

WG3 - Rare Decays - Theory Summary

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Rare D decays: theory [Petrov]

- D decays often controlled by long distance effects

- ◆ $D \rightarrow \mu\mu$: $BR_{SD} \sim 10^{-18}$ and $BR_{LD} \sim 10^{-13}$

correlation with D-mixing

- ◆ $D \rightarrow (\pi, \eta, \rho, \omega, \phi, K, K^*, \pi\pi, \pi K, KK, \pi\pi\pi)$

- ◆ $BR(D \rightarrow \pi\mu\mu) \sim 10^{-12}$

Laboratory for NP, e.g. RPV-SUSY, LQ

- $D^*(B^*) \rightarrow ee$: $BR \sim 10^{-19}$, cannot be measured but it might be studied via resonant production!

- ◆ $ee \rightarrow D^*(B^*) \rightarrow D\pi$

- ◆ BEPCII (BESIII) and VEPP-2000

(Novosibirsk) can be tuned to m_{D^*/B^*}

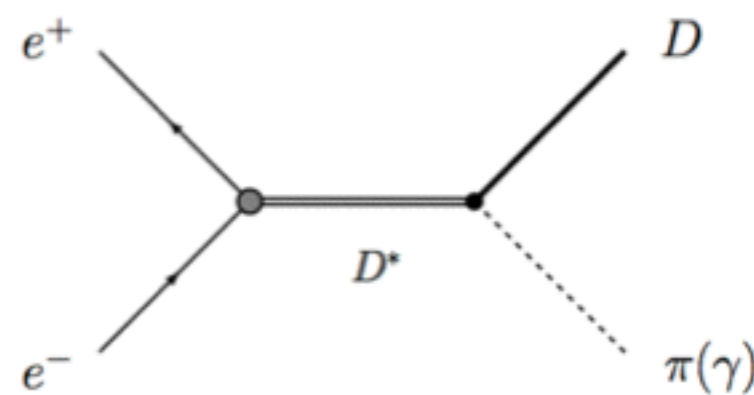
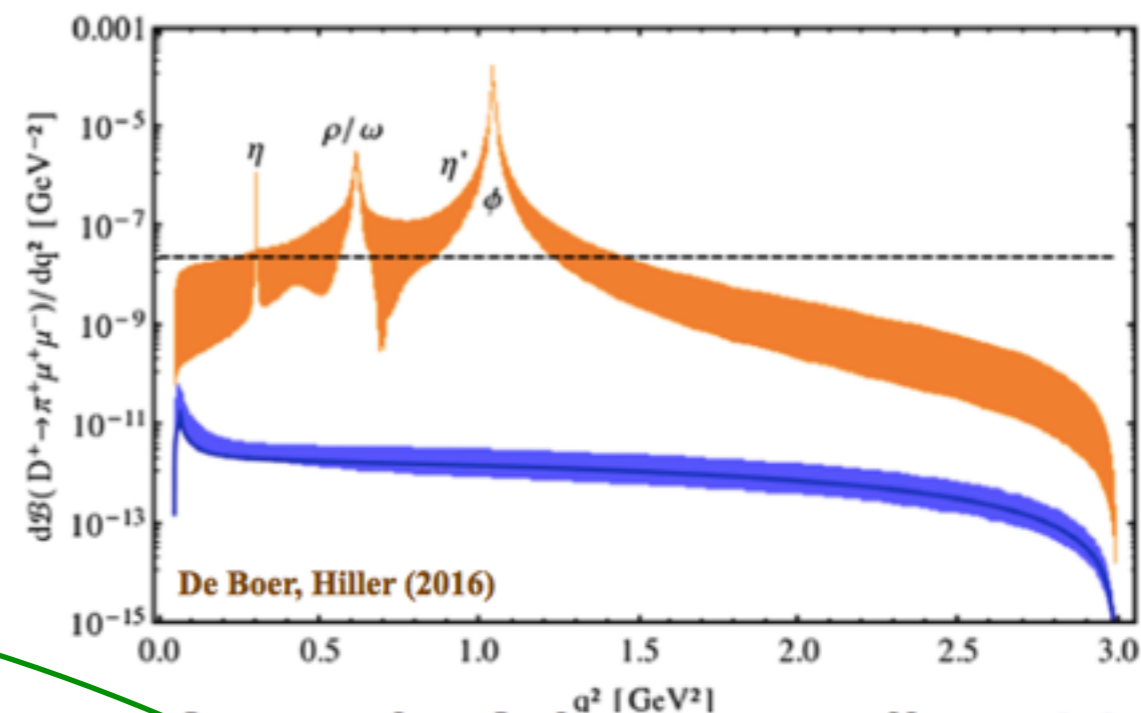
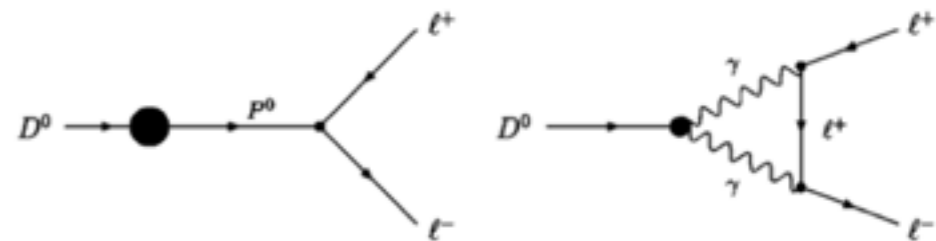
- Lepton Flavor Violation

- ◆ $D \rightarrow \mu e, \gamma\mu e, \pi\mu e, \rho\mu e, \dots$

- Rare decays with missing energy

- ◆ $D \rightarrow \nu\nu, \nu\nu\gamma$

- ◆ Extremely rare but can be used to test dark matter models!



Rare K decays: theory [d'Ambrosio]

$K \rightarrow \pi \nu \nu$

Extremely rare, precisely predicted in SM:

- Amplitude $\propto V_{ts}^* V_{td}$

$K^+ \rightarrow \pi^+ \nu \nu$

- $\text{BR}_{\text{SM}} = (8.22 \pm 0.27_{V_{cb}} \pm 0.29_{\text{non pert}}) \times 10^{-11}$
- Brookhaven E949 (stopped K^+):
 $\text{BR} = (17.3^{+11.5}_{-10.5}) \times 10^{-11}$

$K_L \rightarrow \pi^0 \nu \nu$: never measured

- $\text{BR}_{\text{SM}} = (2.43 \pm 0.25 \pm 0.06_{\text{non pert}}) \times 10^{-11}$
- Grossman-Nir limit on BR:
 $\text{BR}(K_L) \leq \text{BR}(K^+) \times \tau_L / \tau_+ \sim 1.4 \times 10^{-9}$

Other interesting rare K decays

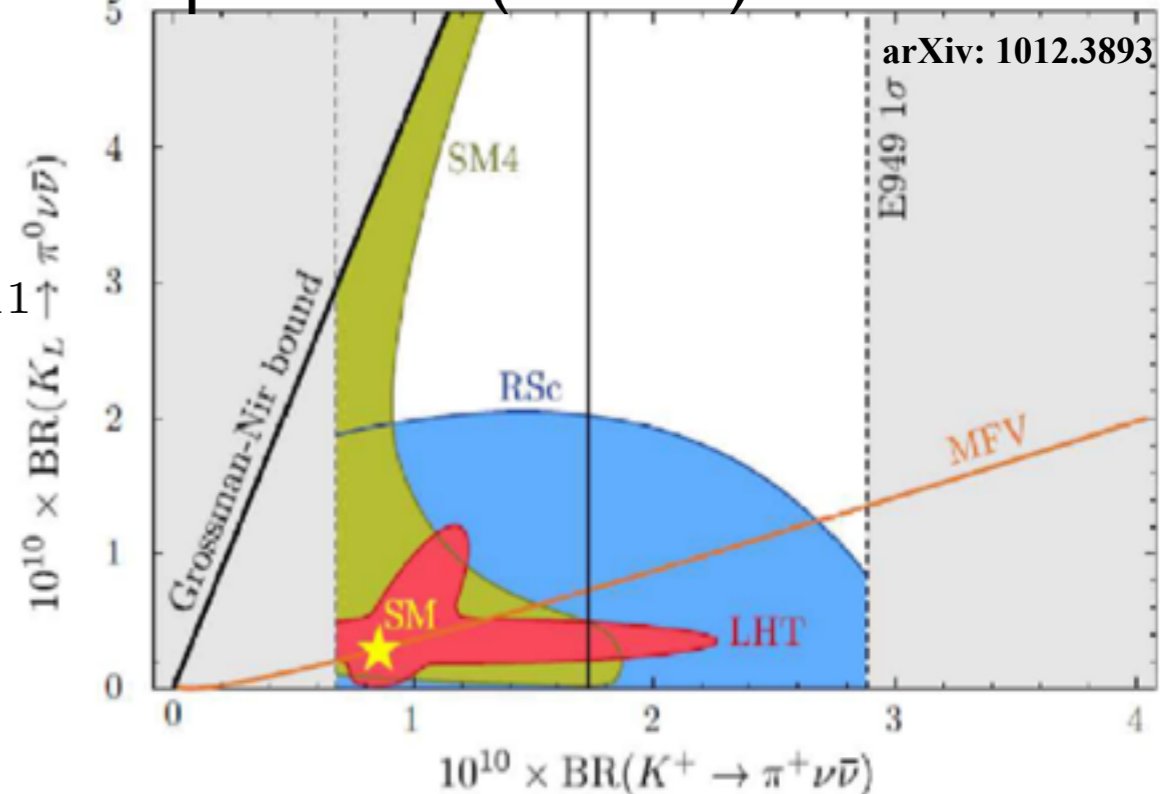
$K^+ \rightarrow \pi^+ ll$ and $K_S \rightarrow \pi^0 ll$

- Controlled by long distance effects
- Test of lepton universality

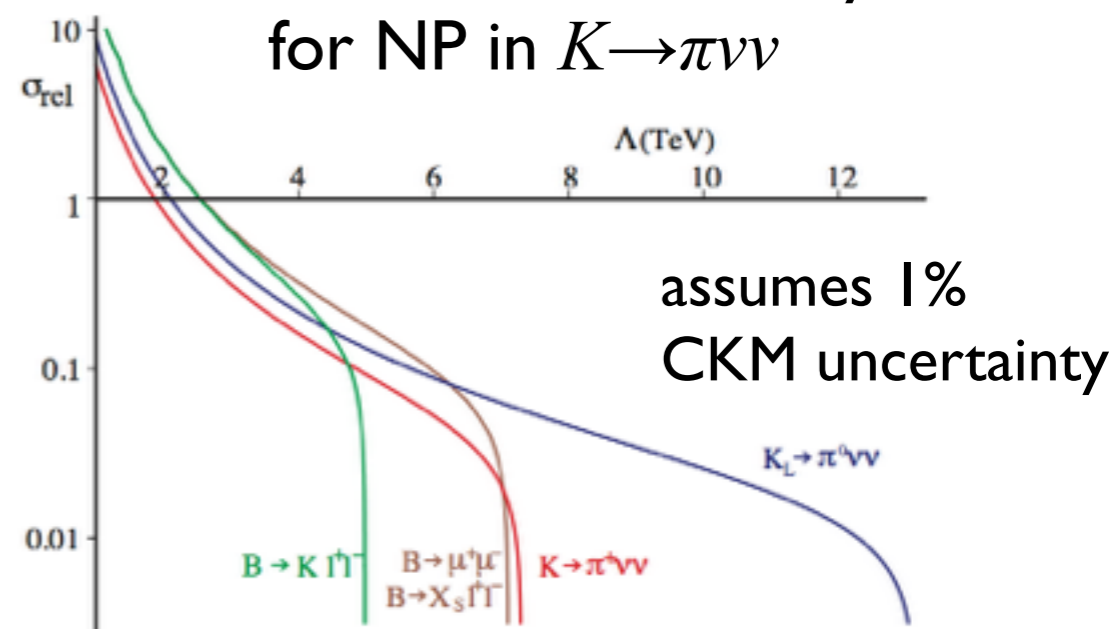
$K^+ \rightarrow \pi^+ \pi^0 \gamma$, $K_L \rightarrow \pi^+ \pi^- ee$, $K^+ \rightarrow \pi^+ \pi^0 ee$, ...

- ChiPT tests
- Direct CP violating charge asymmetry

Expected BR($K \rightarrow \pi \nu \nu$) for NP models



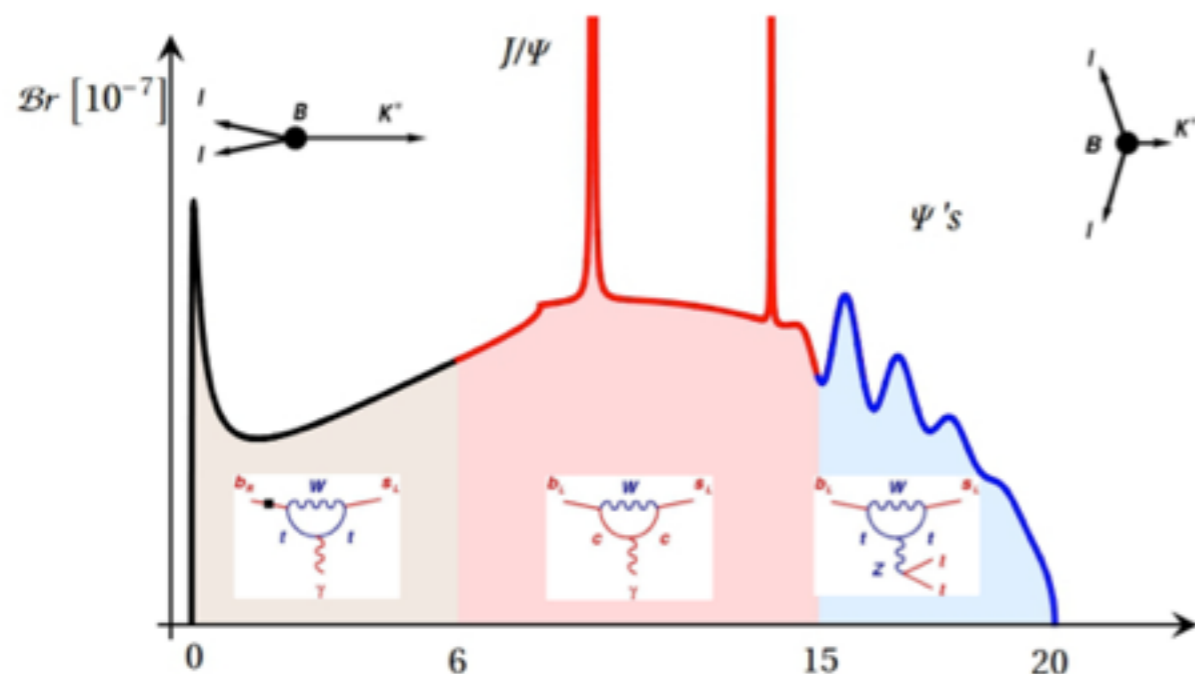
Mass scale sensitivity for NP in $K \rightarrow \pi \nu \nu$



NPB 645 (2002) 155

Theory of exclusive $B \rightarrow K^* l l$ decays [Camalich]

- $R_K = \text{BR}(B^+ \rightarrow K^+ \mu \mu) / \text{BR}(B^+ \rightarrow K^+ e e)$ is very clean
- $B_s \rightarrow \mu \mu$ is clean (depends only on f_{B_s})
- $B \rightarrow K^{(*)} l l$ can be calculated using SCET (at low- q^2) and an OPE (at high- q^2)
 - Many non-perturbative inputs are required. Form factors from lattice-QCD at high- q^2 and LCSR at low- q^2 . Decay constants (f_B, f_K, f_{K^*}) from lattice-QCD. LCDA for $K^{(*)}$ from lattice-QCD. LCDA for B not well known.
 - Presence of charmonium resonances poses a problem at high- q^2 . Violation of quark-hadron duality? Use experimental data (LHCb recent analysis)?
 - Both approaches receive power corrections ($O(\Lambda/m_B)$). How large?

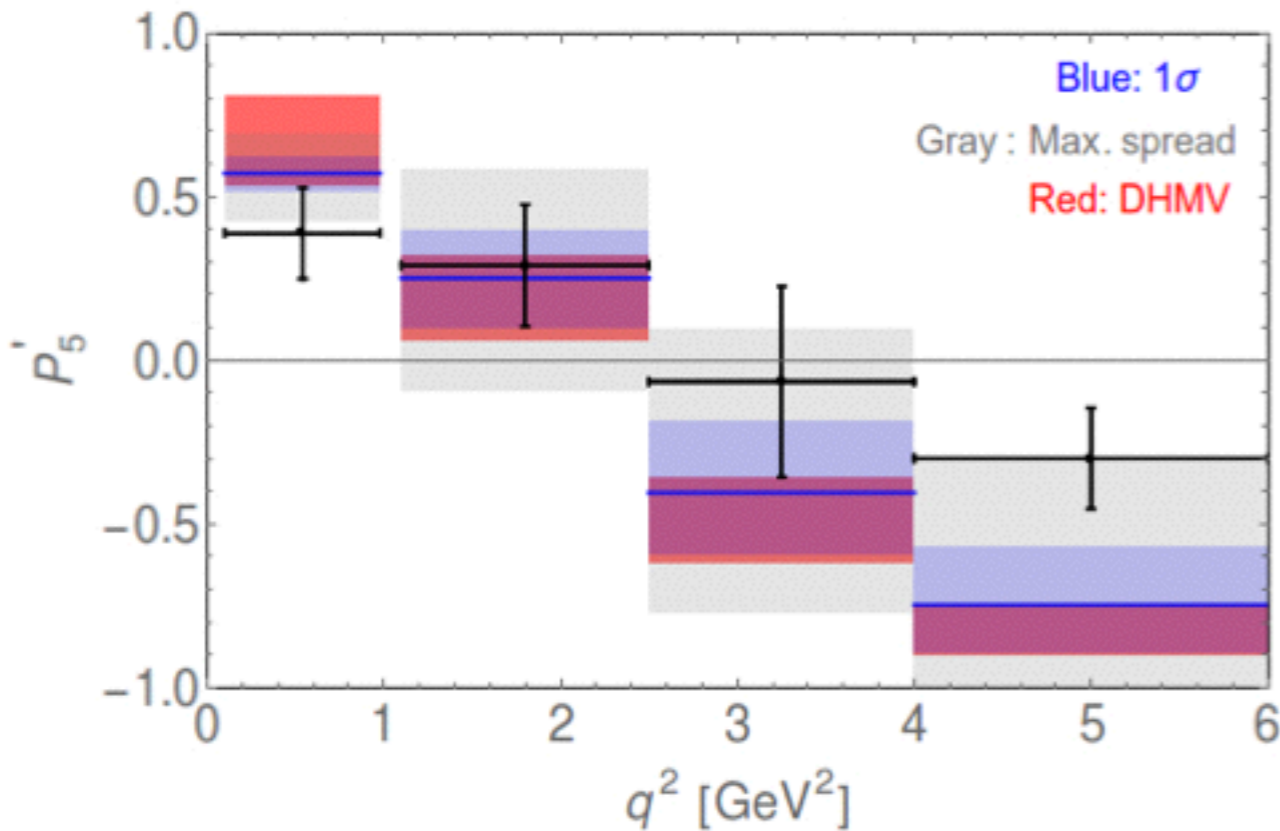


- **Large-recoil region (low q^2)**
 - ▶ LCSR+QCDF/SCET (power-corrections)
 - ▶ Dominant effect of the photon pole
- **Charmonium region**
 - ▶ Dominated by long-distance (hadronic) effects
 - ▶ Starting at the perturbative $c\bar{c}$ threshold $q^2 \simeq 6 - 7 \text{ GeV}^2$
- **Low-recoil region (high q^2)**
 - ▶ LQCD+HQEFT + OPE (duality violation)
 - ▶ Dominated by semileptonic operators

Theory of exclusive $B \rightarrow K^* l l$ decays [Camalich]

$$P'_5 = P'_5|_{\infty} \left(1 + \frac{a_{V_{-}} - a_{T_{-}}}{\xi_{\perp}} \frac{m_B}{|\vec{k}|} \frac{m_B^2}{q^2} C_7^{\text{eff}} \frac{C_{9,\perp} C_{9,\parallel} - C_{10}^2}{(C_{9,\perp}^2 + C_{10}^2)(C_{9,\perp} + C_{9,\parallel})} + \frac{a_{V_0} - a_{T_0}}{\xi_{\parallel}} 2 C_7^{\text{eff}} \frac{C_{9,\perp} C_{9,\parallel} - C_{10}^2}{(C_{9,\parallel}^2 + C_{10}^2)(C_{9,\perp} + C_{9,\parallel})} \right. \\ \left. + 8\pi^2 \frac{\tilde{h}_{-}}{\xi_{\perp}} \frac{m_B}{|\vec{k}|} \frac{m_B^2}{q^2} \frac{C_{9,\perp} C_{9,\parallel} - C_{10}^2}{C_{9,\perp} + C_{9,\parallel}} + \dots \right) + \mathcal{O}(\Lambda^2/m_B^2)$$

Jäger and JMC, PRD93(2016)no.1,014028



Better understanding of had. uncert. desirable!

- **Learn from LCSR** [Bharucha, Straub and Zwicky, arXiv: 1503.05534](#)
- **Charm under control?** [Lyon et al. arXiv:1406.0566, Ciuchini et al. JHEP 1606 \(2016\)](#)

No agreement on this in the literature
See J. Matias, J. Virto



“Extraordinary claims require Extraordinary evidence”

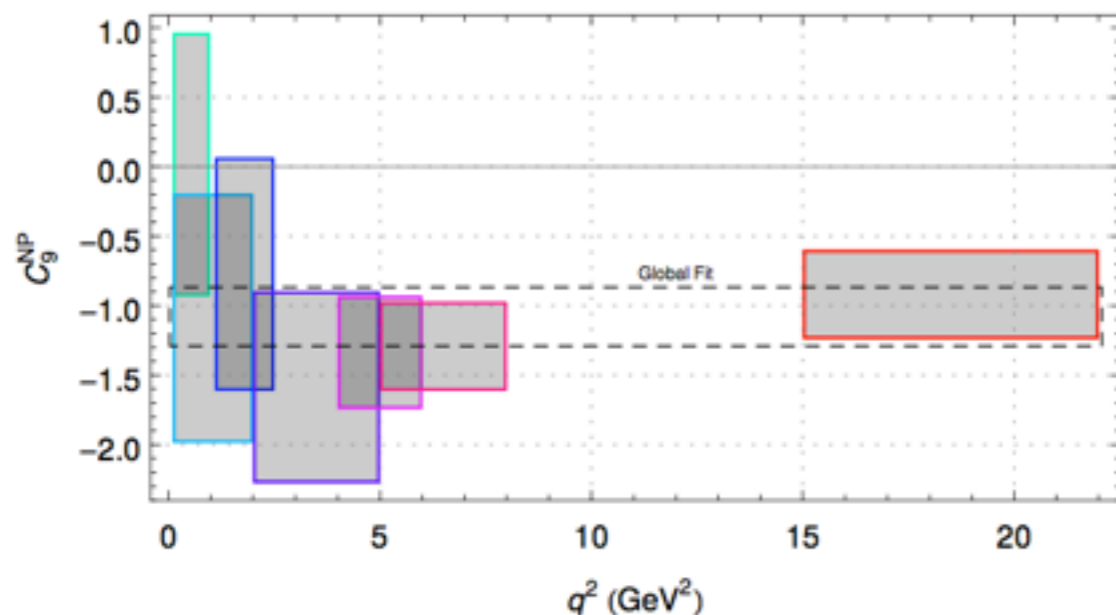
– C. Sagan

Global fits to $b \rightarrow sll$ anomalies [Virto]

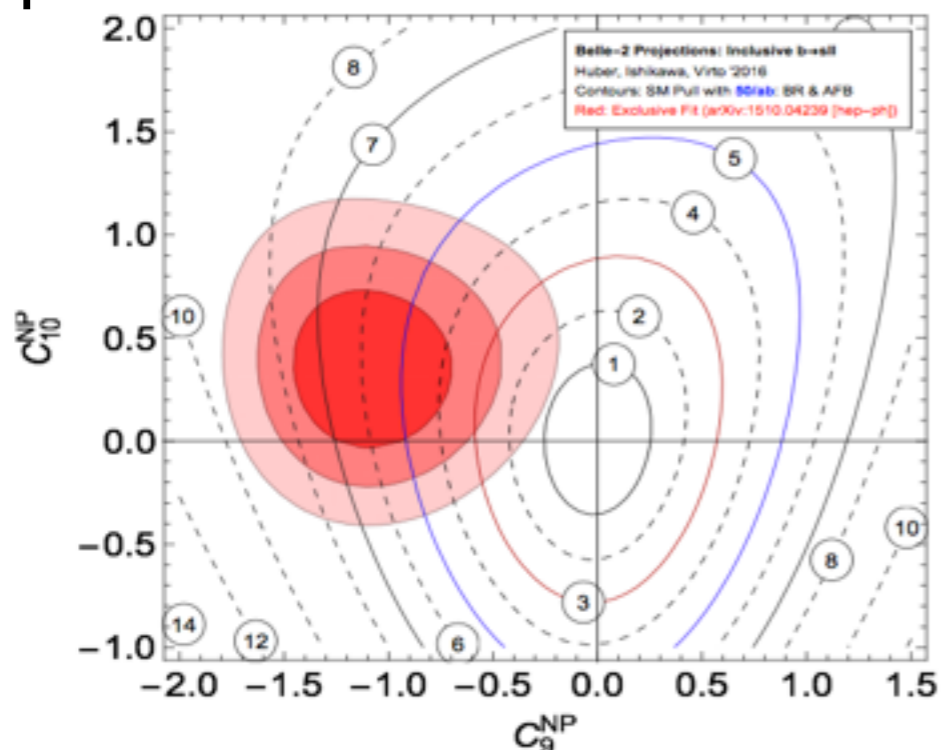
- Inclusion of ~ 100 observables: $B \rightarrow X_s \gamma$, $B \rightarrow X_s ll$, $B_s \rightarrow ll$, $B \rightarrow K^{(*)} \gamma$, $B \rightarrow K^{(*)} ll$, $B_s \rightarrow \phi ll$
- Main theory issues are in $B \rightarrow K^{(*)} ll$
 - ◆ **low- q^2** : SCET, form factors from LCSR [KMPW=Khodjamirian et al 2010], power corrections (correlated central values from KMPW+ uncorrelated 10%), long distance charm effects = [KMPW] \otimes [-1, 1]
 - ☞ assume that LCSR describe correctly size and sign of the power corrections
 - ◆ **high- q^2** : OPE, lattice QCD (HPQCD 2015 for K, Horgan et al 2013 for K^*), possible quark-hadron duality violation modeled as $\pm 10\%$
 - ☞ would be great to have updated results for the K^* form factors
 - ☞ use experimental data to understand interference between charmonium resonances?
- Canonical fit prefers scenarios with non vanishing δC_9 , $\delta C_9 = -\delta C_{10}$ or $\delta C_9 = -\delta C'_9$ with pulls above 4 (but $p_{SM} = 17\%$)

Global fits to $b \rightarrow sl\ell$ anomalies [Virto]

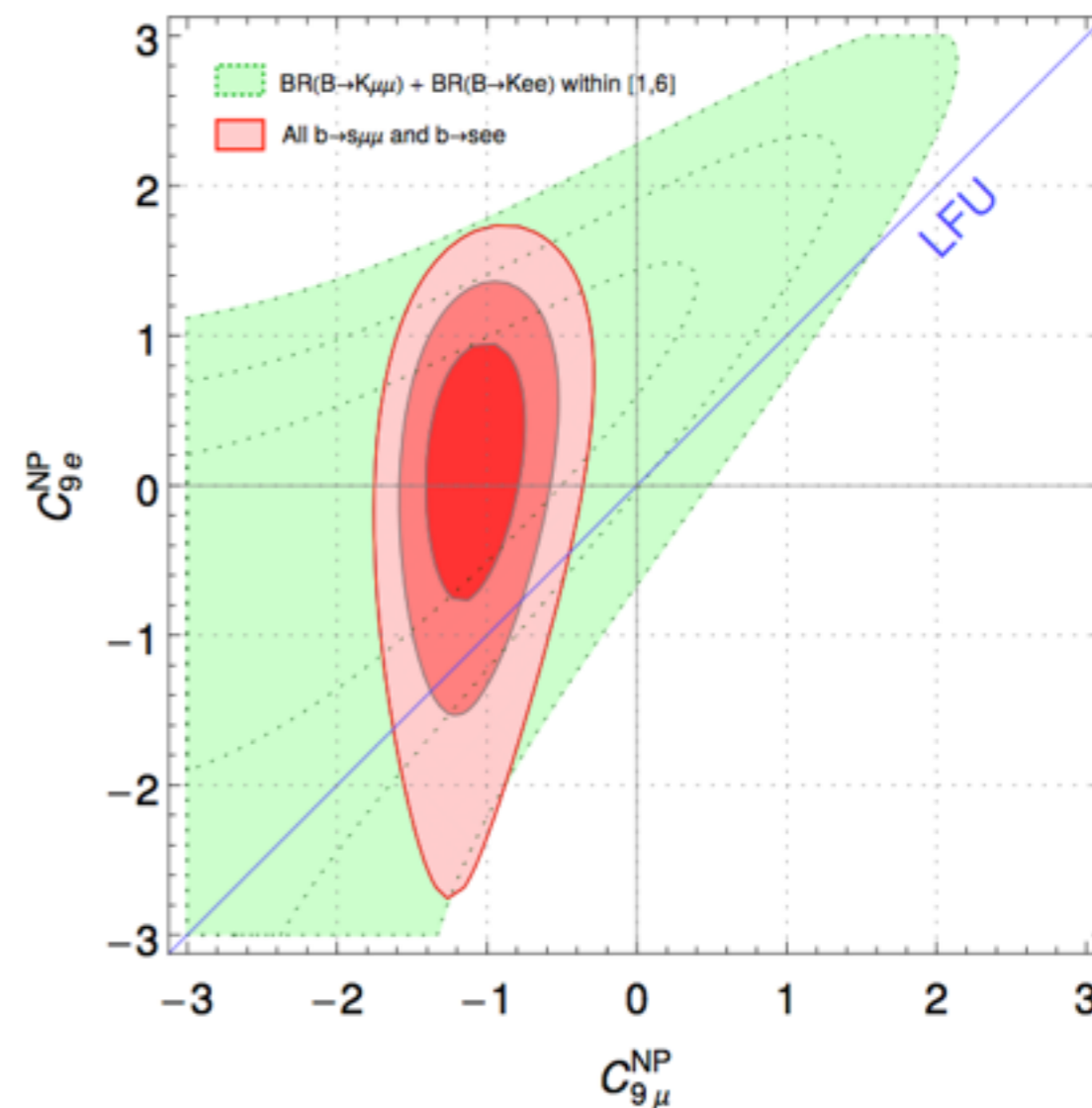
- Fit doesn't show evidence of q^2 dependence:



- Inclusive $b \rightarrow sl\ell$ at Belle-II with 50 ab⁻¹ have the potential to confirm the anomaly:

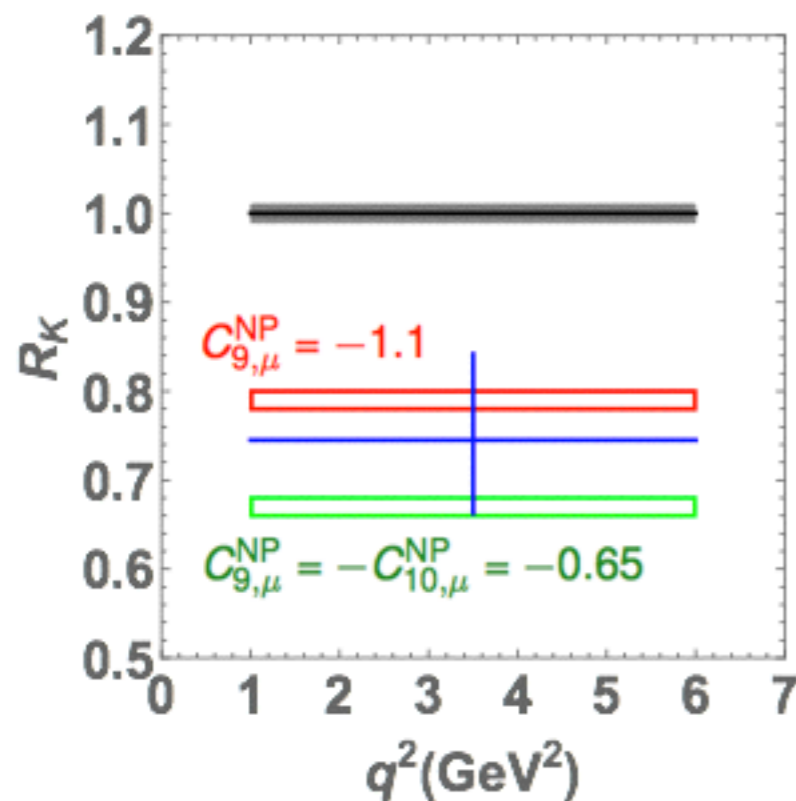


- Assumption of no NP in $(\bar{s}b)(\bar{e}e)$ is supported by the fit:



Lepton Universality Violation in $B \rightarrow K^* ll$ [Matias]

- R_K alone is not sufficient to discriminate between different LFU violating scenarios:



- Can help disentangle NP effects
 - ◆ Q_5' : C_9
 - ◆ $Q_{1,4}$: C_9' , C_{10}' (RH currents)
 - ◆ B_5, B_{6s} : C_{10}

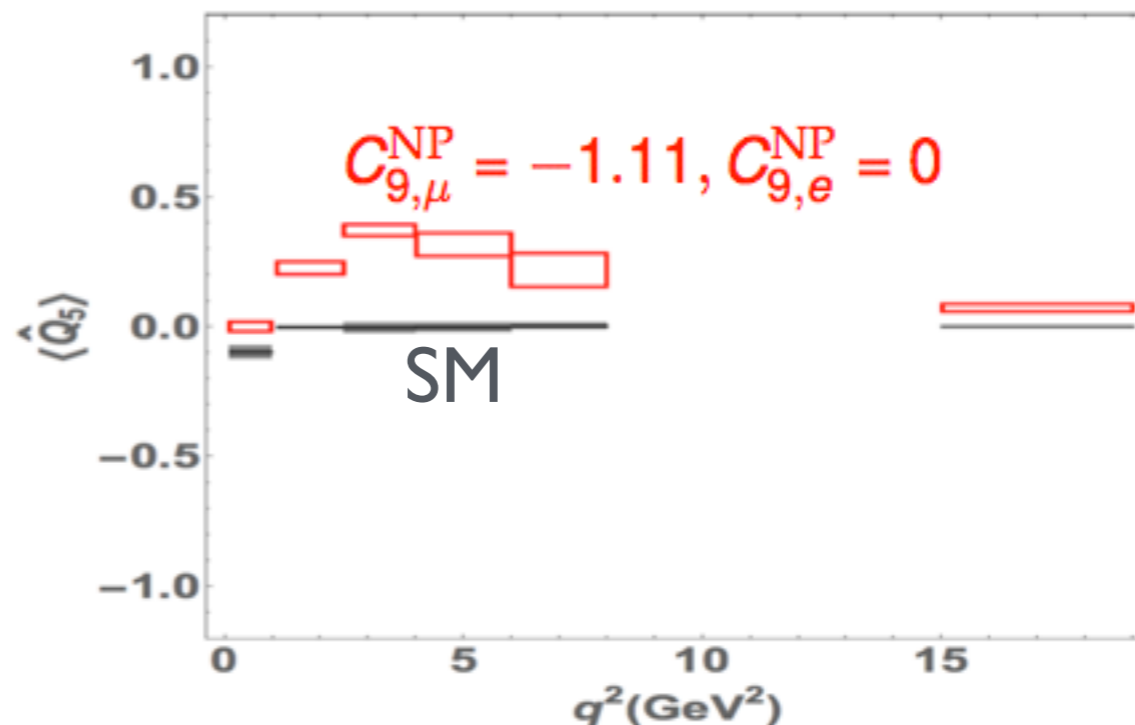
- Introduce new observables which are sensitive to $C_{i,\mu} - C_{i,e}$ without hadronic uncertainties

$$C_{i,\mu} = \begin{cases} C_i + \delta C_i, & i = 10, 9', 10' \\ C_9 + \delta C_9 + \Delta C_9^{(j)} \end{cases} \quad C_{i,e} = \begin{cases} C_i, & i = 10, 9', 10' \\ C_9 + \Delta C_9^{(j)} \end{cases}$$

$j = \perp, \parallel, 0$ same

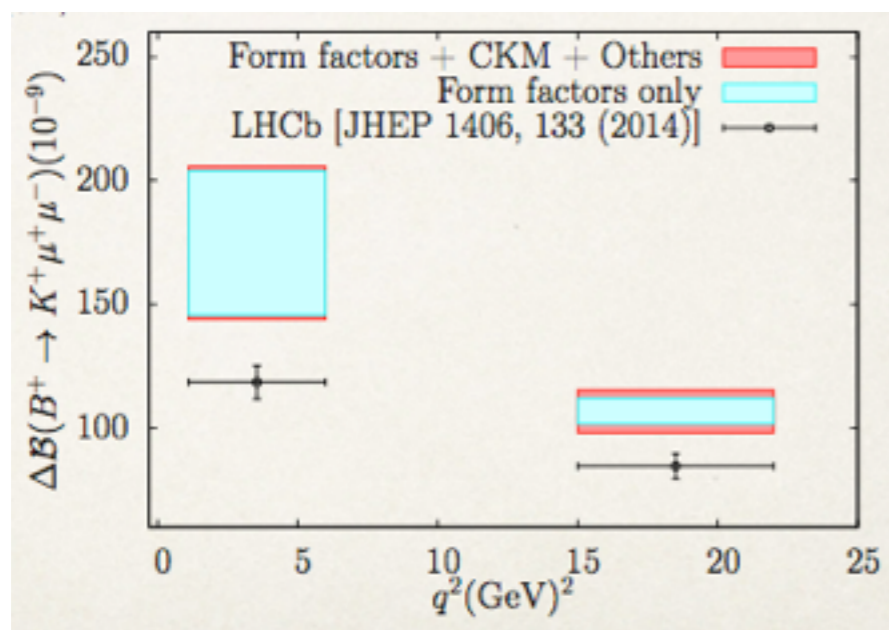
$$\langle Q_i \rangle = \langle P_i^\mu \rangle - \langle P_i^e \rangle \quad \langle \hat{Q}_i \rangle = \langle \hat{P}_i^\mu \rangle - \langle \hat{P}_i^e \rangle$$

$$\langle B_k \rangle = \frac{\langle J_k^\mu \rangle}{\langle J_k^e \rangle} - 1 \quad \langle \tilde{B}_k \rangle = \frac{\langle J_k^\mu / \beta_\mu^2 \rangle}{\langle J_k^e / \beta_e^2 \rangle} - 1$$

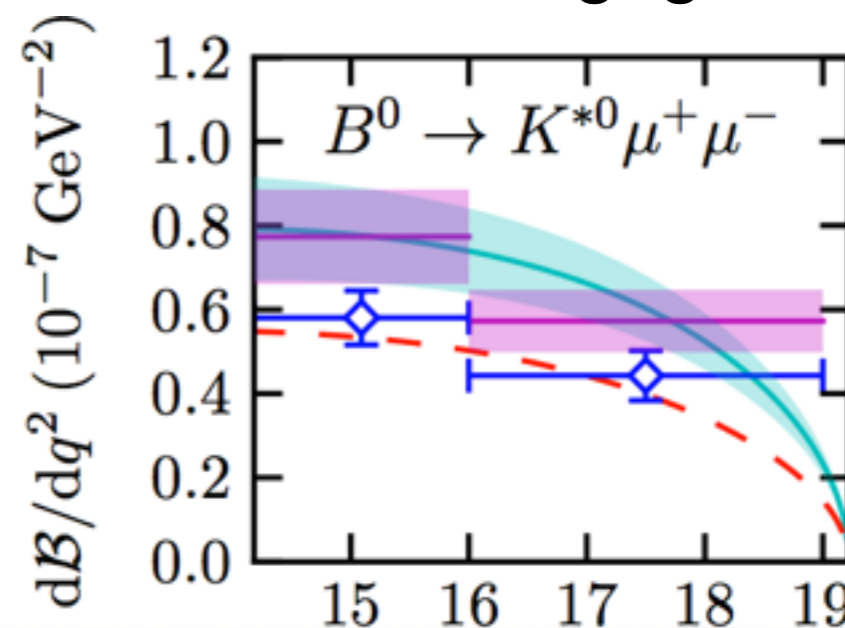


Lattice results for B decays [Wingate]

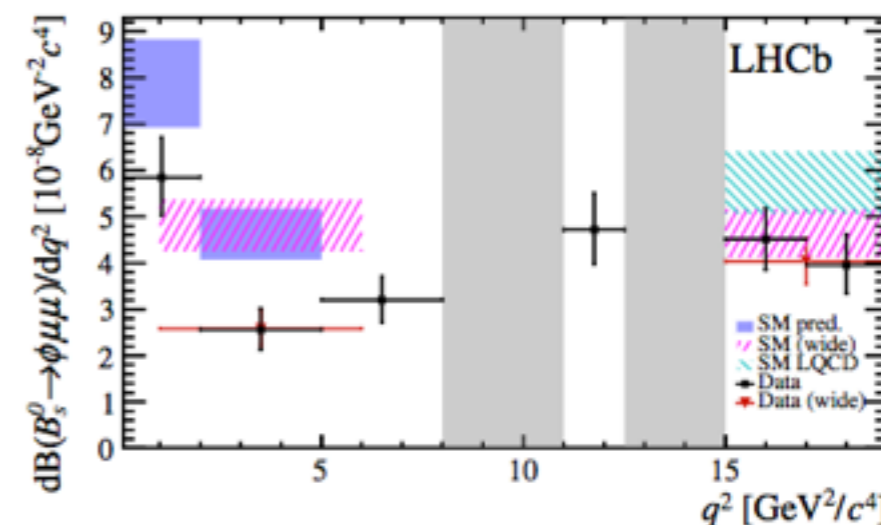
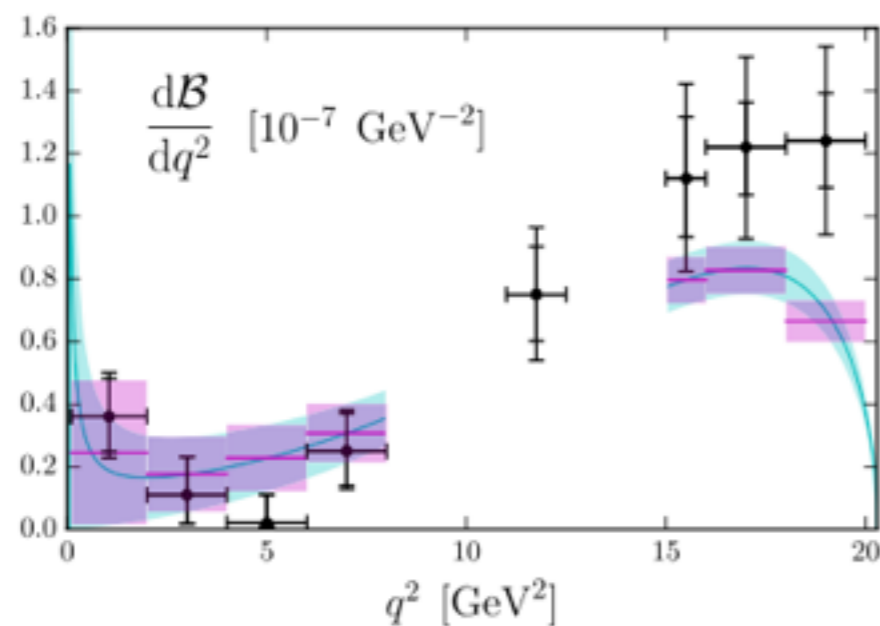
- $B \rightarrow \pi$ and $B \rightarrow K$ form factors are in excellent shape



- $B \rightarrow K^*$ and $B_s \rightarrow \phi$ form factors are much more challenging



- Baryonic modes also possible: $\Lambda_b \rightarrow \Lambda$



- Work in progress on the long distance contributions in $K_S \rightarrow \pi^0 ll$ and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

RH currents in $B \rightarrow K^* l l$ [Mandal]

- Look at endpoint: use exact endpoint relations, expand in $\delta = q^2_{max} - q^2$ and fit to LHCb data.

$$F_L = \frac{1}{3} + F_L^{(1)} \delta + F_L^{(2)} \delta^2 + F_L^{(3)} \delta^3$$

$$F_{\perp} = F_{\perp}^{(1)} \delta + F_{\perp}^{(2)} \delta^2 + F_{\perp}^{(3)} \delta^3$$

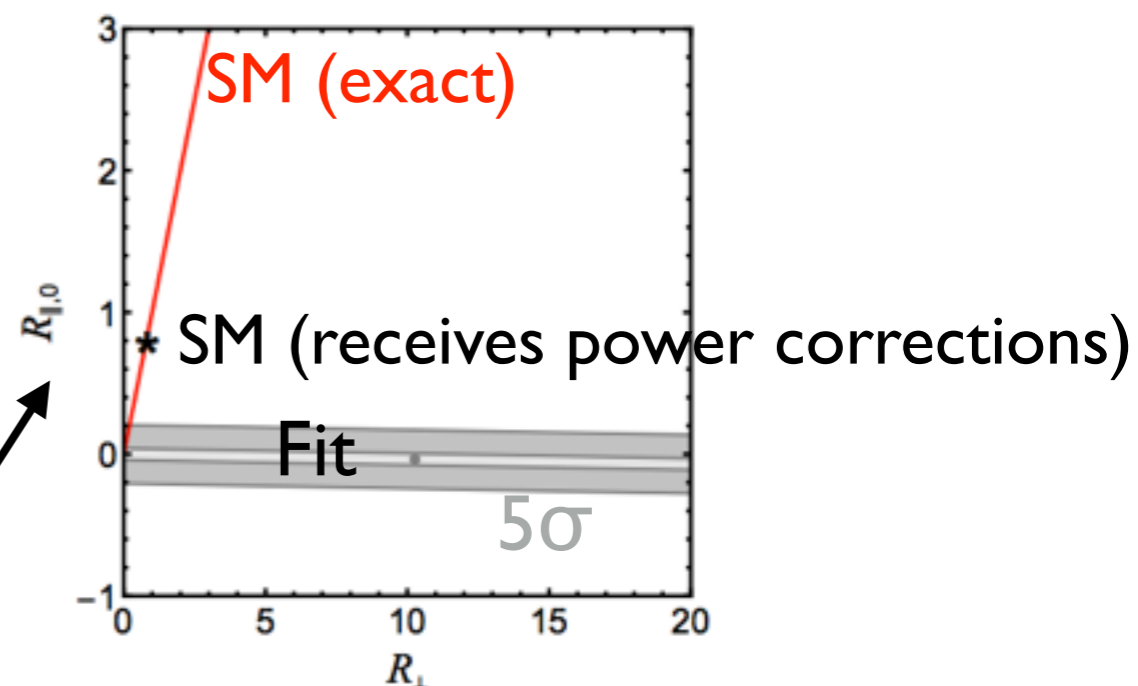
$$A_{FB} = A_{FB}^{(1)} \delta^{\frac{1}{2}} + A_{FB}^{(2)} \delta^{\frac{3}{2}} + A_{FB}^{(3)} \delta^{\frac{5}{2}}$$

$$A_5 = A_5^{(1)} \delta^{\frac{1}{2}} + A_5^{(2)} \delta^{\frac{3}{2}} + A_5^{(3)} \delta^{\frac{5}{2}},$$

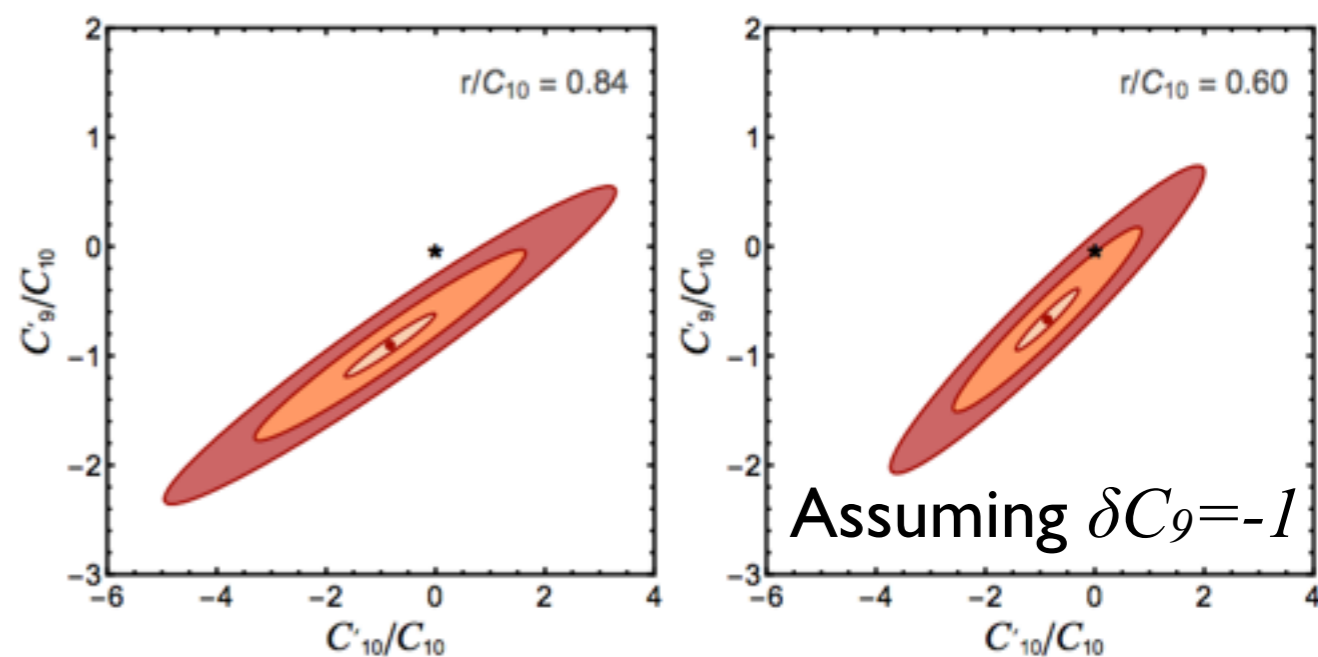


	$O^{(1)}(10^{-2})$	$O^{(2)}(10^{-3})$	$O^{(3)}(10^{-4})$
F_L	-2.94 ± 1.36	12.27 ± 2.05	-5.73 ± 0.72
F_{\perp}	6.83 ± 1.75	-9.67 ± 2.59	3.77 ± 0.90
A_{FB}	-30.59 ± 2.37	26.75 ± 4.42	-4.00 ± 1.83
A_5	-16.57 ± 2.36	6.77 ± 4.18	1.94 ± 1.61

More work on: Dependence on functional form, inclusion of experimental correlations, impact of experimental bins included in the fit

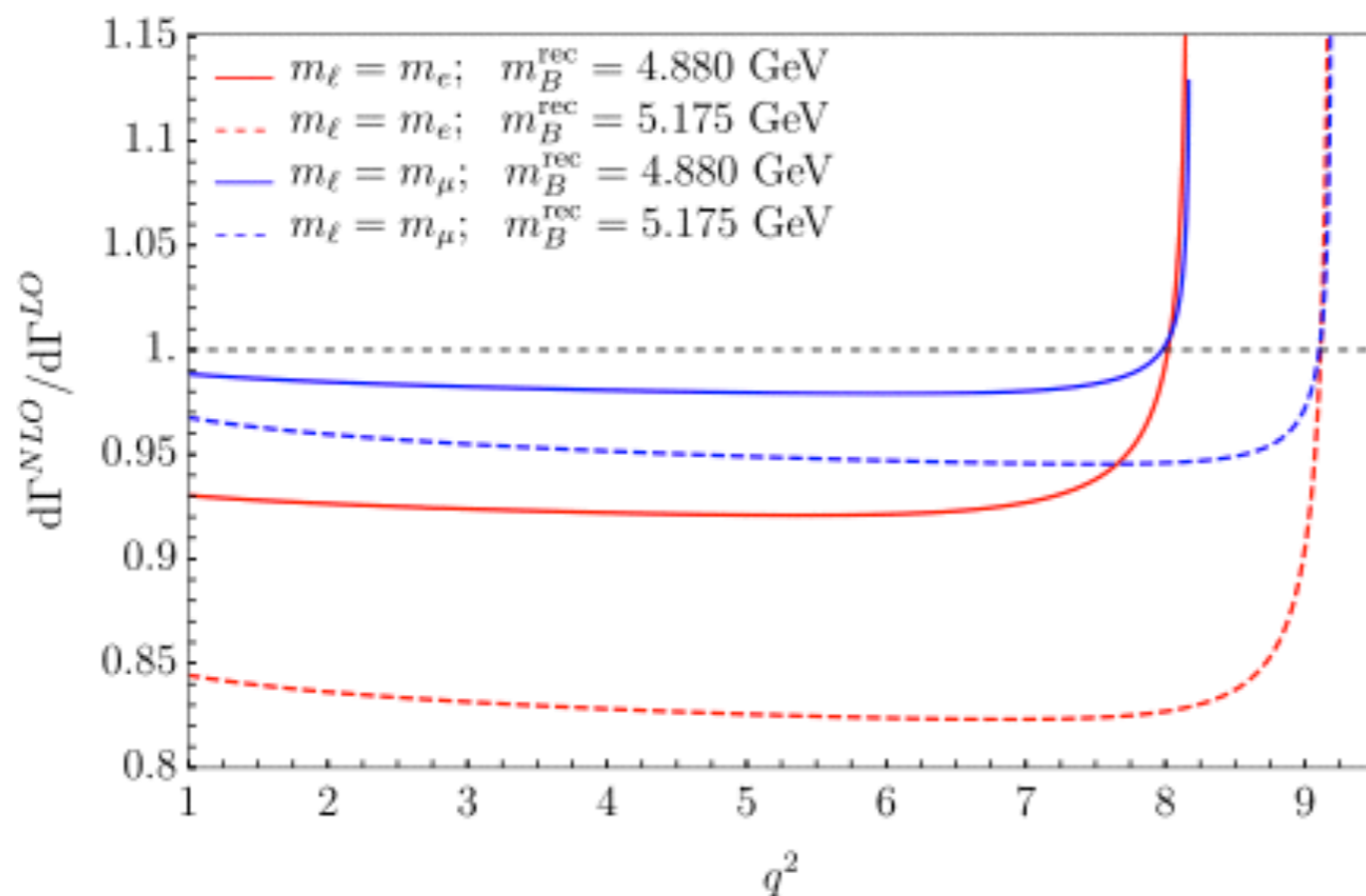


- Interpretation in terms of RH currents depend on SM prediction for r



Theory of $R_{K(*)}$ [Bordone]

- How accurate is the SM prediction for $R_{K(*)}$?
- Only possible effects are related to issues with QED radiation.
- LHCb looks for radiation from final state leptons and puts it back into the q^2 . This relies on EVTGEN ($b \rightarrow sll$ Monte Carlo) and PHOTOS.
- Important to check whether this procedure leads to a systematic bias.
- Some technical aspects are non trivial (e.g. need to model the J/ψ peak)
- Impact of photon radiation is large and depends on details of experimental cuts:



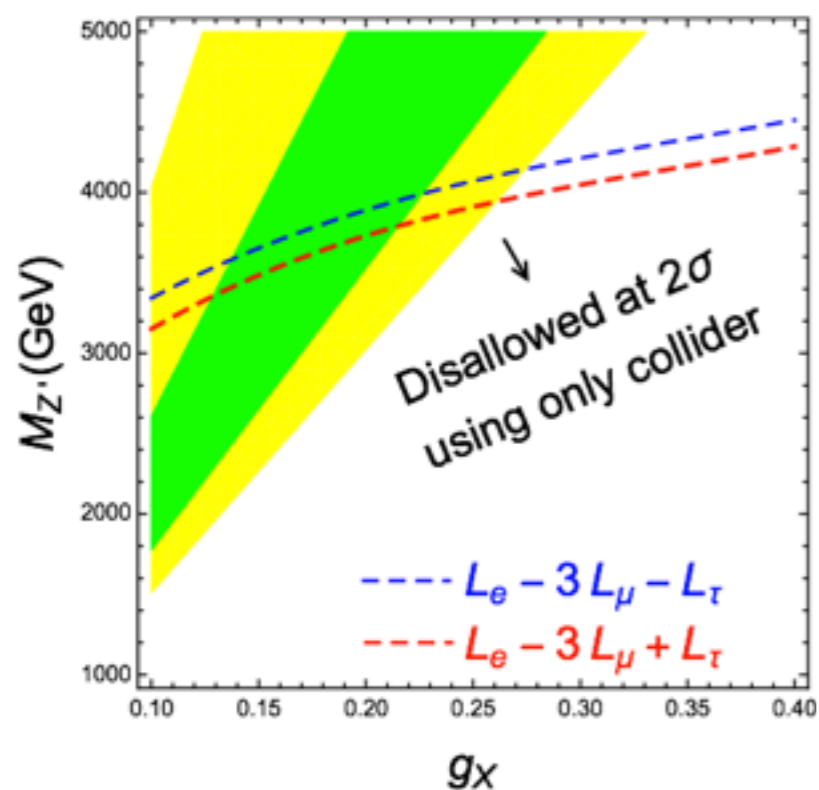
- The most important result is that this analytic procedure and PHOTOS agree within few permil

$$R_{K_{[1,6]}\text{GeV}^2} = 1.00 \pm 0.01$$

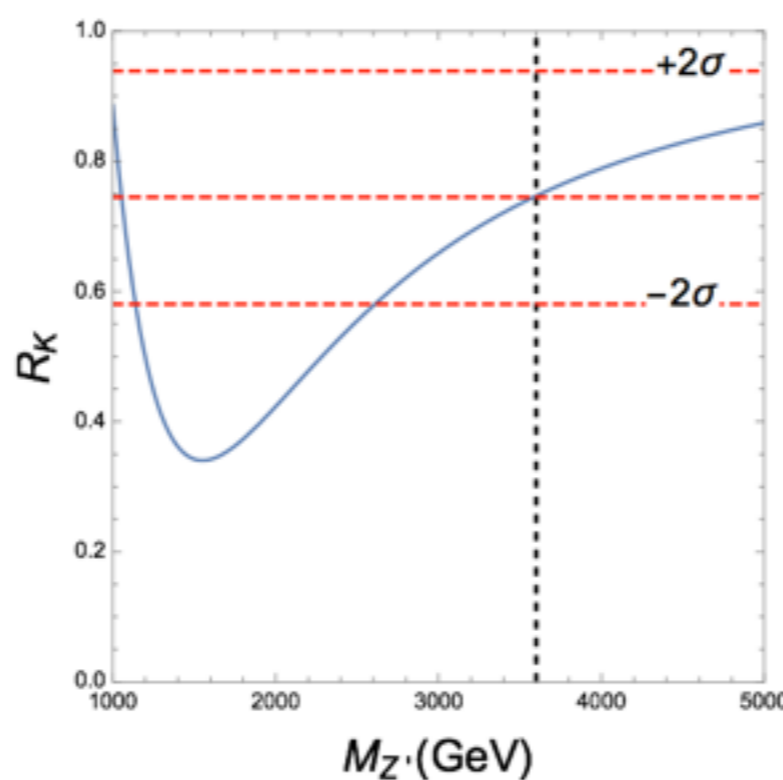
R_K in $U(1)_X$ models [Bhatia]

- Address the $b \rightarrow s$ anomalies (P_5' and R_K) and neutrino mixing in terms of a gauge boson (Z') of a new $U(1)_X$ symmetry
- After imposing all constraints (including anomaly cancellation, Bs mixing, etc..) only one possibility survives: Type-A = $L_e - 3L_\mu \pm L_\tau$

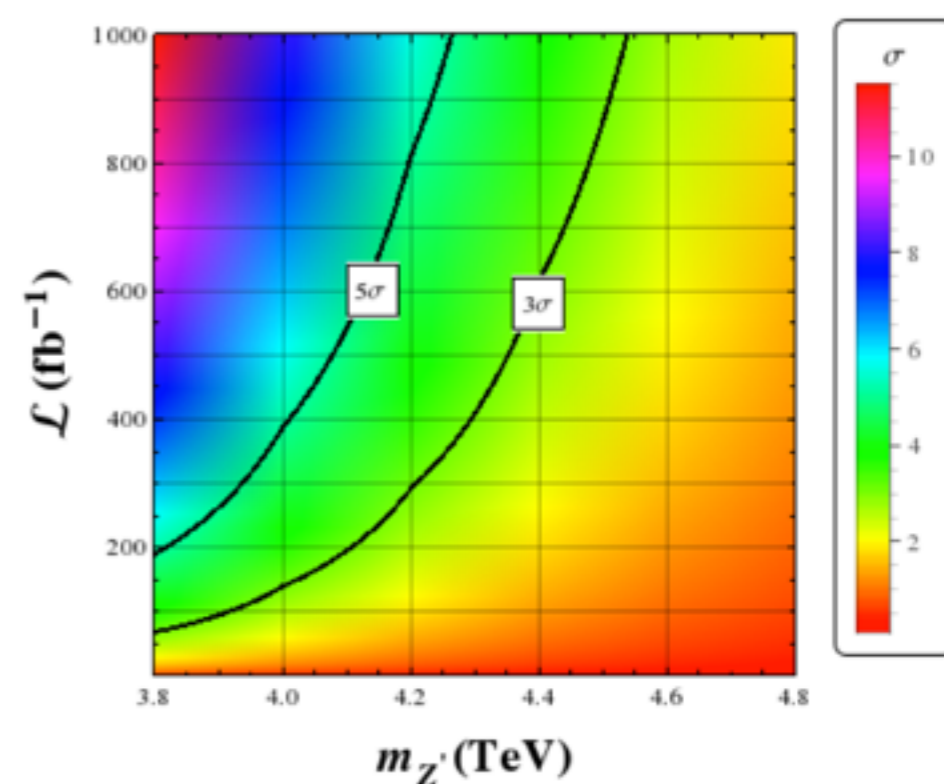
Constraint from $pp \rightarrow Z' \rightarrow \mu\mu$:



Expectations for R_K :



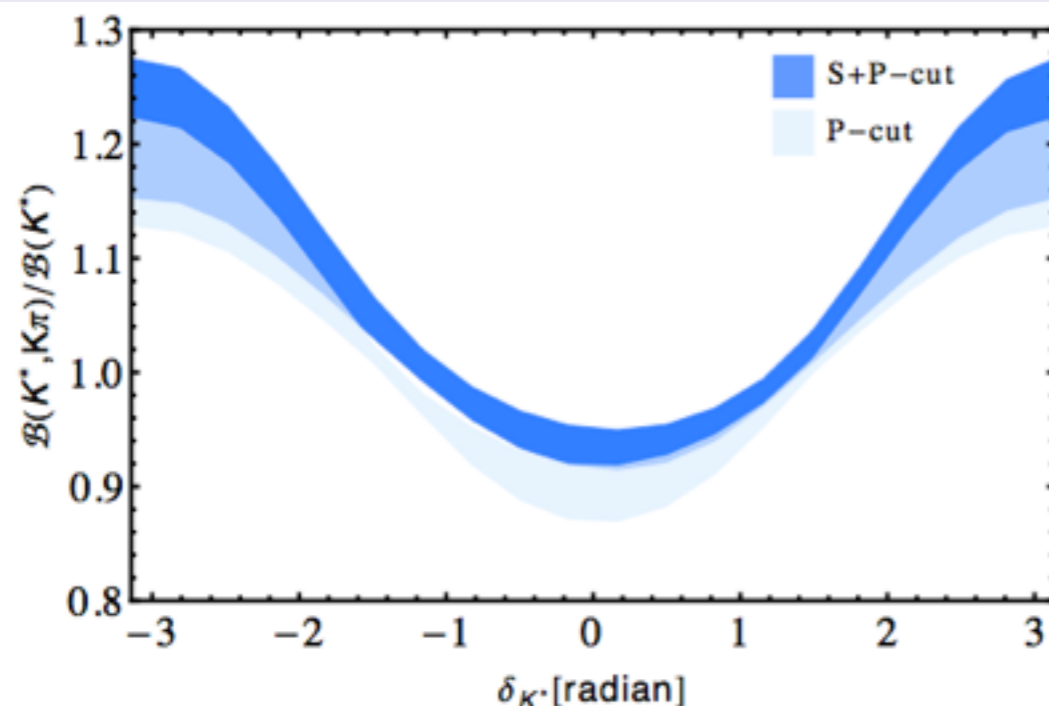
$Z' \rightarrow \mu\mu$ significance for $g_X = 0.2$:



Resonant and non-resonant effects in $B \rightarrow K^* \nu \nu$ [Das]

- $B \rightarrow K^* \nu \nu$ is controlled by form factors only (no charm effects etc...)
- Focus on backgrounds from resonant K_0^* and non-resonant $K\pi$
 - ◆ The K_0^* form factor is taken from LCSR. Its finite width is implemented with Breit-Wigner
 - ◆ Non-resonant $K\pi$ matrix elements are estimated with HH χ PT and yield a non-standard θ_K dependence of the rate
- A strong phase can appear when combining resonant and non-resonant modes:

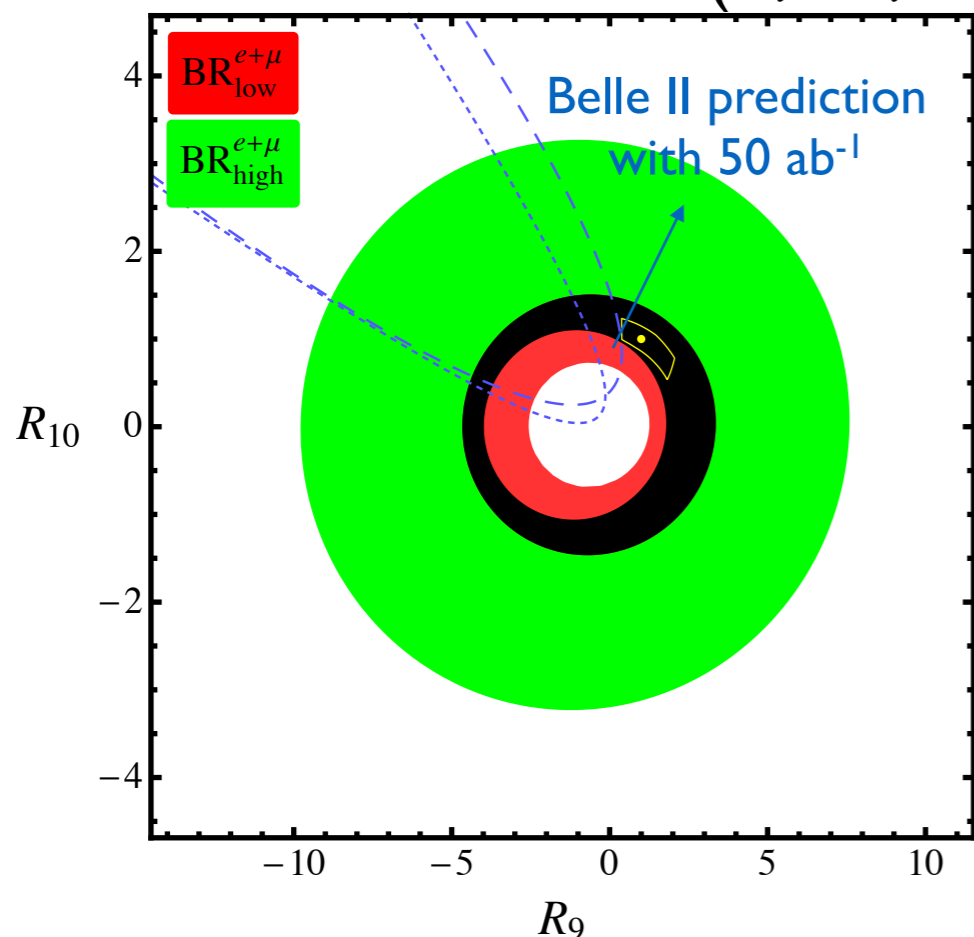
$$\frac{d^3\Gamma}{dq^2 dp^2 d \cos \theta_K} = 3\mathcal{N}(q^2) \left[|\widetilde{H}_\perp + e^{i\delta_{K^*}} H_\perp^{\text{nr}}|^2 + |\widetilde{H}_\parallel + e^{i\delta_{K^*}} H_\parallel^{\text{nr}}|^2 + |\widetilde{H}_0 + e^{i\delta_{K^*}} H_0^{\text{nr}} + \widetilde{H}_0'|^2 \right]$$



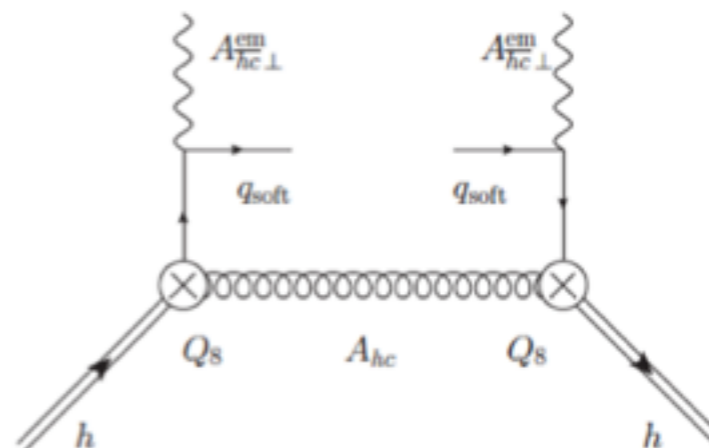
- Non-resonant and K_0^* effects can be up to 30%
- The strong phase can be extracted by looking at interference effects

Theory of inclusive $B \rightarrow X_s ll$ decays [Hurth]

- Only three observables: $\frac{d^2\Gamma}{dq^2 dz} = \frac{3}{8} [(1+z^2) H_T(q^2) + 2z H_A(q^2) + 2(1-z^2) H_L(q^2)]$
- QED corrections enhanced by $\log(m_b/m_l)$ distort the spectrum and are included
- Local Λ^2/m_B^2 and Λ^3/m_B^3 power corrections are known
- Non-local Λ/m_B can be estimated and lead to a 5% extra uncertainty.
- Similar issues as exclusive with charmonium resonances
- Present and future ($R_i = C_i/C_i^{SM}$):



- At low- q^2 , a cut on m_{X_s} is required to remove background
 - ◆ Experiments correct using a Fermi motion model
 - ◆ Effect of the cut can be calculated in SCET (work in progress)



Theory of radiative B decays [Paz]

- Inclusive $B \rightarrow X_{s,d} \gamma$ (OPE)
 - ◆ Good agreement between theory and experiment
 - ◆ Perturbatively known at NNLL ($Q_{1,2}-Q_7$ interference not calculated at physical m_c)
 - ◆ Non-perturbative effects appear at order Λ/m_b , depend on the non-local features of the B meson (shape function) and lead to a 5% uncertainty
 - ◆ Possible to use data (e.g. isospin asymmetry) to reduce some of this uncertainty
 - ◆ CP asymmetries receive large non-perturbative effects
 - ◆ Isospin difference of CP asymmetries is clean (measured by BaBar)
 - ◆ CP asymmetry on the untagged $B \rightarrow X_{s+d} \gamma$ is still almost zero due to U-spin
- Exclusive $B_{(q,s)} \rightarrow (K^*, \phi) \gamma$ and $B_{(q,s)} \rightarrow (\rho/\omega, K^*) \gamma$ (Factorization)
 - ◆ Unlike the $b \rightarrow sll$ case, the inclusive mode is well measured
 - ◆ In order to extract interesting information it is useful to consider ratios and asymmetries:

$$\begin{array}{ll} R_{K^* \gamma / \phi \gamma}^{\text{SM}} = 0.78 \pm 0.18 & R_{K^* \gamma / \phi \gamma}^{\text{exp}} = 1.23 \pm 0.12 \\ \bar{a}_I^{\text{SM}}(K^* \gamma) = (4.9 \pm 2.6)\% & \bar{a}_I^{\text{exp}}(K^* \gamma) = (5.2 \pm 2.6)\% \\ \bar{a}_I^{\text{SM}}(\rho \gamma) = (5.2 \pm 2.8)\% & \bar{a}_I^{\text{exp}}(\rho \gamma) = (30_{-13}^{+16})\% \end{array}$$

$\pi \rightarrow l\nu$ decays in very special relativity [Jain]

- Assume Lorentz invariance violated and fundamental symmetry group is instead SIM(2) subgroup
 - ◆ Implies the existence of a **preferred direction** in space-time
- Construct effective interaction terms that violate Lorentz invariance but respect SIM(2)

- ◆ Hadronic current in $\pi \rightarrow l\nu$ decays picks up a contribution

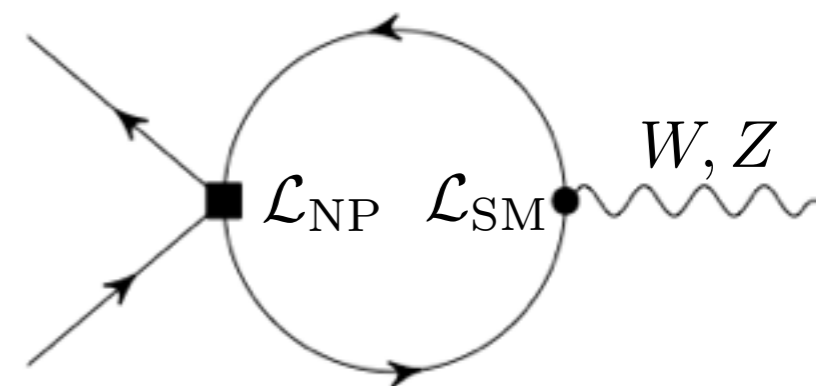
$$L_{VSR} = g \left(\frac{n_\mu}{n \cdot \partial} \pi^- \right) \bar{\psi}_l \gamma^\mu (1 - \gamma^5) \psi_\nu + \text{h.c.}$$

- Gives rise to **anisotropy of lepton momentum** with respect to preferred direction
 - ◆ In lab frame, anisotropy observed in distribution in azimuth ϕ
 - ◆ For $\pi \rightarrow \mu\nu$ could be $\sim 10^{-4}$, based on uncertainty for $\pi \rightarrow \mu\nu$ total partial width
- **Experimental test**
 - ◆ Look for variations as a function of sidereal time in peak position and amplitude for modulation in ϕ

Theory of LFV [Paradisi]

- The R_K anomaly suggests (via global fits) an explanation in terms of **left handed** operators (contribution to $Q_9 = (\bar{s}_L \gamma_\mu b_L)(\bar{\mu}_L \gamma_\mu \mu_L)$). This suggests to solve the R_D and R_D^* anomalies in terms of $(\bar{c}_L \gamma_\mu b_L)(\bar{\tau}_L \gamma_\mu \nu_L)$.
- Assuming NP respects $SU(2)_L \otimes U(1)_Y$ there are only two coefficients:

$$\begin{aligned} \mathcal{L}_{\text{NP}} &= \frac{C_1}{\Lambda^2} (\bar{q}_{3L} \gamma^\mu q_{3L}) (\bar{\ell}_{3L} \gamma_\mu \ell_{3L}) + \frac{C_3}{\Lambda^2} (\bar{q}_{3L} \gamma^\mu \tau^a q_{3L}) (\bar{\ell}_{3L} \gamma_\mu \tau^a \ell_{3L}) \\ &= \frac{1}{\Lambda^2} [(C_1 + C_3) \lambda_{ij}^d \lambda_{kl}^e (\bar{d}_{Li} \gamma^\mu d_{Lj}) (\bar{e}_{Lk} \gamma_\mu e_{Ll}) + \\ &\quad 2C_3 (\lambda_{ij}^{ud} \lambda_{kl}^e (\bar{u}_{Li} \gamma^\mu d_{Lj}) (\bar{e}_{Lk} \gamma_\mu \nu_{Ll}) + h.c.) \\ &\quad (C_1 - C_3) \lambda_{ij}^d \lambda_{kl}^e (\bar{d}_{Li} \gamma^\mu d_{Lj}) (\bar{\nu}_{Lk} \gamma_\mu \nu_{Ll}) + \dots] \end{aligned}$$



- After RG running ($\Lambda_{\text{NP}} \rightarrow 1 \text{ GeV}$), Z and W couplings to fermions are modified (need to impose Z-pole constraints)
- Purely leptonic and semileptonic Lagrangian modified, implying effects in
 - ◆ LFV tau decays, $\tau \rightarrow (3\mu, \mu\rho, \mu\pi)$
 - ◆ LFV B decays, $B \rightarrow K\tau\mu$
 - ◆ LFU breaking in $\tau \rightarrow l\nu\nu$: $R_\tau^{\tau/l_{1,2}} = \frac{\mathcal{B}(\tau \rightarrow \ell_{2,1}\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\tau \rightarrow \ell_{2,1}\nu\bar{\nu})_{\text{SM}}}{\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{SM}}}$

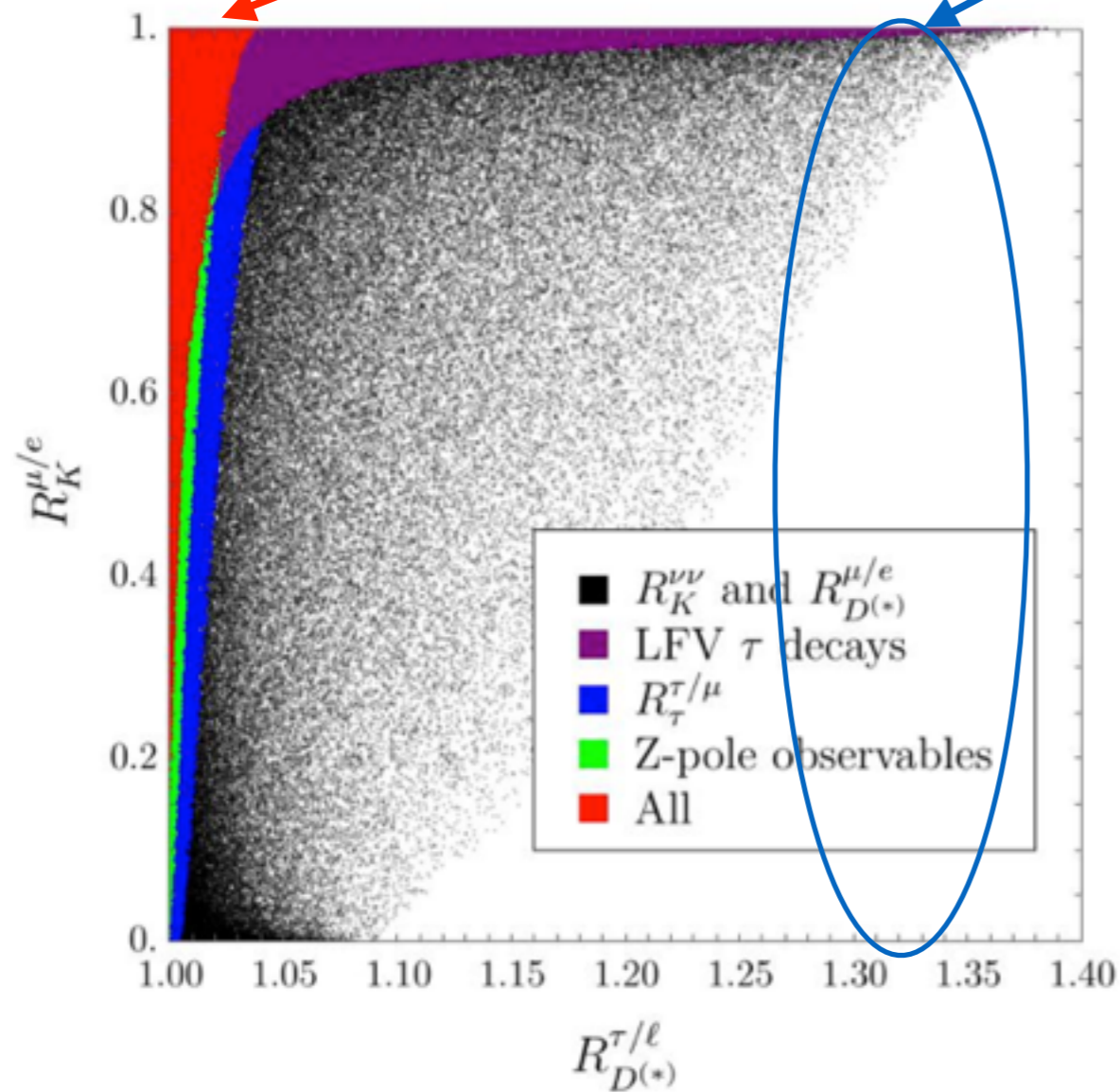
Theory of LFV [Paradisi]

- Tension between $R_{D^{(*)}}$ and R_τ : $R_\tau^{\tau/\mu} = 1.0022 \pm 0.0030$, $R_\tau^{\tau/e} = 1.0060 \pm 0.0030$ [HFAG, '14]

$$R_\tau^{\tau/\ell} \simeq 1 + 2 c_t^{cc} \lambda_{33}^e \approx 1 + \frac{0.008 C_3}{\Lambda^2(\text{TeV})} \lambda_{33}^e$$

$$R_D^{\tau/\ell} = 1.37 \pm 0.17, \quad R_{D^*}^{\tau/\ell} = 1.28 \pm 0.08$$

$$R_{D^{(*)}}^{\tau/\ell} \approx 1 - \frac{0.12 C_3}{\Lambda^2(\text{TeV})} \lambda_{33}^e$$



- Contributions generated by running effects not enough
- Need extra genuine high-scale NP effects

