New Physics Search in D Meson Decays



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Overview

1) Motivation;

2) New physics in charged current transitions;

3) LFV in charm meson semileptonic decays;

4) New physics in FCNC processes;

5) Summary.



In B physics there are three puzzles:

1)
$$R_{D^{(*)}} = \frac{BR(B \to D^{(*)} \tau \nu_{\tau})}{BR(B \to D^{(*)} \mu \nu_{\mu})}$$
3.50 Charged current

2) P₅' in
$$~B
ightarrow K^* \mu^+ \mu^-$$
 3 σ

3)
$$R_K = \frac{\Gamma(B \to K \mu \mu)}{\Gamma(B \to K e e)}$$
 in the dilepton invariant mass bin
 $1 \text{ GeV}^2 \le q^2 \le 6 \text{ GeV}^2$

Question: Is there any chance to see NP in charm ?

Charm decays and CKM

(Semi)leptonic charm inputs to the CKM fit

$\mathcal{B}(B^- \rightarrow \tau^- \overline{\mu})$	$(1.08 \pm 0.21) \times 10^{-4}$
$\mathcal{B}(D^- \to \mu^- \overline{\nu}_{\tau})$ $\mathcal{B}(D^- \to \mu^- \overline{\nu}_{\tau})$	$(5.57 \pm 0.24) \times 10^{-3}$
$\mathcal{B}(D_{-}^{-} o au^{-} \overline{ u}_{ au})$	$(5.55 \pm 0.24) \times 10^{-2}$
$\mathcal{B}(D^- \to \mu^- \overline{\nu}_{\mu})$	$(3.74 \pm 0.17) imes 10^{-4}$
$\mathcal{B}(K^- \to e^- \overline{\nu}_e)$	$(1.581 \pm 0.008) imes 10^{-5}$
${\cal B}(K^- o \mu^- \overline{ u}_\mu)$	0.6355 ± 0.0011
${\cal B}(au^- o K^- \overline{ u}_ au)$	$(0.6955 \pm 0.0096) \times 10^{-2}$
$\mathcal{B}(K^- \to \mu^- \overline{\nu}_\mu) / \mathcal{B}(\pi^- \to \mu^- \overline{\nu}_\mu)$	1.3365 ± 0.0032
${\cal B}(au^- o K^- \overline{ u}_ au) / {\cal B}(au^- o \pi^- \overline{ u}_ au)$	$(6.43\pm0.09) imes10^{-2}$
${\cal B}(B_s o \mu \mu)$	$(2.8^{+0.7}_{-0.6}) imes 10^{-9}$
$ V_{cd} f_{\perp}^{D \to \pi}(0)$	0.148 ± 0.004
$ V_{cs} f_+^{D \to K}(0)$	0.712 ± 0.007

CKMFitter (using unitarity)

 $|V_{cd}| = 0.22529^{+0.00041}_{-0.00032}$ $|V_{cs}| = 0.973394^{+0.000074}_{-0.000096}$

Direct extraction using lattice (HFAG+FLAG $|V_{cd}| = 0.2164(63)$ $|V_{cs}| = 1.008(21)$ Leptonic $|V_{cd}| = 0.214(12)$ Semileptonic $|V_{cs}| = 0.975(32)$ • Great advance in lattice determination of decay constants and form factors enables progress in testing consistency of the SM

• Assuming unitarity of V_{CKM} , the Values of V_{cs} and V_{cd} are dominated by V_{cb} measurement and nuclear & kaon data;

• V_{cs} and V_{cd} values are largely driven by indirect constraints;



Search for NP in charged current transitions (charm mesons)

 \succ Effective Lagrangian approach describing NP in $c \rightarrow s l \nu_l$ transition;

- Pseudoscalar operator Wilson coefficients

- Scalar operator

> NP in branching ratios, forward-backward asymmetry transversal muon polarization;

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1502.07488, S.F., I. Nišandžić, U. Rojec
1404.0454, J. Barranco et al.,
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Why to search for NP in charm meson semileptonic decays?

- \succ Important to know CKM matrix elements V_{cs} and V_{cd};
- > High precision results for the decay constants, or form-factors required!
- \succ In $~B \rightarrow D^{(*)} \tau \nu_{\tau}$ observed disagreement of experimental and SM prediction.



Questions for theory:

- Can current precision on charm meson decay constants/form factors enables to search for New Physics in charm?
- What are the most appropriate observables?

Approach:

Effective Lagrangian to describe NP in $c \rightarrow s l \nu_l$ transition

$$\mathcal{L}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{cs} \sum_{\ell=e,\mu,\tau} \sum_i c_i^{(\ell)} \mathcal{O}_i^{(\ell)} + \text{H.c.}$$

$$\mathcal{O}_{SM}^{(\ell)} = \left(\bar{s}\gamma_{\mu}P_{L}c\right)\left(\bar{\nu}_{\ell}\gamma^{\mu}P_{L}\ell\right) \qquad c_{SM}^{(\ell)} = 1$$

NP proposals in
$$c
ightarrow sl
u_l$$



J. Barranco et al. 1303.3896; Akeyrod and Chen, hep-ph/0701078



e.g.I.Dorsner, S.F.J.F. Kamenik, N. Kosnik, 0906.5585

SUSY A.G. Akeroyd, S. Recksiegel, hep-ph/0210376.

Simplest proposal for NP - scalar/pseudoscalar operators:

$$\begin{bmatrix}
\mathcal{O}_{L(R)}^{(\ell)} = \left(\bar{s}P_{L(R)}c\right)\left(\bar{\nu}_{\ell}P_{R}\ell\right) \\
\mathcal{O}_{V,R}^{(\ell)} = \left(\bar{s}\gamma_{\mu}P_{R}c\right)\left(\bar{\nu}_{\ell}\gamma^{\mu}P_{L}\ell\right)
\end{bmatrix}$$

New physics might modify branching ratios

Examples:

a) THDM type-III, originating from non-holomorpfic Yukawa couplings in the fermion mass-basis;

b) Aligned THDM (Yukawa couplings to neutral scalar flavor diagonal, the complex Yukawa couplings to charged scalar.

$$\mathcal{B}(D_s \to \ell \nu_\ell) = \tau_{Ds} \frac{m_{Ds}}{8\pi} f_{Ds}^2 \left(1 - \frac{m_\ell^2}{m_{Ds}^2} \right)^2 G_F^2 |V_{cs}|^2 m_\ell^2 \left| 1 - c_P^{(\ell)} \frac{m_{Ds}^2}{(m_c + m_s)m_\ell} \right|^2$$

$$c_P^{(\ell)} \equiv c_R^{(\ell)} - c_L^{(\ell)}$$

$$\mathcal{B}(D_s \to \ell \nu_\ell) = \begin{cases} (5.7 \pm 0.21^{+0.31}_{-0.3})\%, & D_s \to \tau \nu_\tau, \\ (0.531 \pm 0.028 \pm 0.020)\%, & D_s \to \mu \nu_\mu, \\ < 1.0 \cdot 10^{-4}, 95\% \,\text{C.L.}, & D_s \to e \nu_e. \end{cases}$$

For $f_{D_s} = 249.0(0.3) \binom{+1.1}{-1.5} \text{ MeV}$ (lattice, Fermilab & MILC) and $V_{cs} = 0.97317 \binom{+0.00053}{-0.00059}$ obtained from global CKM unitarity fit, allowed parameter space of new physics coupling:



 $D \to K^* l \nu_l$

 $c_{\rm P}^{(l)}$ can contribute to $D \to K^* l \nu_l$ (four form-factors necessary!) Using helicity formalism:

$$\begin{split} H_{\pm}(q^2) &= \mp \frac{\sqrt{\lambda(m_P^2, m_V^2, q^2)}}{m_P + m_V} V(q^2) + (m_P + m_V) A_1(q^2) \\ H_0(q^2) &= \frac{1}{2m_V \sqrt{q^2}} \left[(m_P + m_V) (m_P^2 - m_V^2 - q^2) A_1(q^2) - \frac{\lambda(m_P^2, m_V^2, q^2)}{m_P + m_V} A_2(q^2) \right] \\ H_t(q^2) &= \left[1 - c_P^{(\ell)} \frac{q^2}{m_\ell (m_q + m_{\bar{q}})} \right] \frac{\sqrt{\lambda(m_P^2, m_V^2, q^2)}}{\sqrt{q^2}} A_0(q^2). \end{split}$$

$$c_{\rm P}^{(l)}$$
 modifies H_t $H_t \rightarrow \left(1 - c_P^{(\ell)} \frac{q^2}{m_\ell(m_c + m_s)}\right) H_t$

Rather weak knowledge of form-factors. $V(0)/A_1(0) = 1.463 \pm 0.035$ FOCUS performed non-parametric $A_2(0)/A_1(0) = 0.801 \pm 0.03$ measurements of helicity amplitudes $A_1(0) = 0.6200 \pm 0.0057$ (errors too big), hep-ph /0509027; BaBar (1012.1810) single pole parameterization PDG: $R_{L/T} = \frac{\Gamma_L}{\Gamma_T}$ used in our fit: $R_{L/T} = 1.13 \pm 0.08$ $\frac{d\Gamma_L}{dq^2} = \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) |H_0|^2 + \frac{3m_\ell^2}{2q^2} |H_t|^2 \right] \frac{d\Gamma_T}{dq^2} = \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2 + |H_-|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(|H_+|^2\right) \right] \frac{d\Gamma_T}{dq^2} + \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2} \left(1 - \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \left(1 - \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2} \left(1 - \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2} \left(1 - \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{m_\ell^2}{2q^2} \left(1 - \frac{m_\ell^2}{2q^2}\right) \frac{d\Gamma_T}{dq^2} + \frac{$ $\mathcal{N}(q^2) = G_F^2 |V_{cs}|^2 q^2 |\mathbf{q}| / (96\pi^3 m_D^2)$ 1.0 $R_{L/T}$ 0.5 Not competitive with the $\operatorname{Im}(c_{P}^{(\mu)})$ constraints coming from pure 0.0 leptonic decay! -0.5

-1.0

-0.5

0.0

0.5

 $\operatorname{Re}(c_{P}^{(\mu)})$

1.0

15

The Wilson coefficient of the scalar operator

NP in
$$D o K l \nu_l$$

$$\langle K(k')|\bar{s}\gamma_{\mu}c|D(k)\rangle = f_{+}(q^{2})\left((k+k')_{\mu} - \frac{m_{D}^{2} - m_{K}^{2}}{q^{2}}q_{\mu}\right) + f_{0}(q^{2})\frac{m_{D}^{2} - m_{K}^{2}}{q^{2}}q_{\mu}$$

$$f_{+}(0) = f_{0}(0)$$

$$h_{0}(q^{2}) = \frac{\sqrt{\lambda(m_{D}^{2}, m_{K}^{2}, q^{2})}}{\sqrt{q^{2}}} f_{+}(q^{2})$$
Helicity amplitudes
$$h_{t}(q^{2}) = \left(1 + c_{S}^{(l)} \frac{q^{2}}{m_{\ell}(m_{s} - m_{c})}\right) \frac{m_{D}^{2} - m_{K}^{2}}{\sqrt{q^{2}}} f_{0}(q^{2})$$

$$\frac{d\Gamma^{(\ell)}}{dq^2} = \frac{G_F^2 |V_{cs}|^2 |\mathbf{q}| q^2}{96\pi^3 m_D^2} \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[|h_0(q^2)|^2 \left(1 + \frac{m_\ell^2}{2q^2}\right) + \frac{3m_\ell^2}{2q^2} |h_t(q^2)|^2\right]$$

$$\mathcal{B}(D \to K \ell \nu_{\ell}) = \begin{cases} (8.83 \pm 0.22)\%, & D^+ \to \bar{K}^0 e^+ \nu_e, \\ (9.2 \pm 0.6)\%, & D^+ \to \bar{K}^0 \mu^+ \nu_{\mu}, \\ (3.55 \pm 0.04)\%, & D^0 \to K^- e^+ \nu_e, \\ (3.30 \pm 0.13)\%, & D^0 \to K^- \mu^+ \nu_{\mu}. \end{cases}$$

Form-factors calculated by lattice collaboration HPQCD (1305.1462) crosses $D \to K$ circles $D_s \to \eta$





Allowed region for ${\rm c_s}$ from $BR(D \to K l \nu_l)$

NP in differential width distribution



NP, allowed by constraint from the fit of c_s from the branching ratio

Check of lepton universality



Forward-backward asymmetry in $D \rightarrow K l \nu_l$

$$\vec{q} = 0 \qquad \frac{d^2 \Gamma^{(\ell)}}{dq^2 d \cos \theta_{\ell}} = a_{\ell}(q^2) + b_{\ell}(q^2) \cos \theta_{\ell} + c_{\ell}(q^2) \cos^2 \theta_{\ell}.$$

$$b_{\ell}(q^2) = -\frac{G_F^2 |V_{cs}|^2 |\mathbf{q}| q^2}{128\pi^3 m_D^2} \left(1 - \frac{m_{\ell}^2}{q^2}\right)^2 \frac{m_{\ell}^2}{q^2} 2Re(h_0 h_t^*)$$

$$(z^2) = \int_{-1}^0 \frac{d^2 \Gamma^{(\ell)}(q^2)}{dq^2 d \cos \theta_{\ell}} d\cos \theta_{\ell} - \int_0^1 \frac{d^2 \Gamma^{(\ell)}(q^2)}{dq^2 d \cos \theta_{\ell}} d\cos \theta_{\ell} \qquad b_{\ell}(q^2)$$

$$A_{FB}^{(\ell)}(q^2) \equiv \frac{\int_{-1}^0 \frac{d^2 \Gamma^{(\ell)}(q^2)}{dq^2 d \cos \theta_\ell} d \cos \theta_\ell - \int_0^1 \frac{d^2 \Gamma^{(\ell)}(q^2)}{dq^2 d \cos \theta_\ell} d \cos \theta_\ell}{d\Gamma^{(\ell)}/dq^2 (q^2)} = -\frac{b_\ell(q^2)}{d\Gamma^{(\ell)}(q^2)/dq^2}$$



Sensitive on the real part of $c_s!$

SM value:
$$\langle A_{FB}^{(\mu)} \rangle = 0.055(2)$$

Forward-backward asymmetry would not show deviation from SM! THDM with more general flavor structure might lead to different c_S and c_P and A_{FB} can differ from SM.

NP in transversal muon polarization

The relative complex phase between nonstandard scalar Wilson coefficient and V_{cs} is a possible new source of the CP violation.

The measurement of the T-odd transverse polarization of charge lepton might give information on that effect. In SM it is vanishing effect.

$$P_{\perp}^{(\mu)} = \frac{|\mathcal{A}(\vec{s})|^2 - |\mathcal{A}(-\vec{s})|^2}{|\mathcal{A}(\vec{s})|^2 + |\mathcal{A}(-\vec{s})|^2} \qquad \begin{array}{c} \mathcal{A}(\mathbf{spin}) \\ \mathbf{spin} \\ \vec{s} \equiv (\vec{p}) \end{array}$$

 $\mathcal{A}(\pmec{s})$ amplitude for spin projection along $ec{s}$

 $\vec{s} \equiv (\vec{p}_K \times \vec{p}_\ell) / |\vec{p}_K \times \vec{p}_\ell|$

$$P_{\perp}^{(\mu)}(q^2, E_{\mu}) = \left(\frac{d\Gamma}{dq^2 dE_{\mu}}\right)^{-1} \kappa(q^2, E_{\mu}) \operatorname{Im}\left(h_0(q^2)h_t^*(q^2)\right)$$

For allowed value of $c_S^{(\mu)} \simeq \pm \, 0.1 \, i$

$$\langle P_{\perp}^{(\mu)} \rangle \simeq \pm 0.2$$

New physics in charm FCNC processes



NP in
$$c \rightarrow u l^+ l^-$$





The same couplings immediately create contributions to $\,D^0-\bar{D}^0\,$



Properties of FCNC in charm rare decays

- conspiracy: d,s, b quarks are in the loops; =
- very strong GIM suppression;
- $\mathbf{m}_{s,d} \ll \Lambda_{QCD}$

long distance contribution dominant!



up quark weak doublet "talks" to down quark via CKM!

SM effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = \lambda_d \mathcal{H}^d + \lambda_s \mathcal{H}^s - \frac{4G_F \lambda_b}{\sqrt{2}} \sum_{i=3,\dots,10,S,P,\dots} C_i \mathcal{O}_i$$

Tree-level 4-quark operators

(Short-distance) penguin operators

1) At scale m_w all penguin contributions vanish due to GIM;

2) SM contributions to $C_{7...10}$ at scale mc entirely due to mixing of treelevel operators into penguin ones under QCD (de Boer, Hiller, 1510.00311)

3) SM values at m_c $C_7 = 0.12, \quad C_9 = -0.41$

4) All operators' contributions to $D \rightarrow \pi II$ can be absorbed into q^2 dependent effective Wilsons $C_{7,9eff}(q^2)$

Breit-Wigner model for the qq resonances



SM short distance rate not accessible

(borrowed from de Boer, Hiller, 1510.00311)

$$C_9^{\rm res} = \frac{\lambda_d}{\lambda_b} \left[\frac{a_\rho}{q^2 - m_\rho^2 + i\sqrt{q^2}\Gamma_\rho} + \cdots \right]$$
$$C_S^{\rm res} = \frac{\lambda_d}{\lambda_b} \left[\frac{a_\eta m_\eta^2}{q^2 - m_\eta^2 + im_\eta\Gamma_\eta} + \cdots \right]$$

Fix $|a_{\chi}|$ from measured D $\rightarrow X\pi$, X $\rightarrow II$ We marginalise over the unknown phase of a_{χ}



Maximally allowed values of the Wilson coefficents in the low and high energy bins



 $BR(\pi^+\mu^+\mu^-)_I \equiv BR(D^+ \to \pi^+\mu^+\mu^-)_{q^2 \in [0.0625, 0.276] \text{ GeV}^2} < 2.5 \times 10^{-8}$

 $BR(\pi^+\mu^+\mu^-)_{II} \equiv BR(D^+ \to \pi^+\mu^+\mu^-)_{q^2 \in [1.56, 4.00] \text{ GeV}^2} < 2.9 \times 10^{-8}$

	$ ilde{C}_i _{ ext{max}}$		
	$BR(\pi\mu\mu)_{I}$	$BR(\pi\mu\mu)_{II}$	$\mathrm{BR}(D^0 \to \mu \mu)$
\tilde{C}_7	2.4	1.6	-
$ ilde{C}_9$	2.1	1.3	-
$ ilde{C}_{10}$	1.4	0.92	0.63
$ ilde{C}_S$	4.5	0.38	0.049
$ ilde{C}_P$	3.6	0.37	0.049
$ ilde{C}_T$	4.1	0.76	-
$ ilde{C}_{T5}$	4.4	0.74	-
$\left\ \tilde{C}_9 = \pm \tilde{C}_{10}\right\ $	1.3	0.81	0.63

$$|\tilde{C}_i| = |V_{ub}V_{cb}^*C_i|$$
 region l

region II

 $q^2 \in [0.0625, 0.276] \, GeV^2$

 $q^2 \in [1.56, 4.00] \, GeV^2$

$$BR(D^0 \to \mu^+ \mu^-) < 7.6 \times 10^{-9}$$



Forward-backward asymmetry for the resonant background itself (orange) and in the scenario $C_S=0.049/\lambda_b$ $C_T=0.2/\lambda_b$

Test of lepton flavour universality violation

In 1510.0311 (de Beor and Hiller) it was pointed out that bounds on electron-positron mode are weaker:

$$BR(D^{+} \to \pi^{+}e^{+}e^{-}) < 1.1 \times 10^{-6}$$
$$BR(D^{0} \to e^{+}e^{-}) < 7.9 \times 10^{-8}$$
$$\begin{vmatrix} |C_{S,P}^{(e)} - C_{S,P}^{(e)\prime}| \lesssim 0.3, \\ |C_{9,10}^{(e)} - C_{9,10}^{(e)\prime}| \lesssim 4, \\ |C_{T,T5}^{(e)}| \lesssim 5, \quad |C_{7} \left(C_{9}^{(e)} - C_{9}^{(e)\prime} \right)| \lesssim 2 \end{vmatrix}$$

In 1510.0965 (S.F. and N. Košnik) it was suggested, assuming as in the case $B \to K e^+ e^-$ that NP does not affect electron-positron mode, that tests of LFU can be performed either in I or II bin

$$R_{\pi}^{\mathrm{I}} = \frac{\mathrm{BR}(D^+ \to \pi^+ \mu^+ \mu^-)_{q^2 \in [0.25^2, 0.525^2] \mathrm{GeV}^2}}{\mathrm{BR}(D^+ \to \pi^+ e^+ e^-)_{q^2 \in [0.25^2, 0.525^2] \mathrm{GeV}^2}}$$

$$R_{\pi}^{\mathrm{II}} = \frac{\mathrm{BR}(D^+ \to \pi^+ \mu^+ \mu^-)_{q^2 \in [1.25^2, 1.73^2] \mathrm{GeV}^2}}{\mathrm{BR}(D^+ \to \pi^+ e^+ e^-)_{q^2 \in [1.25^2, 1.73^2] \mathrm{GeV}^2}}$$

	$ ilde{C}_i _{\max}$	R_{π}^{II}
SM	-	0.999 ± 0.001
$ ilde{C}_7$	1.6	$\sim 6 100$
	1.3	~ 6120
$ ilde{C}_{10}$	0.63	$\sim 3 – 30$
$ ilde{C}_S$	0.05	$\sim 1-2$
$ ilde{C}_P$	0.05	$\sim 1-2$
$ ilde{C}_T$	0.76	~ 670
$ ilde{C}_{T5}$	0.74	$\sim 6-60$
$\tilde{C}_9 = \pm \tilde{C}_{10}$	0.63	$\sim 3-60$
$\left\ \tilde{C}_{9}' = -\tilde{C}_{10}'\right\ _{\mathrm{LQ}(3,2,7/6)}$	0.34	$\sim 1-20$

 $R_{\pi}^{I,SM} = 0.87 \pm 0.09$ $R_{\pi}^{II,SM} = 0.999 \pm 0.001$

Assumptions:

- e⁺e⁻ mode are SM-like;
- NP enters in $\mu^+\mu^-$ mode only;
- listed Wilson coefficients are maximally allowed by current LHCb data.

Lepton flavor violation

1510.0311 (de Beor and Hiller) $c
ightarrow u \mu^{\pm} e^{\mp}$

$$\mathcal{L}_{\text{eff}}^{\text{weak}}(\mu \sim m_c) = \frac{4G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \sum_i \left(K_i^{(e)} O_i^{(e)} + K_i^{(\mu)} O_i^{(\mu)} \right)$$
$$O_9^{(e)} = (\bar{u}\gamma_\mu P_L c) \left(\bar{e}\gamma^\mu \mu \right) \qquad O_9^{(\mu)} = (\bar{u}\gamma_\mu P_L c) \left(\bar{\mu}\gamma^\mu e \right)$$

$$\begin{split} BR(D^0 \to e^+\mu^- + e^-\mu^+) &< 2.6 \times 10^{-7} \\ BR(D^+ \to \pi^+ e^+\mu^-) &< 2.9 \times 10^{-6} \\ BR(D^+ \to \pi^+ e^-\mu^+) &< 3.6 \times 10^{-6} \end{split}$$

$$\begin{vmatrix} K_{S,P}^{(l)} - K_{S,P}^{(l)\prime} \end{vmatrix} \lesssim 0.4 , \begin{vmatrix} K_{9,10}^{(l)} - K_{9,10}^{(l)\prime} \end{vmatrix} \lesssim 6 , \quad \begin{vmatrix} K_{T,T5}^{(l)} \end{vmatrix} \lesssim 7 ,$$

 $l = e, \mu$

$$BR(D^0 \to e^{\pm}\tau^{\mp}) < 7 \times 10^{-15}$$

Specific models Scalar Leptoquaks (3,2,7/6) $\mathcal{L}^{(5/3)} = (\bar{\ell}_R Y_L u_L) \Delta^{(5/3)*} - (\bar{u}_R Y_R \ell_L) \Delta^{(5/3)} + \text{h.c.}$ generates S, P, T,T_{s} , V and A In the case of Δ C= 2 in $D^0 - \bar{D}^0$ $\mathcal{H} = C_6(\bar{u}_R \gamma^\mu c_R)(\bar{u}_R \gamma_\mu c_R)^+$ oscillation there is also a LQ contribution $C_6(m_{\Delta}) = -\frac{\left(Y_{c\mu}^{R*}Y_{u\mu}^R\right)^2}{64\pi^2 m_{\star}^2} = -\frac{(G_F\alpha)^2}{32\pi^4} m_{\Delta}^2 (\tilde{C}_{10}')^2$ $|C_6(m_{\Delta})| < 2.5 \times 10^{-13} \text{ GeV}^{-2} \implies |\tilde{C}_9', \tilde{C}_{10}'| < 0.34$

Bound from ΔC =2 slightly stronger, but comparable to the bound coming from $D^0 \to \mu^+ \mu^-$

$$-\tilde{C}_{10}'=\tilde{C}_9'=0.63\,,$$

 $4\tilde{C}_T = 4\tilde{C}_{T5} = \tilde{C}_P = \tilde{C}_S = -0.049$

Vector Leptoquark (3,1,5/3)

$$\mathcal{L} = Y_{ij} \left(\bar{\ell}_i \gamma_\mu P_R u_j \right) V^{(5/3)\mu} + \text{h.c.} .$$
$$C'_9 = C'_{10} = \frac{\pi}{\sqrt{2}G_F \lambda_b \alpha} \frac{Y_{\mu c} Y^*_{\mu u}}{m_V^2}$$
$$C_6(m_V) = \frac{(Y_{\mu u} Y^*_{\mu c})^2}{32\pi^2 m_V^2} = \frac{(G_F \alpha)^2}{16\pi^4} m_V^2 (\tilde{C}'_{10})^2$$
$$|\tilde{C}'_9, \tilde{C}'_{10}| < 0.24$$

 $D \to \pi \mu^+ \mu^-$ In the high q² region branching ratio is 1.4×10^{-8} two times smaller then the experimental bound

Two Higgs doublet model type III

Two neutral scalars, h and H, one pseudoscalar A, two charged H[±]; Flavor changing neutral couplings at tree level generated.

$$\mathcal{L} = \frac{y_{ij}^{(\ell)H_k}}{\sqrt{2}} H_k \bar{\ell}_{L,i} \ell_{R,j} + \frac{y_{ij}^{(u)H_k}}{\sqrt{2}} H_k \bar{u}_{L,i} u_{R,j} + \text{h.c.} \quad H_k = (H, h, A)$$

$$-C_P = C_S = \frac{\pi}{4\sqrt{2}G_F \alpha \lambda_b} \frac{m_\mu}{v} \frac{\epsilon_{12}^{u*} \tan \beta}{m_H^2} \qquad \qquad \text{from } \frac{\text{BR}(D^0 \to \mu^+ \mu^-)}{|\tilde{C}_S - \tilde{C}'_S| \le 0.05}$$

$$C'_P = C'_S = \frac{\pi}{4\sqrt{2}G_F \alpha \lambda_b} \frac{m_\mu}{v} \frac{\epsilon_{21}^{u} \tan \beta}{m_H^2} \qquad \qquad |\tilde{C}_P - \tilde{C}'_P| \le 0.05$$

$$|\tilde{C}_P - \tilde{C}'_P| \le 0.05$$

 v_u

Anomalies in B decays often explained by Z'. $D^0 - \overline{D}^0$ transitions constrain $C_6(m_{Z'}) = \frac{|C^u|^2}{2m_{Z'}^2}$ $c \to u\mu^+\mu^-$

 $m_{Z'} \sim 1 \,\,{
m TeV} \quad |C_9| \lesssim 8 \quad |C_{10}| \lesssim 100$ negligible effects!

Model	Effect	Size of the effect
Spin-1 weak triplet	$C_9 = -C_{10}$	C ₉ < 10
Scalar leptoquark (3,2,7/6)	C _S ,C _P , C _S ',C _P ',C _T ,C _{T5} , C ₉ ,C ₁₀ ,C ₉ ',C ₁₀ '	V _{cb} V _{ub} C _{9,} C ₁₀ < 0.34
Vector leptoquark (3,1,5/3)	C ₉ ' = C ₁₀ '	V _{cb} V _{ub} C ₉ ′, C ₁₀ ′ < 0.24
Two Higgs doublet Model type III	C _S ,C _P , C _S ',C _P '	$V_{cb}V_{ub} C_{s}-C_{s}' < 0.005$ $V_{cb}V_{ub} C_{P}-C_{P}' < 0.005$
Z' model	C ₉ ',C ₁₀ '	V _{cb} V _{ub} C ₉ ', <0.001 V _{cb} V _{ub} C ₁₀ ' <0.014



a) Prospect of NP in charged current D meson transitions

Scalar and pseudoscalar operators describing NP contributions considered in Cabibbo allowed leptonic and semileptonic charmed meson decays;

> A number of variables suitable to test NP contributions were discussed as: differential branching ratio, forward-backward asymmetry, transversal muon asymmetry for $D \to K l \nu_l$ and $R_{L/T}$ for $D \to K^* l \nu_l$;

> In order to get tight constraints on NP one needs:

a) Lattice calculations of form factors in $D \to P$ and $D \to V$; b) High precision experimental studies of all observables.

b) Prospect of NP in FCNC D decays

- ➢ Effective Lagrangian approach used to described NP effects: NP can appear in as in SM in C₇, C₉, C₁₀ or in C_s, C_P, C_T, C₇', C₉', C₁₀', C_s', C_P', CT₅;
- > All these Wilson coefficents can be bounded by LHCb results on nonresonant background in $D^+ \to \pi^+ \mu^+ \mu^-$;
- Models of NP : Spin-1 weak triplet, Scalar leptoquark (3,2,7/6), Vector leptoquark (3,1,5/3), Two Higgs doublet model type III, Z' model might contribute to Wilson coefficients;
- Suggestion: to check of LFU violation.

Thanks!



$$\begin{aligned} a_{CP}(\sqrt{q^2}) &\equiv \frac{|\mathcal{A}|^2 - |\overline{\mathcal{A}}|^2}{|\mathcal{A}|^2 + |\overline{\mathcal{A}}|^2} \\ &= \frac{-3}{2\pi^2} \frac{f_T(q^2)}{a_\phi} \frac{m_c}{m_D + m_\pi} \operatorname{Im} \left[\frac{\lambda_b}{\lambda_s} C_7 \right] \left[\cos \delta_\phi - \frac{q^2 - m_\phi^2}{m_\phi \Gamma_\phi} \sin \delta_\phi \right] \end{aligned}$$

G. Isidori et al, PLB 711, (2012) 46 $|\operatorname{Im}[C_7(m_c)]| \simeq |\operatorname{Im}[C_8^{NP}(m_c)]|$

at scale M≈ 1TeV $|Im[\lambda_b C_7(m_c)]| \simeq (0.1 - 0.4) \times 10^{-2}$



$$D^+ \to \pi^+ \mu^+ \mu^-$$

Relevant matrix elements

$$\langle \pi(k) \,|\, \bar{u}\gamma^{\mu}(1\pm\gamma_5)c \,|\, D(p)\rangle = f_+(q^2) \left[(p+k)^{\mu} - \frac{m_D^2 - m_\pi^2}{q^2} q^{\mu} \right] + f_0(q^2) \frac{m_D^2 - m_\pi^2}{q^2} q^{\mu}$$

$$\langle \pi(k) \, | \, \bar{u}\sigma^{\mu\nu}(1\pm\gamma_5)c \, | \, D(p) \rangle = i \frac{f_T(q^2)}{m_D + m_\pi} \left[(p+k)^\mu q^\nu - (p+k)^\nu q^\mu \pm i\epsilon^{\mu\nu\alpha\beta}(p+k)_\alpha q_\beta \right]$$

Most general parametrisation of the amplitude with NP contributions:

$$\mathcal{A}_{\rm SD}(D^+(p) \to \pi^+(p')\mu^+(k_+)\mu^-(k_-)) = \\ = \frac{iG_F\lambda_b\alpha}{\sqrt{2}\pi} \left[V \,\bar{u}\not\!\!\!\!p v + A \,\bar{u}\not\!\!\!p\gamma_5 v + (S + T\cos\theta)\bar{u}v + (P + T_5\cos\theta)\bar{u}\gamma_5 v \right]$$

NP enters through such combinations:

$$\begin{split} V &= \frac{2m_c f_T(q^2)}{m_D + m_\pi} (C_7 + C_7') + f_+(q^2)(C_9 + C_9') + \frac{8f_T(q^2)m_\ell}{m_D + m_\pi} C_T ,\\ A &= f_+(q^2)(C_{10} + C_{10}') ,\\ S &= \frac{m_D^2 - m_\pi^2}{2m_c} f_0(q^2)(C_S + C_S') ,\\ P &= \frac{m_D^2 - m_\pi^2}{2m_c} f_0(q^2)(C_P + C_P') - m_\ell \left[f_+(q^2) - \frac{m_D^2 - m_\pi^2}{q^2} \left(f_0(q^2) - f_+(q^2) \right) \right] (C_{10} + C_{10}') ,\\ T &= \frac{2f_T(q^2)\beta_\ell\lambda^{1/2}}{m_D + m_\pi} C_T ,\\ T_5 &= \frac{2f_T(q^2)\beta_\ell\lambda^{1/2}}{m_D + m_\pi} C_{T5} . \end{split}$$

V, A, S, P, T, T₅ are functions of the appropriate Wilson coefficients.