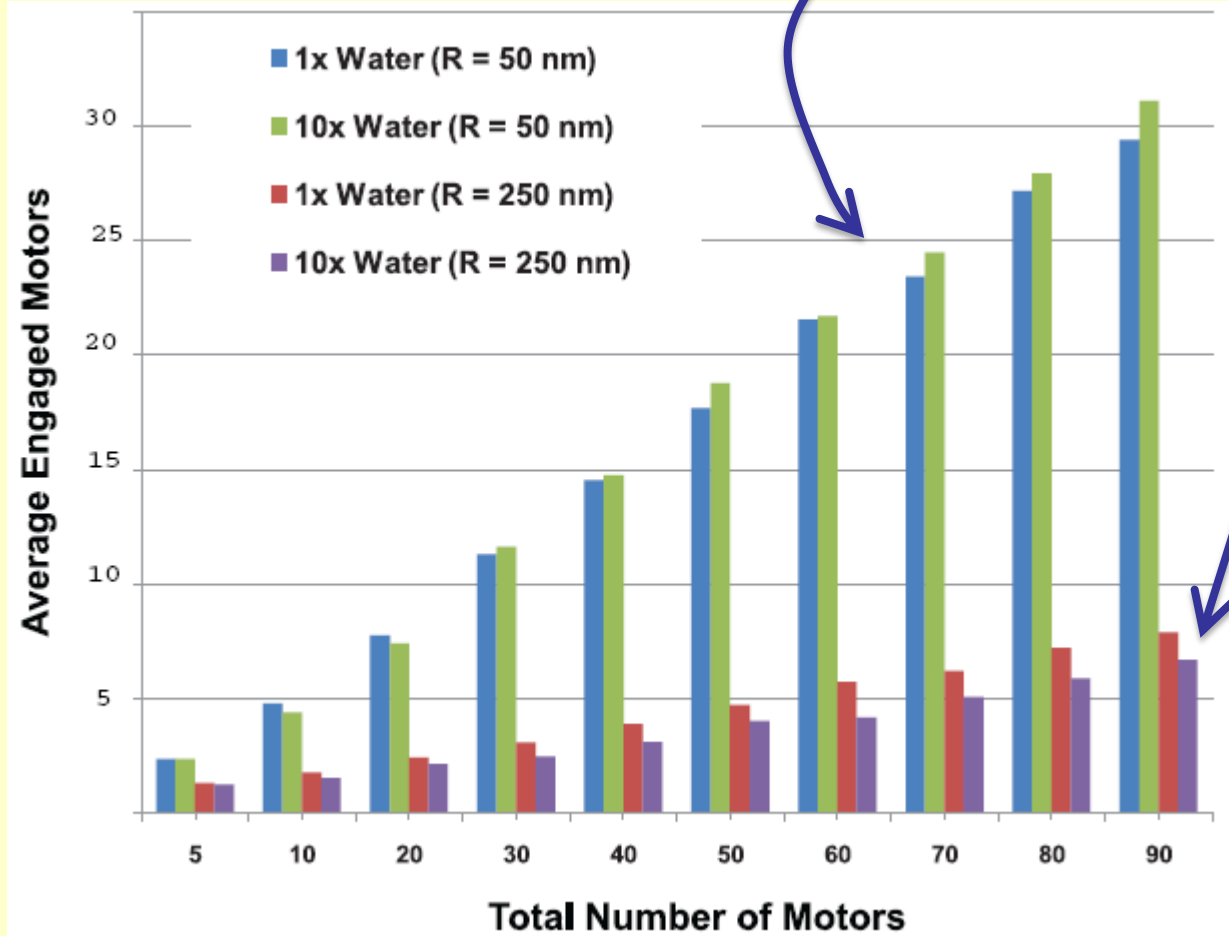
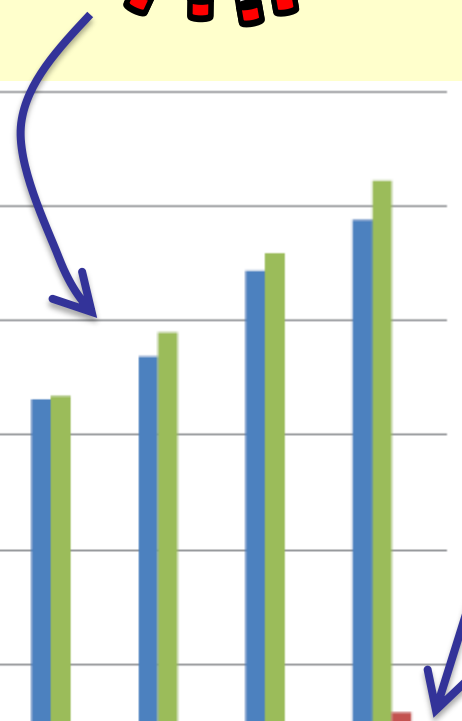
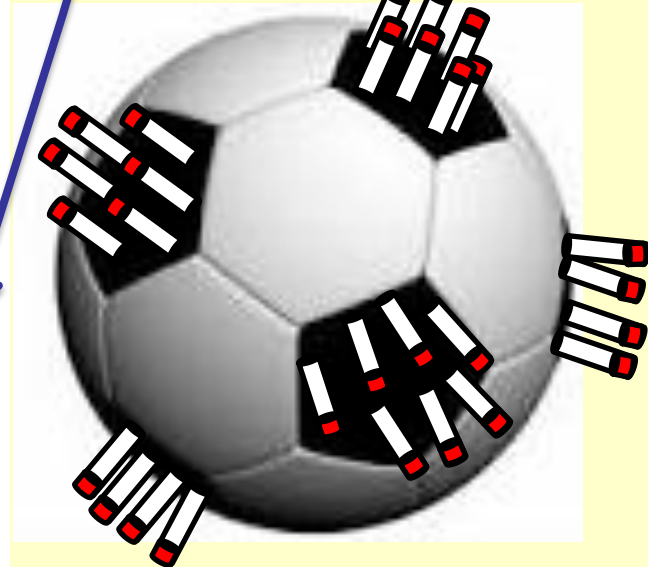


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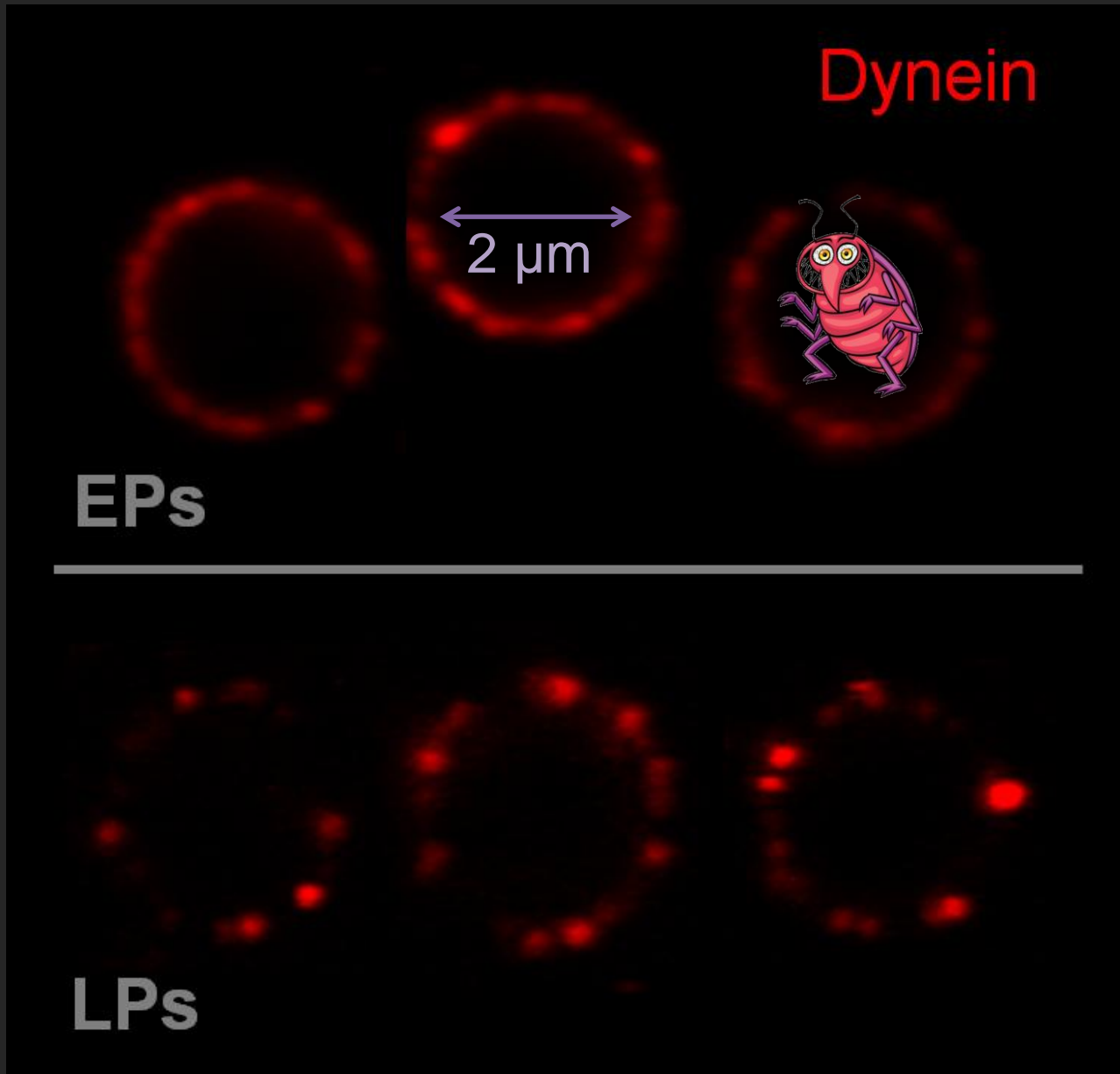


$$D_{CARGO} / L_{MOTOR}$$

Erickson et al, PLoS Comp Biol 2011



# Lipid induced “Memory” in Bidirectional Transport ??



Ashim



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## Reagents/Discussion/Criticism

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