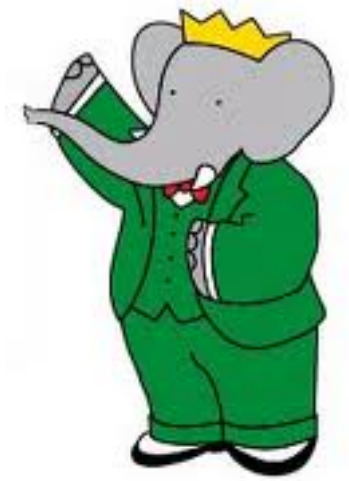




Recent results from the B factories on multi-body charmless B decays

Tim Gershon,
University of Warwick
on behalf of the BaBar & Belle collaborations

CKM2016, 29th November 2016



Selected results from the B factories on multi-body charmless B decays

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A potential treasure trove

- Multi-body charmless B decays have (in general)
 - contributions from both tree and penguin diagrams
 - potential for large CP violation effects ...
 - ... and for new physics contributions
 - various overlapping resonant & nonresonant structures
 - possibility to determine relative phases via amplitude analysis
 - not accessible for 2-body decays
 - need for accurate modelling of lineshapes
 - large samples available, with even more to look forward to soon
- Huge potential ... but equally huge challenges

Snyder-Quinn method for α

PHYSICAL REVIEW D

VOLUME 48, NUMBER 5

1 SEPTEMBER 1993

Measuring CP asymmetry in $B \rightarrow \rho\pi$ decays without ambiguities

Arthur E. Snyder and Helen R. Quinn

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94309

(Received 24 February 1993)

PRD 48 (1993) 2139

- Methods to measure α exploit time-dependent CP violation in B_d decays via $b \rightarrow u$ transitions (eg. $B_d \rightarrow \pi^+\pi^-$)

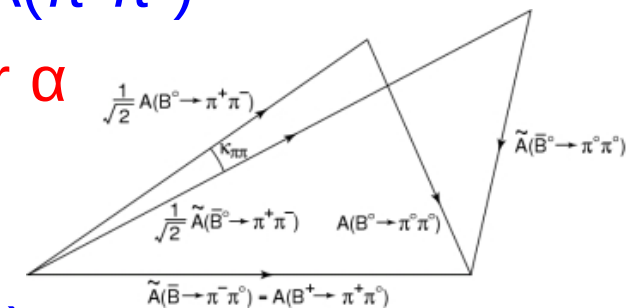
PRL 65 (1990) 3381

- Penguin “pollution” can be subtracted using Gronau-London isospin triangles built from $A(\pi^+\pi^-)$, $A(\pi^+\pi^0)$, $A(\pi^0\pi^0)$

- Expect discrete ambiguities in the solution for α

- Ambiguities can be resolved if you measure both real and imaginary parts of $\lambda = (q/p)(\bar{A}/A)$

– ie. measure $\cos(2\alpha)$ as well as $\sin(2\alpha)$



Toy model for $B \rightarrow \pi^+ \pi^- \pi^0$ Dalitz plot

Contributions only from $\rho^+ \pi^-$, $\rho^- \pi^+$ and $\rho^0 \pi^0$

PRD 48 (1993) 2139

Time dependence	Kinematic form	Amplitude measured	α dependence (all $P_i=0$)
1	$f^+ f^{+*}$	$S_3 S_3^* + \bar{S}_4 \bar{S}_4^*$	1
$\cos(\Delta Mt)$	$f^+ f^{+*}$	$S_3 S_3^* - \bar{S}_4 \bar{S}_4^*$	1
$\sin(\Delta Mt)$	$f^+ f^{+*}$	$\text{Im}(q \bar{S}_4 S_3^*)$	$\sin(2\alpha)$
1	$f^- f^{-*}$	$S_4 S_4^* + \bar{S}_3 \bar{S}_3^*$	1
$\cos(\Delta Mt)$	$f^- f^{-*}$	$S_4 S_4^* - \bar{S}_3 \bar{S}_3^*$	1
$\sin(\Delta Mt)$	$f^- f^{-*}$	$\text{Im}(q \bar{S}_3 S_4^*)$	$\sin(2\alpha)$
1	$f^0 f^{0*}$	$(S_5 S_5^* + \bar{S}_5 \bar{S}_5^*)/4$	1
$\cos(\Delta Mt)$	$f^0 f^{0*}$	$(S_5 S_5^* - \bar{S}_5 \bar{S}_5^*)/4$	1
$\sin(\Delta Mt)$	$f^0 f^{0*}$	$\text{Im}(q \bar{S}_5 S_5^*)/4$	$\sin(2\alpha)$
1	$\text{Re}(f^+ f^{-*})$	$\text{Re}(S_3 S_4^* + \bar{S}_4 \bar{S}_3^*)$	1
$\cos(\Delta Mt)$	$\text{Re}(f^+ f^{-*})$	$\text{Re}(S_3 S_4^* - \bar{S}_4 \bar{S}_3^*)$	1
$\sin(\Delta Mt)$	$\text{Re}(f^+ f^{-*})$	$\text{Im}(q \bar{S}_4 S_4^* - q^* S_3 \bar{S}_3^*)$	$\sin(2\alpha)$
1	$\text{Im}(f^+ f^{-*})$	$\text{Im}(S_3 S_4^* + \bar{S}_4 \bar{S}_3^*)$	1
$\cos(\Delta Mt)$	$\text{Im}(f^+ f^{-*})$	$\text{Im}(S_3 S_4^* - \bar{S}_4 \bar{S}_3^*)$	1
$\sin(\Delta Mt)$	$\text{Im}(f^+ f^{-*})$	$\text{Re}(q \bar{S}_4 S_4^* - q^* S_3 \bar{S}_3^*)$	$\cos(2\alpha)$
1	$\text{Re}(f^+ f^{0*})$	$\text{Re}(S_3 S_5^* + \bar{S}_4 \bar{S}_5^*)/2$	1
$\cos(\Delta Mt)$	$\text{Re}(f^+ f^{0*})$	$\text{Re}(S_3 S_5^* - \bar{S}_4 \bar{S}_5^*)/2$	1
$\sin(\Delta Mt)$	$\text{Re}(f^+ f^{0*})$	$\text{Im}(q \bar{S}_4 S_5^* + q^* S_3 \bar{S}_5^*)/2$	$\sin(2\alpha)$
1	$\text{Im}(f^+ f^{0*})$	$\text{Im}(S_3 S_5^* + \bar{S}_4 \bar{S}_5^*)/2$	1
$\cos(\Delta Mt)$	$\text{Im}(f^+ f^{0*})$	$\text{Im}(S_3 S_5^* - \bar{S}_4 \bar{S}_5^*)/2$	1
$\sin(\Delta Mt)$	$\text{Im}(f^+ f^{0*})$	$\text{Re}(q \bar{S}_4 S_5^* - q^* S_3 \bar{S}_5^*)/2$	$\cos(2\alpha)$
1	$\text{Re}(f^- f^{0*})$	$\text{Re}(S_4 S_5^* + \bar{S}_3 \bar{S}_5^*)/2$	1
$\cos(\Delta Mt)$	$\text{Re}(f^- f^{0*})$	$\text{Re}(S_4 S_5^* - \bar{S}_3 \bar{S}_5^*)/2$	1
$\sin(\Delta Mt)$	$\text{Re}(f^- f^{0*})$	$\text{Im}(q \bar{S}_3 S_5^* - q^* S_4 \bar{S}_5^*)$	$\sin(2\alpha)$
1	$\text{Im}(f^- f^{0*})$	$\text{Im}(S_4 S_5^* + \bar{S}_3 \bar{S}_5^*)/2$	1
$\cos(\Delta Mt)$	$\text{Im}(f^- f^{0*})$	$\text{Im}(S_4 S_5^* - \bar{S}_3 \bar{S}_5^*)/2$	1
$\sin(\Delta Mt)$	$\text{Im}(f^- f^{0*})$	$\text{Re}(q \bar{S}_3 S_5^* - q^* S_4 \bar{S}_5^*)/2$	$\cos(2\alpha)$

Note: physical observables depend on either $\sin(2\alpha)$ or $\cos(2\alpha)$ – never “directly” on α

27 parameters renamed “U” and “I” in commonly used notation

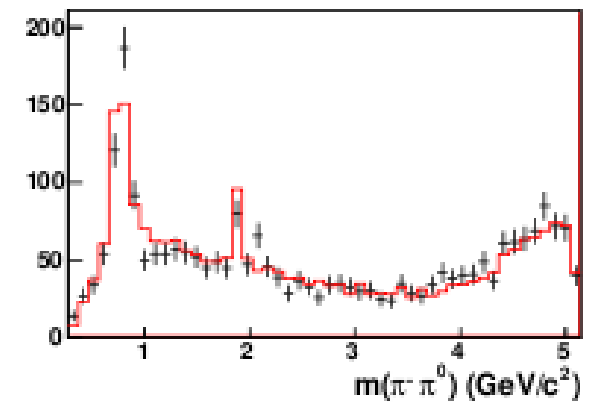
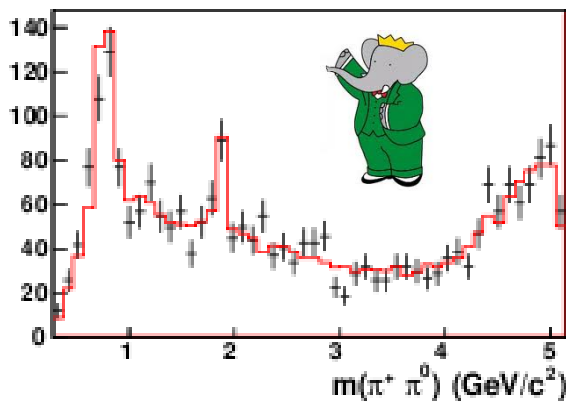
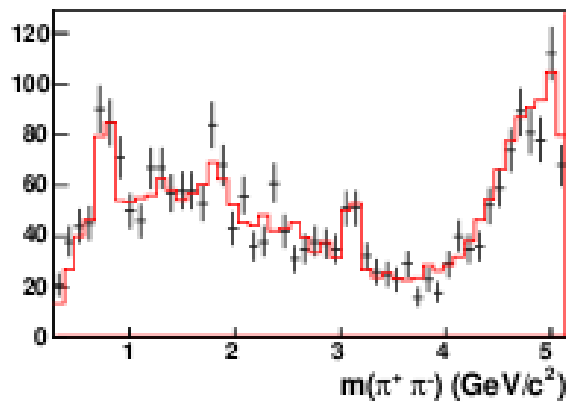
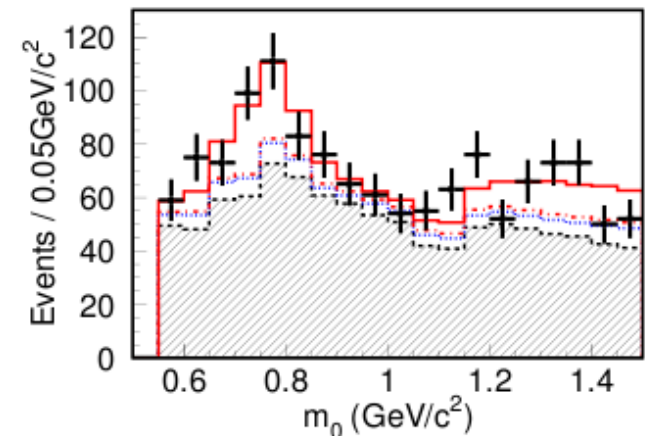
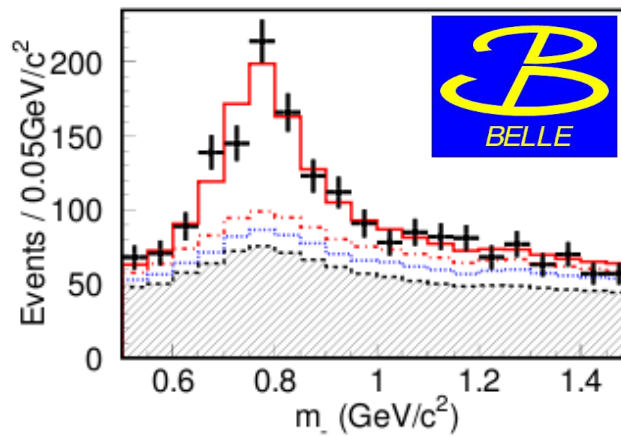
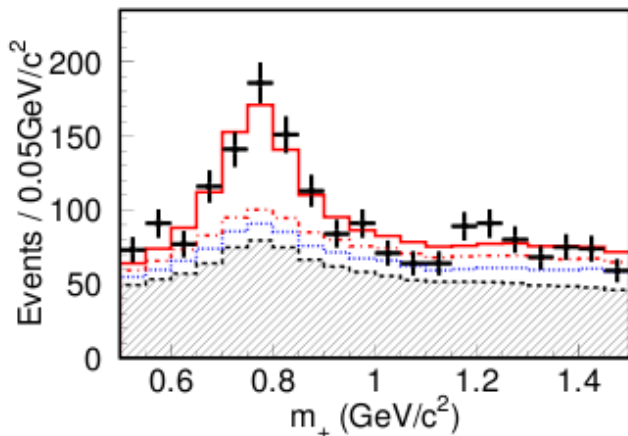
H. Quinn and J. Silva, PRD 62 (2000) 054002

f terms contain hadronic physics (lineshape, spin)

$S_3 = A(\rho^+ \pi^-)$, $S_4 = A(\rho^- \pi^+)$, $S_5 = A(\rho^0 \pi^0)$,

$B \rightarrow \pi^+ \pi^- \pi^0$ – B factory results

- Belle, 449 M $B\bar{B}$ pairs: PRL 98 (2007) 221602, PR D77 (2008) 072001
- BaBar, 471 M $B\bar{B}$ pairs: PR D88 (2013) 012003



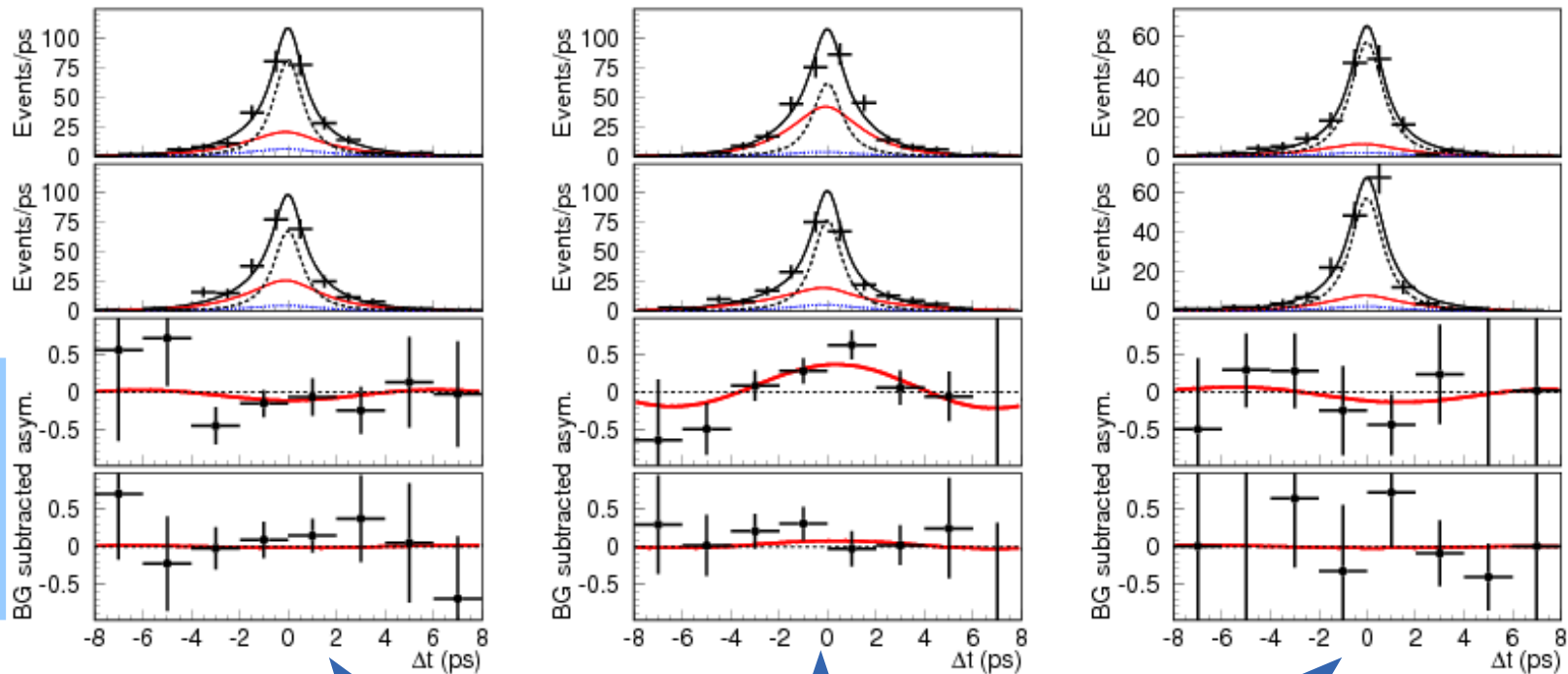
$B \rightarrow \pi^+ \pi^- \pi^0$ – B factory results

- Belle, 449 M $B\bar{B}$ pairs: PRL 98 (2007) 221602, [PR D77 \(2008\) 072001](#)
- BaBar, 471 M $B\bar{B}$ pairs: PR D88 (2013) 012003

Tagged
as B^0

Tagged
as B^0

Asymmetry
shown
separately for
(top) good
tags and
(bottom) less
good tags



$\rho^+ \pi^-$

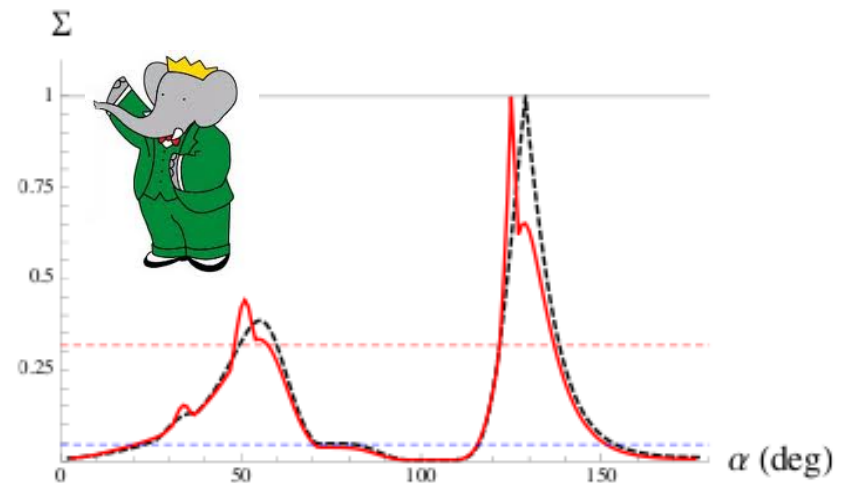
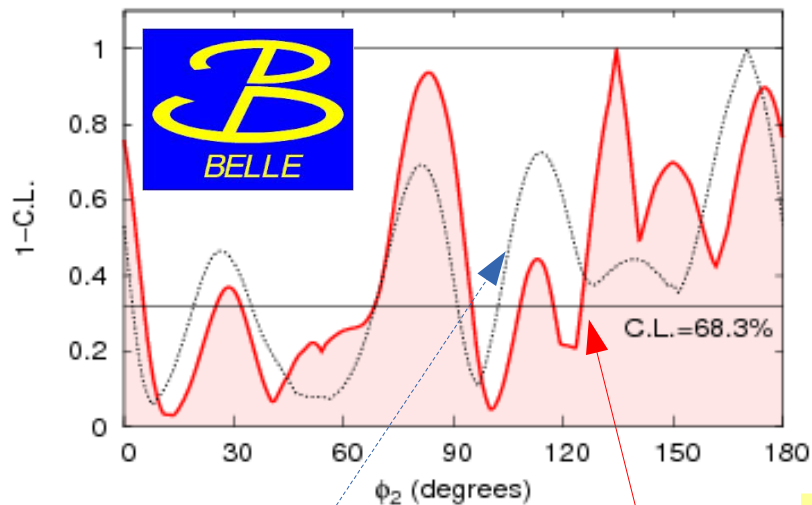
$\rho^- \pi^+$

$\rho^0 \pi^0$

$B \rightarrow \pi^+ \pi^- \pi^0$ – B factory results

- Results from

- Belle, 449 M $B\bar{B}$ pairs: PRL 98 (2007) 221602, PR D77 (2008) 072001
- BaBar, 471 M $B\bar{B}$ pairs: PR D88 (2013) 012003



Contour from $B \rightarrow \pi^+ \pi^- \pi^0$ only

“the extraction of α with our current sample size is not robust”

B → Kππ

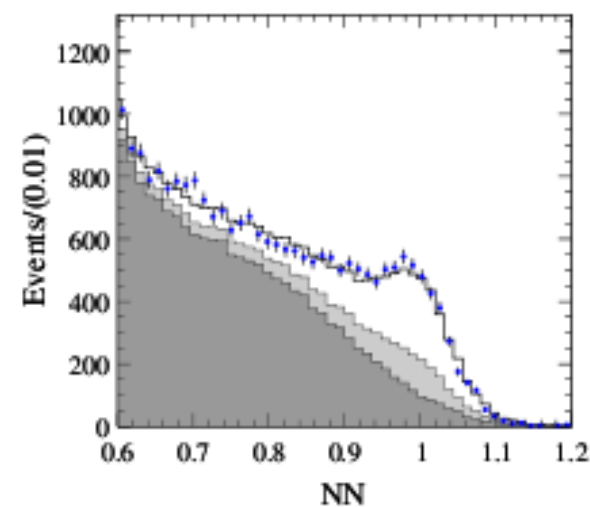
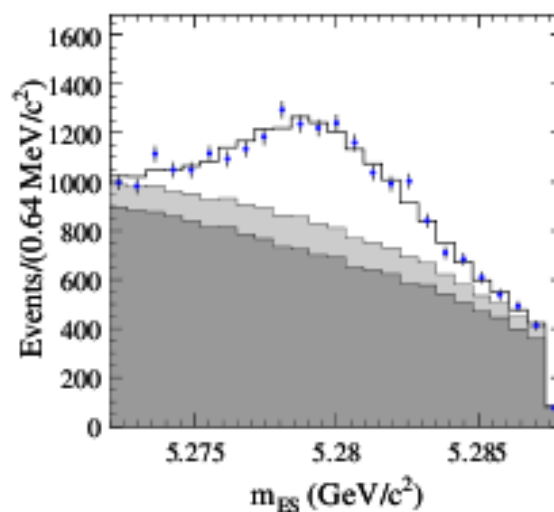
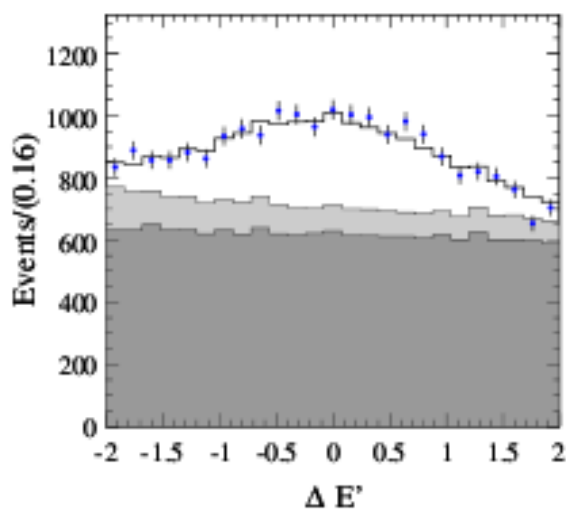
- Method to constrain γ from B → Kππ Dalitz plot (DP) analyses
 - See [PRD 74 \(2006\) 051301](#), [PRD 75 \(2007\) 014002](#)

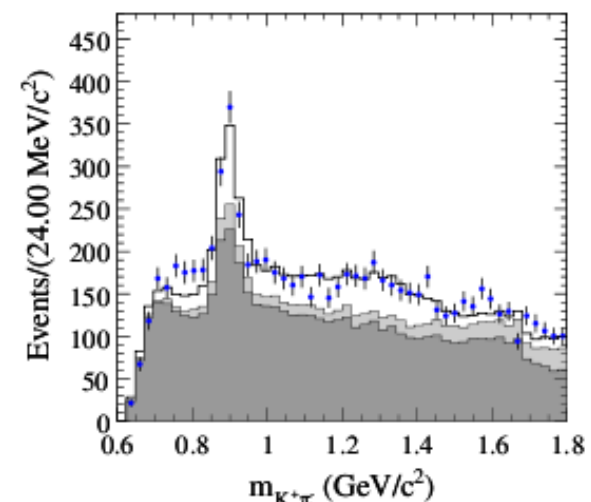
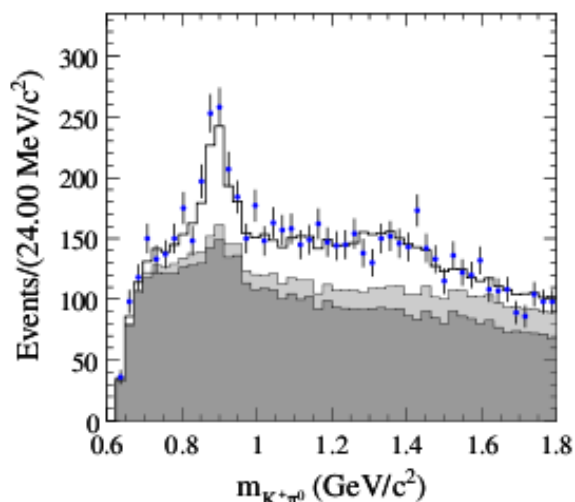
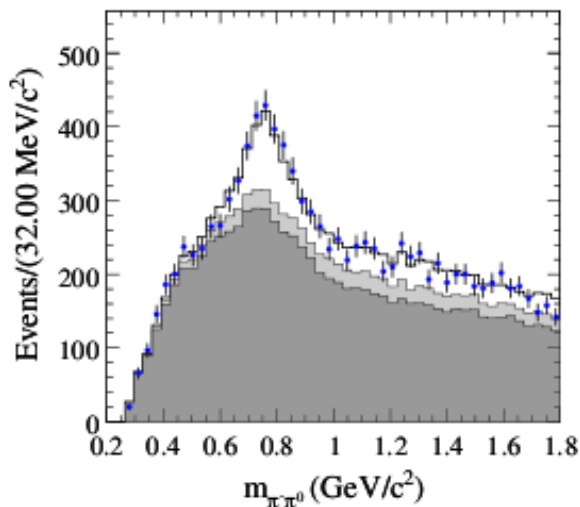
$$\mathcal{A}_{\frac{3}{2}}(K^*\pi) = \frac{1}{\sqrt{2}}\mathcal{A}(B^0 \rightarrow K^{*+}\pi^-) + \mathcal{A}(B^0 \rightarrow K^{*0}\pi^0).$$

- Construct pure I=3/2 amplitude for B and \bar{B}
 - Dalitz plot analysis of $B^0 \rightarrow K^+\pi^-\pi^0$
- Relative phase between B and \bar{B} gives γ
 - Dalitz plot analysis of $B^0 \rightarrow K_S\pi^+\pi^-$
 - corrections due to electroweak penguins



- Signal yield of $3670 \pm 96 \pm 94$ decays
 - separated from background with $\Delta E'$, m_{ES} and neural network (NN)
 - n.b.: $\Delta E'$ modified version of standard $\Delta E'$ variable; removes dependence on π^0 energy & hence DP position
- Branching fraction measured
 - $B(B^0 \rightarrow K^+ \pi^- \pi^0) = [38.5 \pm 1.0 \text{ (stat.)} \pm 3.9 \text{ (syst.)}] \times 10^{-6}$





Results need to construct isospin triangles

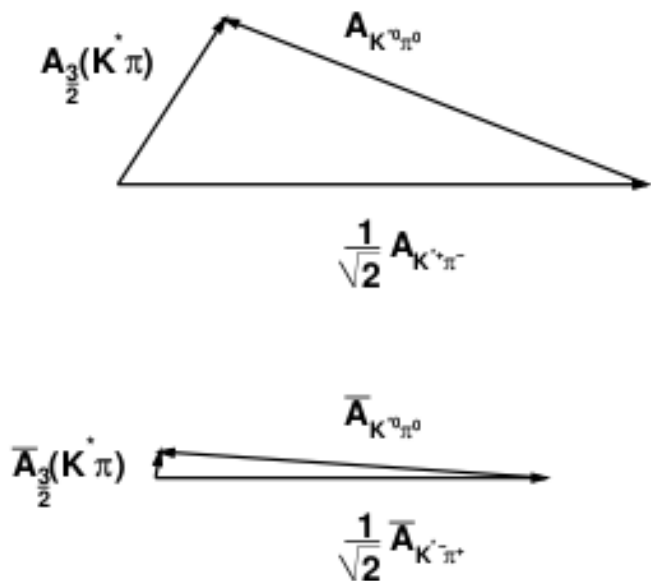
Isobar	$\mathcal{B} (\times 10^{-6})$	$\bar{\Phi} [^\circ]$	$\Phi [^\circ]$	A_{CP}
$\rho(770)^- K^+$	$6.6 \pm 0.5 \pm 0.8$	0 (fixed)	0 (fixed)	$0.20 \pm 0.09 \pm 0.08$
$\rho(1450)^- K^+$	$2.4 \pm 1.0 \pm 0.6$	$75 \pm 19 \pm 9$	$126 \pm 25 \pm 26$	$-0.10 \pm 0.32 \pm 0.09$
$\rho(1700)^- K^+$	$0.6 \pm 0.6 \pm 0.4$	$18 \pm 36 \pm 16$	$50 \pm 38 \pm 20$	$-0.36 \pm 0.57 \pm 0.23$
$K^*(892)^+ \pi^-$	$8.0 \pm 1.1 \pm 0.8$	$33 \pm 22 \pm 20$	$39 \pm 25 \pm 20$	$-0.29 \pm 0.11 \pm 0.02$
$K^*(892)^0 \pi^0$	$3.3 \pm 0.5 \pm 0.4$	$29 \pm 18 \pm 6$	$17 \pm 20 \pm 8$	$-0.15 \pm 0.12 \pm 0.04$
$(K\pi)_0^{*+} \pi^-$	$34.2 \pm 2.4 \pm 4.1$	$-167 \pm 16 \pm 37$	$-130 \pm 22 \pm 22$	$0.07 \pm 0.14 \pm 0.01$
$(K\pi)_0^{*0} \pi^0$	$8.6 \pm 1.1 \pm 1.3$	$13 \pm 17 \pm 12$	$10 \pm 17 \pm 16$	$-0.15 \pm 0.10 \pm 0.04$
NR	$2.8 \pm 0.5 \pm 0.4$	$48 \pm 14 \pm 6$	$90 \pm 21 \pm 15$	$0.10 \pm 0.16 \pm 0.08$

Combined with results from $B^0 \rightarrow K_S \pi^+ \pi^-$

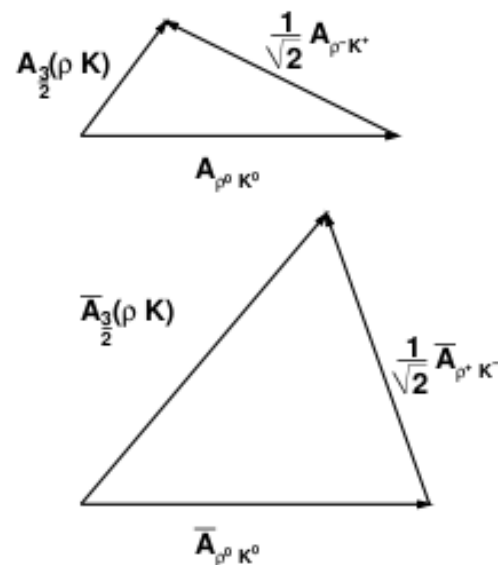
$$A_{CP}(K^{*+} \pi^-) = -0.24 \pm 0.07 \text{ (stat.)} \pm 0.02 \text{ (syst.)} [3.1 \sigma]$$



Isospin triangles drawn to scale of experimental results (without uncertainties)



Cancellation makes pure $I=3/2$ amplitude small – impossible to determine its relative phase



Method may work better for ρK amplitudes – but current uncertainty is large

The $B \rightarrow K\pi$ puzzle

- QCD may also be a cause of apparently anomalous CP violation effects

$$\Delta A_{CP}(K\pi) = A_{CP}(K^+\pi^-) - A_{CP}(K^+\pi^0) \neq 0$$

-0.082 ± 0.006
e.g. LHCb PRL 110
(2013) 221601

$+0.040 \pm 0.021$
e.g. Belle PR D87
(2013) 031103

HFAG averages
most precise single
measurement

- Look for similar effects in $K^*\pi$ & $K\rho$ systems

Precision of PV
modes often worse
as all available data
not yet analysed

$K^*\pi$

-0.23 ± 0.06
e.g. BaBar PR D83
(2011) 112010

-0.39 ± 0.13
e.g. BaBar
[arXiv:1501.00705](https://arxiv.org/abs/1501.00705)

$K\rho$

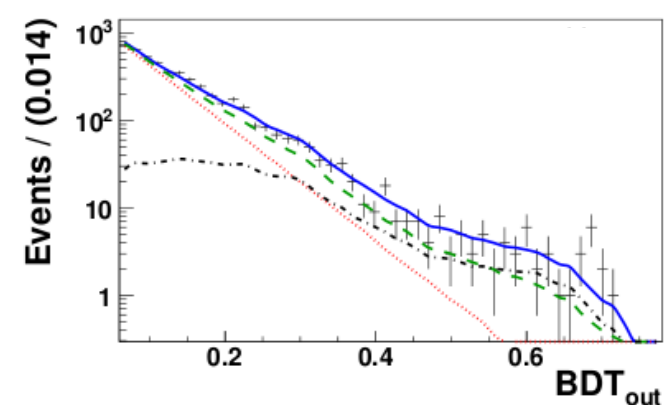
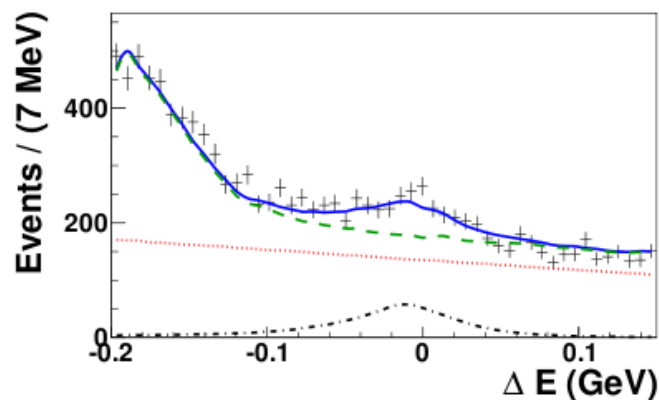
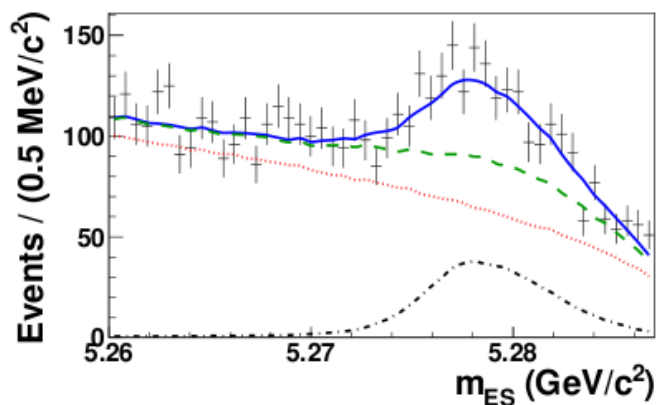
$+0.20 \pm 0.11$
e.g. BaBar PR D83
(2011) 112010

$+0.37 \pm 0.11$
BaBar PR D78 (2008)
012004 & Belle PRL 96
(2006) 251803



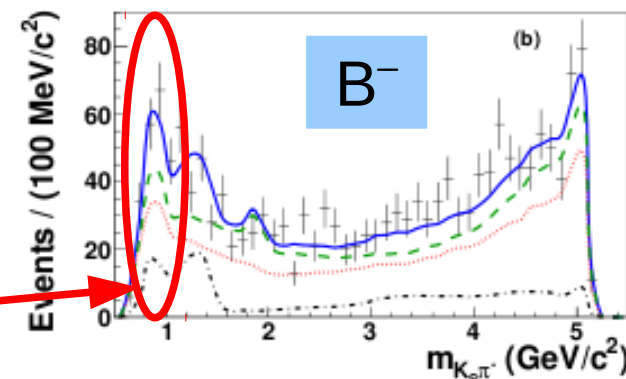
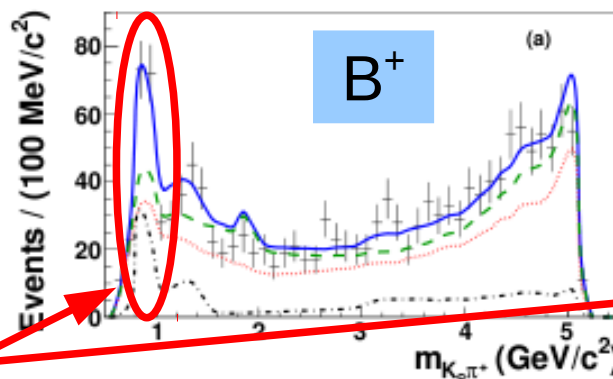
$$B^+ \rightarrow K_S \pi^+ \pi^0$$

- Signal yield of 1014 ± 60 decays
 - Separated from background with ΔE , m_{ES} and boosted decision tree (BDT) output
 - Simultaneous fit with Dalitz plot distribution
 - Dependence of ΔE on π^0 energy treated with conditional PDF

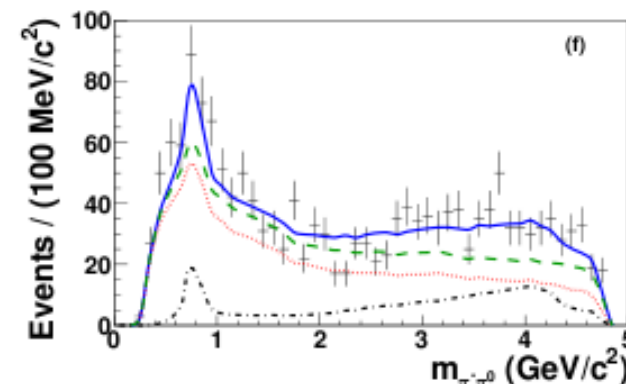
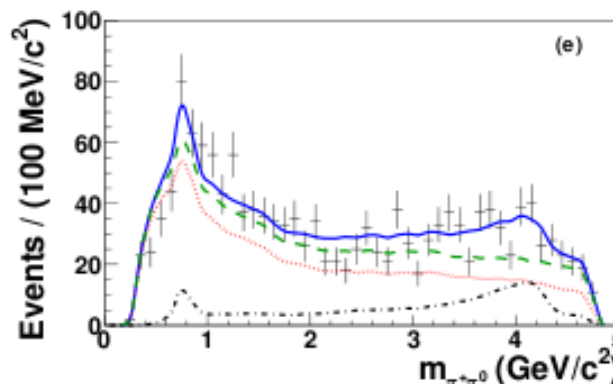
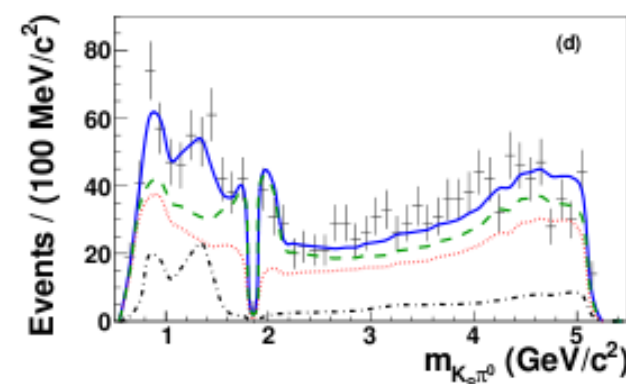
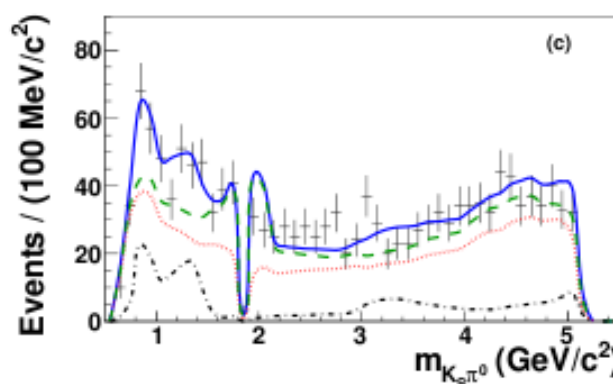




Evidence for CP violation in $B^+ \rightarrow K^{*+} \pi^0$



Decay channel	A_{CP}
$K^0 \pi^+ \pi^0$	$0.07 \pm 0.05 \pm 0.03^{+0.02}_{-0.03}$
$K^*(892)^0 \pi^+$	$-0.12 \pm 0.21 \pm 0.08^{+0.0}_{-0.11}$
$K^*(892)^+ \pi^0$	$-0.52 \pm 0.14 \pm 0.04^{+0.04}_{-0.02}$
$K_0^*(1430)^0 \pi^+$	$0.14 \pm 0.10 \pm 0.04^{+0.13}_{-0.05}$
$K_0^*(1430)^+ \pi^0$	$0.26 \pm 0.12 \pm 0.08^{+0.12}_{-0.0}$
$\rho(770)^+ K^0$	$0.21 \pm 0.19 \pm 0.07^{+0.23}_{-0.19}$



Summary

- Much physics potential in charmless hadronic decays ...
 - and in three-body decays in particular
- Need smart methods to overcome hadronic uncertainties
- These often involve analyses of >1 Dalitz plot
 - cannot rely on only all-charged final states
 - need modes with K_S &/or π^0 too
 - often highly challenging but have been successfully analysed
- Despite many publications, there is still untapped potential in existing data samples
 - even more soon to come with Belle II

B factory Dalitz plot analyses



$K^+K^+K^-$

PR D85 (2012) 112010

PR D71 (2005) 092003

$K^+K^+K_S$

PR D85 (2012) 112010

PR D82 (2010) 073011

$K^+K_S K_S$

PR D85 (2012) 112010

No amplitude analysis

$K_S K_S K_S$

PR D85 (2012) 054023

No amplitude analysis

$K^+\pi^+\pi^-$

PR D78 (2008) 012004

PRL 96 (2006) 251803

$K_S \pi^+\pi^-$

PR D80 (2009) 112001

PR D79 (2009) 072004

$K^+\pi^-\pi^0$

PR D83 (2011) 112010

No amplitude analysis

$K_S \pi^+\pi^0$

arXiv:1501.00705

No amplitude analysis

$\pi^+\pi^+\pi^-$

PR D79 (2009) 072006

No amplitude analysis

$\pi^+\pi^+\pi^0$

PR D88 (2013) 012003

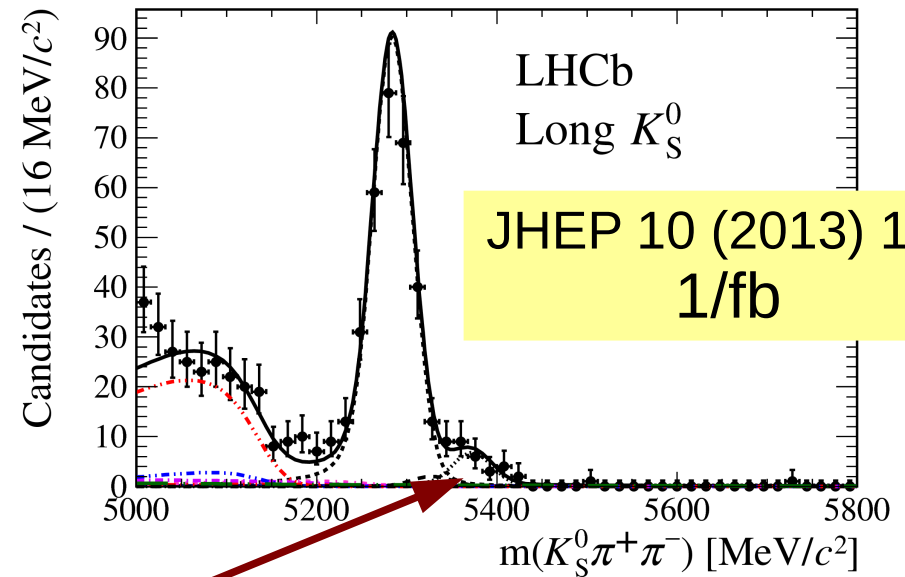
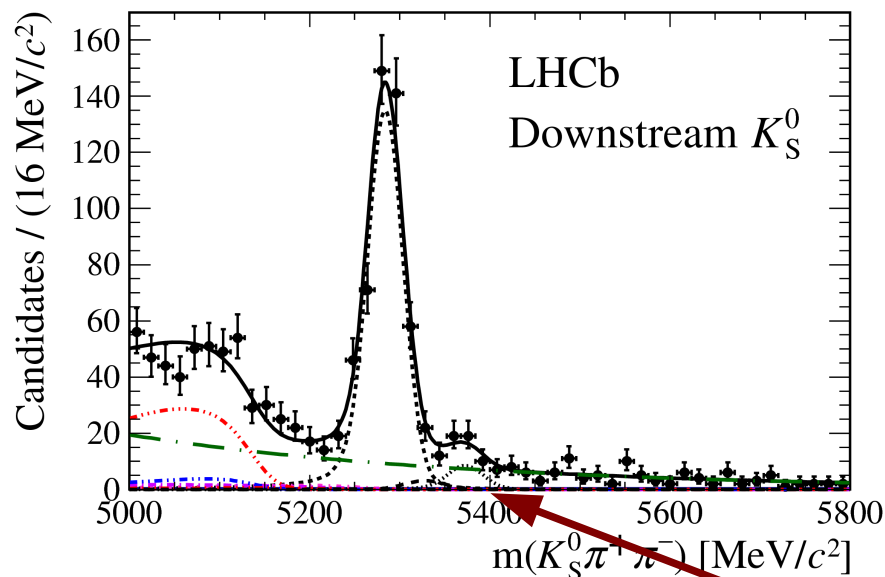
PR D77 (2008) 072001

All modes with 0, 1 or 3 kaons (K^\pm or K_S) & 0 or 1 π^0



Aside: $B_s^0 \rightarrow K_S \pi^+ \pi^-$?

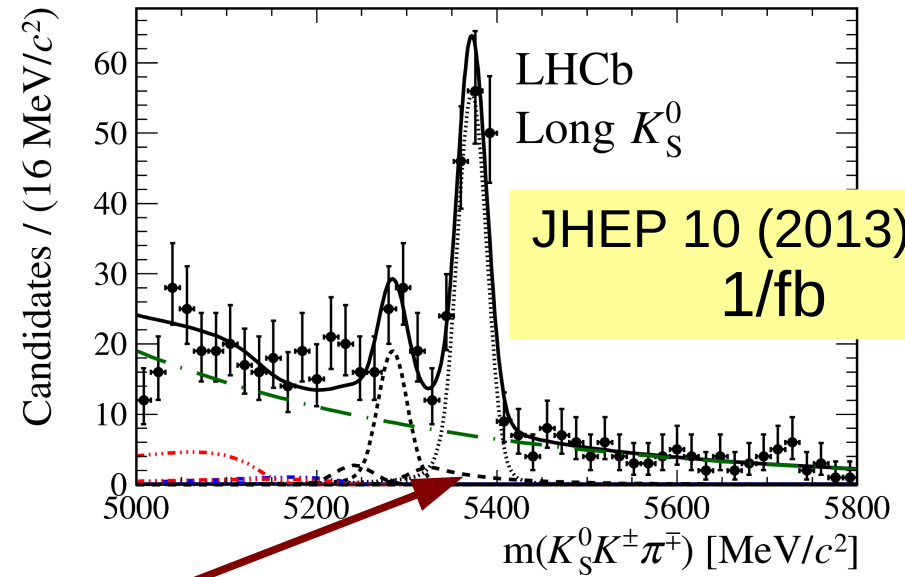
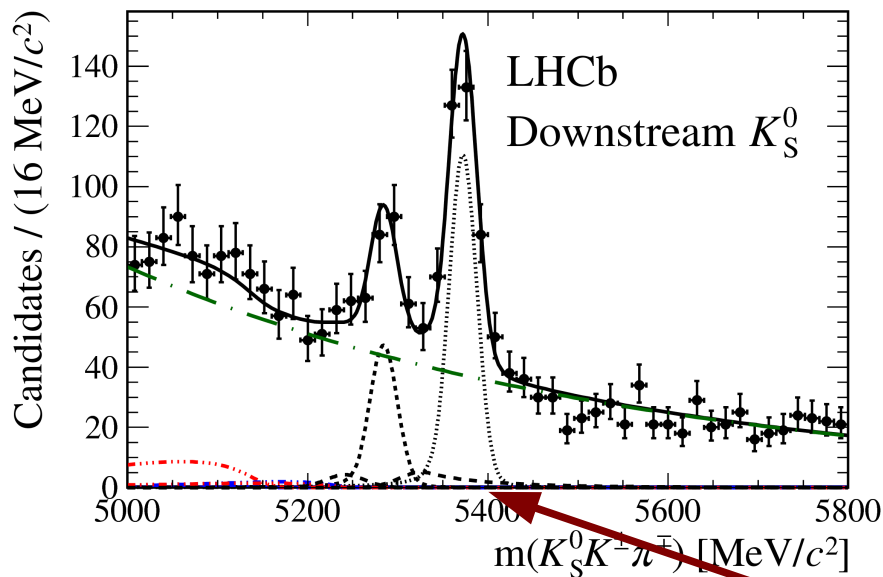
- Similar method works, in principle, for $B_s^0 \rightarrow K_S \pi^+ \pi^-$
- Tagged time-dependent analysis not possible at B-factories, but could be done at LHCb [arXiv:1411.2018](https://arxiv.org/abs/1411.2018)
- Yields available are, however, small



Observation of $B_s^0 \rightarrow K_S \pi^+ \pi^-$

Aside: $B_s^0 \rightarrow KK\pi$?

- Similar method works, in principle, for $B_s^0 \rightarrow KK\pi$
- Tagged time-dependent analysis not possible at B-factories, but could be done at LHCb
- Reasonable yields available, but low tagging power
 - $B_s^0 \rightarrow K_S K^+ \pi^-$ requires double Dalitz plot analysis (two final states)



Observation of $B_s^0 \rightarrow K_S K^+ \pi^-$