

9th International Workshop on the Unitarity Triangle (CKM2016) TIFR, Mumbai, 1/12/2016

**Measurements of Mixing and Indirect CPV in
multi-body Charm decays at LHCb**

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on behalf the LHCb Collaboration

Outline

- **Mixing and Indirect CP Violation in Charm decays**
- **Mixing and Coherence Factor in $D^0 \rightarrow K^{\mp} \pi^{\pm} \pi^{\mp} \pi^{\pm}$**
- **Mixing in $D^0 \rightarrow K^0_S \pi^+ \pi^-$**
- **LHCb Prospects for Run2**

Mixing in Charm Decays

Mixing of Neutral Mesons

- Pure Quantum Mechanics effect

$$i \frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = \left(\mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}$$

- By labelling the mass eigenstates

$$|D_{1,2}\rangle = p |D^0\rangle \pm q |\bar{D}^0\rangle$$

- The mixing parameters can be defined

$$x \equiv \frac{m_2 - m_1}{\Gamma} = \frac{\Delta M}{\Gamma} \quad y \equiv \frac{\Gamma_2 - \Gamma_1}{2\Gamma} = \frac{\Delta\Gamma}{2\Gamma}$$

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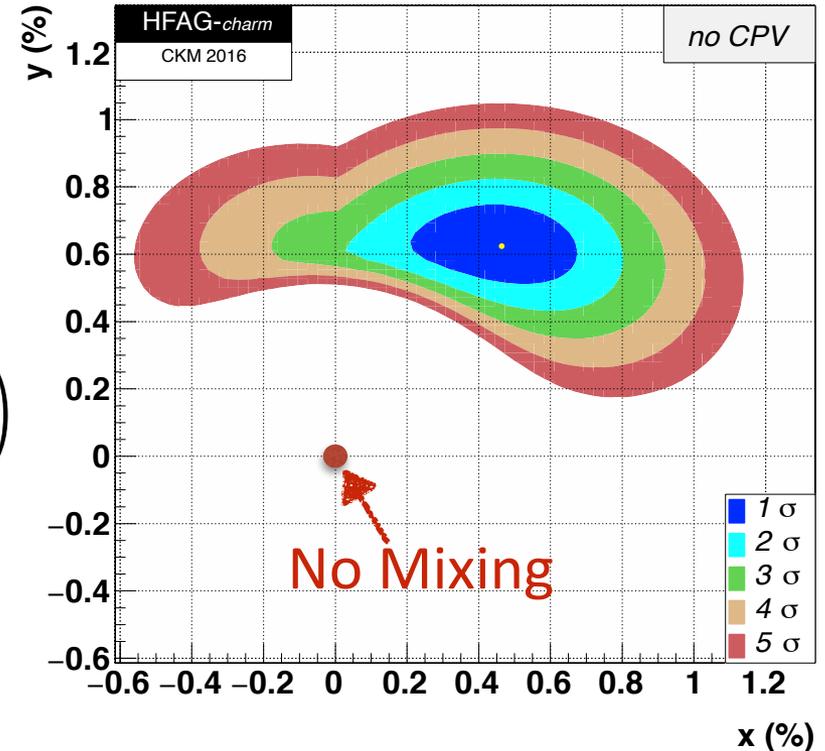
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- Established!



Mixing and Indirect CPV in Charm Decays

CPV and Mixing

- CPV can arise from mixing

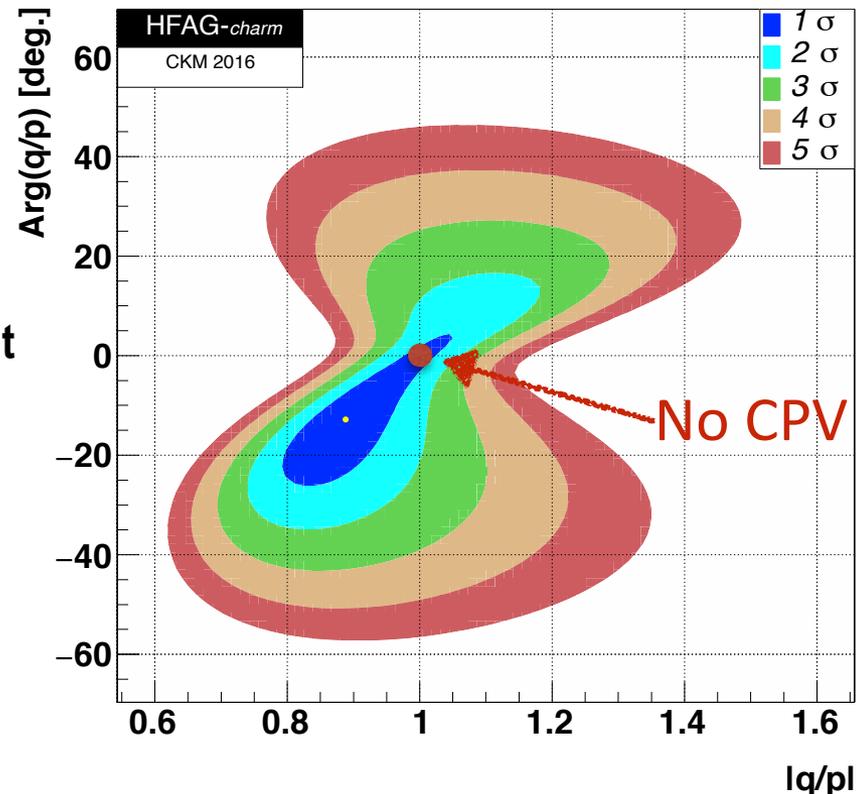
$$\left| \frac{q}{p} \right| \neq 1$$

- or from interference of decay with and without mixing $D^0 \rightarrow f; D^0 \rightarrow \bar{D}^0 \rightarrow f$

$$\arg(\lambda_f) + \arg(\lambda_{\bar{f}}) \neq 0$$

$$\lambda_f \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

- Still consistent with no CPV



A Portal for BSM Physics

Indirect Searches

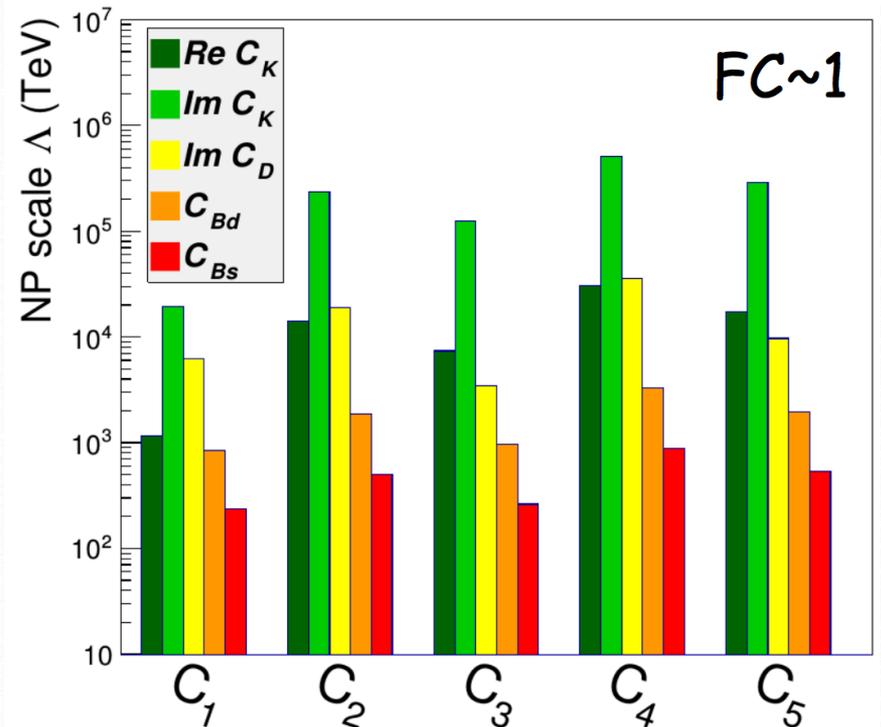
- Charm mixing sets the second stringent bounds on NP from $\Delta F=2$ processes
- Not as much powerful on other models (NMFV), but still worth considering

Up-sector

- Charm probes up-sector quark mixing
Alternative path to NP
- Very small SM expectations

UTFit Collaboration, 2016

Bounds from $\Delta F=2$ processes,
generic flavour structure



$\Delta F=2$ processes scale as $1/\Lambda^2$

Multi-Body Decays

Cons

- Lower efficiency than two-body
- Long-range dynamics more difficult to predict
- May need understanding the resonant structure of the decay

Pros

- Large number of intermediate states offer many possible interference patterns
- More observables exploiting the underlying resonant structure
- Useful for γ measurement using $B \rightarrow D^0 K$

$$D^0 \rightarrow K\pi\pi\pi$$

Mixing and Coherence Factor

$D^0 \rightarrow K\pi\pi\pi$ - Mixing and Coherence Factor

WS/RS Ratio

- Exploits mixing by measuring the time-dependent ratio of $D^0 \rightarrow K^+\pi^-\pi^+\pi^-$ (WS) decays to $D^0 \rightarrow K^-\pi^+\pi^+\pi^-$ (RS) decays (assuming CP symmetry)

$$R(t) \approx \left(r_D^{K3\pi} \right)^2 - r_D^{K3\pi} R_D^{K3\pi} y'_{K3\pi} \frac{t}{\tau} + \frac{x^2 + y^2}{4} \left(\frac{t}{\tau} \right)^2$$

$r_D^{K3\pi}$ phase space averaged ratio of DCS/CF amplitudes

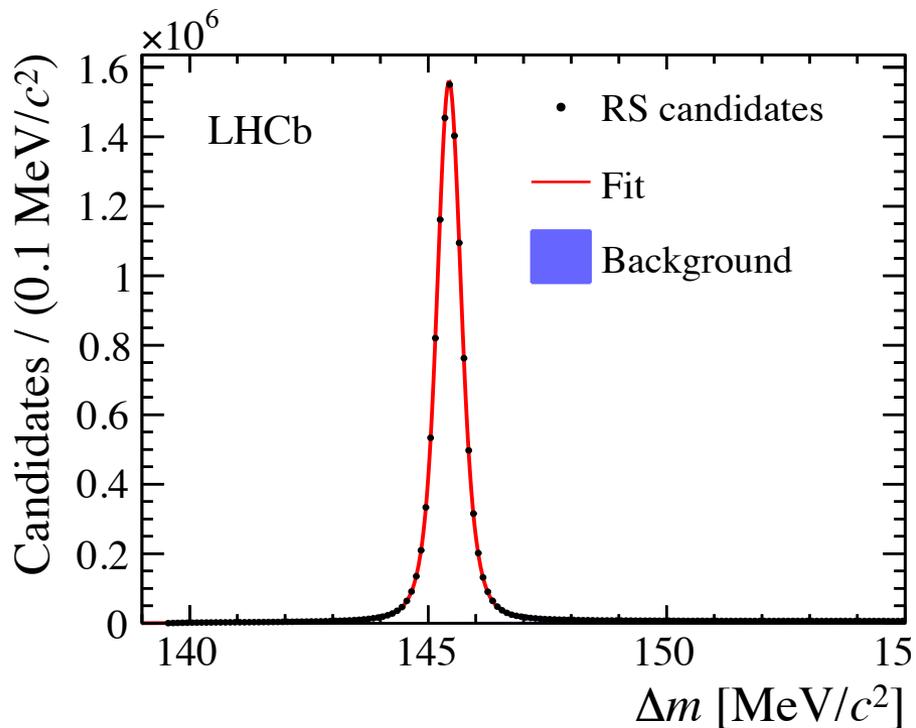
$R_D^{K3\pi}$ coherence factor: $R_D^{K3\pi} e^{-i\delta_D^{K3\pi}} \equiv \langle \cos \delta \rangle + i \langle \sin \delta \rangle$

$y'_{K3\pi}$ interference term: $y'_{K3\pi} \equiv y \cos \delta_D^{K3\pi} - x \sin \delta_D^{K3\pi}$

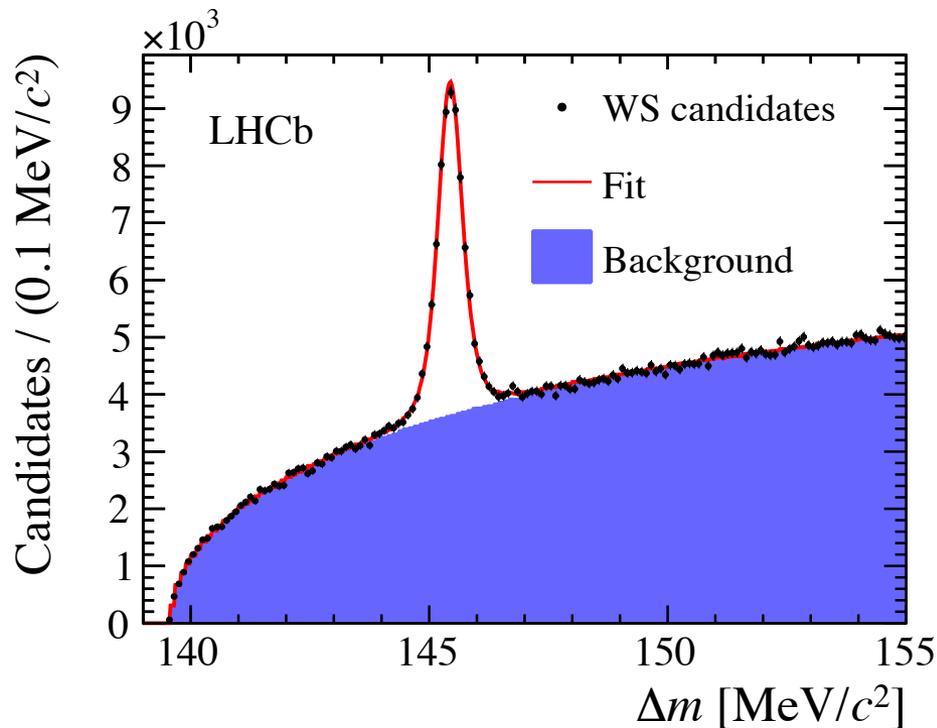
All the three parameters are needed for measuring γ with $B \rightarrow D^0(K\pi\pi\pi)K$

Dataset

- Prompt $D^{*+} \rightarrow D^0 \pi^+$ decays
- Run1: 3fb^{-1} at 7 and 8 TeV



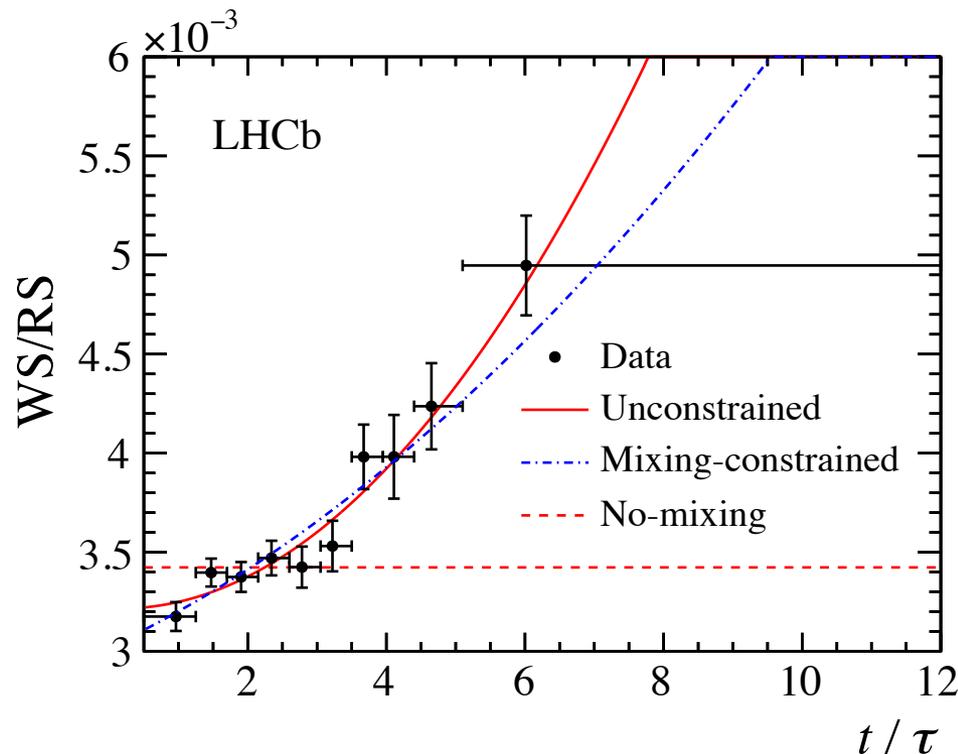
$$N_{RS} = 11.4 \times 10^6$$



$$N_{WS} = 42.5 \times 10^3$$

Ratios Fit

- The WS/RS ratio measured in 10 decay time bins in $[0.5, 12.0] \tau_D$
- $R = \sqrt{N_{WS}^{D^0} N_{WS}^{\bar{D}^0} / N_{RS}^{D^0} N_{RS}^{\bar{D}^0}}$ to cancel production or π_s^\pm detection asymmetries
- Uncertainties in the plot include systematics
 - double mis-id ($K^+\pi^- \rightarrow K^-\pi^+$)
 - $D^0 \rightarrow K^+\pi^- K_S^0$
 - contribution from secondary decays (bin-by-bin)
 - trigger efficiency
- A few hypotheses are tested
 - Mixing
 - No Mixing (excluded at 8.2σ)
 - WA Mixing (compatible at 1.8σ)



Fit Type χ^2/ndf (p-value)	Parameter	Fit result	Correlation coefficient		
			$r_D^{K3\pi}$	$R_D^{K3\pi} \cdot y'_{K3\pi}$	$\frac{1}{4}(x^2 + y^2)$
Unconstrained 7.8/7 (0.35)	$r_D^{K3\pi}$	$(5.67 \pm 0.12) \times 10^{-2}$	1	0.91	0.80
	$R_D^{K3\pi} \cdot y'_{K3\pi}$	$(0.3 \pm 1.8) \times 10^{-3}$		1	0.94
	$\frac{1}{4}(x^2 + y^2)$	$(4.8 \pm 1.8) \times 10^{-5}$			1

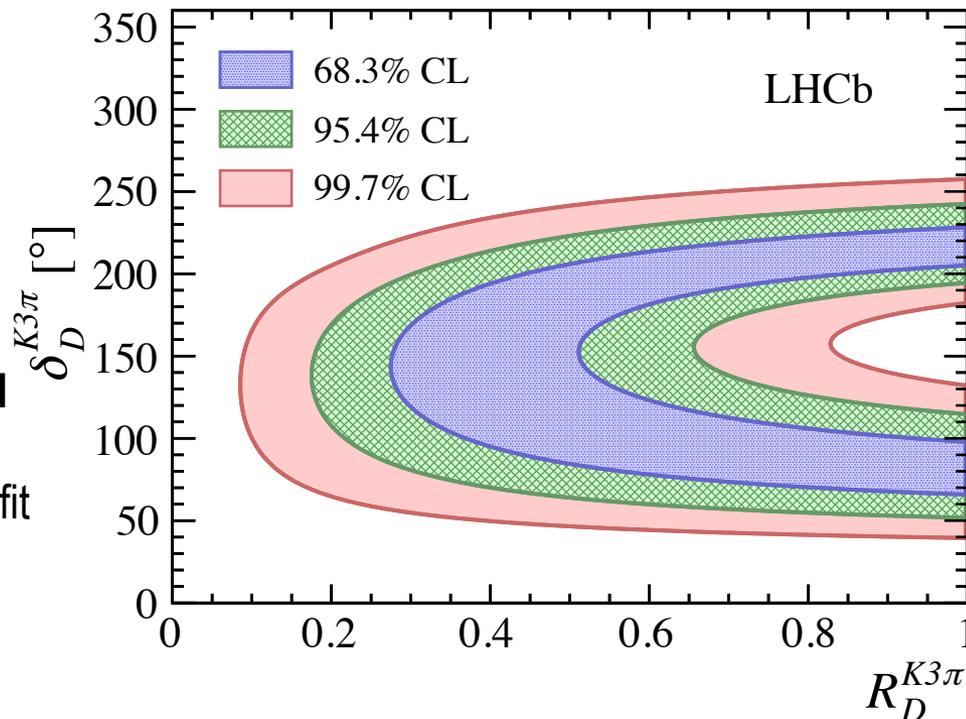
$D^0 \rightarrow K\pi\pi\pi$ - Coherence Factor

Phys. Rev. Lett. 116, 241801 (2016)

The Constrained Fit

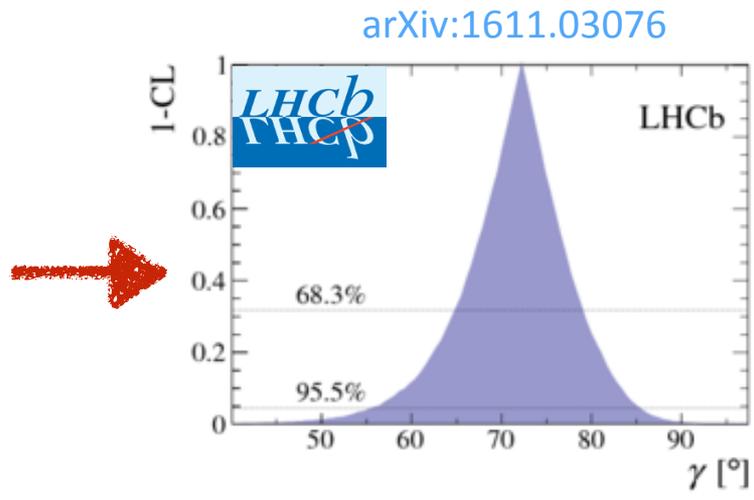
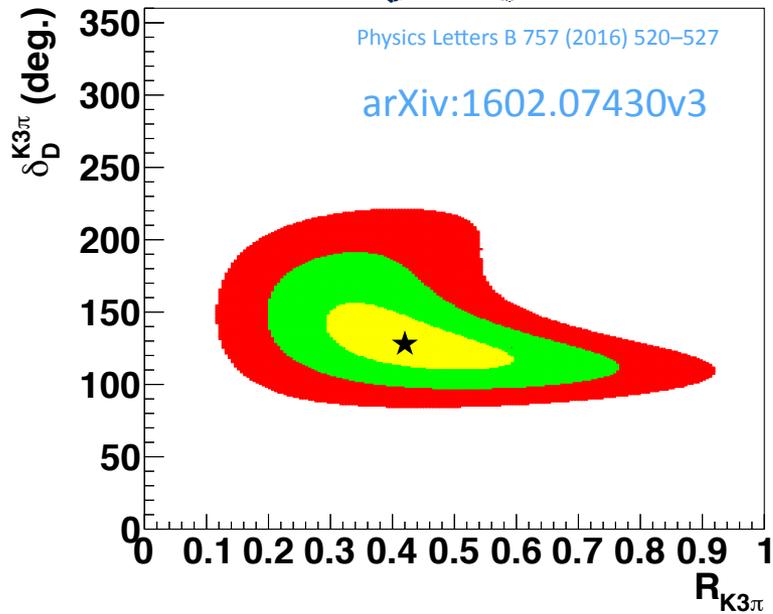
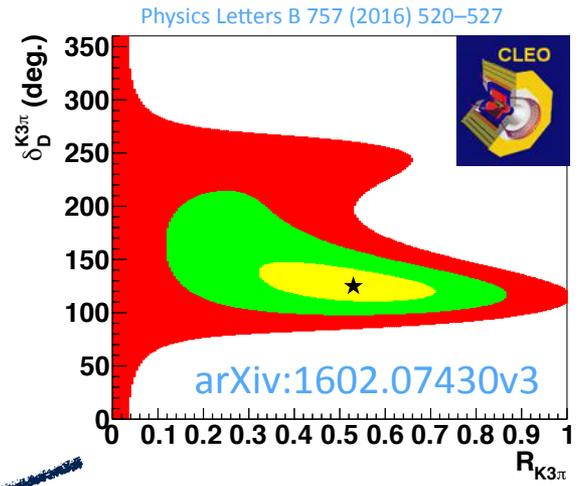
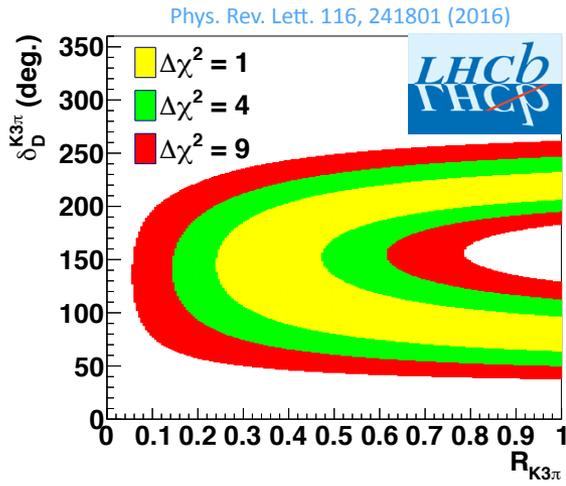
- Allows to determine a line of solutions in the $(\delta_D^{K3\pi}, R_D^{K3\pi})$ plane
Uncertainties on $r_D^{K3\pi}$ and $R_D^{K3\pi} y'_{K3\pi}$ are greatly reduced
- Improves constraints previously produced by CLEO-c
But a combination would require a combined fit
- Will increase the sensitivity to γ in $B \rightarrow D^0(K\pi\pi\pi)K$

OSS: $y'_{K3\pi} \equiv y \cos \delta_D^{K3\pi} - x \sin \delta_D^{K3\pi}$



	$r_D^{K3\pi}$	$R_D^{K3\pi} \cdot y'_{K3\pi}$	x	y
Mixing-constrained	$(5.50 \pm 0.07) \times 10^{-2}$	1	0.83	0.17
11.2/8 (0.19)	$(-3.0 \pm 0.7) \times 10^{-3}$	1	0.34	0.20
	$(4.1 \pm 1.7) \times 10^{-3}$		1	-0.40
	$(6.7 \pm 0.8) \times 10^{-3}$			1

Combination with CLEO-c



$D^0 \rightarrow K^0_S \pi^+ \pi^-$ Mixing

Mixing and CPV in $D^0 \rightarrow K^0_S \pi^+ \pi^-$

A Golden Mode for Mixing and CPV

- Both CF and DCS components are present in the same final state
- It gives direct access to all the mixing parameters
 $x, y, q/p, \arg(q/p)$
- Thanks to the various contributions in the Dalitz plot, whose time dependence is modified by mixing parameters

All that Glitters is not Gold...

- Amplitude structure
- Time dependence of the Amplitude structure
Time-dependent Dalitz-plot Analysis
- Presence of varying strong phases across the DP need to be treated with care
It is fixed in two-body decays
- A time-dependent amplitude analysis approach has been pioneered by CLEO and later followed by BaBar and Belle
- At LHCb this approach is more challenging
Run1 trigger has decay-time dependent selections \rightarrow need to model that bias
(Things should be better in Run2...)

$D^0 \rightarrow K^0_S \pi^+ \pi^-$ - Model Independent Approach (I)

External Input

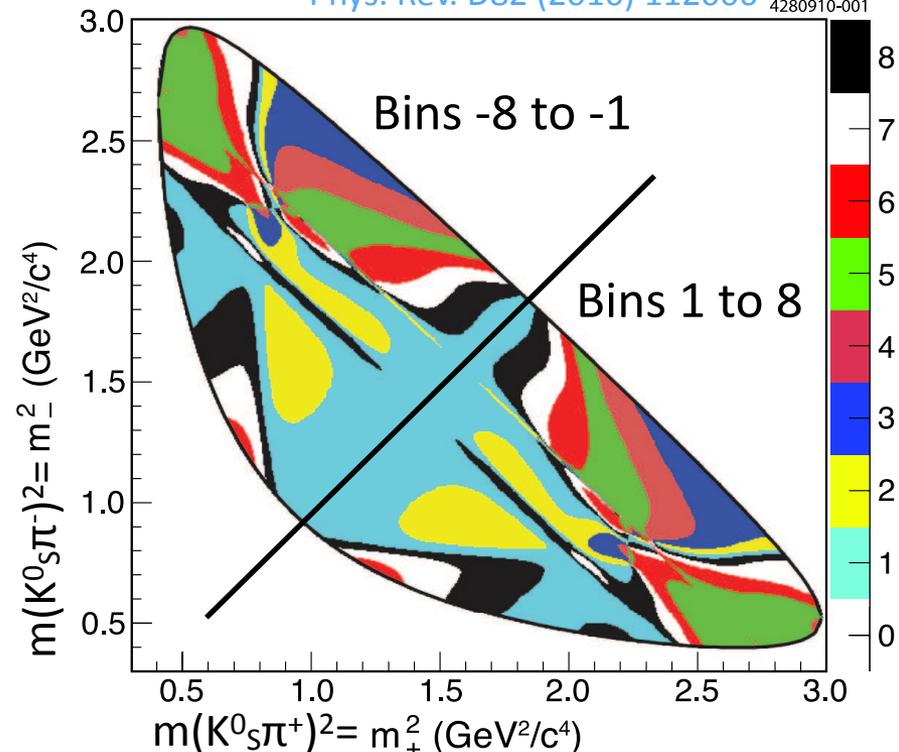
- In reality one does not need to know perfectly the Amplitude structure
- Just how the strong phases vary along the Dalitz plot
- External input can be used

Phys. Rev. D78 (2008) 034023

Phys. Rev. D82 (2010) 112006

Strong Phases Measurement

- Quantum coherence of D^0 - \bar{D}^0 needed to separate D^0 and \bar{D}^0 decays
- Assuming an amplitude model as a reference, the difference of strong phase between bin -i and i is measured



$D^0 \rightarrow K^0_S \pi^+ \pi^-$ - Model Independent Approach (II)

Formalism

- Fraction of events in a bin

$$T_i = \int_i |\mathcal{A}| dm_{12}^2 dm_{13}^2$$

- Interference terms

$$c_i = \frac{1}{\sqrt{T_i T_{-i}}} \int_i |\mathcal{A}_{D^0}^*| |\mathcal{A}_{\bar{D}^0}| \cos \Delta\delta_i dm_+^2 dm_-^2$$

$$s_i = \frac{1}{\sqrt{T_i T_{-i}}} \int_i |\mathcal{A}_{D^0}^*| |\mathcal{A}_{\bar{D}^0}| \sin \Delta\delta_i dm_+^2 dm_-^2$$

- Time-dependent decay rate

$$\mathcal{P}_{D^0}(i; t) \approx e^{\Gamma t} \left(T_i - \Gamma t \sqrt{T_i T_{-i}} (y c_i + x s_i) \right)$$

$$\mathcal{P}_{\bar{D}^0}(i; t) \approx e^{\Gamma t} \left(T_{-i} - \Gamma t \sqrt{T_i T_{-i}} (y c_i - x s_i) \right)$$

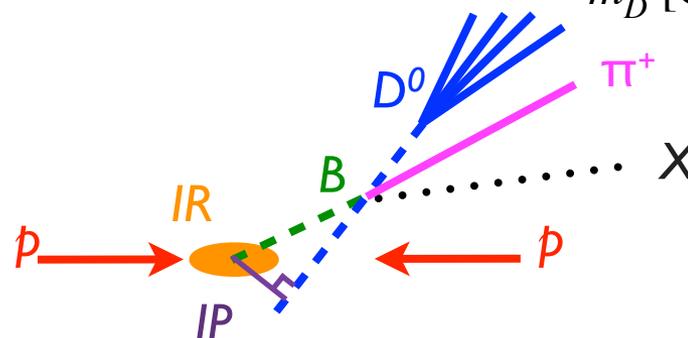
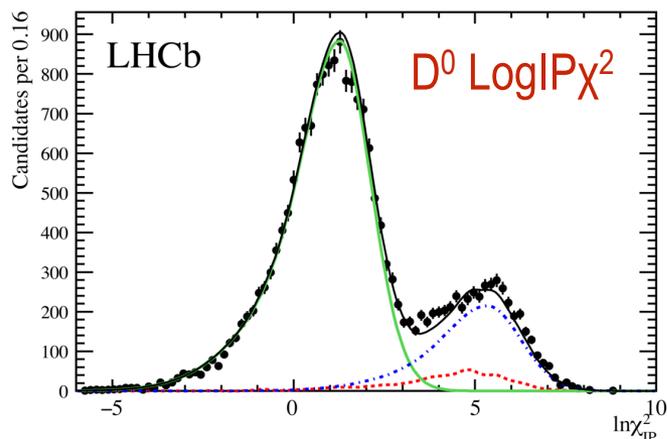
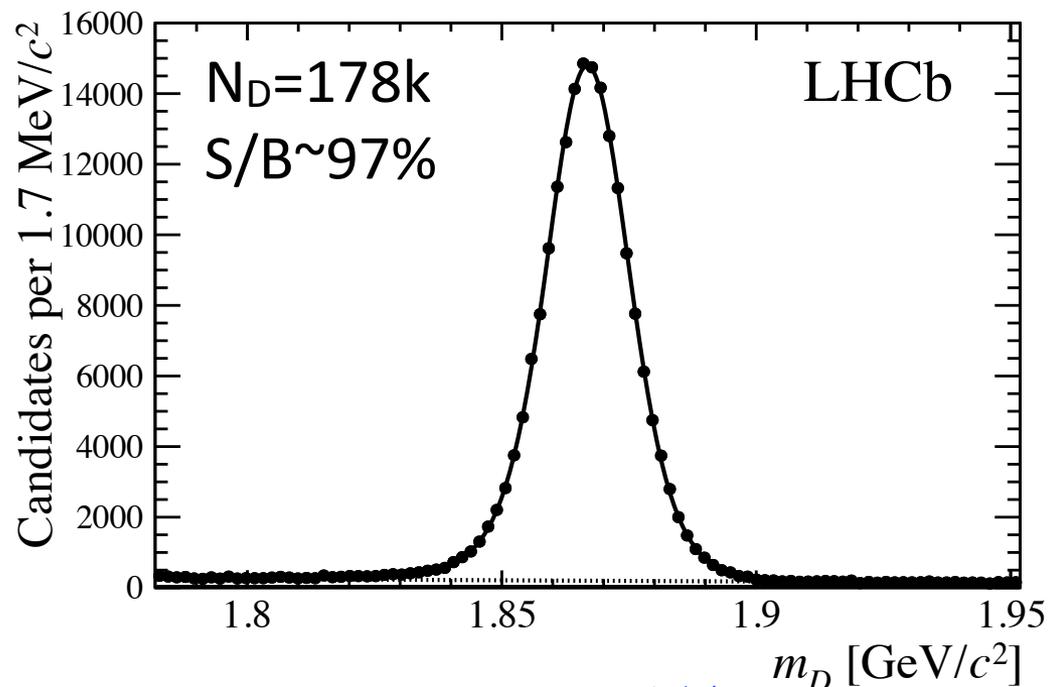
x, y can be measured from the decay-time distribution of events in the DP bins

Dataset

- Prompt $D^{*+} \rightarrow D^0 \pi^+$ decays
- 2011 data: 1fb^{-1}

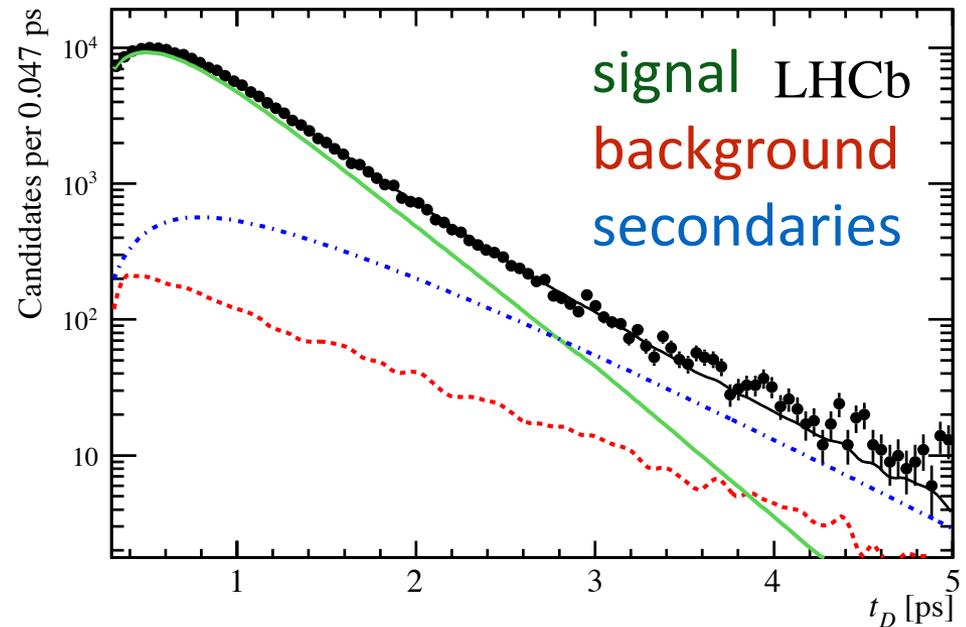
Challenges

- Per-event decay-time acceptance
Data-driven (swimming¹)
- Secondary ($B \rightarrow D^{*+} X$) candidates rejection



Analysis

- The distributions of D^0 mass, $D^0 \text{ LogLP}\chi^2$ and D^0 decay time are fit separately in various steps and finally simultaneously to measure the mixing parameter
- Systematic uncertainties studying by measuring the impact on final result
 - external input (T_i)
 - mass resolution
 - decay time resolution
 - combinatorial background
 - efficiency over PS
 - per-event decay time acceptance



$$x = (-0.86 \pm 0.53 \pm 0.17) \times 10^{-2},$$
$$y = (+0.03 \pm 0.46 \pm 0.13) \times 10^{-2}.$$

WA (HFAG2016)

$$x = (0.46 \pm 0.15)\%$$

$$y = (0.62 \pm 0.08)\%$$



External Inputs

- Quantum coherence of D^0 - \bar{D}^0 mesons produced at c factories allows complementary measurements to LHCb
- A proposal is out describing where branching fraction and strong phases measurements could help ([LHCb-PUB-2016-025](#))
- Focused on the determination of γ at LHCb, but applies also to mixing and CPV in Charm

Synergy of BESIII and LHCb physics programmes

LHCb Collaboration

LHCb Run2 Prospects

Much Larger Yields

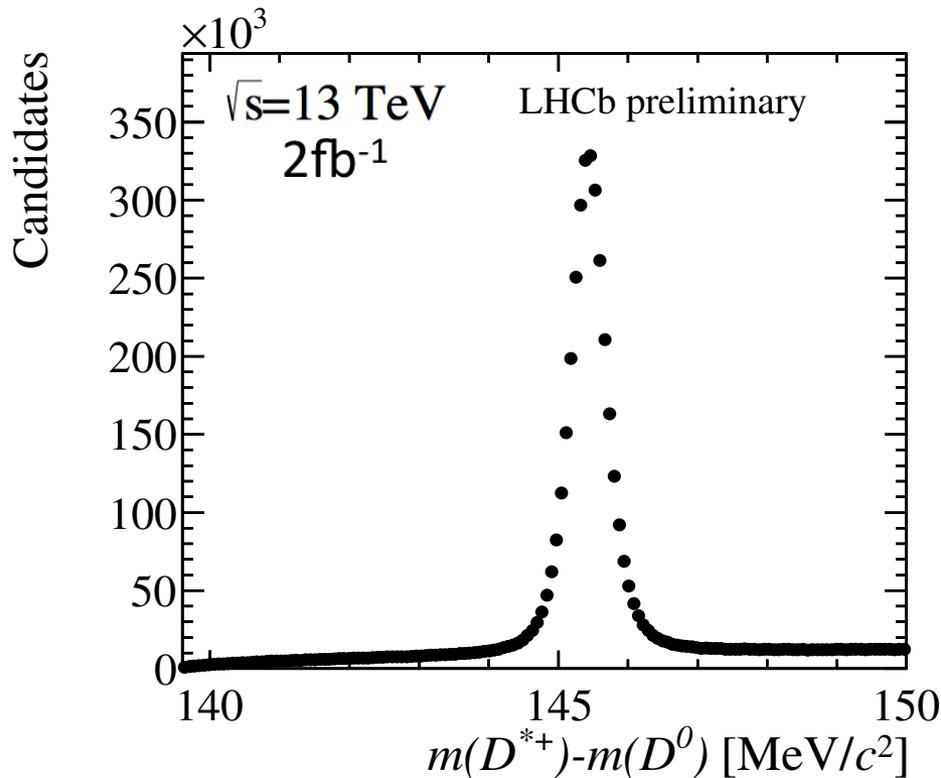
- $c\bar{c}$ cross-section almost doubled
- Extensive work during LS1 on Charm triggers (Turbo)
 - Larger efficiency
 - Improved acceptance
- Online Alignment and Calibration

Alternative Techniques

- Amplitude analyses in Charm are gaining momentum
- Useful for measuring Mixing and CPV

$D^0 \rightarrow K^0_S \pi^+ \pi^-$ Run2 Preview

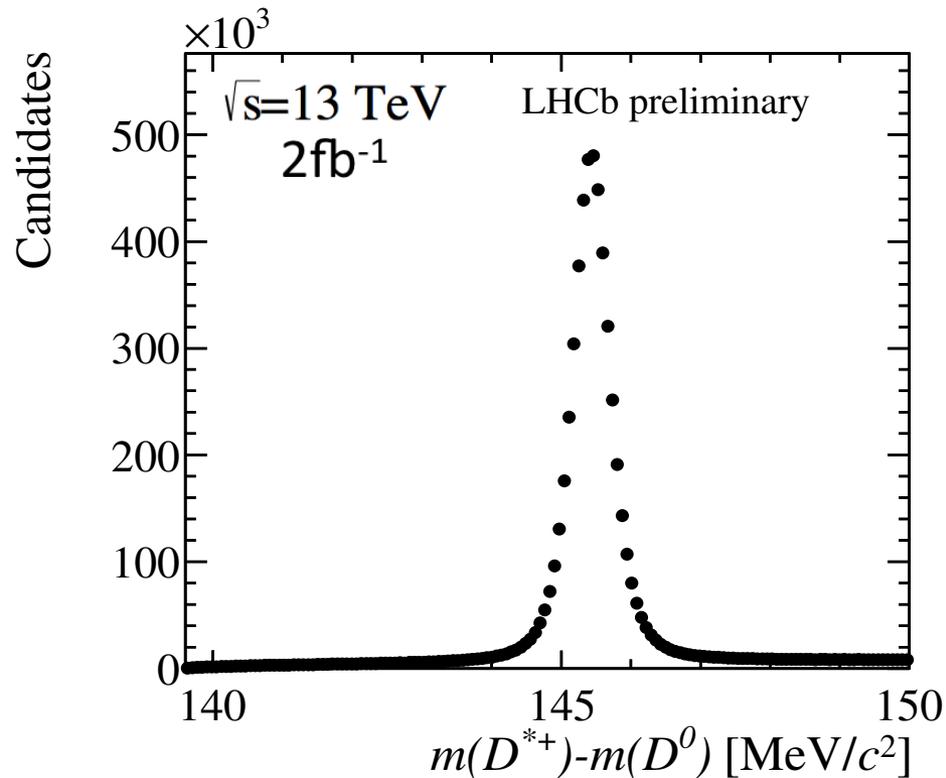
K^0_S vtx inside VELO



$N_D \approx 3.2 \times 10^6$ (1.6M/fb)

Run1: 0.3M/fb

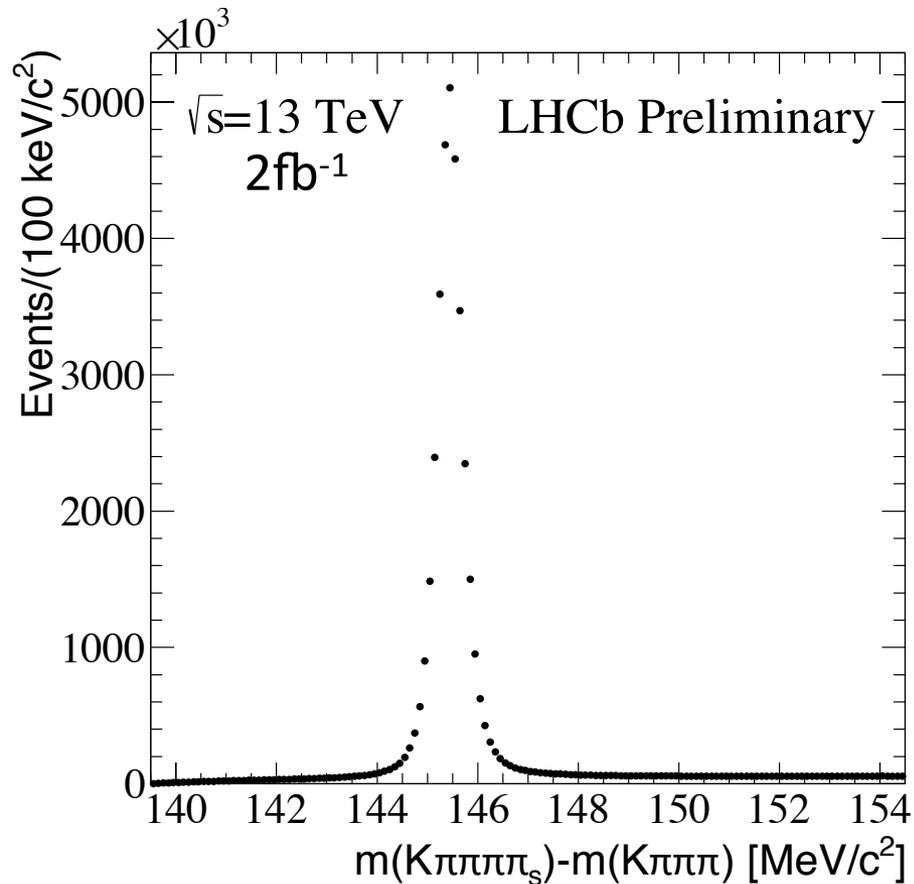
K^0_S vtx outside VELO



$N_D \approx 5.0 \times 10^6$ (2.5M/fb)

Run1: 0.4M/fb

$D^0 \rightarrow K\pi\pi\pi$ Run2 Preview



$N_D \approx 33 \times 10^6$ (16M/fb)

Run1: 3.7M/fb

Summary

Just Started

- The study of Mixing and CPV in Charm multi-body decays at LHCb has just started
- Many more analysis are in the pipeline
- More experience with the detector will favour amplitude analyses

The Best is Yet to Come

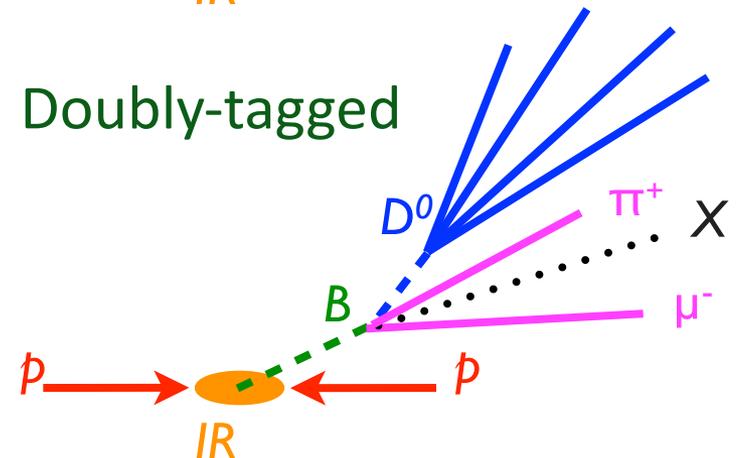
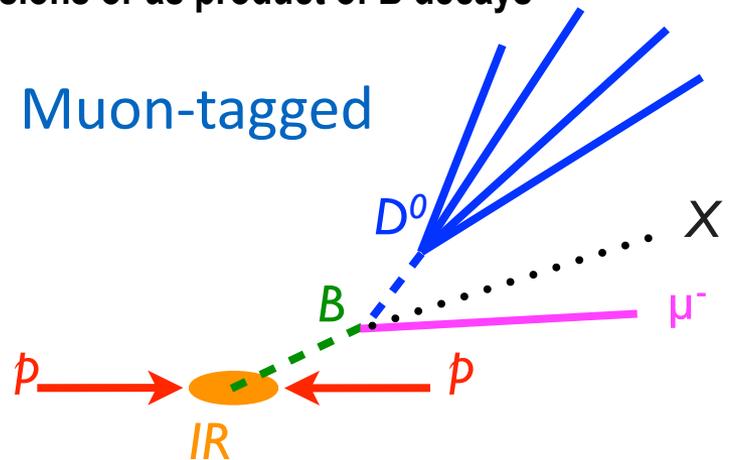
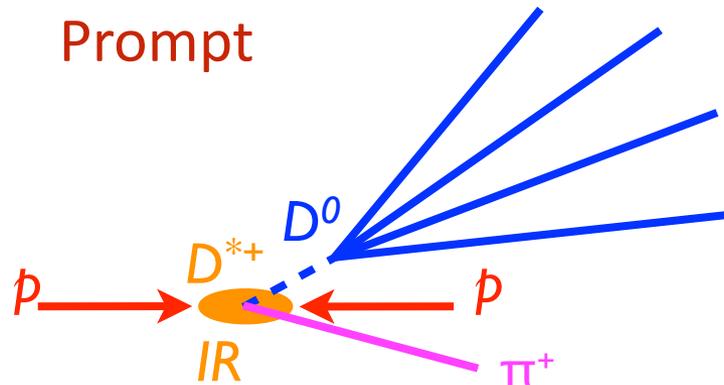
- Run2 data are very promising
- Improved trigger provides us unprecedented yields of Charm decays

Spare

Prompt and Secondary Decays

Two Ways of Selecting and Tagging Charm Hadrons at LHCb

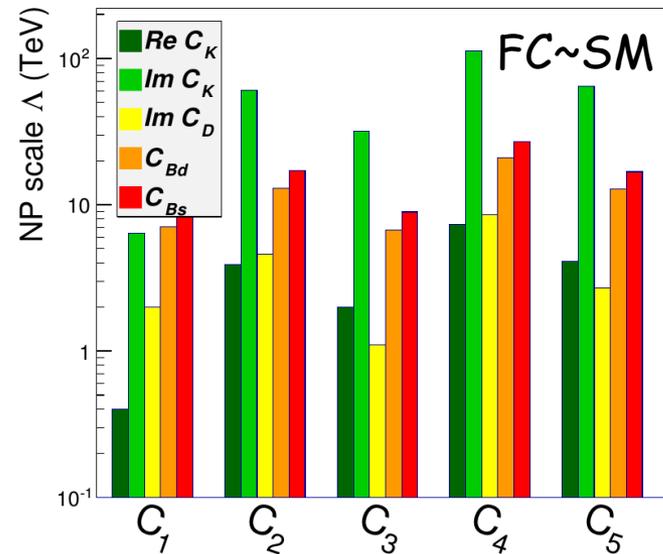
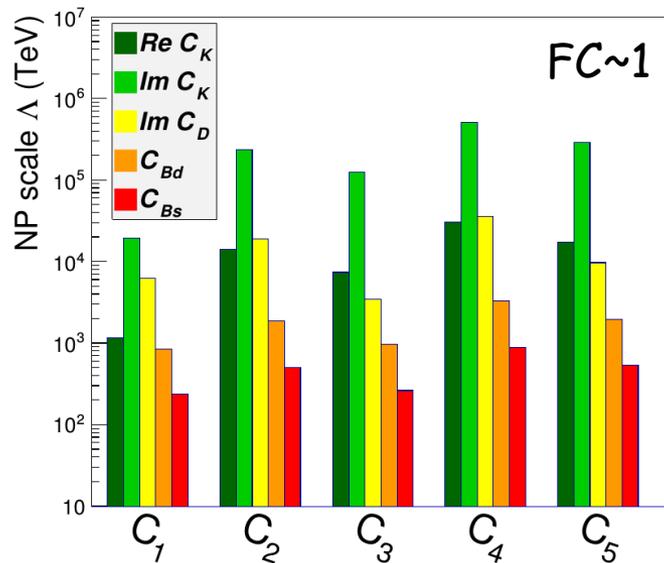
- Charm hadrons can be promptly produced in pp collisions or as product of B decays



New Physics and Indirect CPV in Charm

Comparison with other meson mixing

Λ (TeV)	K	D	B_d	B_s
FC~1	5×10^5	3.5×10^4	3.3×10^3	880
FC~SM	113	8.5	21	27



$D^0 \rightarrow K^0_S \pi^+ \pi^-$ 2011 Systematic Uncertainties

Table 1: Systematic uncertainties on x and y . The statistical uncertainties, which include the uncertainties associated with the CLEO parameters (c_i, s_i) , are shown for comparison.

Source	$x (\times 10^{-2})$	$y (\times 10^{-2})$
Fit bias	0.021	0.020
Decay time resolution	0.065	0.039
Turning point (TP) resolution	0.020	0.022
Invariant mass resolution	0.073	0.028
Prompt/secondary TP distributions	0.051	0.023
Efficiency over phase space	0.057	0.071
Tracking efficiency parameterisation	0.015	0.025
Kinematic boundary	0.012	0.006
Combinatorial background	0.061	0.052
Treatment of secondary D decays	0.046	0.025
Uncertainty from T_i	0.079	0.056
Uncertainties from $(m_D, \Delta m)$ fits	0.000	0.000
Uncertainties from lifetime fit	0.020	0.043
D^0 background	0.001	0.006
Variation of signal components across the phase space	0.013	0.017
Total systematic uncertainty	0.171	0.134
Statistical uncertainty	0.527	0.463