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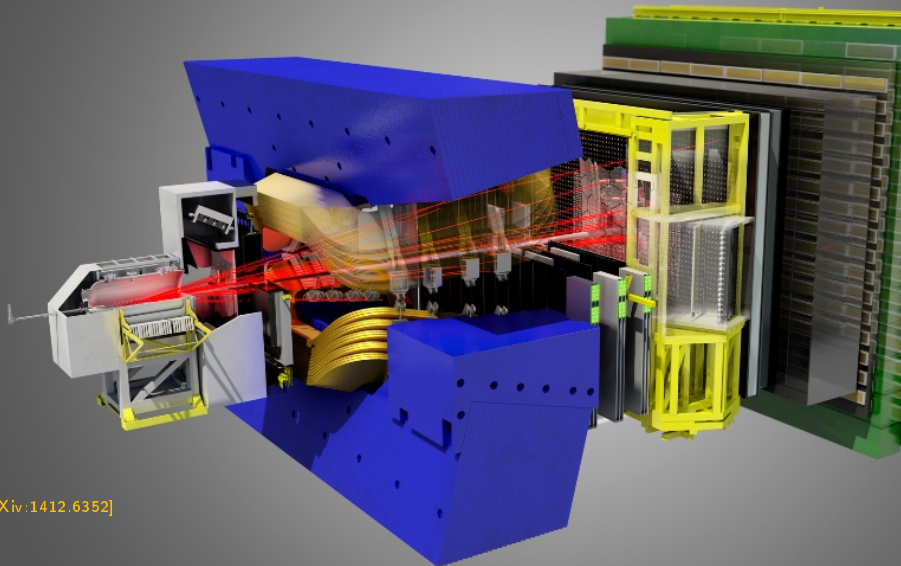
# Measurements of mixing and indirect CPV in two-body charm decays at LHCb

Kevin S. Maguire, on behalf of LHCb and University of Manchester

CKM2016, TIFR Mumbai, December 1st, 2016

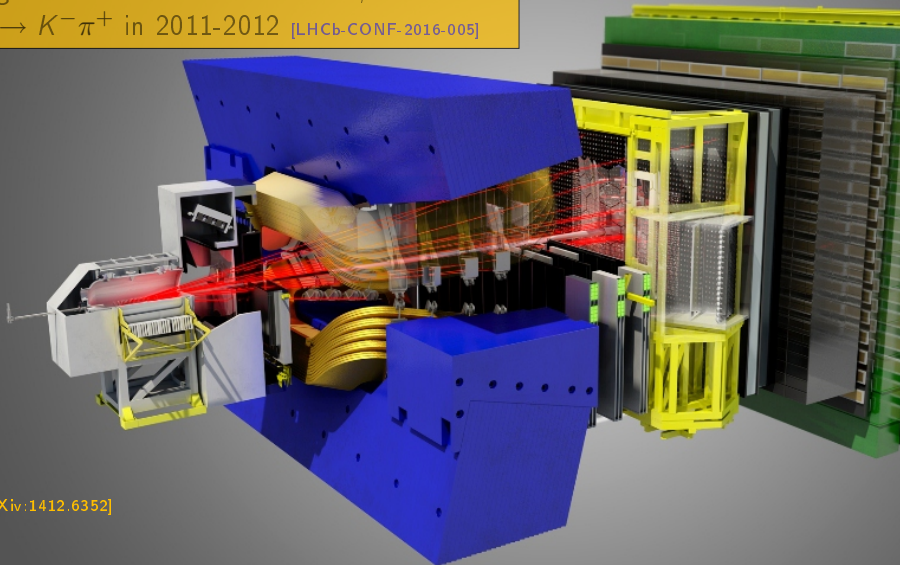


# Charm at LHCb



[arXiv:1412.6352]

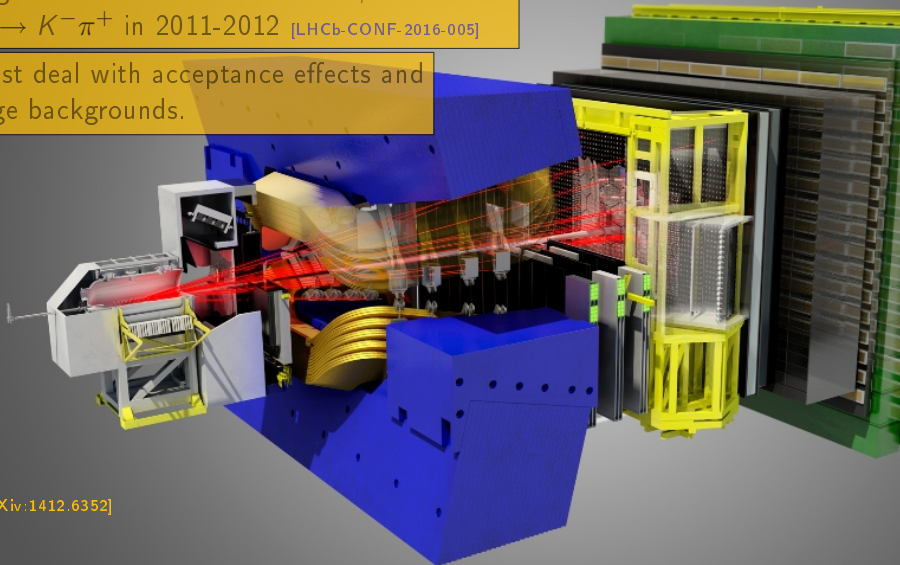
Huge datasets of charm at LHCb, 630 million  
 $D^0 \rightarrow K^- \pi^+$  in 2011-2012 [LHCb-CONF-2016-005]



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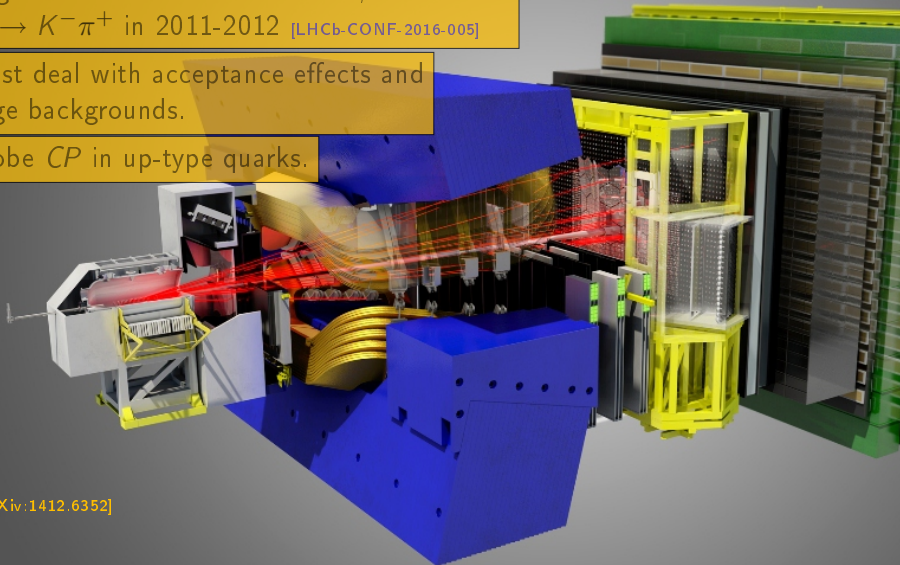


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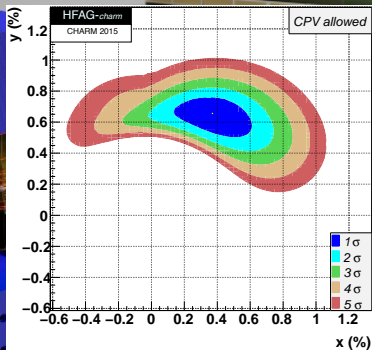


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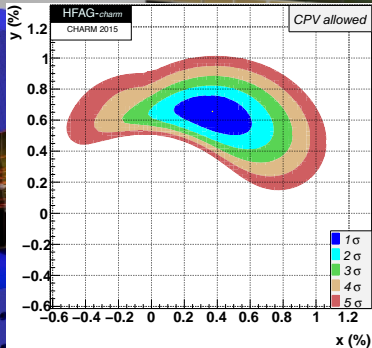
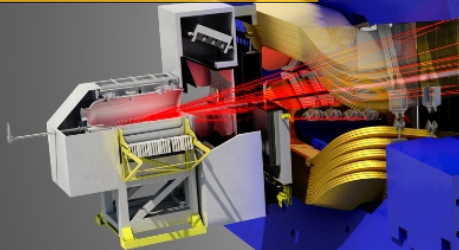
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$D^0$  mixing already established.

$CP$  violation not observed in  $D$  system.

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- 1  $A_{\Gamma}$  measurements in  $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ .
- 2 Charm mixing and CPV ( $R(t)^{\pm}$ ) in  $D^0 \rightarrow K^{\pm}\pi^{\mp}$ .

# $A_\Gamma$ measurements

- 1 Unbinned maximum likelihood of effective decay times [[LHCb-CONF-2016-010](#)].
  - $2 \text{ fb}^{-1}$  collected in 2012, and combined with a previous measurement on  $1 \text{ fb}^{-1}$  from 2011 data [[Phys. Rev. Lett., 112:041801, 2014.](#)].

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- 
- Both flavour tagged with  $D^{*+} \rightarrow D^0 \pi^+$ .
  - Same dataset and selection, except for one condition.
  - A paper including both measurements is in preparation.

- Asymmetry of the effective decay widths,  $\hat{\Gamma}(D^0 \rightarrow f)$  to  $CP$ -eigenstates  $f$ ,

$$A_\Gamma = \frac{\hat{\Gamma}(D^0 \rightarrow f) - \hat{\Gamma}(\bar{D}^0 \rightarrow f)}{\hat{\Gamma}(D^0 \rightarrow f) + \hat{\Gamma}(\bar{D}^0 \rightarrow f)}.$$

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- Improvements in precision are now valuable for testing SM predictions.

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- represent CPV in **mixing** and in the **interference** of decays.
- $x$  and  $y$  are the charm mixing parameters,
- $\phi = \arg((q\bar{A}_f)/(pA_f))$ ,
- where  $A_f(\bar{A}_f)$  is the amplitude of  $D^0 \rightarrow f(\bar{D}^0 \rightarrow f)$  decay,
- $|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$ .

- Measure the  $D^0$  and  $\bar{D}^0$  effective lifetimes,  $\hat{\tau} = 1/\hat{\Gamma}(D^0 \rightarrow f)$

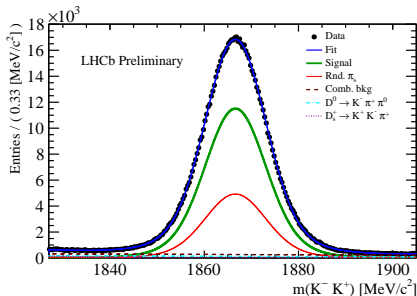
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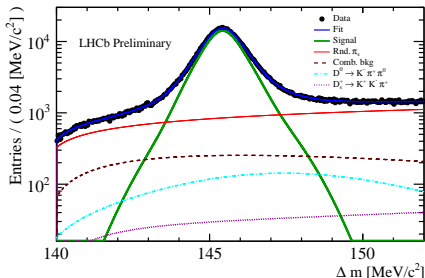


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- First stage:

$D^0$  Invariant mass



$\Delta m = D^{*+} - D^0$  mass difference

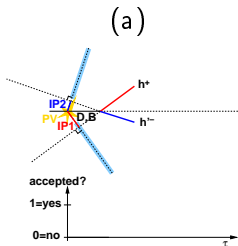


- Event selection introduces a lifetime bias.

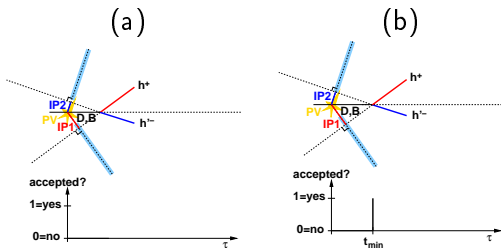
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- Move the PV along the momentum direction of the  $D^0$  and recalculate the selection.

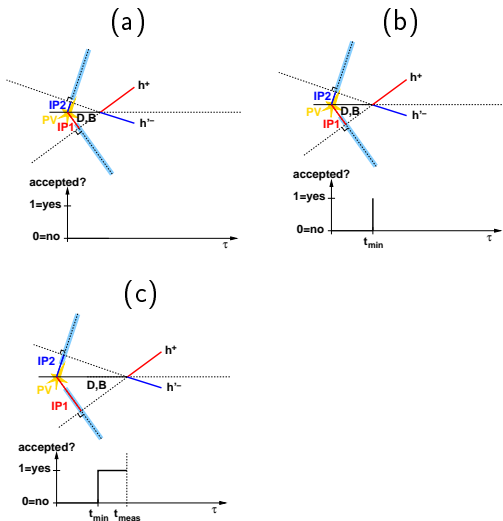
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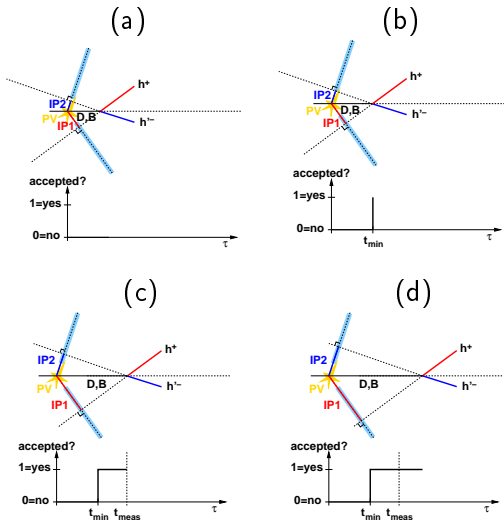
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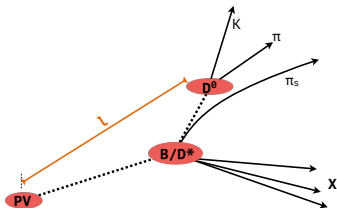


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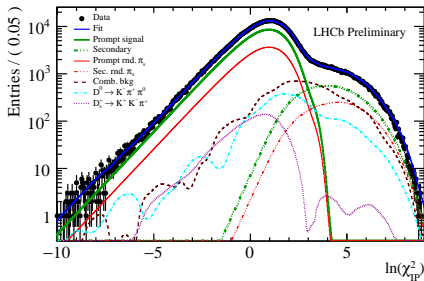
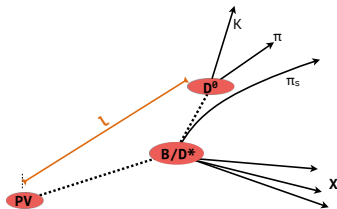




- Irreducible background of  $D^0$  from a long lived particle, like  $B^0$ .



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- Separated using  $\ln(\chi_{IP}^2)$ . Where  $\chi_{IP}^2$  is defined as the difference between the  $\chi^2$  of the PV reconstructed with and without the considered particles.



- Per-candidate probability density function (PDF) for prompt signal:

$$f(t|sig., prompt) = \frac{1}{\tau} e^{-t'\tau} \otimes R(t', t)$$

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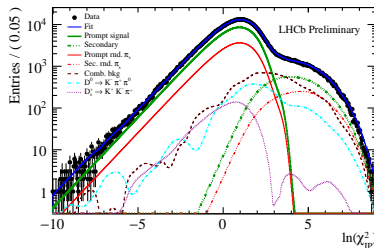
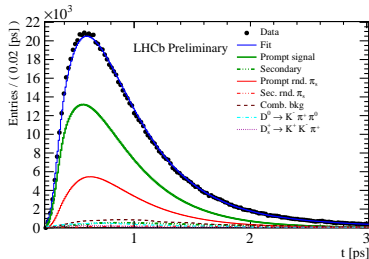
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- Second Stage:

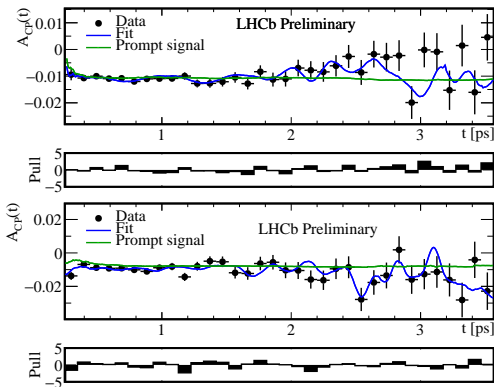


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- Result: pseudo- $A_{\Gamma} = (-0.07 \pm 0.15) \times 10^{-3}$ .



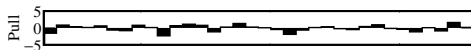
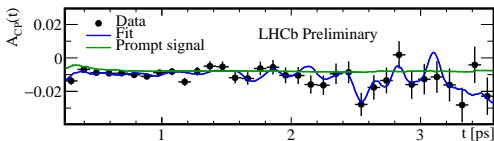
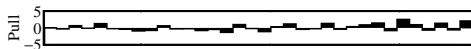
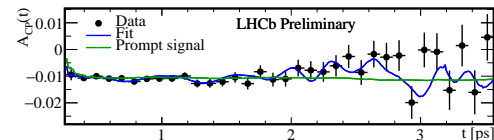
- $A_F$  for the Cabibbo favoured mode  $D^0 \rightarrow K^- \pi^+$  should be zero.
- Result: pseudo- $A_F = (-0.07 \pm 0.15) \times 10^{-3}$ .



Preliminary  
 $K^+ K^-$   $2 \text{ fb}^{-1}$  Result:  
 $(-0.03 \pm 0.46 \pm 0.10) \times 10^{-3}$

Preliminary  
 $\pi^+ \pi^-$   $2 \text{ fb}^{-1}$  Result:  
 $(0.03 \pm 0.79 \pm 0.16) \times 10^{-3}$

- $A_{CP}$  for the Cabibbo favoured mode  $D^0 \rightarrow K^- \pi^+$  should be zero.
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 $K^+ K^-$  2 fb<sup>-1</sup> Result:  
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 $\pi^+ \pi^-$  2 fb<sup>-1</sup> Result:  
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- Main systematics from **mismodelling** of low decay-time, **secondary** contamination, ignored **correlations** and **combinatoric** backgrounds.

- This result is combined with the previous LHCb measurement with  $1 \text{ fb}^{-1}$  [*Phys. Rev. Lett.*, 112:041801, 2014.].

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Preliminary: [[LHCb-CONF-2016-010](#)]

$$A_{\Gamma}(D^0 \rightarrow K^+ K^-) = (-0.14 \pm 0.37 \pm 0.10) \times 10^{-3},$$

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$$\Delta A_{\Gamma} = (0.28 \pm 0.73 \pm 0.05) \times 10^{-3},$$

$$A_{\Gamma} = (-0.07 \pm 0.32 \pm 0.11) \times 10^{-3},$$

- Simple counting experiment in bins of decay time.

$$A_{\text{raw}}^i = \frac{n_i(D^0 \rightarrow f) - n_i(\bar{D}^0 \rightarrow f)}{n_i(D^0 \rightarrow f) + n_i(\bar{D}^0 \rightarrow f)} \quad i = 1, \dots, m$$

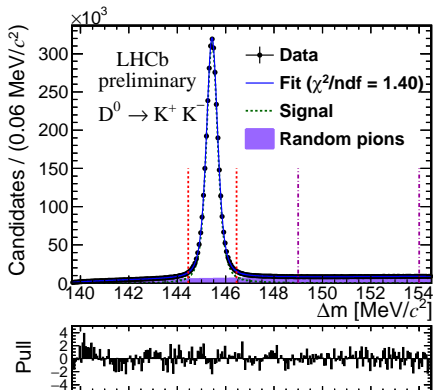
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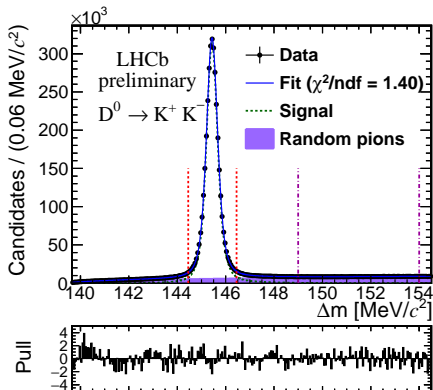
- Straight line fit.

$$A_{\text{raw}}(t) = A_0 - \frac{t}{\tau_{D^0}} A_{\Gamma}$$

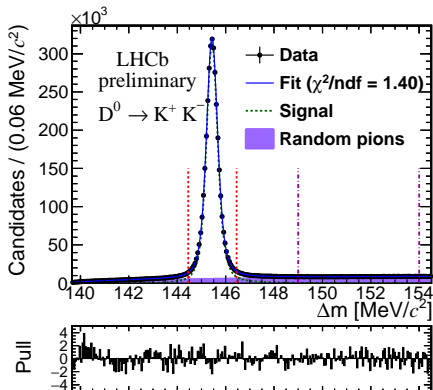




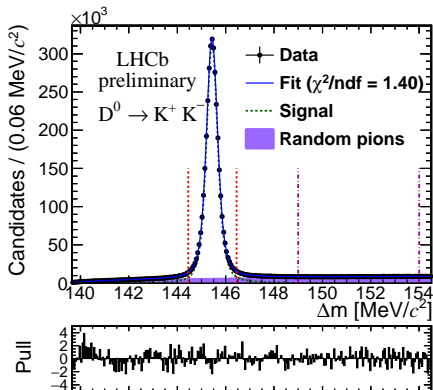
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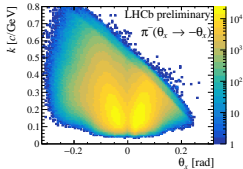
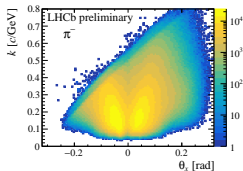
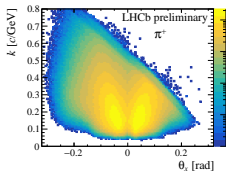
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- Candidates in the sideband region are given negative weights.
- Cut on  $\ln(\chi_{IP}^2) < 2$  removes secondaries. Systematic assigned for residual contamination.

- Momentum dependent charge-asymmetry in detection of “soft” pions creates a time-dependent detection asymmetry.
- Due to  $D^0$  momentum and decay-time correlation.

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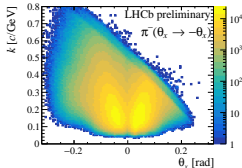
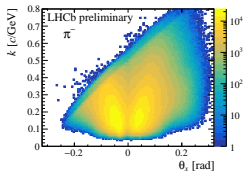
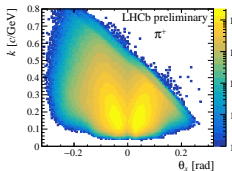
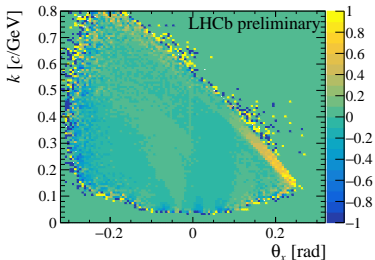


$$k = \frac{1}{\sqrt{p_x^2 + p_y^2}},$$

$$\theta_x = \arctan(p_x/p_y),$$

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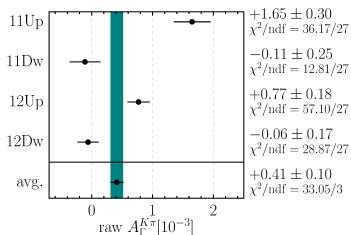
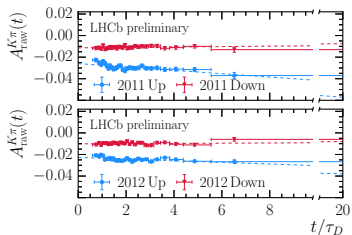
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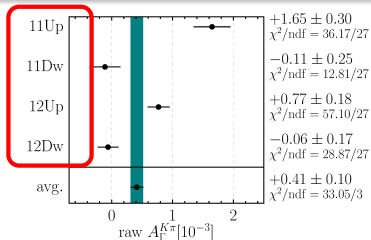
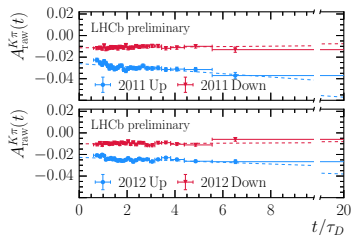
- Equalise the asymmetries with  $(k, \theta_x, \theta_y)$ .
- $R = \frac{(k, \theta_x, \theta_y)_{\pi^+}}{(k, \theta_x, \theta_y)_{\pi^-}(\theta_x \rightarrow -\theta_x)}$
- Reweight  $R$  to 1.

Preliminary: Before Correction: [LHCb-CONF-2016-009]

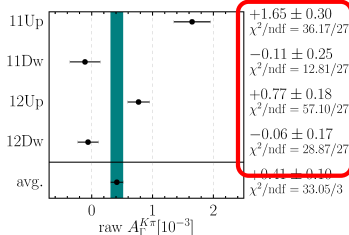
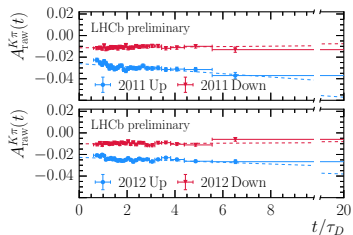




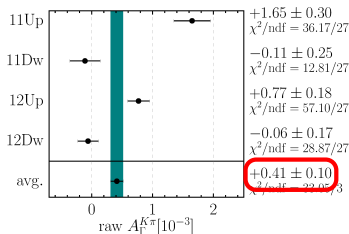
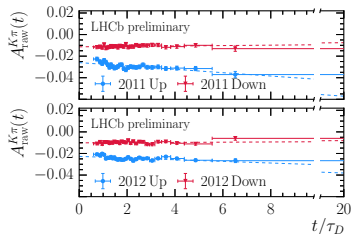
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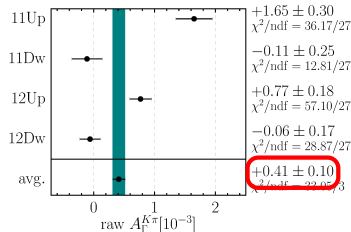
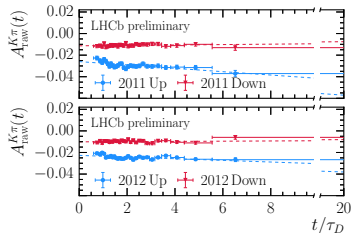
Preliminary: Before Correction: [LHCb-CONF-2016-009]



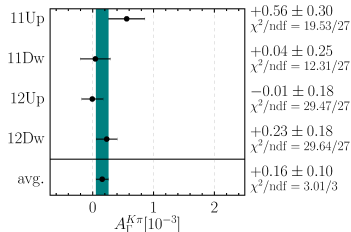
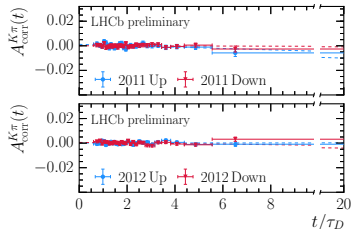
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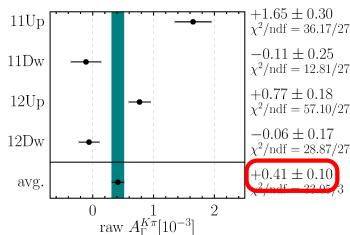
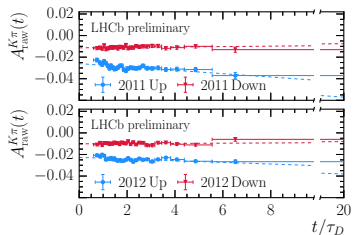
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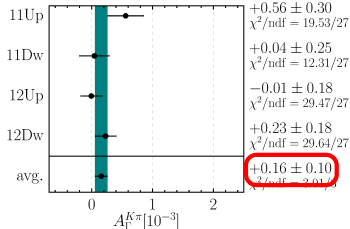
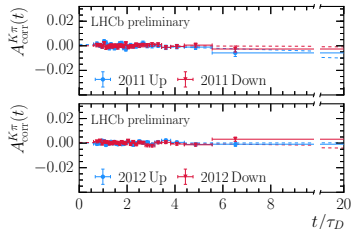
Preliminary: After Correction:



Preliminary: Before Correction: [LHCb-CONF-2016-009]

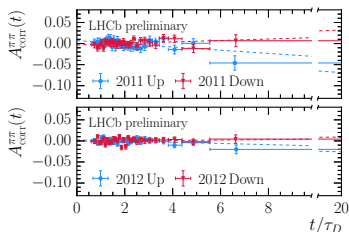
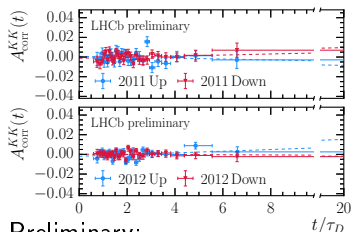


Preliminary: After Correction:



$$D^0 \rightarrow K^+ K^-$$

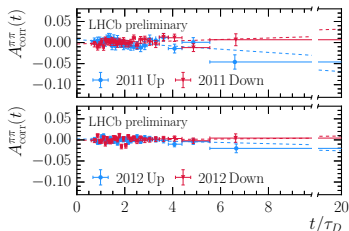
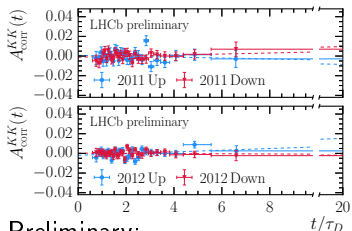
$$D^0 \rightarrow \pi^+ \pi^-$$



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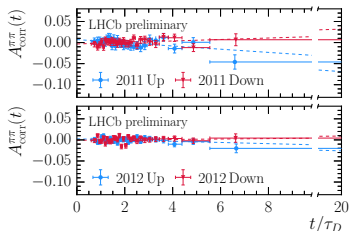
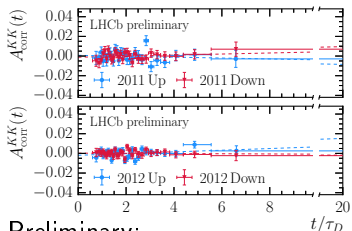
Preliminary:

$$A_{\Gamma}(D^0 \rightarrow K^+ K^-) = (-0.30 \pm 0.32 \pm 0.10) \times 10^{-3},$$

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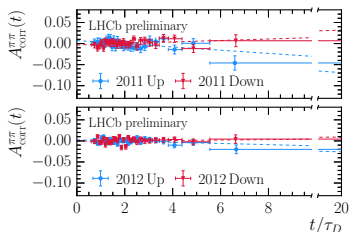
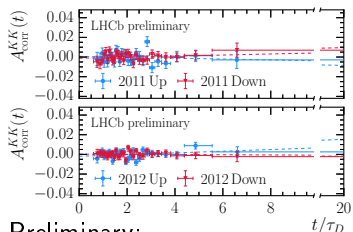
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**World's best measurement!**



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$$\Delta A_{\Gamma} = (-0.76 \pm 0.66 \pm 0.04) \times 10^{-3},$$

$$A_{\Gamma} = (-0.13 \pm 0.28 \pm 0.10) \times 10^{-3},$$

Unbinned maximum likelihood [[LHCb-CONF-2016-010](#)]

$$A_{\Gamma}(D^0 \rightarrow K^+ K^-) = (-0.14 \pm 0.37 \pm 0.10) \times 10^{-3},$$

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Yield asymmetry in bins (more accurate) [[LHCb-CONF-2016-009](#)]

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Yield asymmetry in bins (more accurate) [[LHCb-CONF-2016-009](#)]

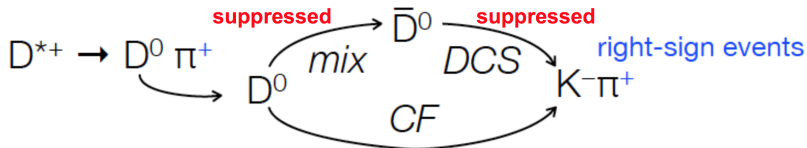
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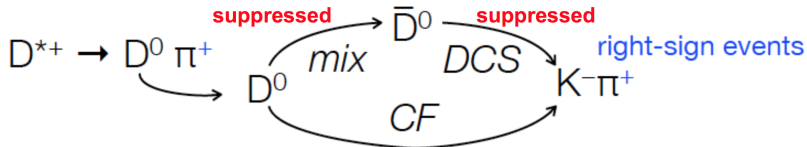
- The more accurate yield asymmetry in bins is taken as the final result.
- Toy tests using both methods on datasets with randomised flavour tags show that the results are compatible.

$$R^\pm(t) \text{ of } D^0 \rightarrow K^\pm \pi^\mp$$

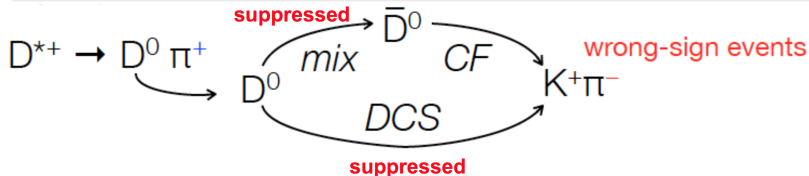
$$D^0 \rightarrow K^- \pi^+ (\text{Right Sign})(\text{CF}),$$



$D^0 \rightarrow K^- \pi^+$  (Right Sign)(CF),



$D^0 \rightarrow K^+ \pi^-$  (Wrong Sign)(DCS),



- Time dependent ratio of amplitudes for small  $x$  and  $y$  (sign indicates flavour tag):

$$\frac{WS^\pm(t)}{RS^\pm(t)} := R^\pm(t) \approx R_D^\pm + \sqrt{R_D^\pm} y'^{\pm} \Gamma t + \frac{x'^{\pm 2} + y'^{\pm 2}}{4} (\Gamma t)^2$$

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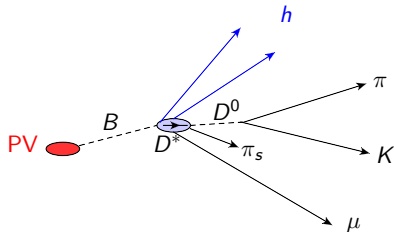
- Three models
  - $CP$  symmetry:  $R^+ = R^-$ ,  $(x'^+)^2 = (x'^-)^2$ ,  $y'^+ = y'^-$ .
  - $CP$  symmetry in decay amplitudes:  $R^+ = R^-$ .
  - All  $CP$  violation allowed.



- Single tag prompt with “soft” pion only

[*Phys. Rev. Lett.*, 111:251801, 2013].

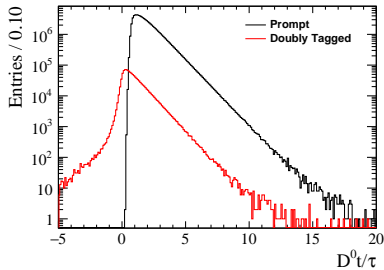
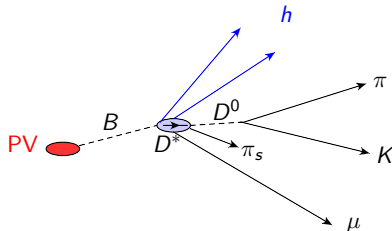
- Double tag (DT) secondary  $B$  decays with muon and “soft” pion [arXiv:1611.06143].



- Single tag prompt with “soft” pion only

[Phys. Rev. Lett., 111:251801, 2013].

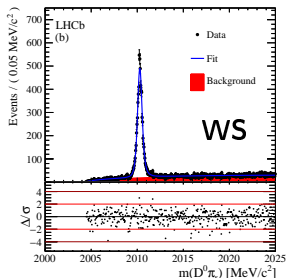
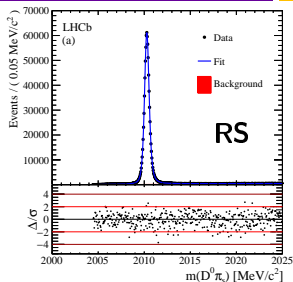
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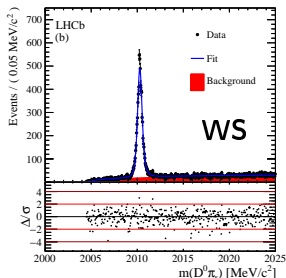
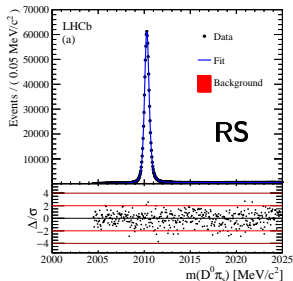
- DT cleaner and provides measurements at low decay times.
- Single tag has larger statistics and covers longer decay times.
- DT adds 3% of the statistics but removes 10%-20% from the errors.

- Make unphysical sample of  $\bar{B} \rightarrow \mu^+ D^{*+} X$  (same sign).
- Remove muon mistags by reweighting with the same sign distributions.

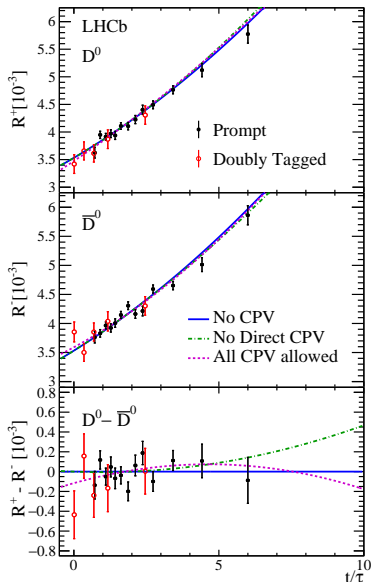
- Make unphysical sample of  $\bar{B} \rightarrow \mu^+ D^{*+} X$  (same sign).
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- Make unphysical sample of  $\bar{B} \rightarrow \mu^+ D^{*+} X$  (same sign).
- Remove muon mistags by reweighting with the same sign distributions.
- Extract the signal yields from  $\Delta m$  in bins of time.
- One  $\Delta m$  fit of the time-integrated RS data is used to constrain the signal parameters for all bins.
- Do this for RS and WS and both flavours.

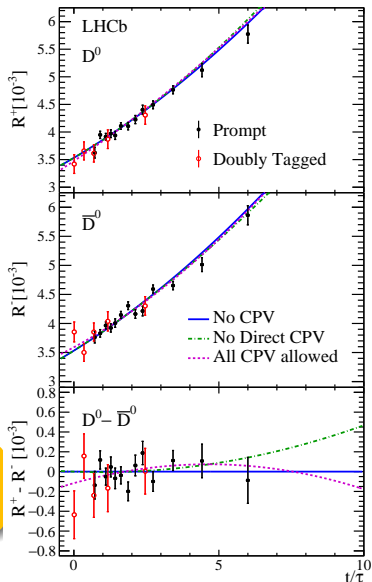


- Use the three mixing hypotheses to fit the measured  $R(t)^\pm$ .
- **(top)** The ratio of  $D^0$  to WS over  $D^0$  to RS.
- **(middle)** The ratio of  $\bar{D}^0$  to WS over  $\bar{D}^0$  to RS.
- **(bottom)** The difference of the two.



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- **(middle)** The ratio of  $\bar{D}^0$  to WS over  $\bar{D}^0$  to RS.
- **(bottom)** The difference of the two.

Consistent with the No CPV, mixing only hypothesis.



# Conclusion



- Results of two complimentary  $A_{\Gamma}$  measurements.
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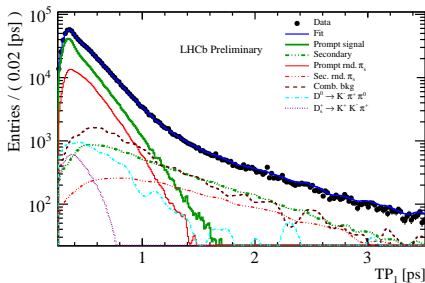
All results consistent with No CPV in  $D$ .



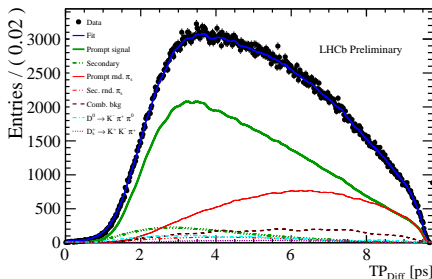
# Backup

- Swimming returns a tuple of turning points (TPs) which define decay-time acceptance intervals.
- Only the first acceptance interval is considered.
- The acceptance for each fit component is determined using an iterative process of unfolding.
- Validate by comparing the sum of the component TP distributions to data.

First TP,  $TP_1$



First TP - Second TP,  $TP_{diff}$



- The per-candidate probability density functions (PDFs) are normalised in the accepted interval.

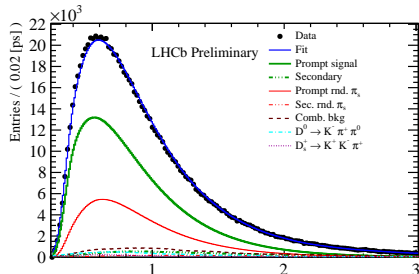
$$f(t|TP_1, TP_{diff}, class) = \frac{f(t|class)\Theta(t-TP_1)\Theta(TP_1+TP_{diff}-t)}{\int_{TP_1}^{TP_1+TP_{diff}} f(t|class) dt}$$

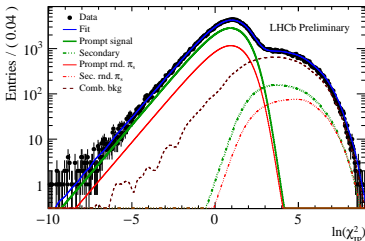
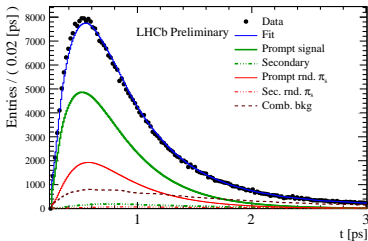
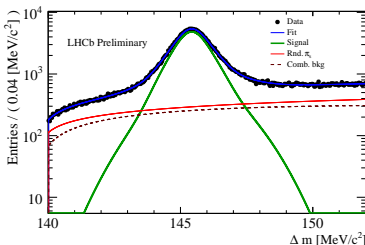
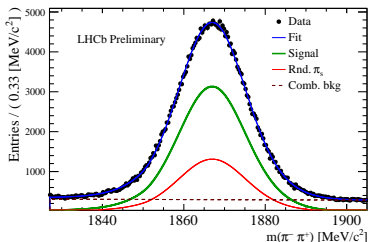
- where  $\Theta(t)$  is the heavy-side function.
- $f(t|class)$  is the “unbiased” PDF, for prompt signal:

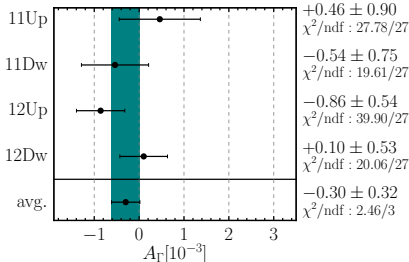
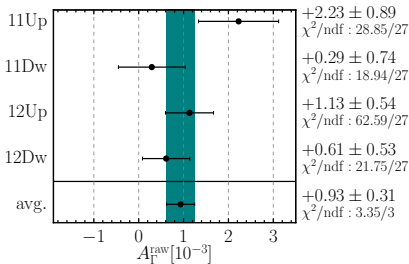
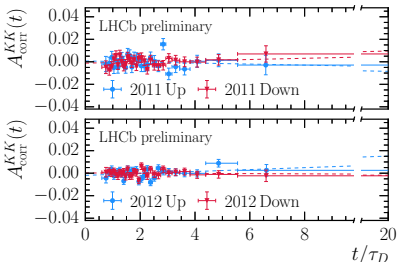
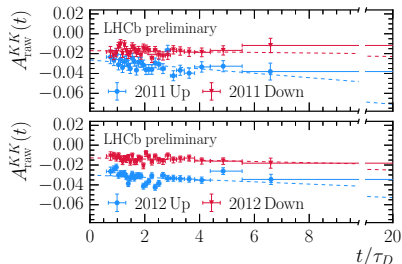
$t$  projection

$$f(t|sig., prompt) = \frac{1}{\tau} e^{-t'\tau} \otimes R(t', t)$$

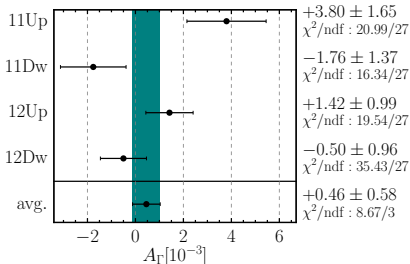
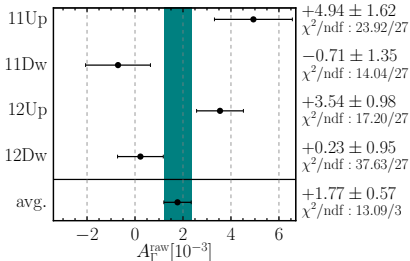
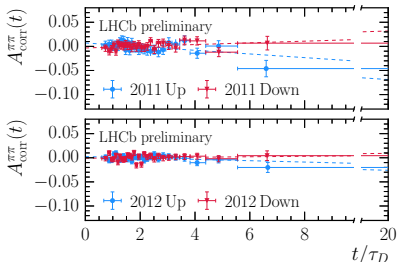
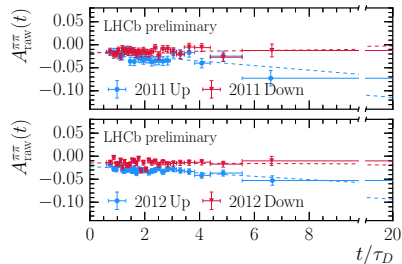
- Where  $R(t', t)$  is the detector decay-time resolution.











- Define mixing parameters:

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

$$x := \frac{\delta m}{\Gamma} := \frac{2(m_1 - m_2)}{\Gamma_1 + \Gamma_2}, \quad y := \frac{\Gamma_2 - \Gamma_1}{\Gamma_2 + \Gamma_1}, \quad \begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \delta & \sin \delta \\ -\sin \delta & \cos \delta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

- Counting experiment for N observed WS and RS decays for two flavours ( $\pm$ ).

$$R(t)_{\text{obs}}^{\pm} = R(t)^{\pm} (1 - \Delta_p^{\pm}) \left( \frac{\epsilon(K^+\pi^-)}{\epsilon(K^-\pi^+)} \right)^{\pm 1} + p_{\text{other}}^{\pm}$$

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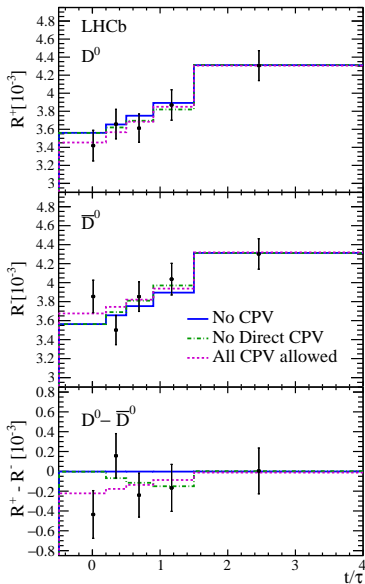
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- Time-dependent ratio.
- $\propto$  fraction of prompt in DT sample.
- Detection efficiency asymmetry.
- MisID and peaking backgrounds.

Parameter	DT + Prompt	Prompt-only
No CPV		
$R_D[10^{-3}]$	$3.533 \pm 0.054$	$3.568 \pm 0.067$
$x'^2[10^{-4}]$	$0.36 \pm 0.43$	$0.55 \pm 0.49$
$y'[10^{-3}]$	$5.23 \pm 0.84$	$4.8 \pm 0.9$
$\chi^2/\text{ndf}$	96.6/111	86.4/101
No direct CPV		
$R_D[10^{-3}]$	$3.533 \pm 0.054$	$3.568 \pm 0.067$
$(x'^+)^2[10^{-4}]$	$0.49 \pm 0.50$	$0.64 \pm 0.56$
$y'^+[10^{-3}]$	$5.14 \pm 0.91$	$4.8 \pm 1.1$
$(x'^-)^2[10^{-4}]$	$0.24 \pm 0.50$	$0.46 \pm 0.55$
$y'^-[10^{-3}]$	$5.32 \pm 0.91$	$4.8 \pm 1.1$
$\chi^2/\text{ndf}$	96.1/109	86.0/99
All CPV allowed		
$R_D^+[10^{-3}]$	$3.474 \pm 0.081$	$3.545 \pm 0.095$
$(x'^+)^2[10^{-4}]$	$0.11 \pm 0.65$	$0.49 \pm 0.70$
$y'^+[10^{-3}]$	$5.97 \pm 1.25$	$5.1 \pm 1.4$
$R_D^-[10^{-3}]$	$3.591 \pm 0.081$	$3.591 \pm 0.090$
$(x'^-)^2[10^{-4}]$	$0.61 \pm 0.61$	$0.60 \pm 0.68$
$y'^-[10^{-3}]$	$4.50 \pm 1.21$	$4.5 \pm 1.4$
$\chi^2/\text{ndf}$	95.0/108	85.9/98





Parameter	Value
No CPV	
$R_D[10^{-3}]$	$3.48 \pm 0.10 \pm 0.01$
$x'^2[10^{-4}]$	$0.28 \pm 3.10 \pm 0.11$
$y'[10^{-3}]$	$4.60 \pm 3.70 \pm 0.18$
$\chi^2/\text{ndf}$	6.3/7
No direct CPV	
$R_D[10^{-3}]$	$3.48 \pm 0.10 \pm 0.01$
$(x'^+)^2[10^{-4}]$	$1.94 \pm 3.67 \pm 1.17$
$y'^+[10^{-3}]$	$2.79 \pm 4.27 \pm 0.98$
$(x'^-)^2[10^{-4}]$	$-1.53 \pm 4.04 \pm 1.68$
$y'^-[10^{-3}]$	$6.51 \pm 4.38 \pm 1.66$
$\chi^2/\text{ndf}$	5.6/5
All CPV allowed	
$R_D^+[10^{-3}]$	$3.38 \pm 0.15 \pm 0.06$
$(x'^+)^2[10^{-4}]$	$-0.19 \pm 4.46 \pm 0.32$
$y'^+[10^{-3}]$	$5.81 \pm 5.25 \pm 0.31$
$R_D^-[10^{-3}]$	$3.60 \pm 0.15 \pm 0.07$
$(x'^-)^2[10^{-4}]$	$0.79 \pm 4.31 \pm 0.38$
$y'^-[10^{-3}]$	$3.32 \pm 5.21 \pm 0.40$
$\chi^2/\text{ndf}$	4.5/4