



CKM 2016 Workshop

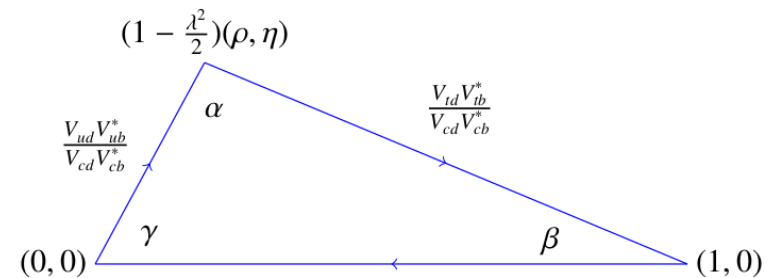
**Measurement of γ from $B_u \rightarrow DK^{(*)}$ decays
and $B_c^+ \rightarrow D^0 h^+$ mode in LHCb**

Frederic Machefert, LAL(Orsay)
On behalf of the LHCb collaboration

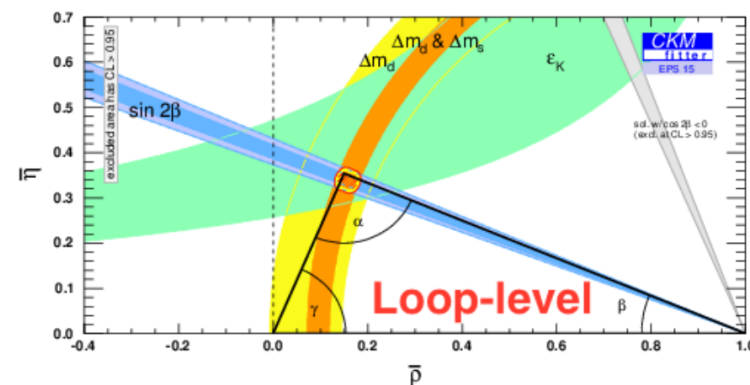
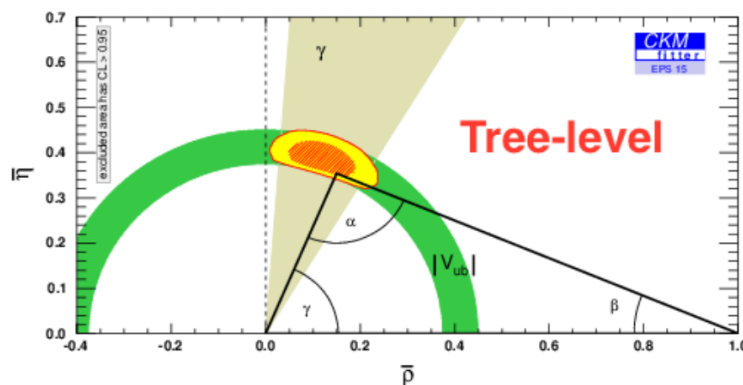
Introduction

The γ angle

$$\gamma \equiv \arg \left(-\frac{V_{ud} \cdot V_{ub}^*}{V_{cd} \cdot V_{cb}^*} \right) \simeq \arg \left(-\frac{V_{ub}^*}{V_{cb}^*} \right)$$



- The angle γ can be measured when the $b \rightarrow u$ and $b \rightarrow c$ type decays interfere to exhibit CP violation
- γ can be measured in CPV tree decays with tiny theory uncertainties [JHEP01 051]
 - No V_{tx} term \rightarrow the only angle that that be measured without penguin pollution (indirect measurements contain loops)
- $B \rightarrow D^{(*)}K^{(*)}$ decays satisfy those criteria and some potentially give large CP violation



Babar
Belle
LHCb



$$\gamma = (73.2^{+6.3}_{-7.0})^\circ$$

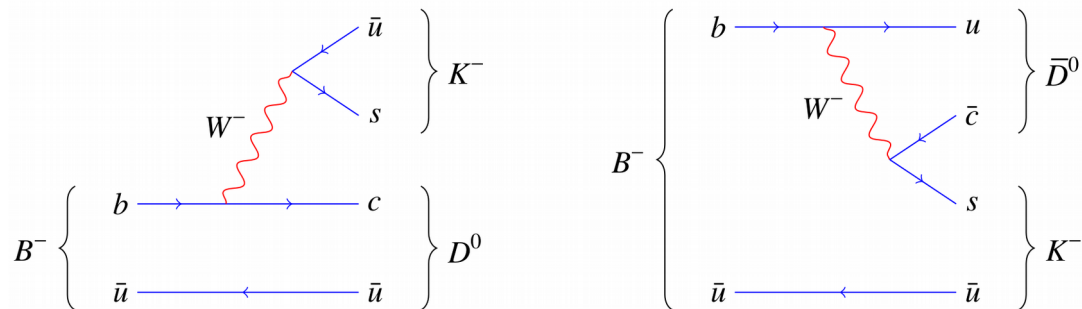
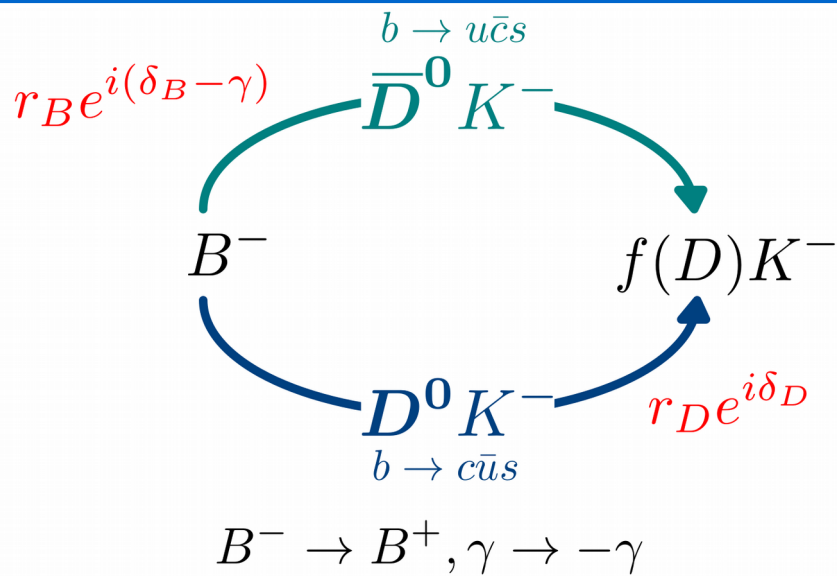
(direct)

$$\gamma = (66.85^{+0.94}_{-3.44})^\circ$$

(indirect)

Standard Candle [PRD 92(3) 033002]
LHCb has to measure it
at degree-level precision

The methods to measure γ



$$\gamma \equiv \arg \left(-\frac{V_{ud} \cdot V_{ub}^*}{V_{cd} \cdot V_{cb}^*} \right) \simeq \arg \left(-\frac{V_{ub}^*}{V_{cb}^*} \right)$$

- The typical CP violation observables which are measured are

$$\frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B - \gamma)}$$

- Charge asymmetries

$$A = \frac{\Gamma(B^- \rightarrow f_D K^-) - \Gamma(B^+ \rightarrow \bar{f}_D K^+)}{\Gamma(B^- \rightarrow f_D K^-) + \Gamma(B^+ \rightarrow \bar{f}_D K^+)}$$

- Partial width ratios

$$R = \frac{\Gamma(B^- \rightarrow f_D K^-) + \Gamma(B^+ \rightarrow \bar{f}_D K^+)}{\Gamma(B^- \rightarrow f'_D K^-) + \Gamma(B^+ \rightarrow \bar{f}'_D K^+)}$$

- The hadronic parameters (measured) are

- Amplitude ratio r_B

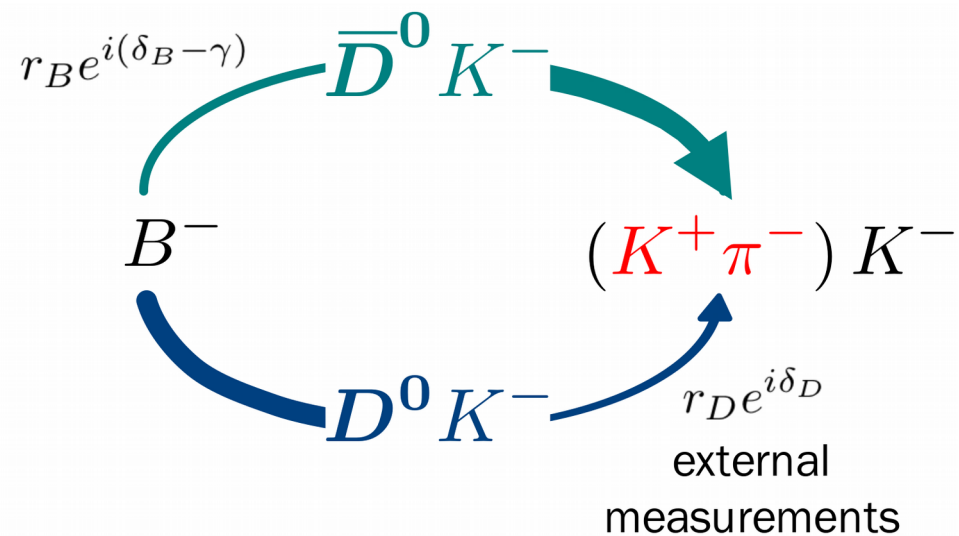
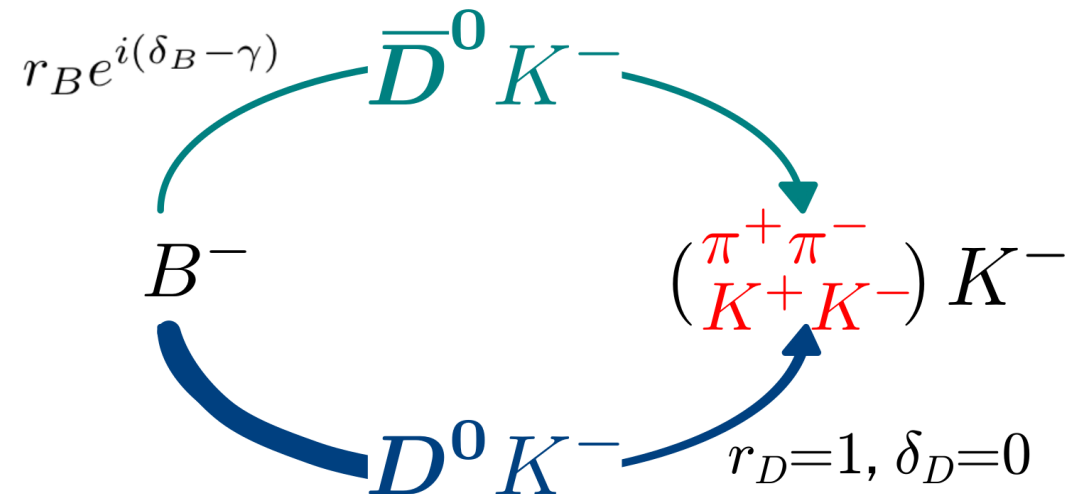
- Strong phase difference δ_B

- Many methods using different D decays (D decay parameters needed)

GLW versus ADS methods

GLW: CP eigenstates
 Gronau, London, Wyler
 [PLB 352 (1991), 483]
 [PLB 265 (1991), 172]

ADS: large interference
 (=large asymmetries)
 [PRL 78 (1997) 3257]



Favoured and suppressed decays in both
 Interfering decay amplitudes

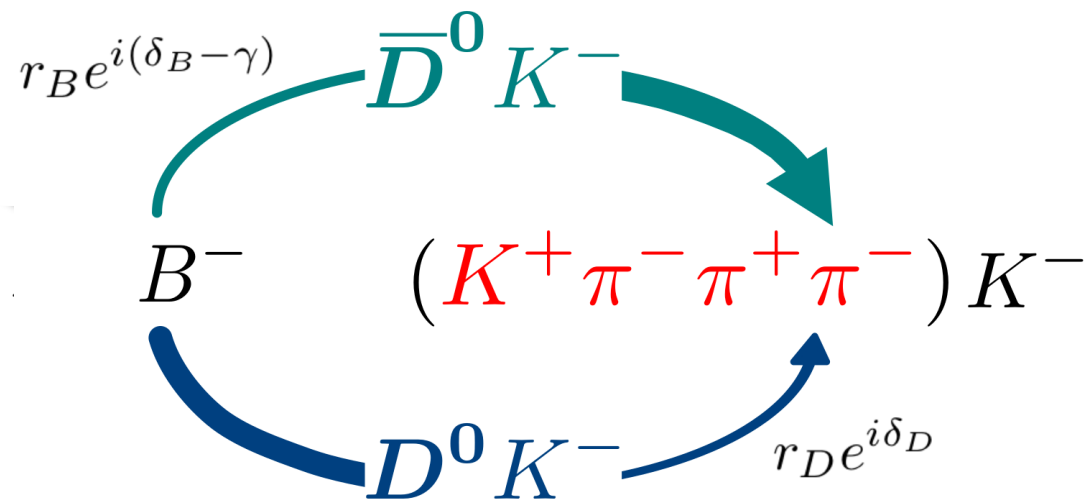
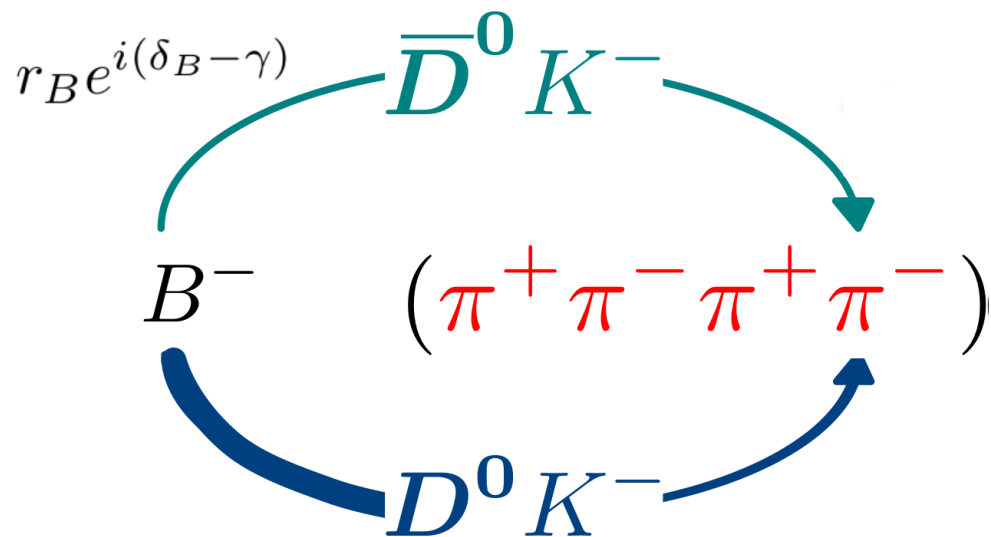
$$\text{GLW: } \Gamma(B^{\mp} \rightarrow f_D K^{\mp}) \propto 1 + r_B + 2r_B \cos(\delta_B \mp \gamma)$$

$$\text{ADS: } \Gamma(B^{\mp} \rightarrow f_D K^{\mp}) \propto (r_D^f)^2 r_B^2 + 2r_B r_D^f \cos(\delta_B + \delta_D^f \mp \gamma)$$

GLW versus ADS methods: D four body decays

Quasi - GLW

Quasi - ADS



Fractional CP-even content
 $F_+ = 0.737 \pm 0.028$
 $2F_+ - 1 \sim 0.5$

Coherence factor
 $\kappa_D^{3\pi} = 0.43^{+0.17}_{-0.13}$

[M. Nayak et al. Phys. Lett.B740(2015) 1]
 [Malde et al. PLB 747 (2015) 9]

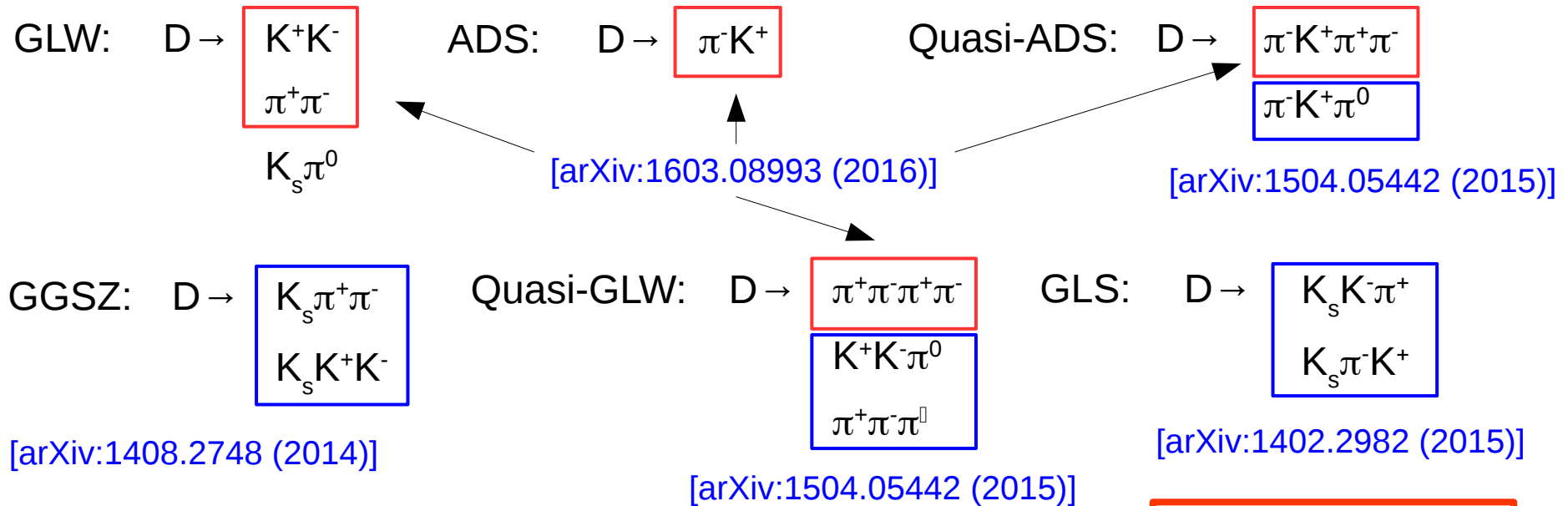
[Atwood and Soni, PRD 68 (2003) 033003]
 [arXiv:1602.07430]

$$\text{GLW: } \Gamma(B^{\mp} \rightarrow f_D K^{\mp}) \propto 1 + r_B + (2F_+ - 1) 2r_B \cos(\delta_B \mp \gamma)$$

$$\text{ADS: } \Gamma(B^{\mp} \rightarrow f_D K^{\mp}) \propto (r_D^f)^2 r_B^2 + 2r_B r_D^f \kappa_D^f \cos(\delta_B + \delta_D^f \mp \gamma)$$

Measurements from LHCb in the charged modes

- Several methods permit to exhibit the interference in $B \rightarrow DK$



- and in the $B \rightarrow DK^*$ modes

[LHCb-CONF-2016-014]

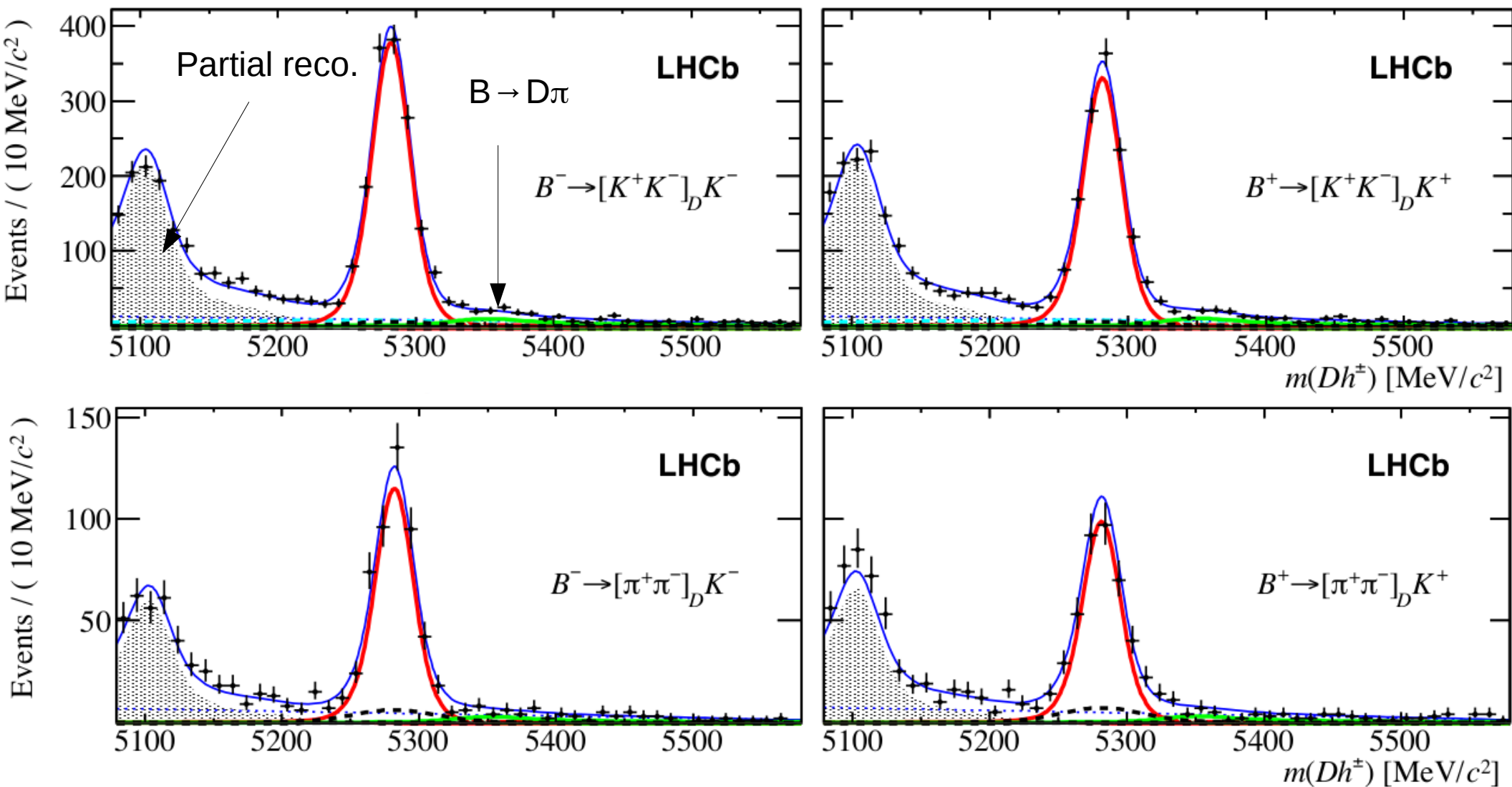
Shown in this talk

Already published

- Analysis based on 4fb^{-1}
 - 1fb^{-1} collected during the Run 2 (2015-2016)
 - Higher cross-section, improved PID and online selection
 - x3 signal rate increase with respect to Run 1

(quasi-) GLW modes

GLW modes: $D \rightarrow KK$, $D \rightarrow \pi\pi$



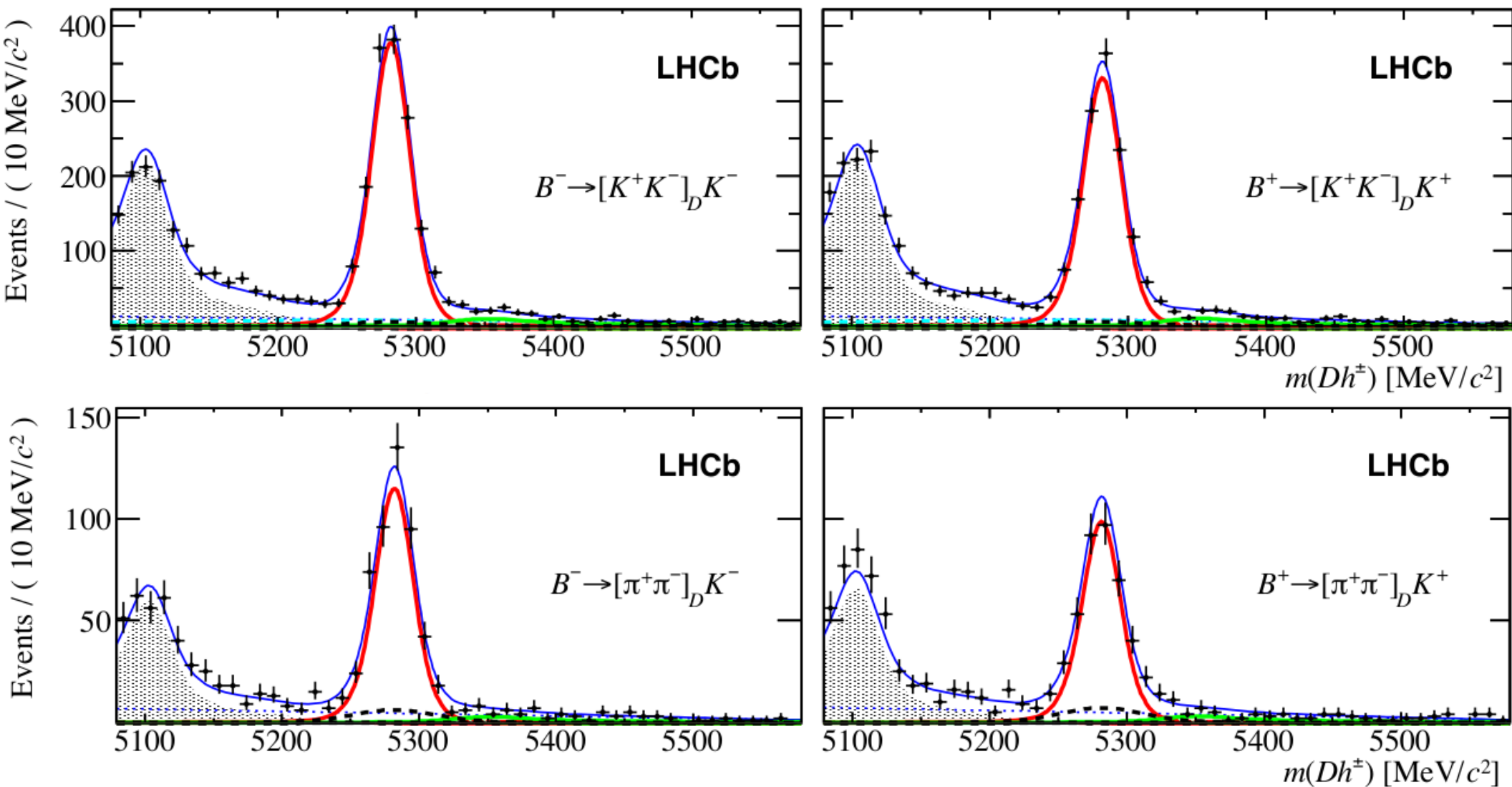
● B meson yields are

[arXiv:1603.08993 (2016)]

3.0 fb⁻¹

- $D \rightarrow KK$ mode: 3816 ± 92 ($B^+ + B^-$)
- $D \rightarrow \pi\pi$ mode: 1162 ± 48 ($B^+ + B^-$)

GLW modes: $D \rightarrow KK$, $D \rightarrow \pi\pi$

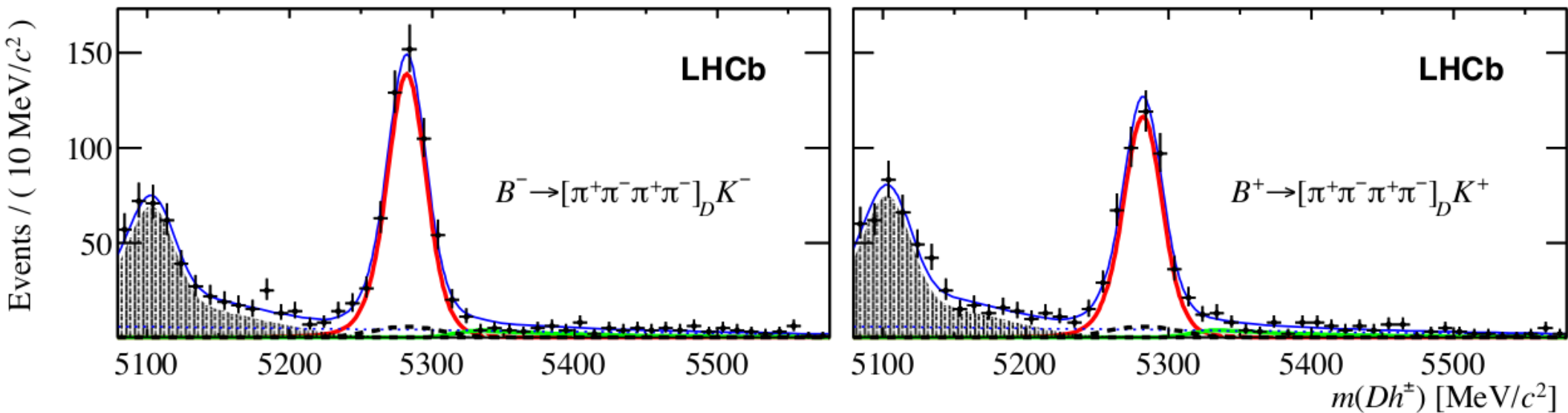


● $A_{\text{K}}^{\text{KK}} = 0.87 \pm 0.020 \pm 0.008$

[arXiv:1603.08993 (2016)]

● $A_{\text{K}}^{\pi\pi} = 0.128 \pm 0.037 \pm 0.012$

Quasi-GLW: $D \rightarrow \pi\pi\pi\pi$ – First Analysis of this mode



- $A_{\pi\pi\pi\pi}^K = 0.100 \pm 0.034 \pm 0.018$
- Compared to the 2-body GLW mode, the interference is diluted by the fractional CP-event content, $(2F_+ - 1) \sim 0.5$ [arXiv:1504.05878]

[arXiv:1603.08993 (2016)]

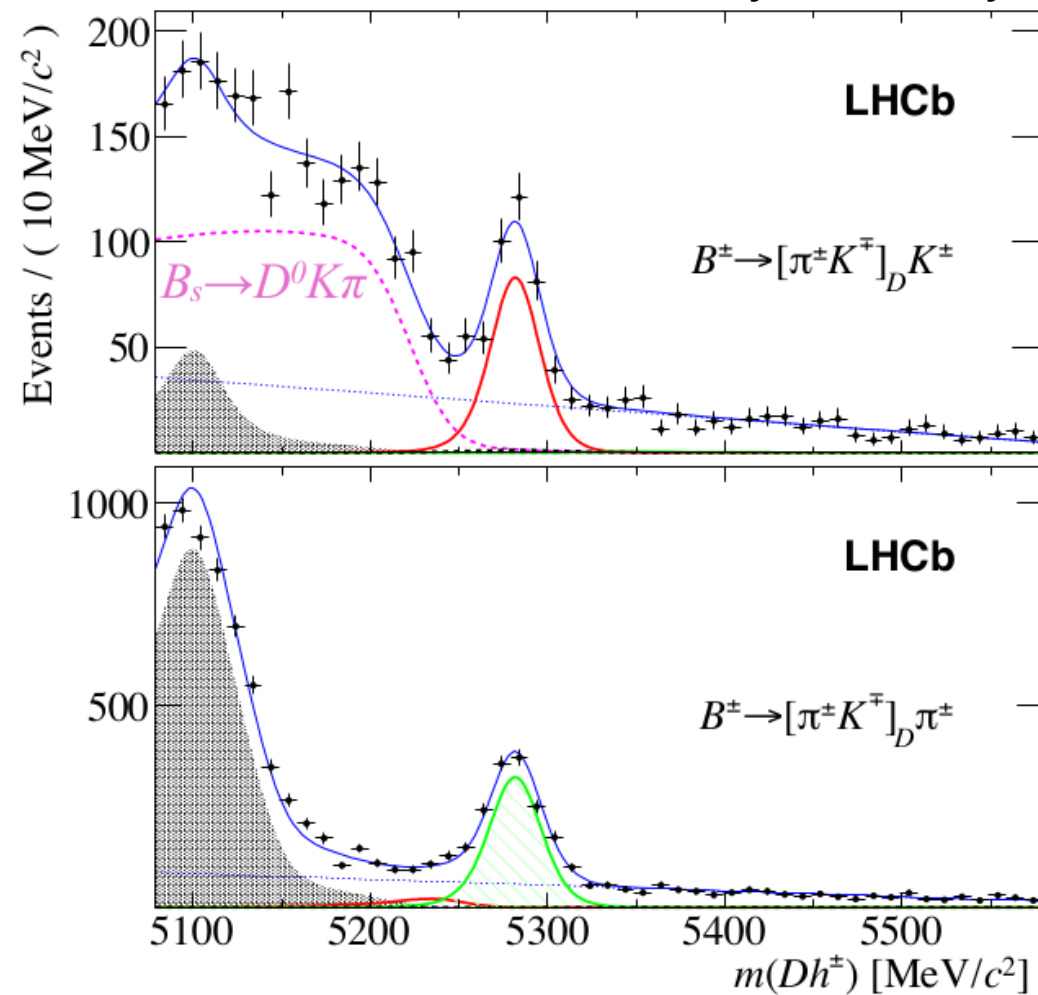
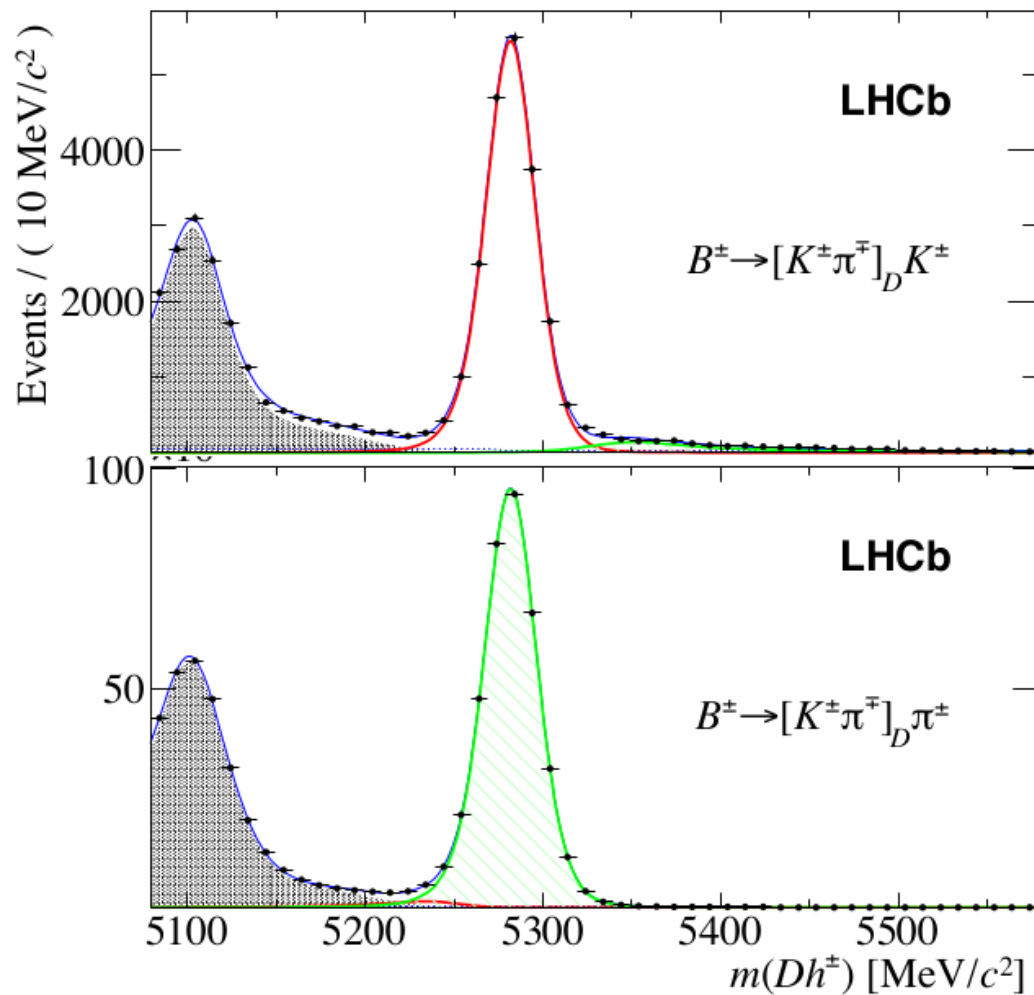
(quasi-) ADS modes

ADS 2-body

● 29500 $B^\pm \rightarrow DK^\pm$, $D \rightarrow K^+\pi^-$

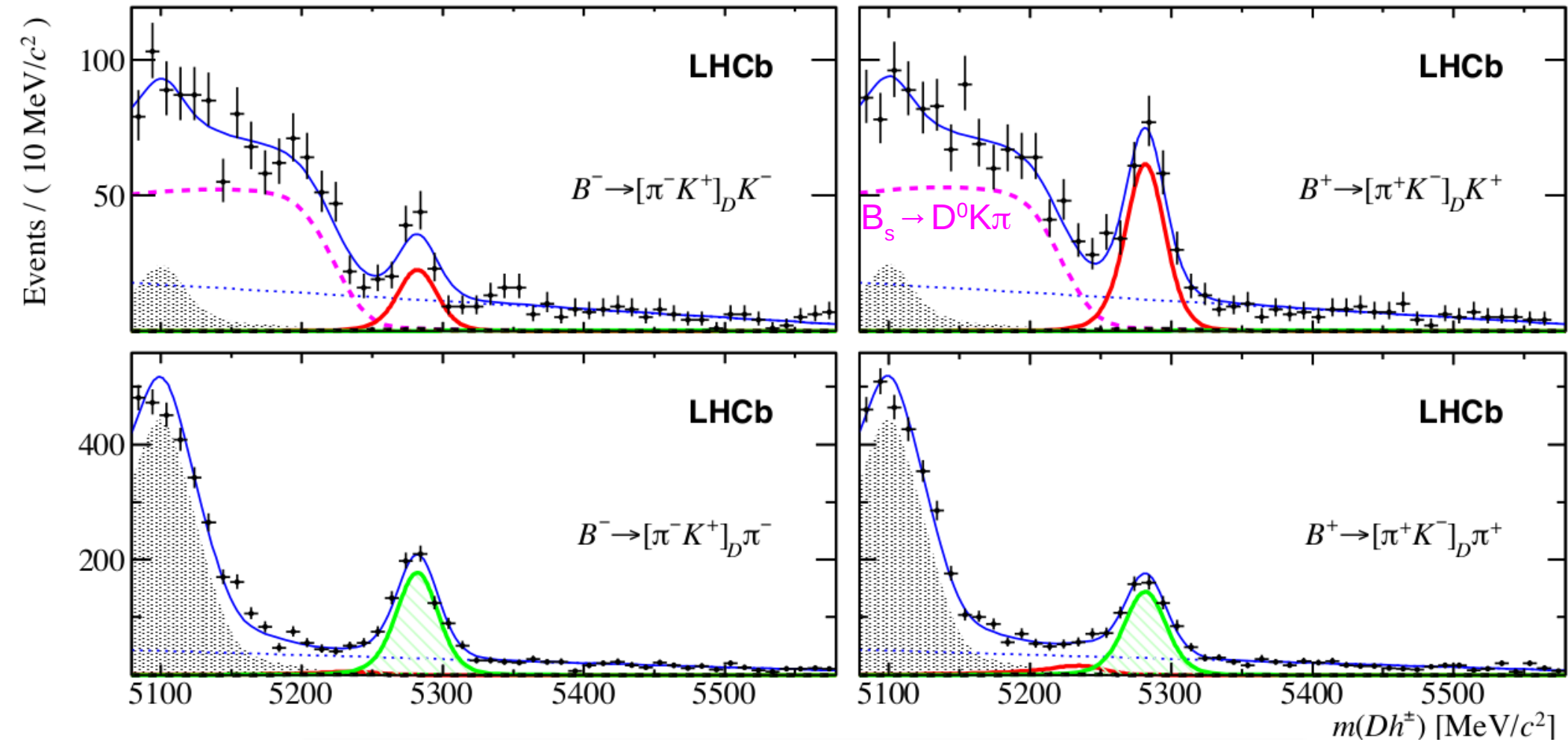
● 550 $B^\pm \rightarrow DK^\pm$, $D \rightarrow \pi^+K^-$

Seen by LHCb only



[arXiv:1603.08993 (2016)]

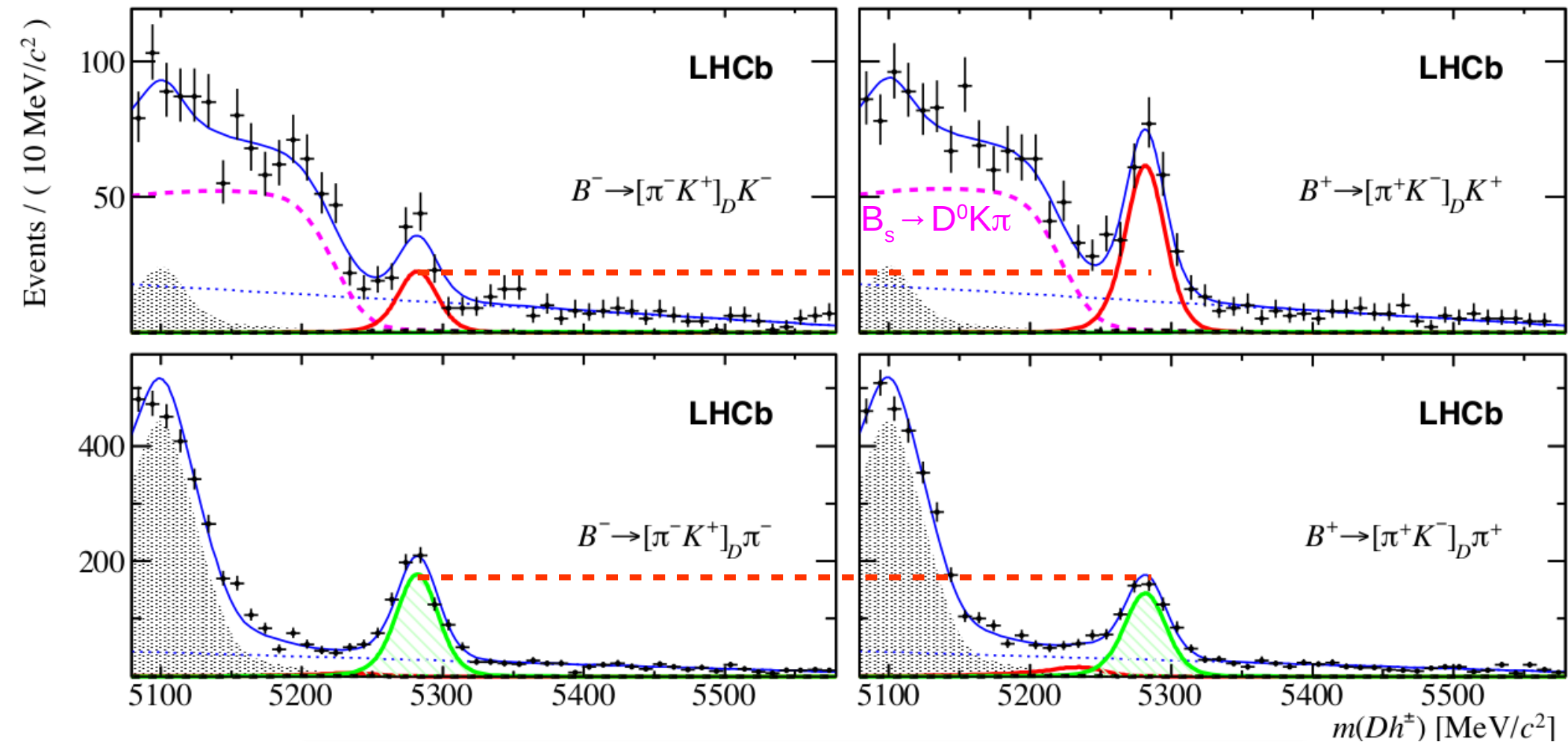
ADS 2-body



● $A_{\text{ADS}(K)}^{\pi K} = -0.403 \pm 0.056 \pm 0.011$

[arXiv:1603.08993 (2016)]

ADS 2-body



First observation of CPV in a single $B \rightarrow Dh$ mode : 8σ

$$\bullet A_{\text{ADS}(K)}^{\pi K} = -0.403 \pm 0.056 \pm 0.011$$

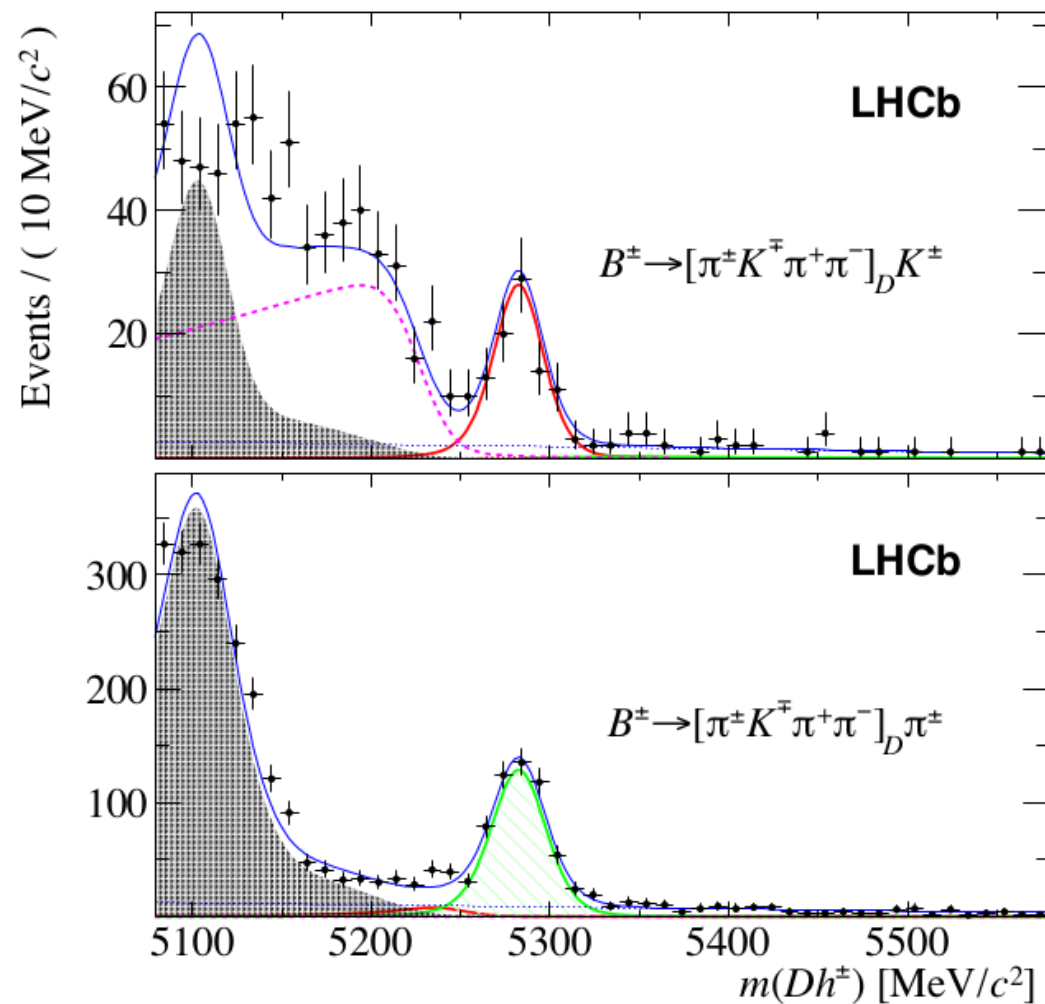
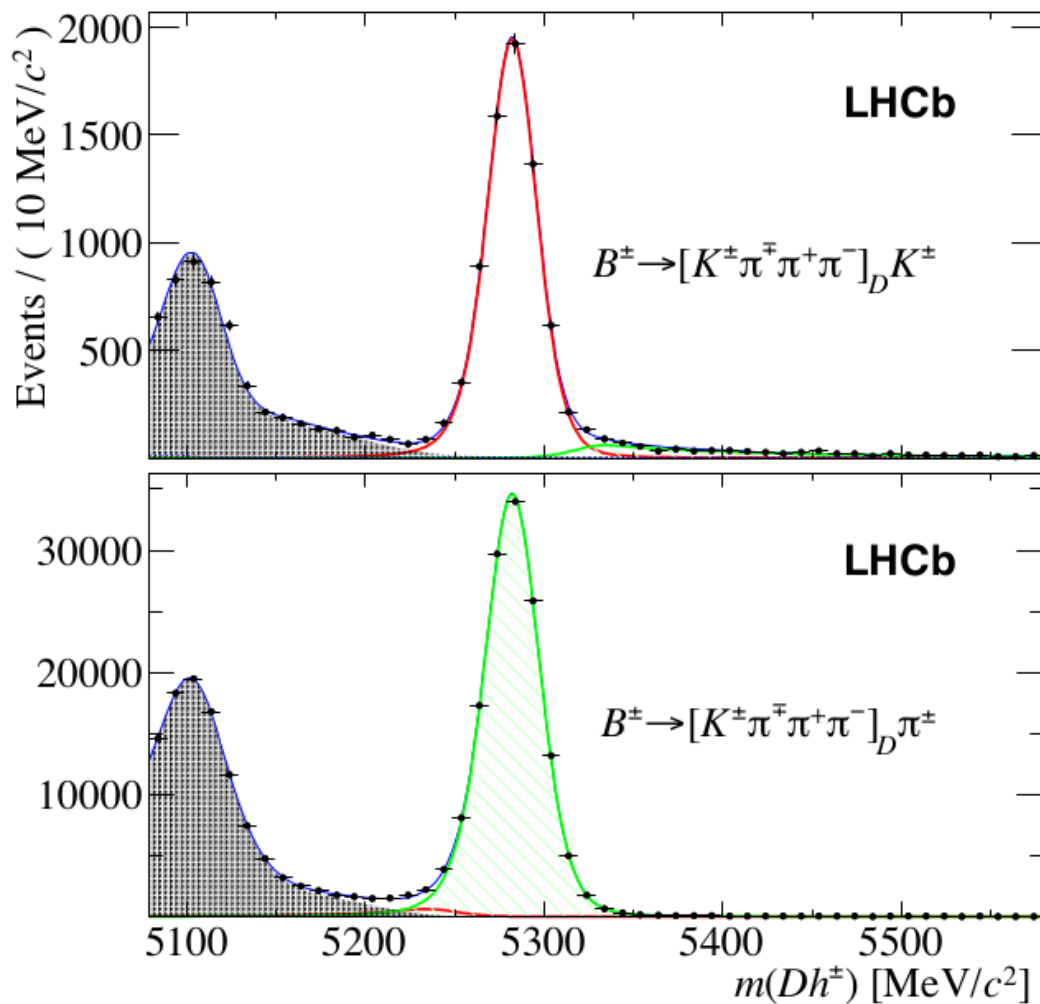
CPV in a rare decay: BR~10⁻⁷

[arXiv:1603.08993 (2016)]

Quasi-ADS: $D \rightarrow \pi K \pi \pi$

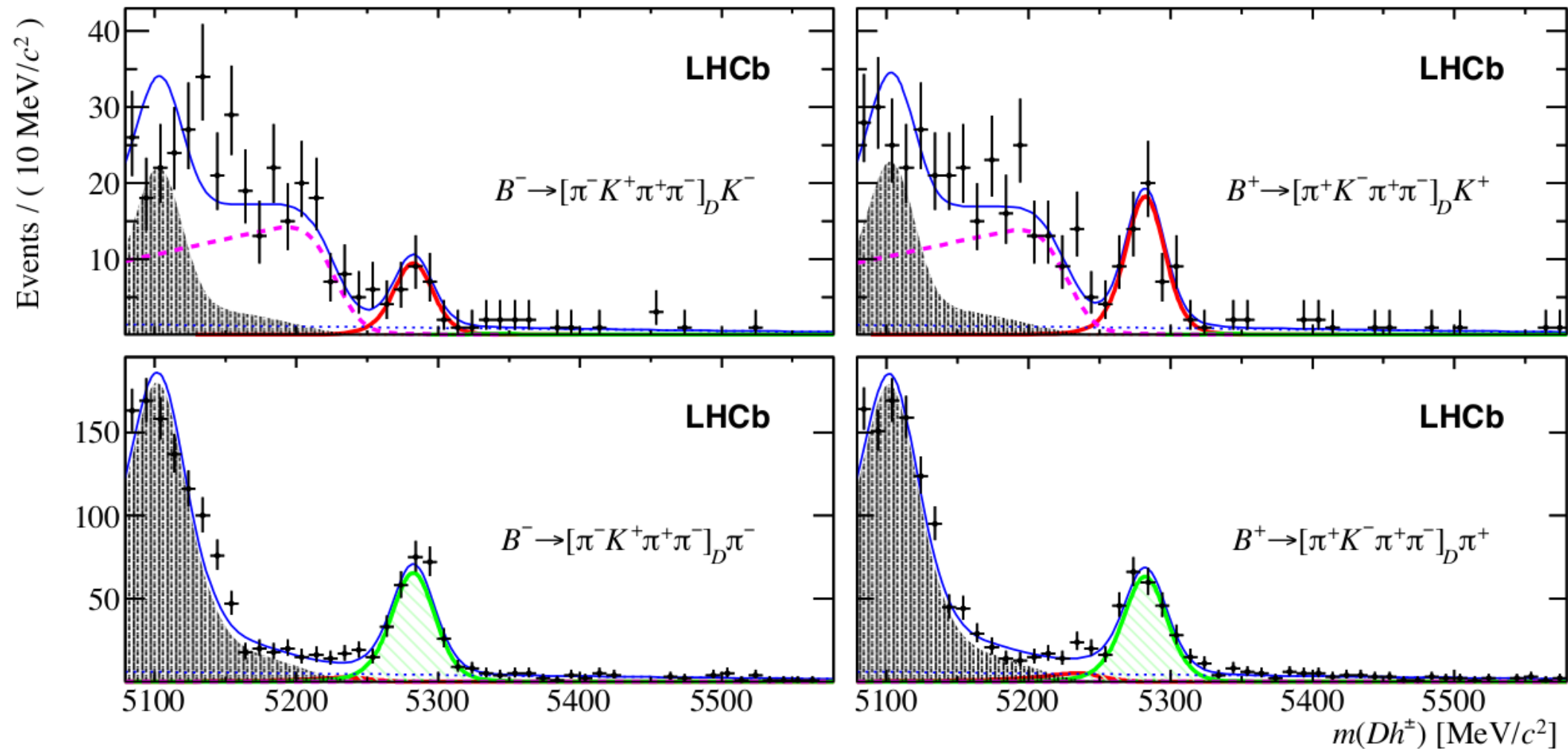
● 11300 $B^\pm \rightarrow DK^\pm, D \rightarrow K^+ \pi^- \pi^+ \pi^-$

● 160 $B^\pm \rightarrow DK^\pm, D \rightarrow \pi^+ K^- \pi^+ \pi^-$



[arXiv:1603.08993 (2016)]

Quasi-ADS: $D \rightarrow \pi K \pi \pi$



● $A_{\text{ADS}(K)}^{\pi K \pi \pi} = -0.313 \pm 0.102 \pm 0.038$

● A negative asymmetry is expected (same sign as for the 2-body ADS mode) from the value of δ_D [arXiv:1602.07430] ($A_{\text{ADS}(K)}^{\pi K} = -0.403 \pm 0.056 \pm 0.011$)

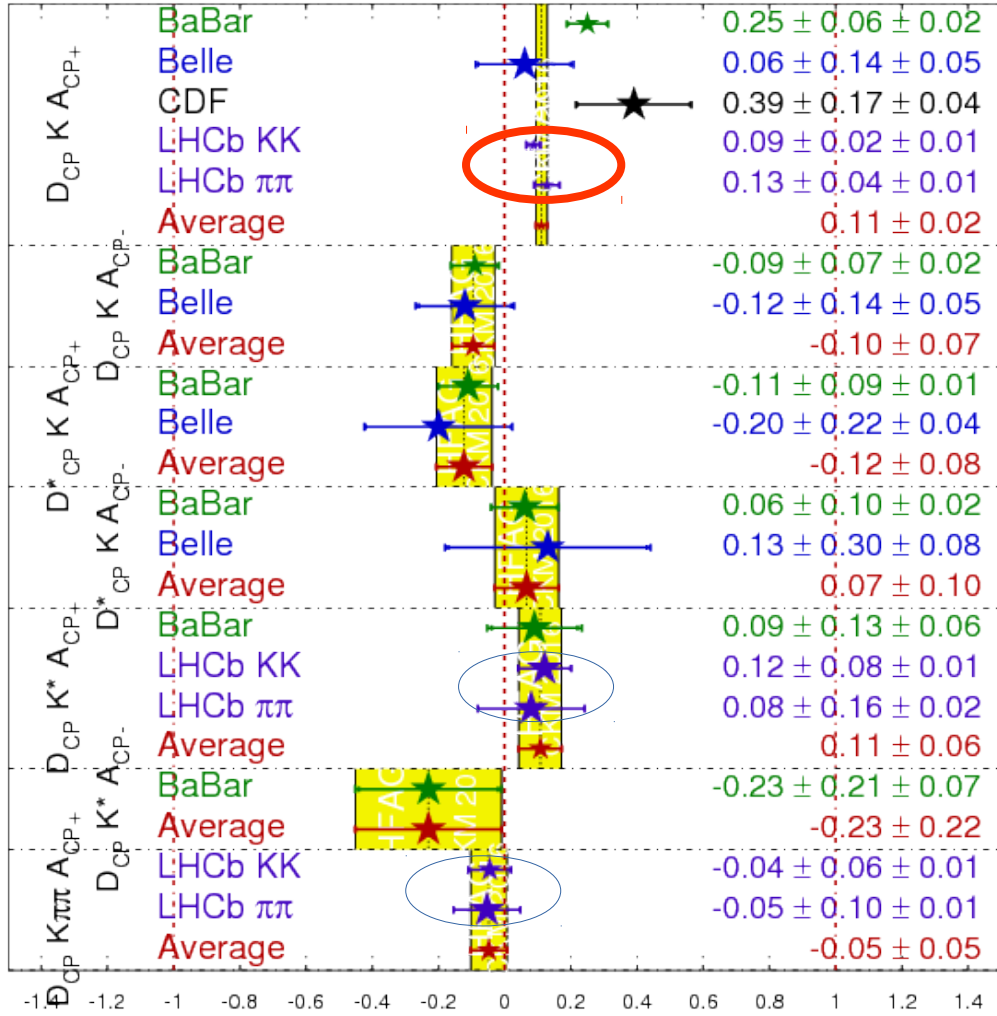
[arXiv:1603.08993 (2016)]

Summary $B^\pm \rightarrow Dh^\pm$, (quasi-)GLW/ADS modes
Combination of the modes

Summary of the $B_{\pm} \rightarrow DK_{\pm}$ modes: GLW

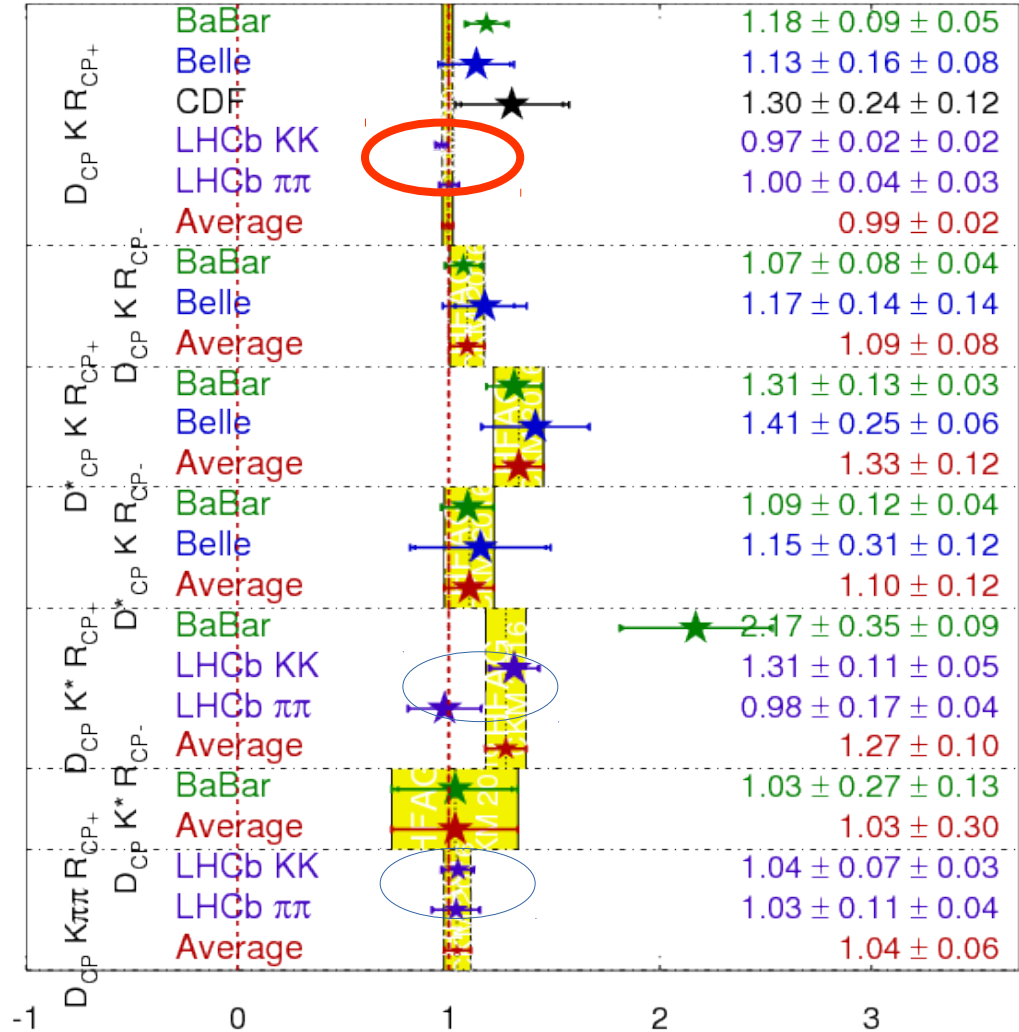
A_{CP} Averages

HFAG
CKM 2016
PRELIMINARY



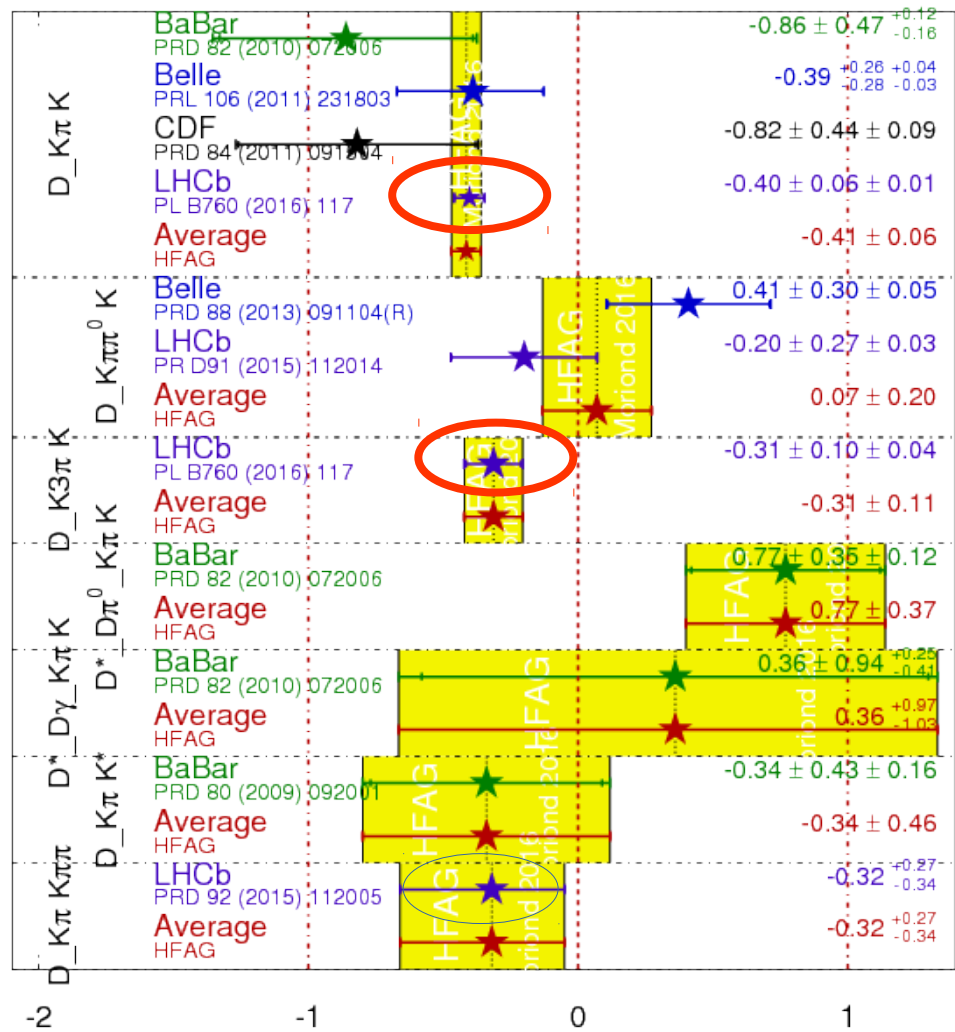
R_{CP} Averages

HFAG
CKM 2016
PRELIMINARY

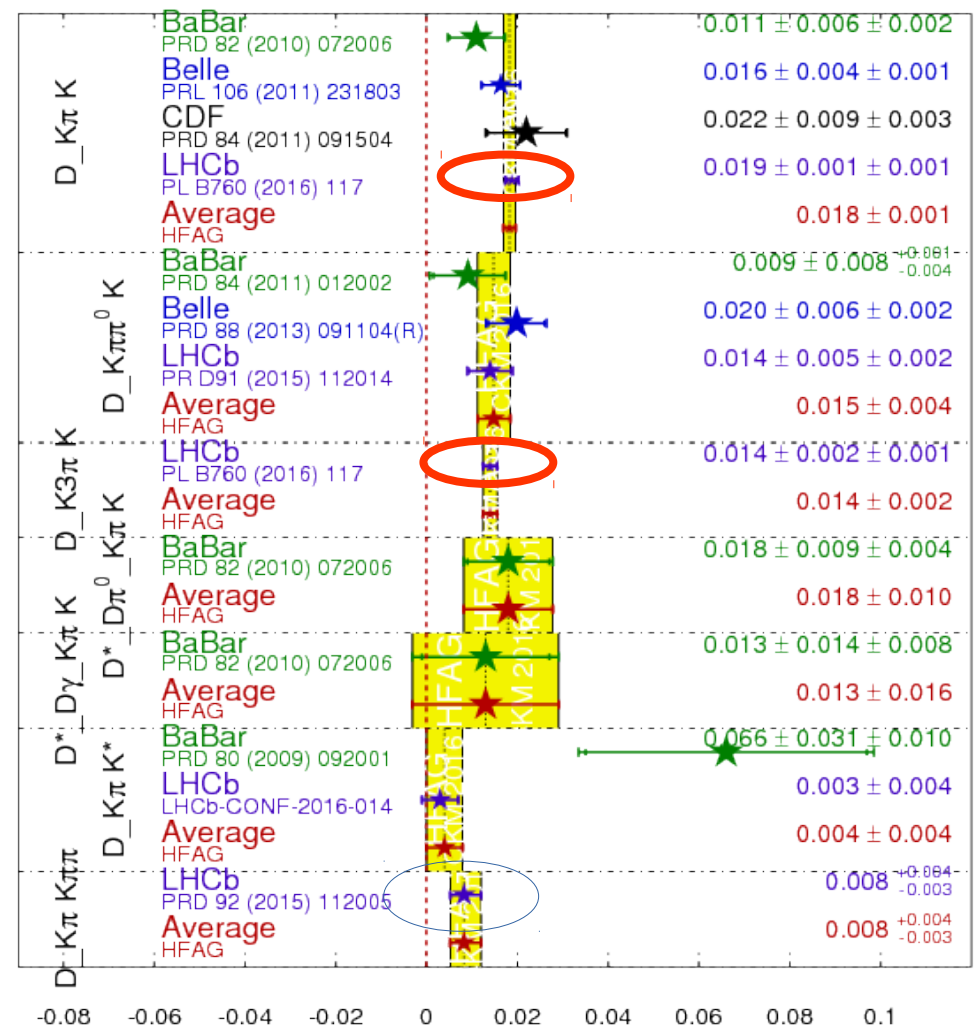


Summary of the $B^\pm \rightarrow DK^\pm$ modes: ADS

A_{ADS} Averages **HFAG** Moriond 2016 PRELIMINARY



R_{ADS} Averages **HFAG** CKM 2016 PRELIMINARY



$B^\pm \rightarrow DK^{*\pm}$ mode

What is measured ?

[LHCb-CONF-2016-014]

- The method uses the same interference as before in a new B final state $B^\pm \rightarrow DK^{*\pm}$
 - CP-eigenstates of the D decay, “GLW” type: $D \rightarrow KK, D \rightarrow \pi\pi$
 - Combinations of fav./sup. B/D decays, “ADS” type: $D \rightarrow K\pi$
- The physical observables are

$$A_{K\pi} = \frac{\Gamma(B^- \rightarrow D(K^- \pi^+) K^{*-}) - \Gamma(B^+ \rightarrow D(K^+ \pi^-) K^{*+})}{\Gamma(B^- \rightarrow D(K^- \pi^+) K^{*-}) + \Gamma(B^+ \rightarrow D(K^+ \pi^-) K^{*+})} \quad \sim \text{no interference, should be } \sim 0$$

$$A_{KK} = \frac{\Gamma(B^- \rightarrow D(KK) K^{*-}) - \Gamma(B^+ \rightarrow D(KK) K^{*+})}{\Gamma(B^- \rightarrow D(KK) K^{*-}) + \Gamma(B^+ \rightarrow D(KK) K^{*+})} \quad \dots \text{ and the other “GLW” related } A_{\pi\pi}$$

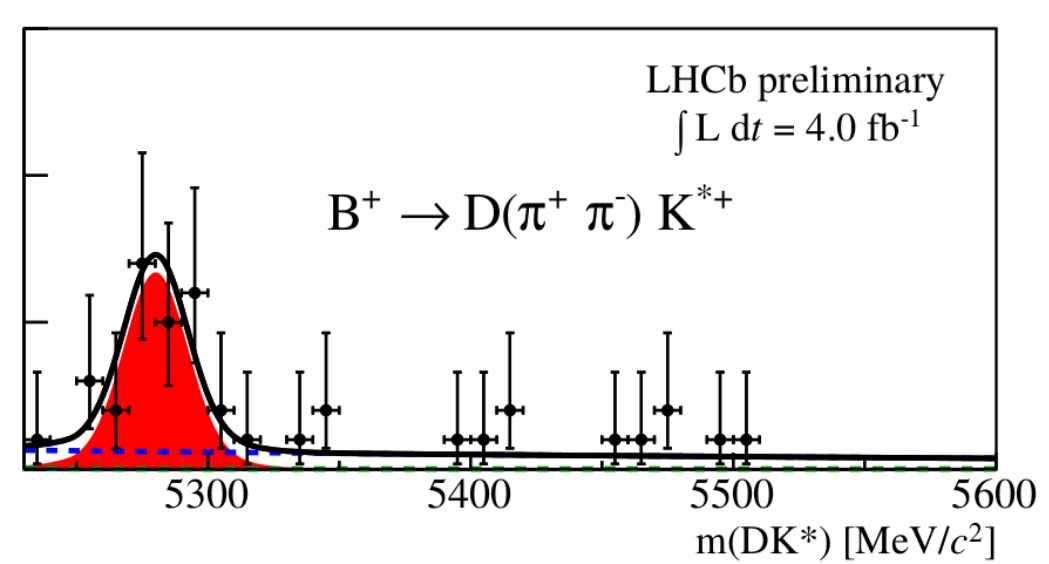
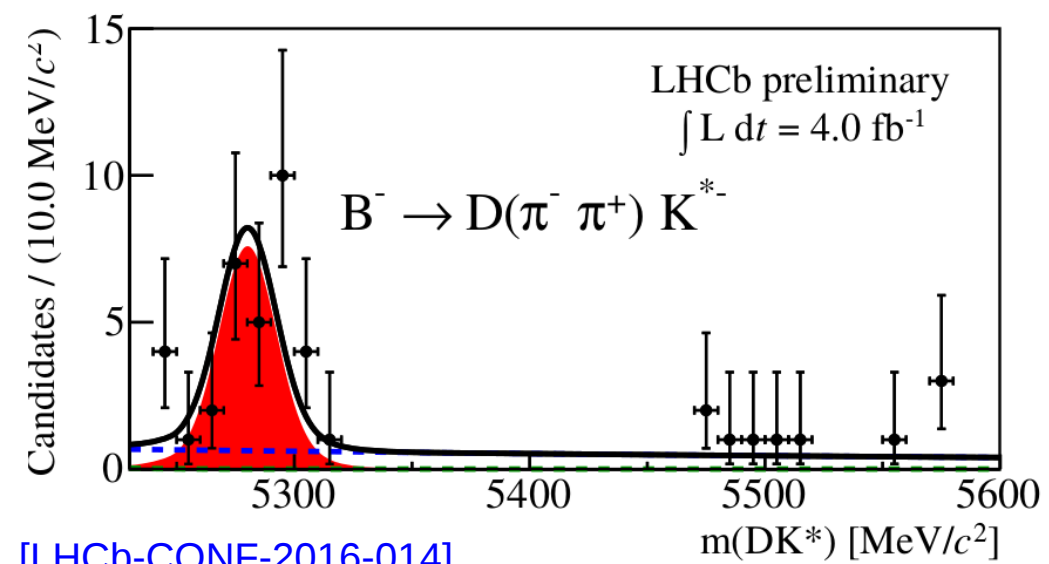
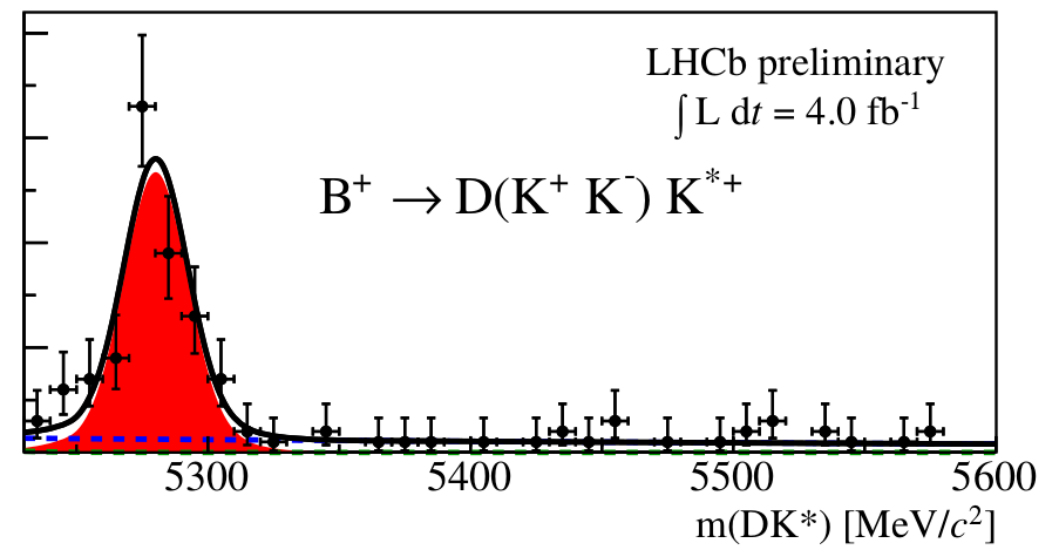
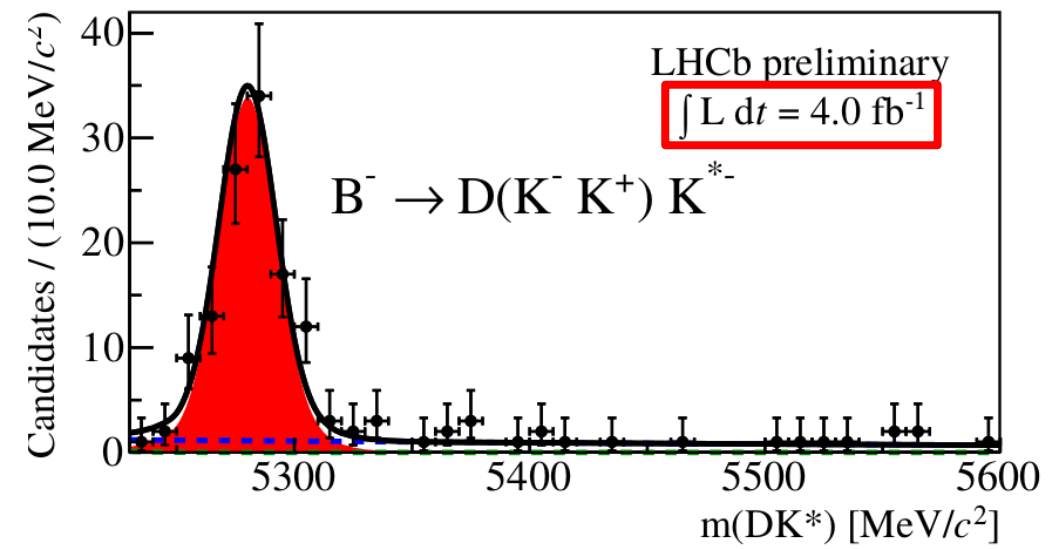
$$R_{KK} = \frac{\Gamma(B^- \rightarrow D(KK) K^{*-}) + \Gamma(B^+ \rightarrow D(KK) K^{*+})}{\Gamma(B^- \rightarrow D(K^- \pi^+) K^{*-}) + \Gamma(B^+ \rightarrow D(K^+ \pi^-) K^{*+})} \times \frac{BR(D^0 \rightarrow K^- \pi^+)}{BR(D^0 \rightarrow KK)} \quad \dots \text{ and similarly } R_{\pi\pi}$$

$$R^+ = \frac{\Gamma(B^+ \rightarrow D(K^- \pi^+) K^{*+})}{\Gamma(B^+ \rightarrow D(K^+ \pi^-) K^{*+})} \quad \dots \text{ and the other “ADS” related ratio } R^-$$

...that depend on r_B, δ_B, κ and γ κ accounts for non-resonant DK(892)* bkg and is extracted from amplitude models

Different from the previous ones

CP-eigenstate modes

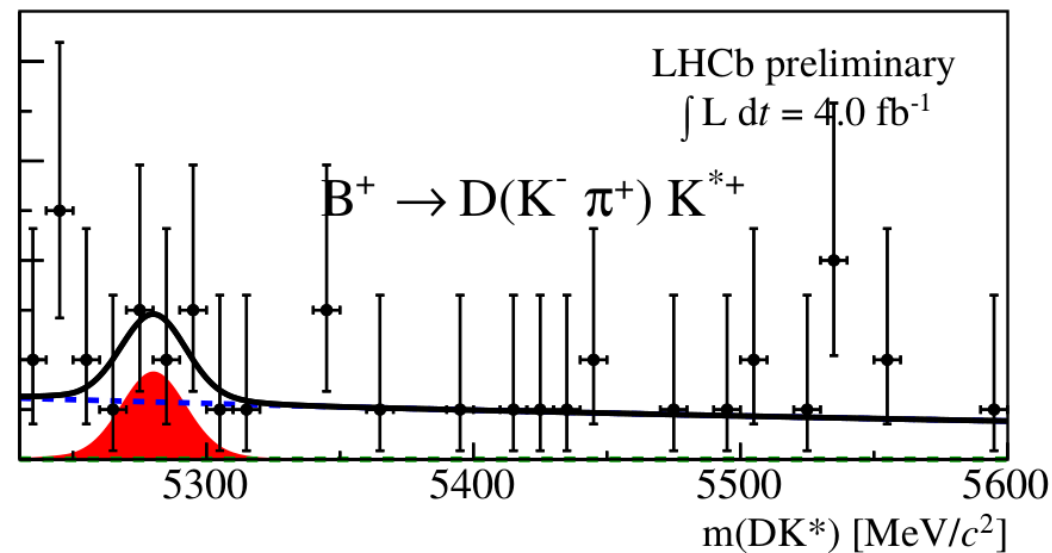
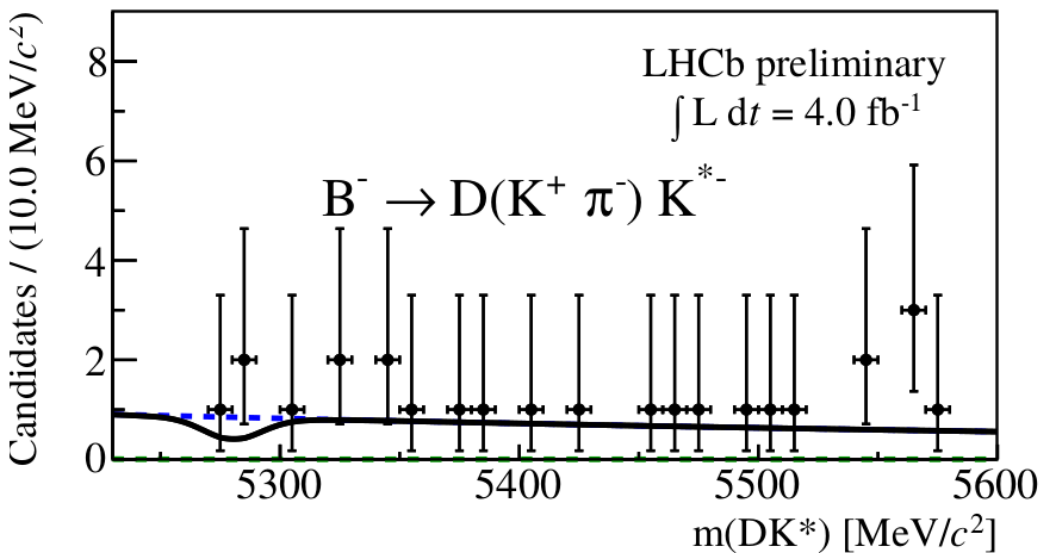


[LHCb-CONF-2016-014]

- $A_{KK} = 0.12 \pm 0.08 \pm 0.01$
- $A_{\pi\pi} = 0.08 \pm 0.16 \pm 0.02$

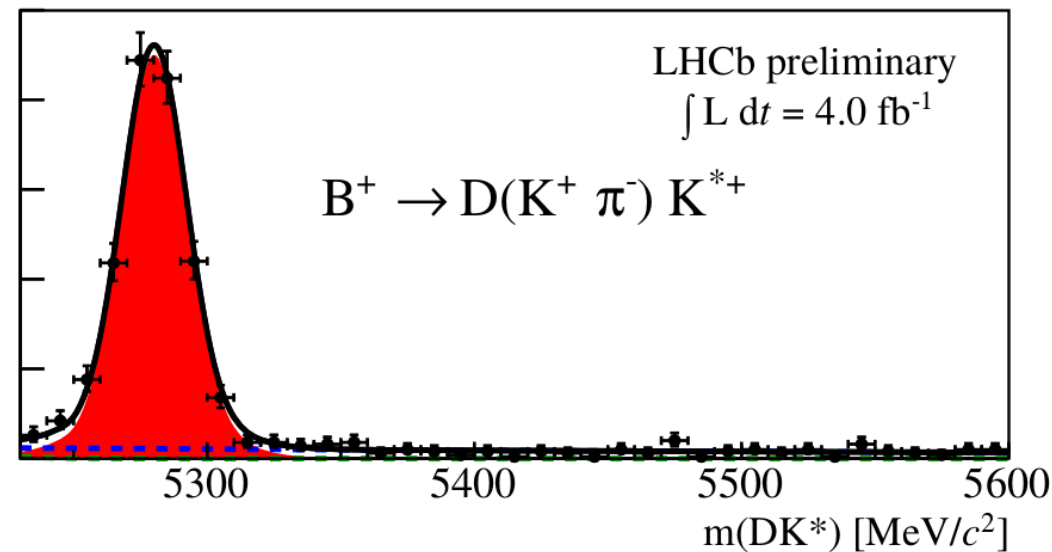
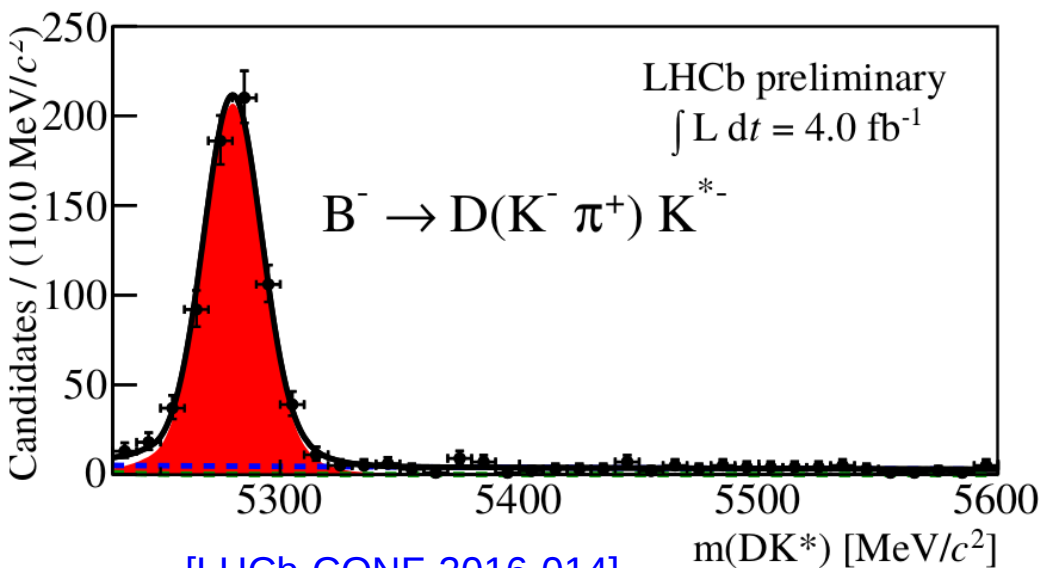
- $R_{KK} = 1.31 \pm 0.11 \pm 0.05$
- $R_{\pi\pi} = 0.98 \pm 0.17 \pm 0.04$

ADS modes



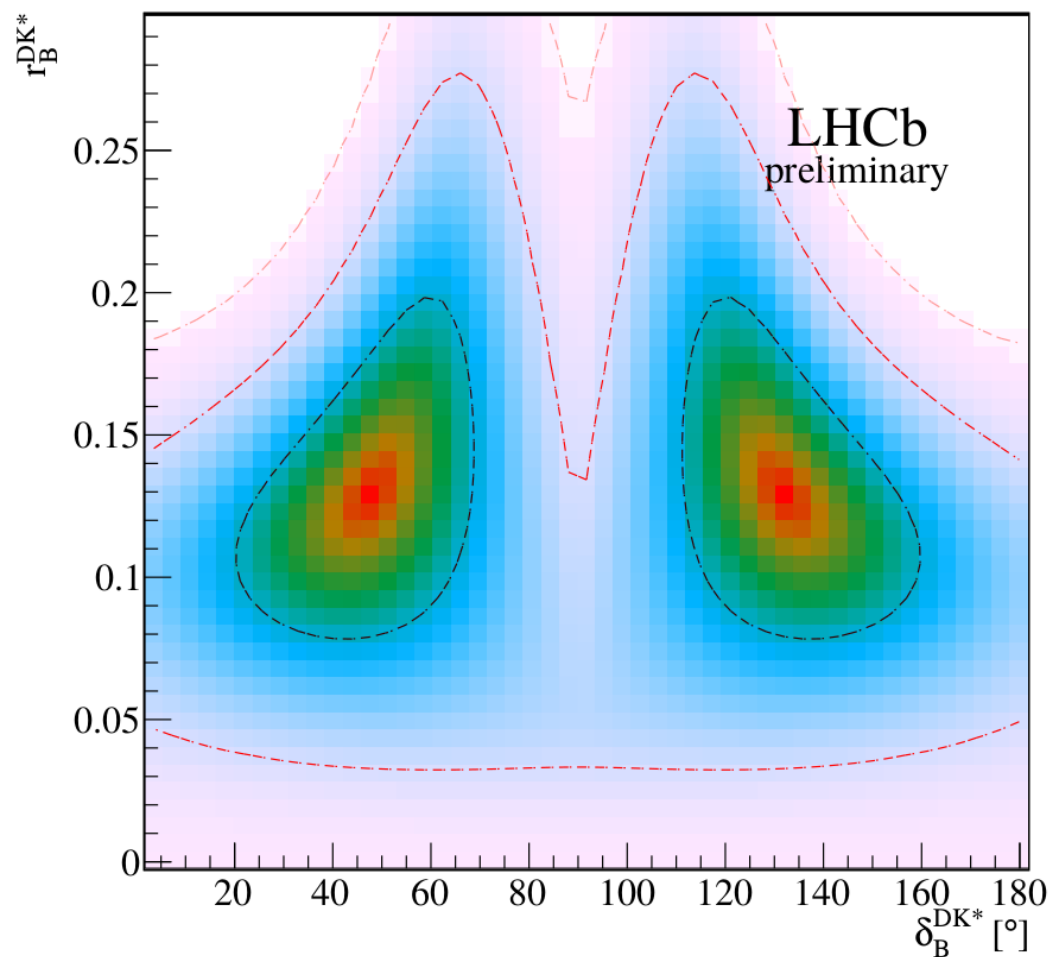
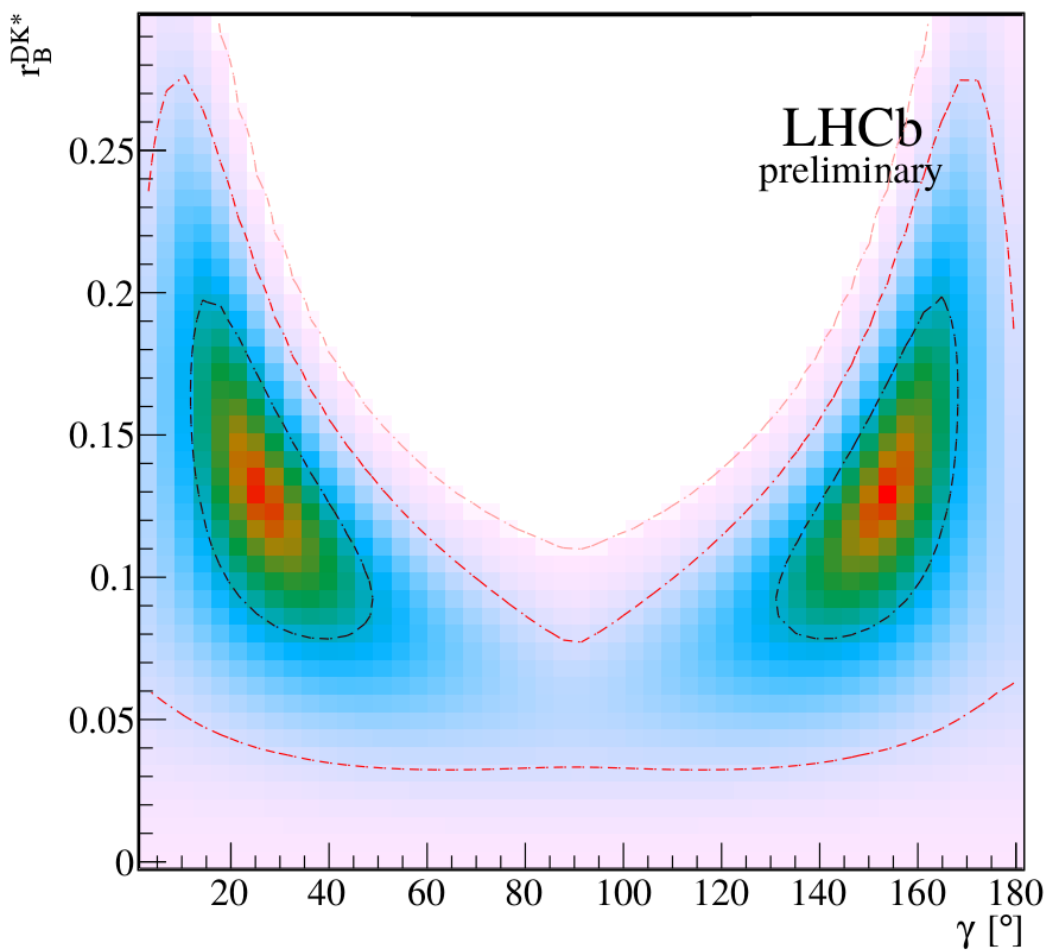
● $R^+ = 0.009 \pm 0.007 \pm 0.002$

● $R^- = -0.003 \pm 0.004 \pm 0.002$



[LHCb-CONF-2016-014]

Interpretation in terms of γ

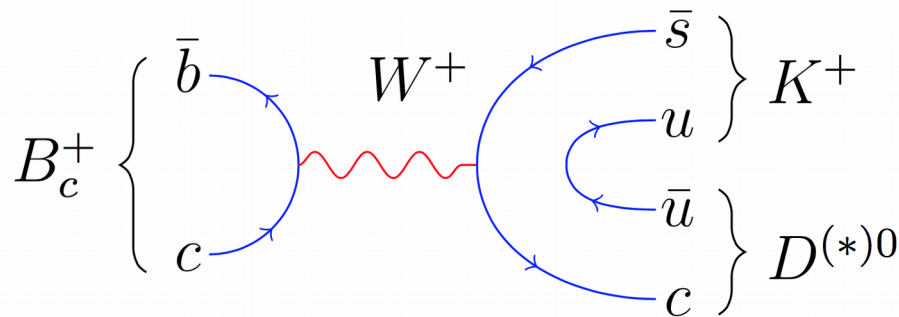


- The data sample is not large enough to exclude large regions of the parameter space, but the result is consistent with $\gamma \sim 70^\circ$

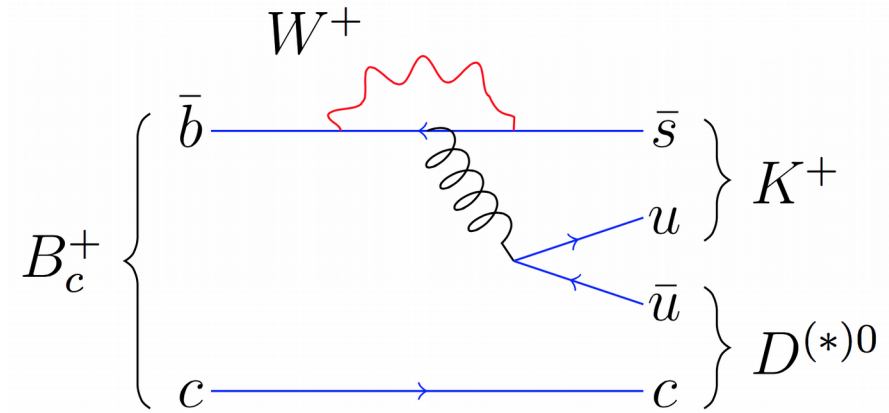
[LHCb-CONF-2016-014]

$B_c^+ \rightarrow D^0 K^+$ mode

- $B_c^+ \rightarrow D^0 h^+$ decays probe processes that are as-yet unobserved with B_c mesons:



Annihilation

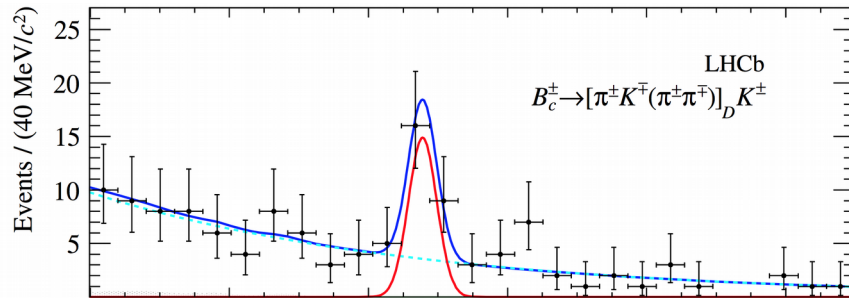


Penguin

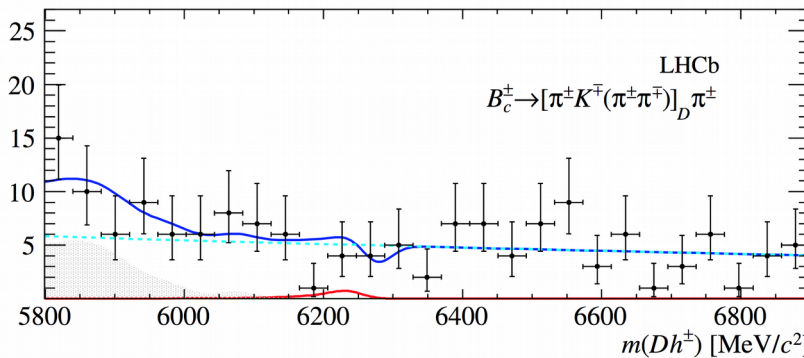
- Extend the ADS-mode reconstruction to higher $m(D^0 h^+)$ invariant mass, using both $D^0 \rightarrow K^+ \pi^-$ and $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$ final states.
- Signal yields are normalized to the favoured $B_u^- \rightarrow D^0 h^-$ mode to quote a branching fraction multiplied by the production ratio:

$$r_{B_c}^{D^{(*)}h} = \frac{f_c}{f_u} \times BR(B_c^+ \rightarrow D^{(*)0} h^+)$$

- Signal observed in $D^0 K^+$ with 5.1σ significance. Nothing in $D^0 \pi^+$



$$r_{B_c}^{DK} = (9.3_{-2.5}^{+2.8} \pm 0.6) \times 10^{-7}$$



$$r_{B_c}^{D\pi} < 3.9 \times 10^{-7} \quad \text{at } 95\% \text{ CL}$$

- f_c/f_u is approx. $\sim 1/200$, this implies a branching fraction $\sim 2 \times 10^{-4}$

- Predictions are a factor ~ 3 smaller: 6.7×10^{-5} <https://arxiv.org/abs/0905.0945v1>
 4.8×10^{-5} Eur. Phys. J. C 5 (1998) 705

- f_c/f_u cancels when compared to equivalent $B_c \rightarrow J/\psi \pi$ result

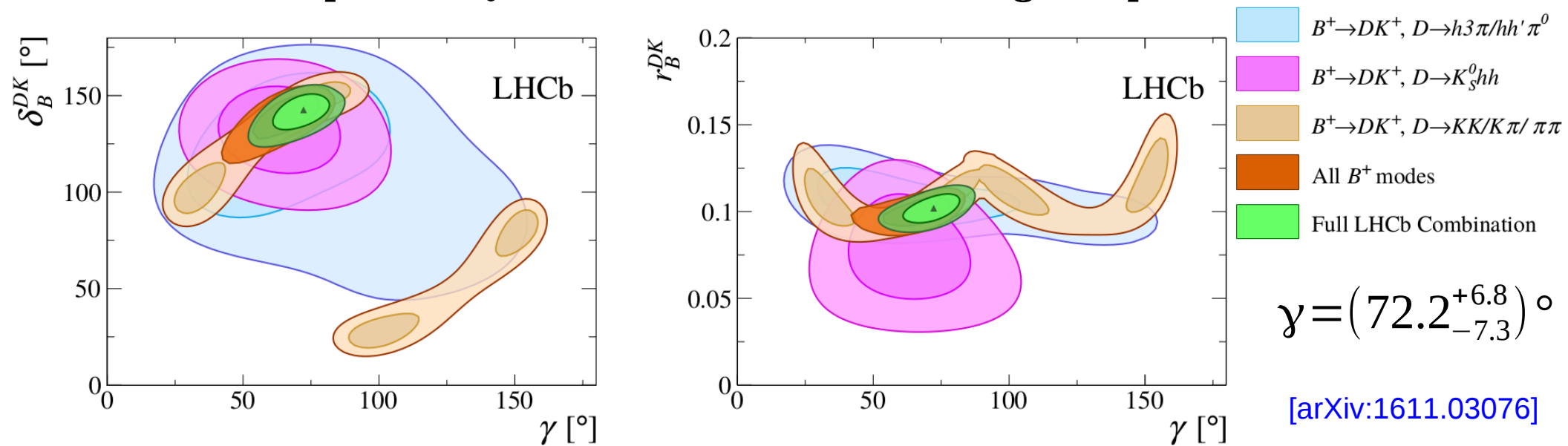
$$\frac{BR(B_c^+ \rightarrow D^0 K^+)}{BR(B_c^+ \rightarrow J/\psi \pi^+)} = 0.13 \pm 0.04 \pm 0.01 \pm 0.01$$

<https://arxiv.org/abs/1411.2943>

Conclusion

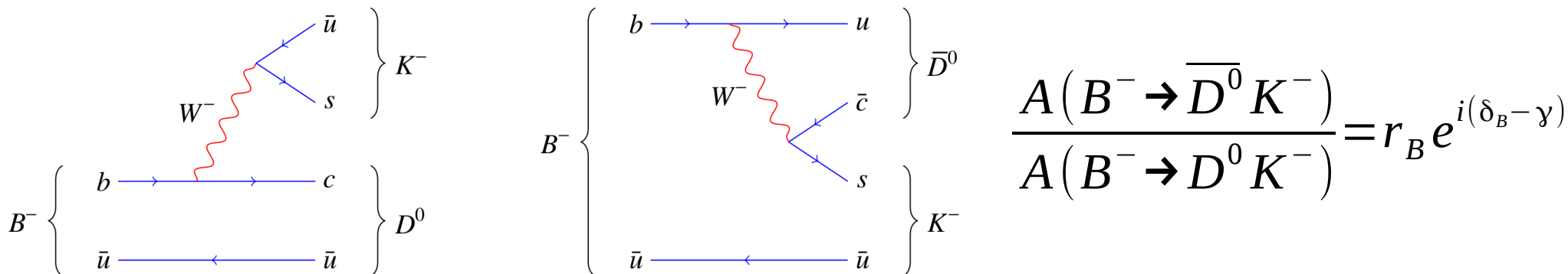
Conclusion

- The most precise γ measurement from a single experiment



- Latest $B \rightarrow DK$ measurements published include new modes
- $B \rightarrow DK^*$ measurement done with 4fb^{-1}
 - not included in combination yet
- Continuing to expand the B and subsequent D modes analysed e.g.
 - $B \rightarrow D^* K$ ADS/GLW/GGSZ analyses
 - $B^\pm \rightarrow D^* K^\pm, D^* \rightarrow D\gamma/\pi^0$
 - $D \rightarrow KK/\pi\pi/K\pi/K_s^0\pi^+\pi^-/K_s^0K^+K^-$

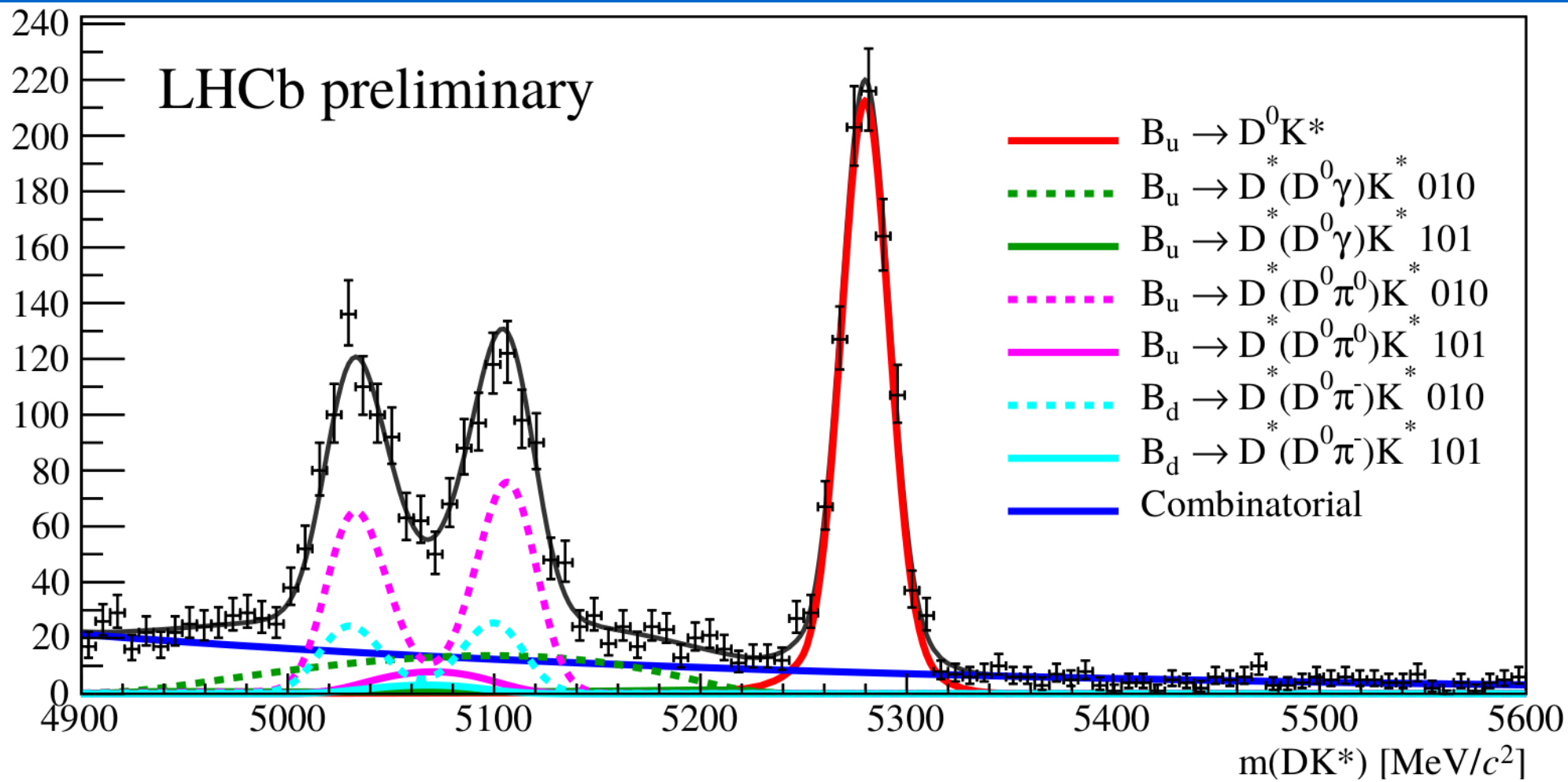
Backup



- The main hadronic parameters are the amplitude ratio r_B and the CP-conserving phase γ
- Several methods permit to exhibit the interference

GLW: $D \rightarrow K^+ K^-$ $\pi^+ \pi^-$ $K_s \pi^0$	ADS: $D \rightarrow \pi^- K^+$	Quasi-ADS: $D \rightarrow \pi^- K^+ \pi^+ \pi^-$ $\pi^- K^+ \pi^0$
GGSZ: $D \rightarrow K_s \pi^+ \pi^-$ $K_s K^+ K^-$	Quasi-GLW: $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ $K^+ K^- \pi^0$ $\pi^+ \pi^- \pi^0$	GLS: $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ $K^+ K^- \pi^0$ $\pi^+ \pi^- \pi^0$

Candidates / (7.0 MeV/c²)

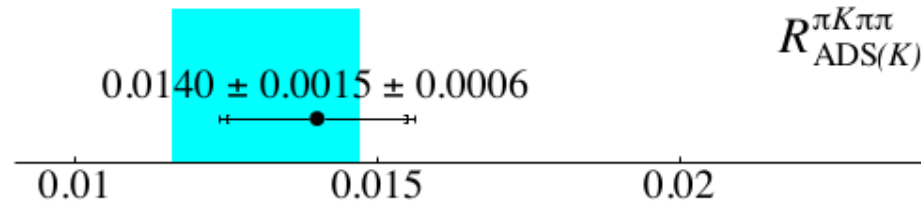
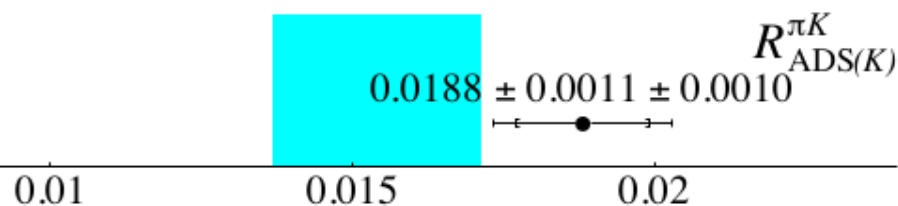
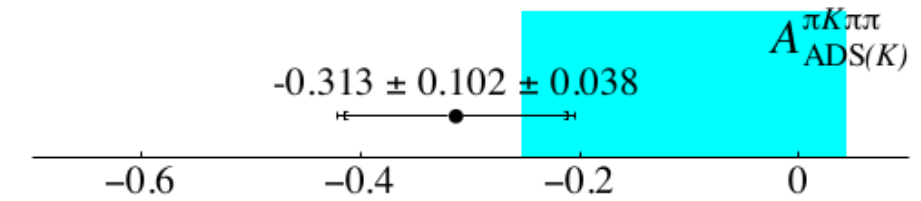
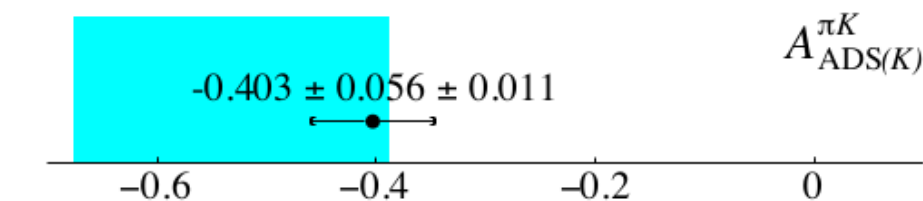


Summary of the $B^\pm \rightarrow DK^\pm$ modes

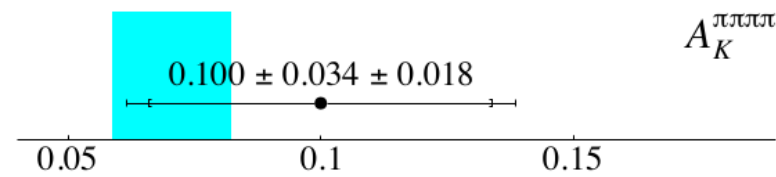
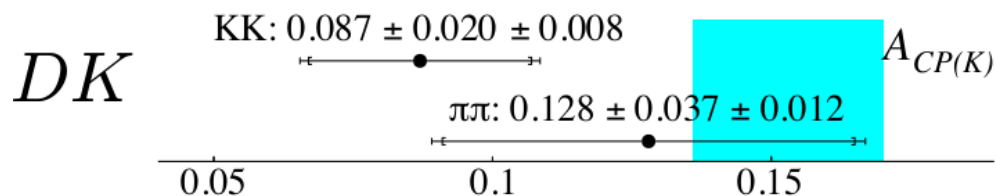
[arXiv:1603.08993]

 = SM 1σ expectation from knowledge of r_B, δ_B, γ

- Significant improvement in knowledge of the ADS observables:

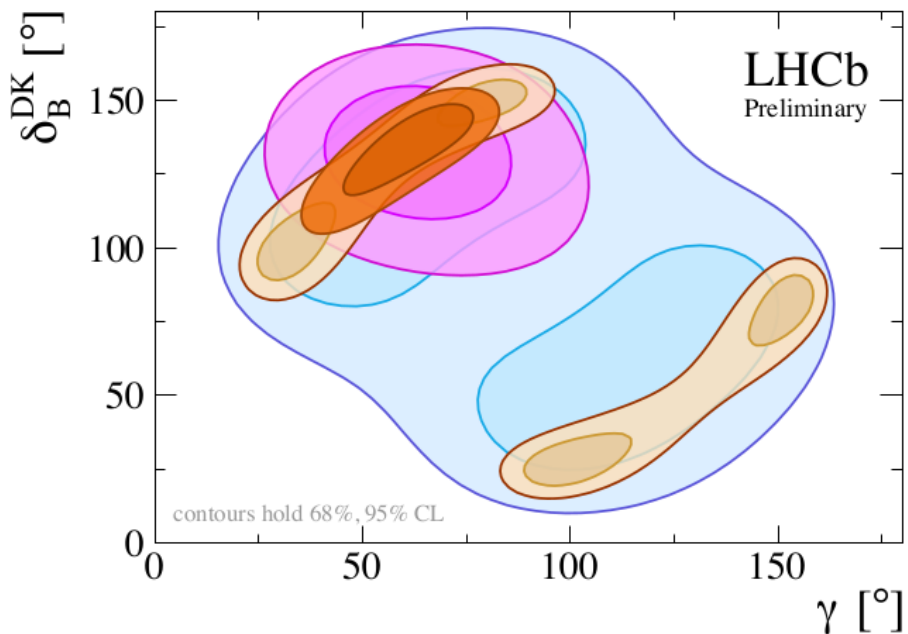
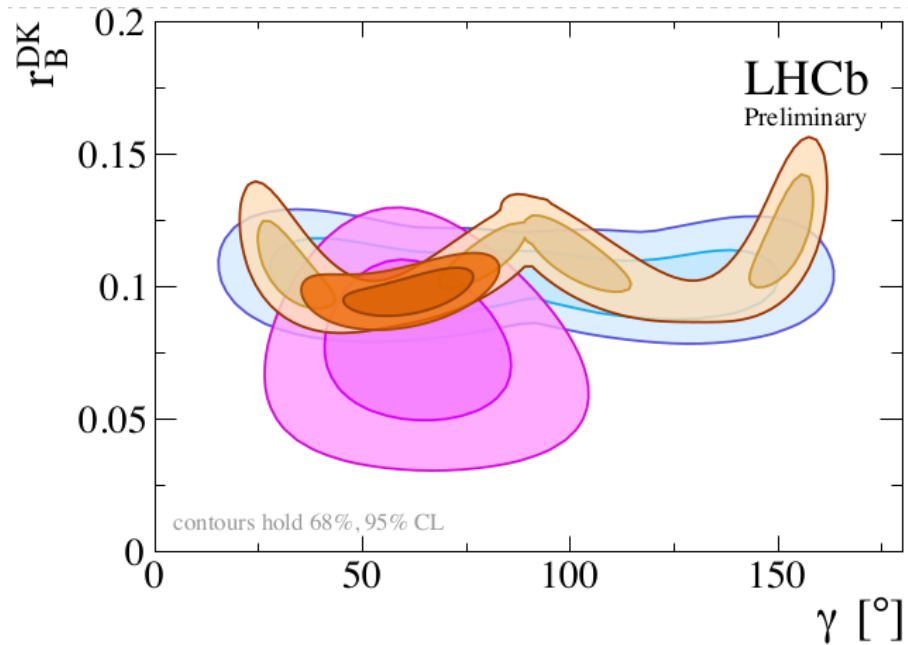


- DK charge asymmetries:



- Result of partial width consistent with expectation
- $D\pi$ mode will provide constraints on upcoming $DK+D\pi$ combination

Combination of the B^\pm modes



B^\pm combination

- $B^+ \rightarrow DK^+, D \rightarrow h3\pi/hh'\pi^0$
- $B^+ \rightarrow DK^+, D \rightarrow K_S hh$
- $B^+ \rightarrow DK^+, D \rightarrow KK/K\pi/\pi\pi$
- All B^+ modes