



BSM Primary Effects

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TIFR Free Meson Seminar



Plan of Talk



- I. BSM Primaries

RSG A. Pomarol and F. Riva ([arxiv: 1405.0181](#))

- II. RG induced constraints

RSG J. Elias-Miro, C. Grojean, D Marzocca ([arxiv: 1312.2928](#))

- III. Measuring higher dimensional deviations at LHC in diboson production.

Banerjee, Englert, RSG, McCullough and Spannowsky
([work in progress](#))

- IV. Expectations in Explicit Models

RSG M. Montull and F. Riva ([arxiv: 1312.2928](#))

RSG H. Rzehak and J.D. Wells ([arxiv:1206.3560](#), [1305.6397](#))



What if new physics is just beyond LHC reach ?



- **Naturalness does not give a strict upper bound on new physics.** A factor of few larger masses can lead to an exponential drop in parton luminosities.
- **New physics might just be beyond LHC reach.** When integrated out this would still lead to indirect effects such as **deviations in couplings involving the Higgs and gauge boson.**
- Eg. : The **S,T parameters** at LEP constrain certain kinds of new Physics to scales higher than a few TeV. Much higher than LEP energies.
- In any case now that we have seen the Higgs we **must measure its properties as precisely as possible.**

+ SM as an EFT

- The absence at the LHC of new states beyond the SM (BSM) suggests that the new-physics scale must be heavier than the electroweak (EW) scale and we can write:

$$\mathcal{L}_{\text{eff}} = \frac{\Lambda^4}{g_*^2} \mathcal{L} \left(\frac{D_\mu}{\Lambda}, \frac{g_* H}{\Lambda}, \frac{g_* f_{L,R}}{\Lambda^{3/2}}, \frac{g F_{\mu\nu}}{\Lambda^2} \right) \simeq \mathcal{L}_4 + \mathcal{L}_6 + \dots$$

+ Part I: BSM Primary effects and
Predictions from the dimension 6
Lagrangian.



+ Variety of Pseudo-observables !

$$hW_{\mu\nu}^+ W^{-\mu\nu} \quad hA_{\mu\nu}A^{\mu\nu}, hA_{\mu\nu}Z^{\mu\nu} \quad hG_{\mu\nu}G^{\mu\nu} \quad h^2\bar{f}f \quad hZ_{\mu\nu}Z^{\mu\nu}$$

$$hW^{+\mu}W_{\mu}^-, h\bar{f}f, h^3$$

$$hZ_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R}$$

$$Z_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R}$$

$$W^{+\mu}\bar{u}_L\gamma_{\mu}d_L$$

$$Z^{\mu}Z^{\nu}W_{\mu}^{-}W_{\nu}^{+}$$

$$g_1^Z c_{\theta_W} Z^{\mu} \left(W^{+\nu}\hat{W}_{\mu\nu}^{-} - W^{-\nu}\hat{W}_{\mu\nu}^{+} \right)$$

$$W^{-\mu}W^{+\nu}W_{\mu}^{-}W_{\nu}^{+}$$

$$\kappa_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} W_{\mu}^{+} W_{\nu}^{-}$$

$$\lambda_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_{\mu}^{-\rho} \hat{W}_{\rho\nu}^{+}$$

Any vertex of SM fields in the EW broken phase in the unitary gauge can be thought of as a pseudo-observable



Any vertex of SM fields in the EW broken phase in the unitary gauge
can be thought of as a pseudo-observable

+

Variety of Pseudo-observables !

(1) Higgs observables:

$$\begin{aligned}
 hW_{\mu\nu}^+ W^{-\mu\nu} & \quad hA_{\mu\nu}A^{\mu\nu}, hA_{\mu\nu}Z^{\mu\nu} \quad hG_{\mu\nu}G^{\mu\nu} \quad h^2\bar{f}f \quad hZ_{\mu\nu}Z^{\mu\nu} \\
 & \quad hW^{+\mu}W_{\mu}^-, h\bar{f}f, h^3 \quad hZ_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R}
 \end{aligned}$$

These contain the physical Higgs constrained for the first time at LHC in Higgs Production/decay

(2) Electroweak precision observables:

$$Z_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R} \quad W^{+\mu}\bar{u}_L\gamma_{\mu}d_L$$

These were measured very precisely at the W/Z-pole in W/Z decays.

(2) Triple and Quartic Gauge couplings:

$$\begin{aligned}
 g_1^Z c_{\theta_W} Z^{\mu} \left(W^{+\nu}\hat{W}_{\mu\nu}^- - W^{-\nu}\hat{W}_{\mu\nu}^+ \right) & \quad Z^{\mu}Z^{\nu}W_{\mu}^-W_{\nu}^+ \\
 \kappa_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu}W_{\mu}^+W_{\nu}^- & \quad W^{-\mu}W^{+\nu}W_{\mu}^-W_{\nu}^+ \\
 \lambda_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu}\hat{W}_{\mu}^{-\rho}\hat{W}_{\rho\nu}^+ &
 \end{aligned}$$

These were measured in ee->WW process at LEP.

+ Organizing principle: Effective Field Theory (EFT)

- All these deformations cannot be independent at dimension 6 level. Only 18 independent operators that are involved in

$$\begin{aligned}\mathcal{O}_H &= \frac{1}{2}(\partial^\mu |H|^2)^2 \\ \mathcal{O}_T &= \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2 \\ \mathcal{O}_6 &= \lambda |H|^6 \\ \mathcal{O}_W &= \frac{ig}{2} \left(H^\dagger \sigma^a \overleftrightarrow{D}^\mu H \right) D^\nu W_{\mu\nu}^a \\ \mathcal{O}_B &= \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\nu B_{\mu\nu}\end{aligned}$$

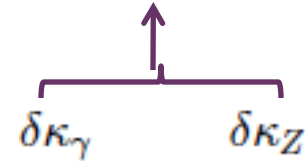
$$\begin{aligned}\mathcal{O}_{BB} &= g'^2 |H|^2 B_{\mu\nu} B^{\mu\nu} \\ \mathcal{O}_{GG} &= g_s^2 |H|^2 G_{\mu\nu}^A G^{A\mu\nu} \\ \mathcal{O}_{HW} &= ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a \\ \mathcal{O}_{HB} &= ig'(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ \mathcal{O}_{3W} &= \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_{\nu\rho}^b W^{c\rho\mu}\end{aligned}$$

$\mathcal{O}_{y_u} = y_u H ^2 \bar{Q}_L \tilde{H} u_R$	$\mathcal{O}_{y_d} = y_d H ^2 \bar{Q}_L H d_R$	$\mathcal{O}_{y_e} = y_e H ^2 \bar{L}_L H e_R$
$\mathcal{O}_R^u = (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{u}_R \gamma^\mu u_R)$	$\mathcal{O}_R^d = (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{d}_R \gamma^\mu d_R)$	$\mathcal{O}_R^e = (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{e}_R \gamma^\mu e_R)$
$\mathcal{O}_L^q = (iH^\dagger \overleftrightarrow{D}_\mu H)(\bar{Q}_L \gamma^\mu Q_L)$		
$\mathcal{O}_L^{(3)q} = (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H)(\bar{Q}_L \sigma^a \gamma^\mu Q_L)$		

+ More observables than operators !

When expanded one operator gives rise to many deformations/vertices/observables.

TGCs



$$(H^\dagger \sigma^a H) W_{\mu\nu}^a B^{\mu\nu} \longrightarrow \hat{h}^2 \left[\hat{W}_{\mu\nu}^3 B^{\mu\nu} + 2igc_{\theta_w} W_\mu^- W_\nu^+ (A^{\mu\nu} - t_{\theta_w} Z^{\mu\nu}) \right]$$

$$\hat{h} = v + h$$

Higgs Physics

$$hA_{\mu\nu}A^{\mu\nu} \quad hA_{\mu\nu}Z^{\mu\nu} \quad hZ_{\mu\nu}Z^{\mu\nu} \quad hW_{\mu\nu}W^{\mu\nu}$$

$$\hat{W}_{\mu\nu}^3 B^{\mu\nu}$$

S-parameter

1 Operator but 7 observables



+ When Lagrangian written in unitary gauge we get many vertices (observables)

$$\begin{aligned}
 \mathcal{L}_h = \xi \left\{ \frac{c_H}{2} \left(1 + \frac{h}{v} \right)^2 \partial^\mu h \partial_\mu h - c_6 \frac{m_H^2}{2v^2} \left(v h^3 + \frac{3h^4}{2} + \dots \right) + c_y \frac{m_f}{v} \bar{f} f \left(h + \frac{3h^2}{2v} + \dots \right) \right. \\
 + \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[\frac{g^2}{2g_\rho^2} (\hat{c}_W W_\mu^- \mathcal{D}^{\mu\nu} W_\nu^+ + \text{h.c.}) + \frac{g^2}{2g_\rho^2} Z_\mu \mathcal{D}^{\mu\nu} \left[\hat{c}_Z Z_\nu + \left(\frac{2\hat{c}_W}{\sin 2\theta_W} - \frac{\hat{c}_Z}{\tan \theta_W} \right) A_\nu \right] \right. \\
 - \frac{g^2}{(4\pi)^2} \left(\frac{c_{HW}}{2} W^{+\mu\nu} W_{\mu\nu}^- + \frac{c_{HW} + \tan^2 \theta_W c_{HB}}{4} Z^{\mu\nu} Z_{\mu\nu} - 2 \sin^2 \theta_W c_{\gamma Z} F^{\mu\nu} Z_{\mu\nu} \right) + \dots \\
 \left. \left. + \frac{\alpha g^2 c_\gamma}{4\pi g_\rho^2} F^{\mu\nu} F_{\mu\nu} + \frac{\alpha_s y_t^2 c_g}{4\pi g_\rho^2} G^{a\mu\nu} G_{\mu\nu}^a \right] \right\} \quad (71)
 \end{aligned}$$

From Giudice, Grojean, Pomarol and Rattazzi
(arxiv: hep-ph/0703164)

+ When Lagrangian written in unitary gauge we get many vertices (observables)

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 \left. + \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[\frac{g^2}{(4\pi)^2} \left(\frac{1}{2} A_\nu^2 + \dots \right) \right] \right. \\
 \left. - \frac{g^2}{(4\pi)^2} \left[\frac{\alpha g^2 c_\gamma}{4\pi g_\rho^2} F^{\mu\nu} F_{\mu\nu} + \frac{\alpha_s g_t^2 c_g}{4\pi g_\rho^2} G^{a\mu\nu} G_{\mu\nu}^a \right] \right\} \quad (71)
 \end{aligned}$$

No of free parameters in this part of the Lagrangian

= No of Wilson coefficients = 18

From Giudice, Grojean, Pomarol and Rattazzi
(arxiv: hep-ph/0703164)

+ 18 EW and Higgs Operators

18 Operators

Many Vertices/pseudo-observables

$$\begin{aligned} \mathcal{O}_H &= \frac{1}{2}(\partial^\mu |H|^2)^2 \\ \mathcal{O}_T &= \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2 \\ \mathcal{O}_6 &= \lambda |H|^6 \\ \mathcal{O}_W &= \frac{ig}{2} \left(H^\dagger \sigma^a \overleftrightarrow{D}_\mu H \right) D^\nu W_{\mu\nu}^a \\ \mathcal{O}_B &= \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right) \partial^\nu B_{\mu\nu} \end{aligned}$$

$$\begin{aligned} \mathcal{O}_{BB} &= g'^2 |H|^2 B_{\mu\nu} B^{\mu\nu} \\ \mathcal{O}_{GG} &= g_s^2 |H|^2 G_{\mu\nu}^A G^{A\mu\nu} \\ \mathcal{O}_{HW} &= ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a \\ \mathcal{O}_{HB} &= ig'(D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ \mathcal{O}_{3W} &= \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_\nu^b W^c{}_{\rho\mu} \end{aligned}$$

$\mathcal{O}_{y_u} = y_u H ^2 \bar{Q}_L \tilde{H} u_R$	$\mathcal{O}_{y_d} = y_d H ^2 \bar{Q}_L H d_R$	$\mathcal{O}_{y_e} = y_e H ^2 \bar{L}_L H e_R$
$\mathcal{O}_R^u = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R)$	$\mathcal{O}_R^d = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{d}_R \gamma^\mu d_R)$	$\mathcal{O}_R^e = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R)$
$\mathcal{O}_L^q = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{Q}_L \gamma^\mu Q_L)$		
$\mathcal{O}_L^{(3)q} = (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{Q}_L \sigma^a \gamma^\mu Q_L)$		

$hW_{\mu\nu}^+ W^{-\mu\nu}$
 $hA_{\mu\nu}A^{\mu\nu}, hA_{\mu\nu}Z^{\mu\nu}, hG_{\mu\nu}G^{\mu\nu}$
 $h^2\bar{f}f, hZ_{\mu\nu}Z^{\mu\nu}$
 $hW^{+\mu}W_{\mu}^-, h\bar{f}f, h^3$
 $hZ_{\mu}\bar{f}_{L,R}\gamma^\mu f_{L,R}$
 $Z_{\mu}\bar{f}_{L,R}\gamma^\mu f_{L,R}$
 $W^{+\mu}\bar{u}_L\gamma_\mu d_L$
 $g_1^Z c_{\theta_W} Z^\mu \left(W^{+\nu}\hat{W}_{\mu\nu}^- - W^{-\nu}\hat{W}_{\mu\nu}^+ \right)$
 $\kappa_\gamma s_{\theta_W} \hat{A}^{\mu\nu} W_\mu^+ W_\nu^-$
 $\lambda_\gamma s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_\mu^{-\rho} \hat{W}_{\rho\nu}^+$

Number of contributing operators \ll Number of vertices/pseudo-observables

+ 18 EW and Higgs Operators

18 Operators

Many Vertices/pseudo-observables

$$\begin{aligned}\mathcal{O}_H &= \frac{1}{2}(\partial^\mu |H|^2)^2 \\ \mathcal{O}_T &= \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2 \\ \mathcal{O}_6 &= \lambda |H|^6 \\ \mathcal{O}_W &= \frac{ig}{2} \left(H^\dagger \sigma^a \overleftrightarrow{D}^\mu H \right) \\ \mathcal{O}_B &= \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\mu\end{aligned}$$

$$\begin{aligned}\mathcal{O}_{y_u} &= y_u |H|^2 \bar{Q}_L \tilde{H} u_R \\ \mathcal{O}_R^u &= (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R) \\ \mathcal{O}_L^q &= (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{Q}_L \gamma^\mu Q_L) \\ \mathcal{O}_L^{(3)q} &= (i H^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{Q}_L \sigma^a \gamma^\mu Q_L)\end{aligned}$$

At any given order
Number of contributing operators
 \ll Number of vertices/pseudo-observables

Correlations between different vertices/observables

$$h^2 \bar{f} f \quad h Z_{\mu\nu} Z^{\mu\nu}$$

$$h Z_\mu \bar{f}_{L,R} \gamma^\mu f_{L,R}$$

$$W^{+\mu} \bar{u}_L \gamma_\mu d_L$$

$$\lambda_\gamma s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_\mu^{-\rho} \hat{W}_{\rho\nu}^+$$

+ BSM Primaries

- 18 **best** constrained observables become these **18 free parameters**.
- We call these **BSM Primaries**. (see also Pomarol & Riva, 2013, Elias-Miro, Espinosa, Masso & Pomarol, 2013)

Only at LHC

Higgs (8)
Physics

$$\begin{aligned}
 & h \rightarrow \gamma\gamma, h \rightarrow \gamma Z, h \rightarrow gg && h A_{\mu\nu} A^{\mu\nu}, h A_{\mu\nu} Z^{\mu\nu}, h G_{\mu\nu} G^{\mu\nu} \\
 & h \rightarrow VV, h \rightarrow ff, pp \rightarrow h^* \rightarrow hh && h W^{+\mu} W_{\mu}^{-}, h \bar{f} f, h^3
 \end{aligned}$$

Z-pole (7)
Data

$$\begin{aligned}
 & Z \rightarrow ff && Z_{\mu} f_{L,R}^{-} \gamma^{\mu} f_{L,R} \\
 & (2 \text{ can be traded for } S, T)
 \end{aligned}$$

TGC (3)
Data

$$\begin{aligned}
 & ee \rightarrow WW && g_1^Z c_{\theta_W} Z^{\mu} \left(W^{+\nu} \hat{W}_{\mu\nu}^{-} - W^{-\nu} \hat{W}_{\mu\nu}^{+} \right) \\
 & && \kappa_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} \\
 & && \lambda_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_{\mu}^{-\rho} \hat{W}_{\rho\nu}^{+}
 \end{aligned}$$

Already at LEP

- A generalization of the Peskin-Takeuchi parameters.
RSG, A. Pomarol and F. Riva (arxiv: 1405.0181)

+ Primary and Correlated observables

$$hA_{\mu\nu}A^{\mu\nu}, hA_{\mu\nu}Z^{\mu\nu}, hG_{\mu\nu}G^{\mu\nu}$$

$$hW^{+\mu}W_{\mu}^{-}, h\bar{f}f, h^3$$

$$Z_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R}$$

Deformations **correlated**
at dim-6 level

$$g_1^Z c_{\theta_W} Z^{\mu} \left(W^{+\nu} \hat{W}_{\mu\nu}^{-} - W^{-\nu} \hat{W}_{\mu\nu}^{+} \right)$$

$$\kappa_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} W_{\mu}^{+} W_{\nu}^{-}$$

$$\lambda_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_{\mu}^{-\rho} \hat{W}_{\rho\nu}^{+}$$

$$h^2 \bar{f}f, hZ_{\mu\nu} Z^{\mu\nu}$$

$$hZ_{\mu}\bar{f}_{L,R}\gamma^{\mu}f_{L,R}, h^4$$

$$W^{+\mu}\bar{u}_L\gamma_{\mu}d_L$$

$$Z^{\mu}Z^{\nu}W_{\mu}^{-}W_{\nu}^{+}$$

$$h^3 \bar{f}f, W^{-\mu}W^{+\nu}W_{\mu}^{-}W_{\nu}^{+}$$

$$hW_{\mu\nu}^{+} W^{-\mu\nu} \dots\dots$$

18 Primary
Deformations/Observables

Correlated
Deformations/Observables



Higgs Primaries (8)

EWPT Primaries(7)

$$\Delta\mathcal{L}_{GG}^h = \kappa_{GG} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^A G^{A\mu\nu}$$

$$\Delta\mathcal{L}_{ee}^V = \delta g_{eR}^Z \frac{\hat{h}^2}{v^2} Z^\mu \bar{e}_R \gamma_\mu e_R$$

$$+ \delta g_{eL}^Z \frac{\hat{h}^2}{v^2} \left[Z^\mu \bar{e}_L \gamma_\mu e_L - \frac{c_{\theta_W}}{\sqrt{2}} (W^{+\mu} \bar{\nu}_L \gamma_\mu e_L + \text{h.c.}) \right]$$

$$\Delta\mathcal{L}_{ff}^h = \delta g_{ff}^h (h \bar{f}_L f_R + \text{h.c.}) \left(1 + \frac{3h}{v} + \frac{h^2}{2v^2} \right)$$

$\Delta\mathcal{L}_{3h}$

$\Delta\mathcal{L}_{VV}^h$

The electroweak/Higgs part of the dimension 6 Lagrangian can be written in entirely in terms of these 18 already observables (instead of unknown Wilson Coefficients)

18 Primary vertices,
Coefficient of other vertices already determined by these 18.

$$\Delta\mathcal{L}_{Z\gamma}^h = 4\kappa_{Z\gamma} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[t_{\theta_W} A_{\mu\nu} Z^{\mu\nu} + \frac{c_{2\theta_W}}{2c_{\theta_W}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^+ W^{-\mu\nu} \right]$$

$$\Delta\mathcal{L}_{\kappa\gamma} = \frac{1}{v^2} \left[i e t_{\theta_W} (A_{\mu\nu} - t_{\theta_W} Z_{\mu\nu}) W_{\nu\rho}^+ W^{-\rho\mu} + Z_\nu \partial_\mu \hat{h}^2 (t_{\theta_W} A^{\mu\nu} - t_{\theta_W}^2 Z^{\mu\nu}) + \frac{(\hat{h}^2 - v^2)}{2} \times (t_{\theta_W} Z_{\mu\nu} A^{\mu\nu} + \frac{c_{2\theta_W}}{2c_{\theta_W}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^+ W^{-\mu\nu}) \right]$$

$$\Delta\mathcal{L}_{\lambda\gamma} = \frac{i\lambda_\gamma}{m_W^2} [(eA^{\mu\nu} + g c_{\theta_W} Z^{\mu\nu}) W_\nu^{-\rho} W_{\rho\mu}^+]$$

+

Higgs Primaries (8)

$$\Delta\mathcal{L}_{GG}^h = \kappa_{GG} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^A G^{A\mu\nu}$$

$$\Delta\mathcal{L}_{ff}^h = \delta g_{ff}^h (h \bar{f}_L f_R + \text{h.c.}) \left(1 + \frac{3h}{2v} + \frac{h^2}{2v^2} \right)$$

$$\Delta\mathcal{L}_{3h} = \delta g_{3h} h^3 \left(1 + \frac{3h}{2v} + \frac{3h^2}{4v^2} + \frac{h^3}{8v^3} \right),$$

$$\begin{aligned} \Delta\mathcal{L}_{VV}^h = & \delta g_{VV}^h \left[h \left(W^{+\mu} W_{\mu}^- + \frac{Z^{\mu} Z_{\mu}}{2c_{\theta_w}^2} \right) \left(1 + \frac{2h}{v} \right. \right. \\ & \left. \left. + \frac{4h^2}{3v^2} + \frac{h^3}{3v^3} \right) + \frac{m_h^2}{12m_W^2} \left(\frac{h^4}{v} + \frac{3h^5}{4v^2} + \frac{h^6}{8v^3} \right) \right. \\ & \left. + \frac{m_f}{4m_W^2} \left(\frac{h^2}{v} + \frac{h^3}{3v^2} \right) (\bar{f}_L f_R + \text{h.c.}) \right], \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{\gamma\gamma}^h = & 4\kappa_{\gamma\gamma} s_{\theta_w}^2 \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[A_{\mu\nu} A^{\mu\nu} \right. \\ & \left. + Z_{\mu\nu} Z^{\mu\nu} + 2W_{\mu\nu}^+ W^{-\mu\nu} \right], \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{Z\gamma}^h = & 4\kappa_{Z\gamma} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[t_{\theta_w} A_{\mu\nu} Z^{\mu\nu} \right. \\ & \left. + \frac{c_{2\theta_w}}{2c_{\theta_w}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^+ W^{-\mu\nu} \right]. \end{aligned}$$

EWPT Primaries(7)

$$\begin{aligned} \Delta\mathcal{L}_{ee}^V = & \delta g_{eR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{e}_R \gamma_{\mu} e_R \\ & + \delta g_{eL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{e}_L \gamma_{\mu} e_L - \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{\nu}_L \gamma_{\mu} e_L + \text{h.c.}) \right] \\ & + \delta g_{\nu L}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{\nu}_L \gamma_{\mu} \nu_L + \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{\nu}_L \gamma_{\mu} e_L + \text{h.c.}) \right] \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{qq}^V = & \delta g_{uR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{u}_R \gamma_{\mu} u_R + \delta g_{dR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{d}_R \gamma_{\mu} d_R \\ & + \delta g_{dL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{d}_L \gamma_{\mu} d_L - \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{u}_L \gamma_{\mu} d_L + \text{h.c.}) \right] \\ & + \delta g_{uL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{u}_L \gamma_{\mu} u_L + \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{u}_L \gamma_{\mu} d_L + \text{h.c.}) \right] \end{aligned}$$

TGC Primaries (3)

$$\begin{aligned} \Delta\mathcal{L}_{g_1^Z} = & \delta g_1^Z c_{\theta_w}^2 \frac{\hat{h}^2}{v^2} \left[\frac{e^2 \hat{h}^2}{4c_{\theta_w}^4} Z^{\mu} Z_{\mu} \right. \\ & \left. - g(W_{\mu}^- J_{\mu}^+ + \text{h.c.}) - \frac{gc_{2\theta_w}}{c_{\theta_w}^3} Z_{\mu} J_{\mu}^Z - 2et_{\theta_w} Z_{\mu} J_{em}^{\mu} \right] \\ \Delta\mathcal{L}_{\kappa\gamma} = & \frac{\delta\kappa_{\gamma}}{v^2} \left[ie\hat{h}^2 (A_{\mu\nu} - t_{\theta_w} Z_{\mu\nu}) W^{+\mu} W^{-\nu} \right. \\ & \left. + Z_{\nu} \partial_{\mu} \hat{h}^2 (t_{\theta_w} A^{\mu\nu} - t_{\theta_w}^2 Z^{\mu\nu}) + \frac{(\hat{h}^2 - v^2)}{2} \right. \\ & \left. \times \left(t_{\theta_w} Z_{\mu\nu} A^{\mu\nu} + \frac{c_{2\theta_w}}{2c_{\theta_w}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^+ W^{-\mu\nu} \right) \right] \\ \Delta\mathcal{L}_{\lambda\gamma} = & \frac{i\lambda_{\gamma}}{m_W^2} [(eA^{\mu\nu} + gc_{\theta_w} Z^{\mu\nu}) W_{\nu}^{-\rho} W_{\rho\mu}^+] \end{aligned}$$

+ BSM Primaries

- 18 observables **best** constrain all Higgs and EW deformations.
- We call these **BSM Primaries**. (see also Pomarol & Riva, 2013, Elias-Miro, Espinosa, Masso & Pomarol, 2013)

Only at LHC

Higgs (8)
Physics

$$\begin{aligned}
 & h \rightarrow \gamma\gamma, h \rightarrow \gamma Z, h \rightarrow gg && h A_{\mu\nu} A^{\mu\nu}, h A_{\mu\nu} Z^{\mu\nu}, h G_{\mu\nu} G^{\mu\nu} \\
 & h \rightarrow VV, h \rightarrow ff, pp \rightarrow h^* \rightarrow hh && h W^{+\mu} W_{\mu}^{-}, h \bar{f} f, h^3
 \end{aligned}$$

Z-pole (7)
Data

$$\begin{aligned}
 & Z \rightarrow ff && Z_{\mu} f_{L,R}^{-} \gamma^{\mu} f_{L,R} \\
 & (2 \text{ can be traded for } S, T)
 \end{aligned}$$

TGC (3)
Data

$$\begin{aligned}
 & ee \rightarrow WW && g_1^Z c_{\theta_W} Z^{\mu} \left(W^{+\nu} \hat{W}_{\mu\nu}^{-} - W^{-\nu} \hat{W}_{\mu\nu}^{+} \right) \\
 & && \kappa_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} W_{\mu}^{+} W_{\nu}^{-} \\
 & && \lambda_{\gamma} s_{\theta_W} \hat{A}^{\mu\nu} \hat{W}_{\mu}^{-\rho} \hat{W}_{\rho\nu}^{+}
 \end{aligned}$$

Already at LEP

- A generalization of the Peskin-Takeuchi parameters.
RSG, A. Pomarol and F. Riva (arxiv: 1405.0181)

+ Z-pole Primaries + TGC



\mathcal{L}_4

\mathcal{L}_6

δg_{ZWW}

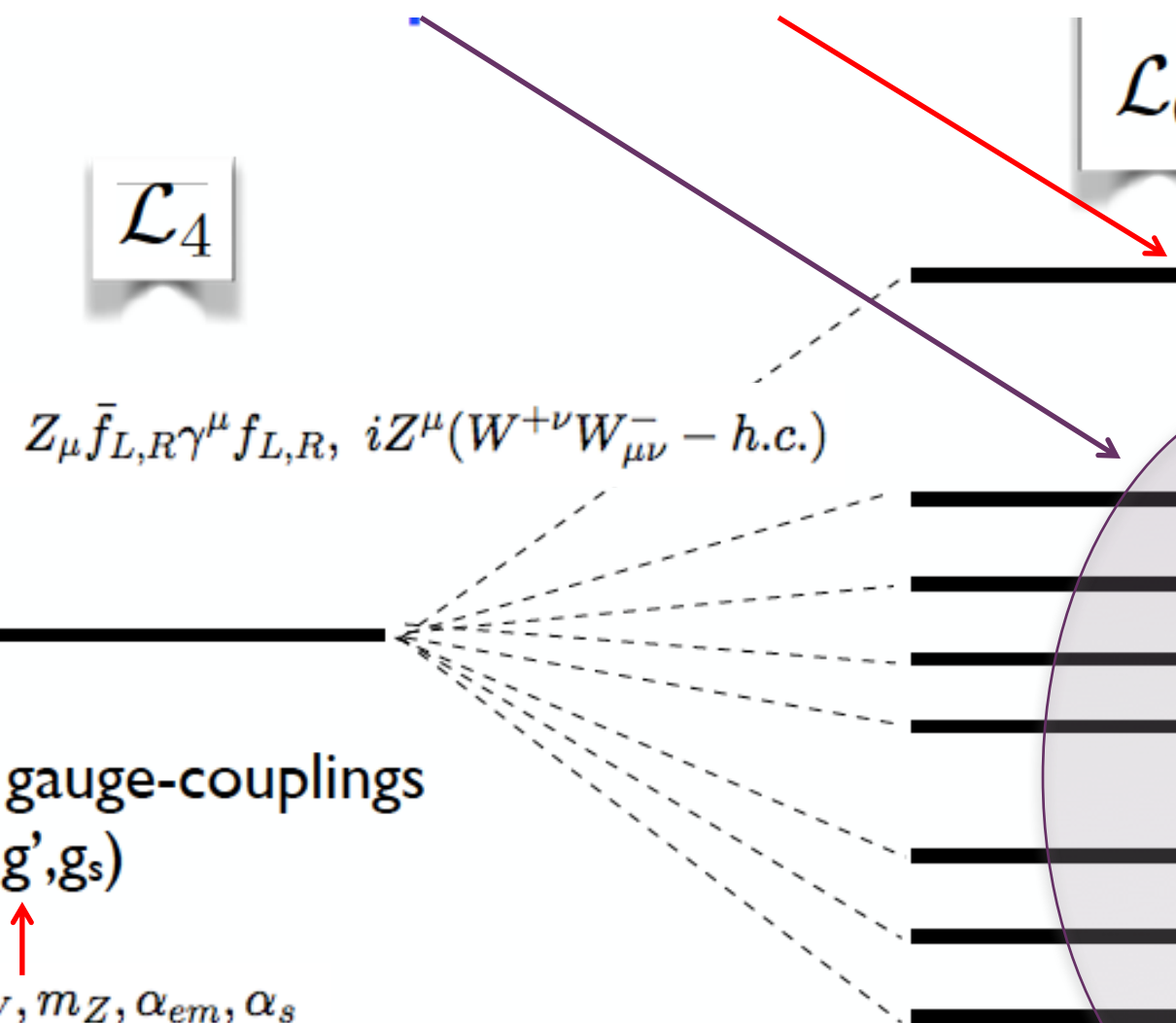
Vertices: $Z_\mu \bar{f}_{L,R} \gamma^\mu f_{L,R}, iZ^\mu (W^{+\nu} W_{\mu\nu}^- - h.c.)$

—

universal gauge-couplings
(g, g', g_s)

Input: $m_W, m_Z, \alpha_{em}, \alpha_s$

- δg_{ZuR}
- δg_{ZdR}
- δg_{ZuL}
- δg_{ZdL}
- δg_{ZeR}
- δg_{ZeL}
- $\delta g_{Z\nu L}$



+ Z-pole Primaries + TGC

\mathcal{L}_4

\mathcal{L}_6

Vertices: $Z_\mu \bar{f}_{L,R} \gamma^\mu f_{L,R}, iZ^\mu (W^{+\nu} W_{\mu\nu}^- - h.c.)$

universal gauge-couplings
(g, g', g_s)

Input: $m_W, m_Z, \alpha_{em}, \alpha_s$

per-cent splittings

per-mile splittings

δg_{ZWW}

δg_{ZuR}

δg_{ZdR}

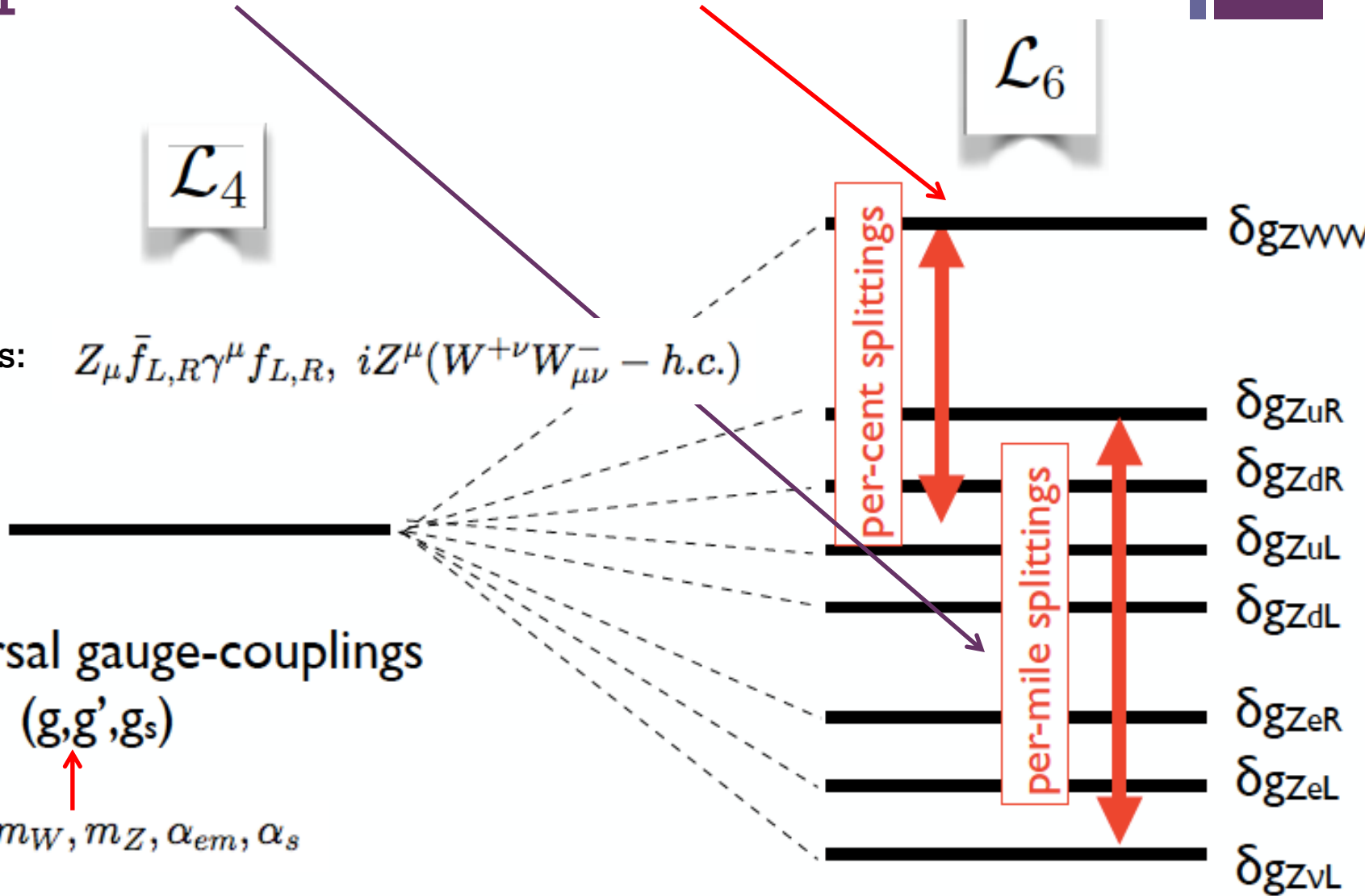
δg_{ZuL}

δg_{ZdL}

δg_{ZeR}

δg_{ZeL}

$\delta g_{Z\nu L}$



+ Z-pole Primaries + TGC

\mathcal{L}_4

\mathcal{L}_6

splittings

δg_{ZWW}

Vertices: $Z_\mu \bar{f}_L \gamma^\mu f_L + i Z^\mu (W^{+\nu} W^{-\nu} - h.c.)$

1. *Very precisely measured at LEP.*

2. *W couplings not primaries. Totally determined once Z couplings are measured.*

3. *S, T parameters are two oblique linear combinations of these.*

4. *All corrections to the gauge propagators can be written in terms of the above vertex corrections using EoM.*

δg_{ZuR}

δg_{ZdR}

δg_{ZuL}

δg_{ZdL}

δg_{ZeR}

δg_{ZeL}

$\delta g_{Z\nu L}$

univers

Input: m

+ Other TGC primaries

- 2 more TGC vertices are primaries:

$$\delta\kappa^\gamma W_\mu^+ W_\nu^- A^{\mu\nu}$$

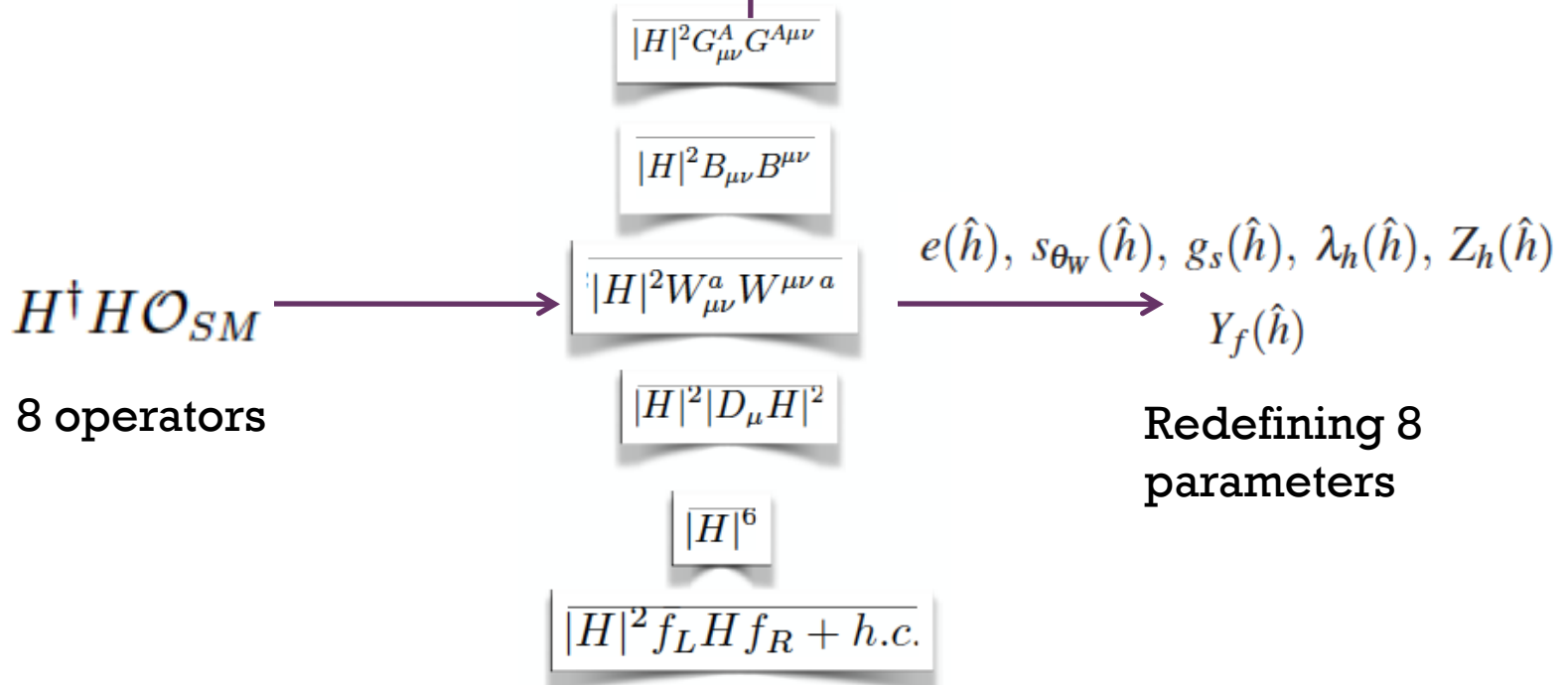
$$\lambda_\gamma s_{\theta_W} A^{\mu\nu} W_\nu^{-\rho} W_{\rho\mu}^+$$

- Measured at per cent level in $ee \rightarrow WW$ process at LEP.

+ The Dimension 6 Lagrangian

$$\Delta\mathcal{L}_{h^2SM} = c_V g^2 \hat{h}^4 (W^2 + Z^2/2c_{\theta_W}^2) + c_6 \hat{h}^6 + \frac{\hat{h}^2}{\Lambda^2} [c_{WW} g^2 W_{\mu\nu}^a W^{\mu\nu a} + c_{BB} g'^2 B_{\mu\nu} B^{\mu\nu}] + c_{y_f} y_f (\hat{h}^3 \bar{f}_L f_R + h.c.),$$

$\hat{h} = v + h$



+ The Dimension 6 Lagrangian

$$\Delta\mathcal{L}_{h^2SM} = c_V g^2 \hat{h}^4 (W^2 + Z^2/2c_{\theta_W}^2) + c_6 \hat{h}^6 + \frac{\hat{h}^2}{\Lambda^2} [c_{WW} g^2 W_{\mu\nu}^a W^{\mu\nu a} + c_{BB} g'^2 B_{\mu\nu} B^{\mu\nu}] + c_{y_f} y_f (\hat{h}^3 \bar{f}_L f_R + h.c.),$$

$\uparrow \quad \hat{h} = v + h$

These operators could never have been probed at LEP as they only redefine parameters in dim-4 Lagrangian in the vacuum.

$\lambda_h(\hat{h}), Z_h(\hat{h})$

8 operators

$$|H|^2 |D_\mu H|^2$$

Redefining 8 parameters

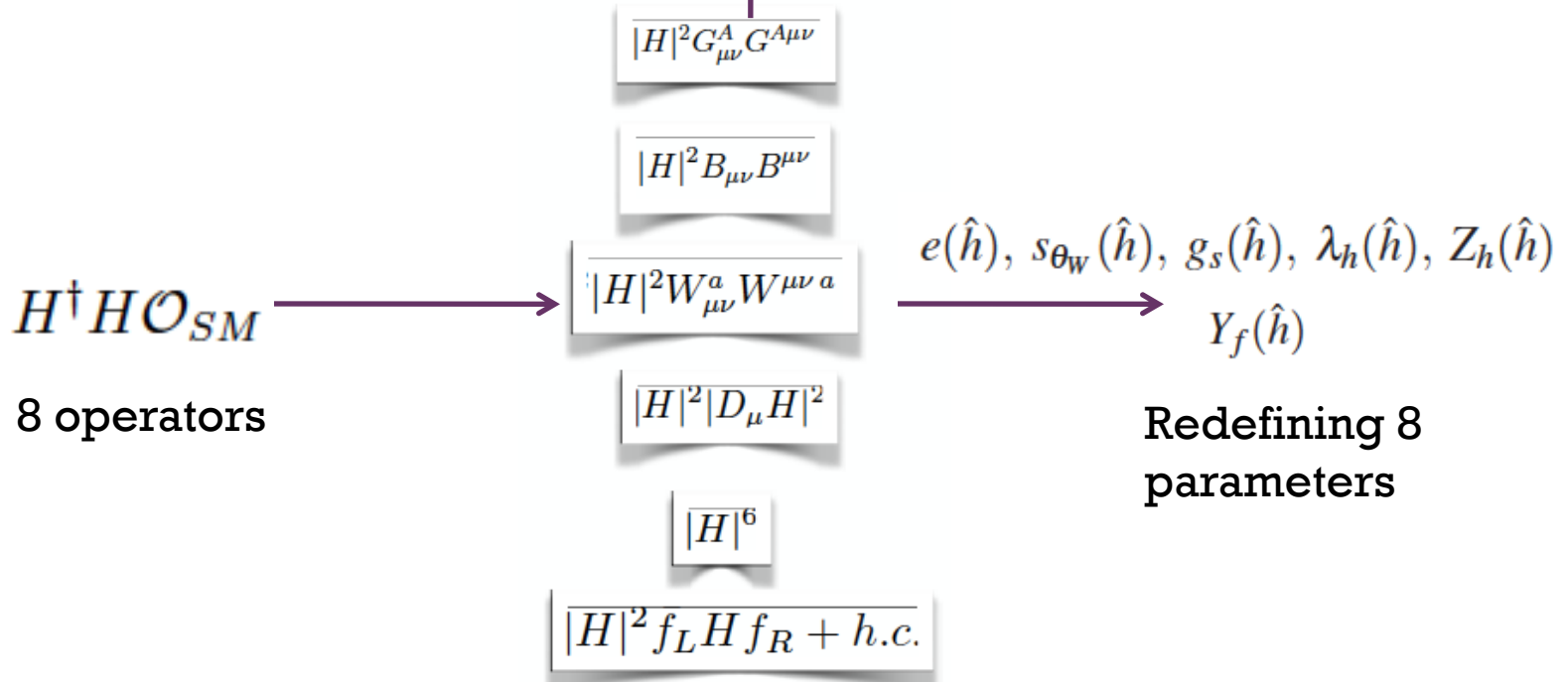
$$|H|^6$$

$$|H|^2 \bar{f}_L H f_R + h.c.$$

+ The Dimension 6 Lagrangian

$$\Delta\mathcal{L}_{h^2SM} = c_V g^2 \hat{h}^4 (W^2 + Z^2 / 2c_{\theta_W}^2) + c_6 \hat{h}^6 + \frac{\hat{h}^2}{\Lambda^2} [c_{WW} g^2 W_{\mu\nu}^a W^{\mu\nu a} + c_{BB} g'^2 B_{\mu\nu} B^{\mu\nu}] + c_{y_f} y_f (\hat{h}^3 \bar{f}_L f_R + h.c.),$$

$\hat{h} = v + h$

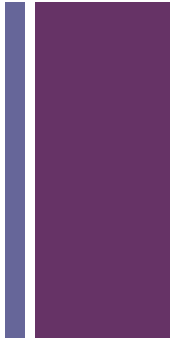




7 Z couplings + 3 TGCs + 8 Higgs
observables = 18 Primaries

Measurement of these would determine
all vertices involved in
electroweak/Higgs processes

Amplitudes for all physical processes,
eg. $h \rightarrow Vff$, $pp \rightarrow Vh$, $VV \rightarrow h$ etc can be
computed as a function of the **BSM
primary parameters** using the above
Lagrangian.



+

Higgs Primaries (8)

$$\Delta\mathcal{L}_{GG}^h = \kappa_{GG} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^A G^{A\mu\nu}$$

$$\Delta\mathcal{L}_{ff}^h = \delta g_{ff}^h (h \bar{f}_L f_R + \text{h.c.}) \left(1 + \frac{3h}{2v} + \frac{h^2}{2v^2} \right)$$

$$\Delta\mathcal{L}_{3h} = \delta g_{3h} h^3 \left(1 + \frac{3h}{2v} + \frac{3h^2}{4v^2} + \frac{h^3}{8v^3} \right),$$

$$\begin{aligned} \Delta\mathcal{L}_{VV}^h = & \delta g_{VV}^h \left[h \left(W^{+\mu} W_{\mu}^{-} + \frac{Z^{\mu} Z_{\mu}}{2c_{\theta_w}^2} \right) \left(1 + \frac{2h}{v} \right. \right. \\ & \left. \left. + \frac{4h^2}{3v^2} + \frac{h^3}{3v^3} \right) + \frac{m_h^2}{12m_W^2} \left(\frac{h^4}{v} + \frac{3h^5}{4v^2} + \frac{h^6}{8v^3} \right) \right. \\ & \left. + \frac{m_f}{4m_W^2} \left(\frac{h^2}{v} + \frac{h^3}{3v^2} \right) (\bar{f}_L f_R + \text{h.c.}) \right], \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{\gamma\gamma}^h = & 4\kappa_{\gamma\gamma} s_{\theta_w}^2 \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[A_{\mu\nu} A^{\mu\nu} \right. \\ & \left. + Z_{\mu\nu} Z^{\mu\nu} + 2W_{\mu\nu}^{+} W^{-\mu\nu} \right], \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{Z\gamma}^h = & 4\kappa_{Z\gamma} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) \left[t_{\theta_w} A_{\mu\nu} Z^{\mu\nu} \right. \\ & \left. + \frac{c_{2\theta_w}}{2c_{\theta_w}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^{+} W^{-\mu\nu} \right]. \end{aligned}$$

EWPT Primaries(7)

$$\begin{aligned} \Delta\mathcal{L}_{ee}^V = & \delta g_{eR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{e}_R \gamma_{\mu} e_R \\ & + \delta g_{eL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{e}_L \gamma_{\mu} e_L - \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{\nu}_L \gamma_{\mu} e_L + \text{h.c.}) \right] \\ & + \delta g_{\nu L}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{\nu}_L \gamma_{\mu} \nu_L + \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{\nu}_L \gamma_{\mu} e_L + \text{h.c.}) \right] \end{aligned}$$

$$\begin{aligned} \Delta\mathcal{L}_{qq}^V = & \delta g_{uR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{u}_R \gamma_{\mu} u_R + \delta g_{dR}^Z \frac{\hat{h}^2}{v^2} Z^{\mu} \bar{d}_R \gamma_{\mu} d_R \\ & + \delta g_{dL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{d}_L \gamma_{\mu} d_L - \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{u}_L \gamma_{\mu} d_L + \text{h.c.}) \right] \\ & + \delta g_{uL}^Z \frac{\hat{h}^2}{v^2} \left[Z^{\mu} \bar{u}_L \gamma_{\mu} u_L + \frac{c_{\theta_w}}{\sqrt{2}} (W^{+\mu} \bar{u}_L \gamma_{\mu} d_L + \text{h.c.}) \right] \end{aligned}$$

TGC Primaries (3)

$$\begin{aligned} \Delta\mathcal{L}_{g_1^Z} = & \delta g_1^Z c_{\theta_w}^2 \frac{\hat{h}^2}{v^2} \left[\frac{e^2 \hat{h}^2}{4c_{\theta_w}^4} Z^{\mu} Z_{\mu} \right. \\ & \left. - g(W_{\mu}^{-} J_{\mu}^{+} + \text{h.c.}) - \frac{gc_{2\theta_w}}{c_{\theta_w}^3} Z_{\mu} J_Z^{\mu} - 2et_{\theta_w} Z_{\mu} J_{em}^{\mu} \right] \\ \Delta\mathcal{L}_{\kappa\gamma} = & \frac{\delta\kappa_{\gamma}}{v^2} \left[ie\hat{h}^2 (A_{\mu\nu} - t_{\theta_w} Z_{\mu\nu}) W^{+\mu} W^{-\nu} \right. \\ & \left. + Z_{\nu} \partial_{\mu} \hat{h}^2 (t_{\theta_w} A^{\mu\nu} - t_{\theta_w}^2 Z^{\mu\nu}) + \frac{(\hat{h}^2 - v^2)}{2} \right. \\ & \left. \times \left(t_{\theta_w} Z_{\mu\nu} A^{\mu\nu} + \frac{c_{2\theta_w}}{2c_{\theta_w}^2} Z_{\mu\nu} Z^{\mu\nu} + W_{\mu\nu}^{+} W^{-\mu\nu} \right) \right] \\ \Delta\mathcal{L}_{\lambda\gamma} = & \frac{i\lambda_{\gamma}}{m_W^2} [(eA^{\mu\nu} + gc_{\theta_w} Z^{\mu\nu}) W_{\nu}^{-\rho} W_{\rho\mu}^{+}] \end{aligned}$$

+ Dimension 6 lagrangian

- So we have finally **constructed the dim-6 lagrangian** in a **bottom up way** (not starting from operators but from measurable deformations):

$$\begin{aligned}\Delta\mathcal{L}_{\text{BSM}} = & \Delta\mathcal{L}_{\gamma\gamma}^h + \Delta\mathcal{L}_{Z\gamma}^h + \Delta\mathcal{L}_{GG}^h + \Delta\mathcal{L}_{ff}^h + \Delta\mathcal{L}_{3h} + \Delta\mathcal{L}_{VV}^h + \Delta\mathcal{L}_{ee}^V + \Delta\mathcal{L}_{qq}^V \\ & + \Delta\mathcal{L}_{g_1^Z} + \Delta\mathcal{L}_{\kappa\gamma} + \Delta\mathcal{L}_{\lambda\gamma} + \Delta\mathcal{L}_{3G} + \Delta\mathcal{L}_{4f} + \Delta\mathcal{L}_{\text{MFV}}^V + \Delta\mathcal{L}_{\text{CPV}}.\end{aligned}$$

+ Dimension 6 lagrangian

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Rest of the 41 operators
not considered here



Predictions for Higgs Physics

Most General interactions of a scalar h .

$$\mathcal{L}_h^{\text{primary}} = g_{VV}^h h \left[W^{+\mu} W_{\mu}^{-} + \frac{1}{2c_{\theta_W}^2} Z^{\mu} Z_{\mu} \right] + g_{3h} h^3 + g_{ff}^h (h \bar{f}_L f_R + h.c.)$$

$$+ \kappa_{GG} \frac{h}{v} G^{A\mu\nu} G_{\mu\nu}^A + \kappa_{\gamma\gamma} \frac{h}{v} A^{\mu\nu} A_{\mu\nu} + \kappa_{Z\gamma} t_{\theta_W} \frac{h}{v} A^{\mu\nu} Z_{\mu\nu},$$

$$\Delta\mathcal{L}_h = \delta g_{ZZ}^h \frac{v}{2c_{\theta_W}^2} h Z^{\mu} Z_{\mu} + g_{Zff}^h \frac{h}{2v} (Z_{\mu} J_N^{\mu} + h.c.) + g_{Wff'}^h \frac{h}{v} (W_{\mu}^{+} J_C^{\mu} + h.c.)$$

$$+ \kappa_{WW} \frac{h}{v} W^{+\mu\nu} W_{\mu\nu}^{-} + \kappa_{ZZ} \frac{h}{v} Z^{\mu\nu} Z_{\mu\nu},$$

Predictions for doublet component h at dim-6 level:

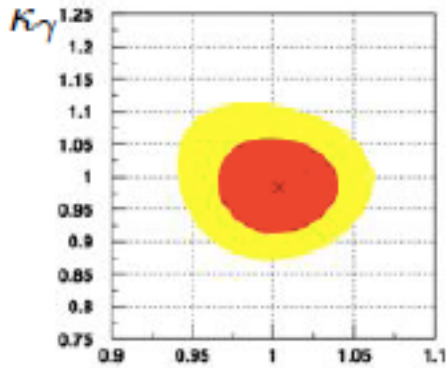
$$\delta g_{ZZ}^h = \delta g_1^Z e^2 - \delta \kappa_{\gamma} \frac{e^2}{c_{\theta_W}^2},$$

$$g_{Zff}^h = 2\delta g_{ff}^Z - 2\delta g_1^Z (g_f^Z c_{2\theta_W} + e Q_f s_{2\theta_W}) + 2\delta \kappa_{\gamma} Y_f \frac{e s_{\theta_W}}{c_{\theta_W}^3}, \quad g_{Wff'}^h = 2\delta g_{ff'}^W - 2\delta g_1^Z g_f^W c_{\theta_W}^2,$$

$$\kappa_{ZZ} = \frac{1}{2c_{\theta_W}^2} (\delta \kappa_{\gamma} + \kappa_{Z\gamma} c_{2\theta_W} + 2\kappa_{\gamma\gamma} c_{\theta_W}^2),$$

$$\kappa_{WW} = \delta \kappa_{\gamma} + \kappa_{Z\gamma} + 2\kappa_{\gamma\gamma},$$

+ Example: $h \rightarrow Zff$

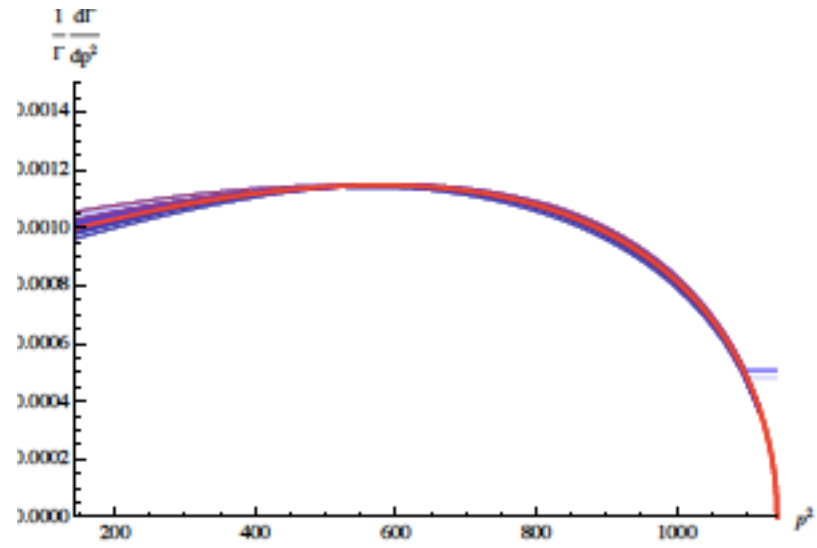
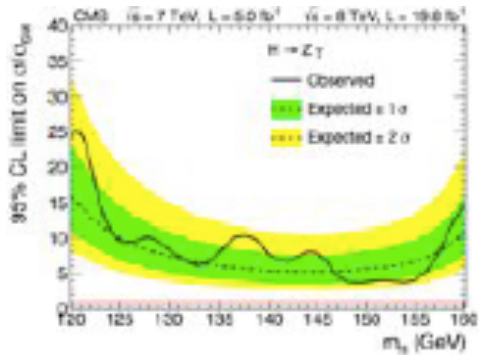


δg_1^Z

+

Already constrained !

$h \rightarrow \gamma Z$





If these predictions are not confirmed, one of our assumptions must have been wrong:

(1) h not part of a doublet.

(2) Scale of new physics not very high and dimension 8 operators cannot be ignored



Other Predictions (not involving Higgs)



- W couplings determined once Z couplings are measured
- Quartic Gauge Couplings (QGCs) determined once



This approach has gained some acceptance. The **LHC Higgs cross-section working group** has now adopted an EFT parametrisation based on this work.

arXiv:1610.07922v2 [hep-ph] 15 May 2017

Handbook of LHC Higgs cross sections:
4. Deciphering the nature of the Higgs sector

Report of the LHC Higgs Cross Section Working Group

Editors: D. de Florian
C. Grojean
F. Maltoni
C. Mariotti
A. Nikitenko
M. Pieri
P. Savard
M. Schumacher
R. Tanaka



+ Inside the report:

equivalent parameterization of the EFT with $D=6$ operators. The idea, put forward in Ref. [632], is to parameterize the space of $D=6$ operators using a subset of couplings in a mass eigenstate Lagrangian, such as the one defined in Eq. (II.2.7) of Section. II.2.1.c. The parameterization described in this section, which differs slightly from that in Ref. [632], is referred to as the *Higgs basis*.^{II.8}

Independent couplings

We now describe the choice of independent couplings which defines the Higgs basis.

Dependent couplings

The number of parameters characterizing departure from the SM Lagrangian in Eq. (II.2.7) is larger than the number of Wilson coefficients in a basis of $D=6$ operators. Due to this fact, there must be relations among these parameters. Working in the Higgs basis, some of the parameters in the mass eigenstate

+ II. Diboson production at LHC



+ Diboson production at LHC

Four channels:

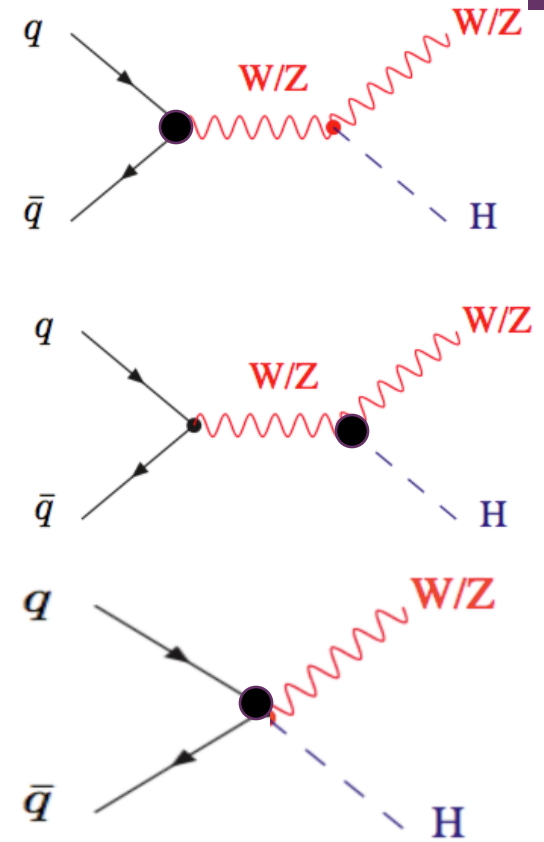
- ZH
- WH
- WW
- WZ



+ VH production at LHC

- The following vertices in the unitary gauge contribute:

$$\begin{aligned}
 \Delta\mathcal{L}_6 \supset & \sum_f \delta g_f^Z Z_\mu \bar{f} \gamma^\mu f + \delta g_{ud}^W (W_\mu^+ \bar{u}_L \gamma^\mu d_L + h.c.) \\
 & + g_{VV}^h h \left[W^{+\mu} W_\mu^- + \frac{1}{2c_{\theta_W}^2} Z^\mu Z_\mu \right] + \delta g_{ZZ}^h h \frac{Z^\mu Z_\mu}{2c_{\theta_W}^2} \\
 & + \sum_f g_{Zff}^h \frac{h}{v} Z_\mu \bar{f} \gamma^\mu f + g_{Wud}^h \frac{h}{v} (W_\mu^+ \bar{u}_L \gamma^\mu d_L + h.c.) \\
 & + \kappa_{Z\gamma} \frac{h}{v} A^{\mu\nu} Z_{\mu\nu} + \kappa_{WW} \frac{h}{v} W^{+\mu\nu} W_{\mu\nu}^- + \kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z_{\mu\nu} .
 \end{aligned}$$



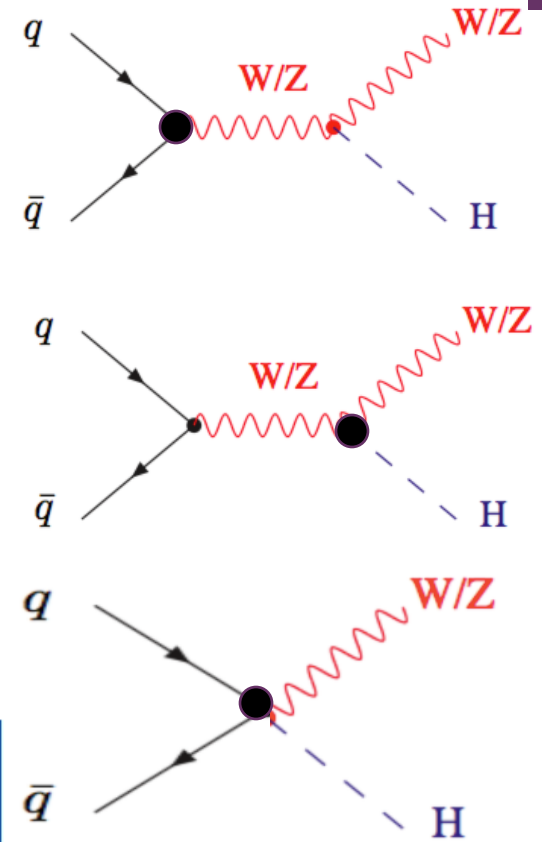
+ VH production at LHC

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 & + g_{VV}^h h \left[W^{+\mu} W_\mu^- + \frac{1}{2c_{\theta_W}^2} Z^\mu Z_\mu \right] + \delta g_{ZZ}^h h \frac{Z^\mu Z_\mu}{2c_{\theta_W}^2} \\
 & + \sum_f g_{Zff}^h \frac{h}{v} Z_\mu \bar{f} \gamma^\mu f + g_{Wud}^h \frac{h}{v} (W_\mu^+ \bar{u}_L \gamma^\mu d_L + h.c.) \\
 & + \kappa_{Z\gamma} \frac{h}{v} A^{\mu\nu} Z_{\mu\nu} + \kappa_{WW} \frac{h}{v} W^{+\mu\nu} W_{\mu\nu}^- + \kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z_{\mu\nu}.
 \end{aligned}$$

$$\mathcal{M}(ff \rightarrow Z_T h) = g_f^Z \frac{\epsilon^* \cdot J_f}{v} \frac{2m_Z^2}{\hat{s}} \left[1 + \left(\frac{g_{Zff}^h}{g_f^Z} - \kappa_{ZZ} \right) \frac{\hat{s}}{2m_Z^2} \right]$$

$$\mathcal{M}(ff \rightarrow Z_L h) = g_f^Z \frac{q \cdot J_f}{v} \frac{2m_Z}{\hat{s}} \left[1 + \frac{g_{Zff}^h}{g_f^Z} \frac{\hat{s}}{2m_Z^2} \right]$$



Leading effect !

+ VH production at LHC

- The following vertices in the unitary gauge contribute:

$$\Delta\mathcal{L}_6 \supset \sum_f \delta g_f^Z Z_\mu \bar{f} \gamma^\mu f + \delta g_{ud}^W (W_\mu^+ \bar{u}_L \gamma^\mu d_L + h.c.)$$

$$+ g_{VV}^h$$

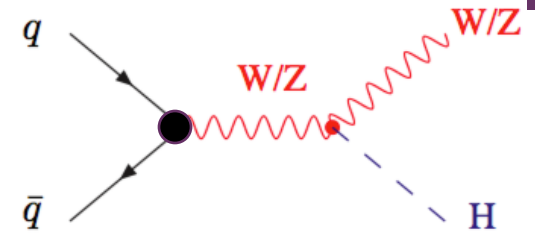
$$+ \sum_f$$

$$+ \kappa_{Z\gamma}$$

But all these vertices already correlated to LEP measurements, thus already constrained! Can LHC do better?... give us new information? May be!

$$\mathcal{M}(ff \rightarrow Z_T h) = g_f^Z \frac{\epsilon^* \cdot J_f}{v} \frac{2m_Z^2}{\hat{s}} \left[1 + \left(\frac{g_{Zff}^h}{g_f^Z} - \kappa_{ZZ} \right) \frac{\hat{s}}{2m_Z^2} \right] \bar{q}$$

$$\mathcal{M}(ff \rightarrow Z_L h) = g_f^Z \frac{q \cdot J_f}{v} \frac{2m_Z}{\hat{s}} \left[1 + \frac{g_{Zff}^h}{g_f^Z} \frac{\hat{s}}{2m_Z^2} \right]$$



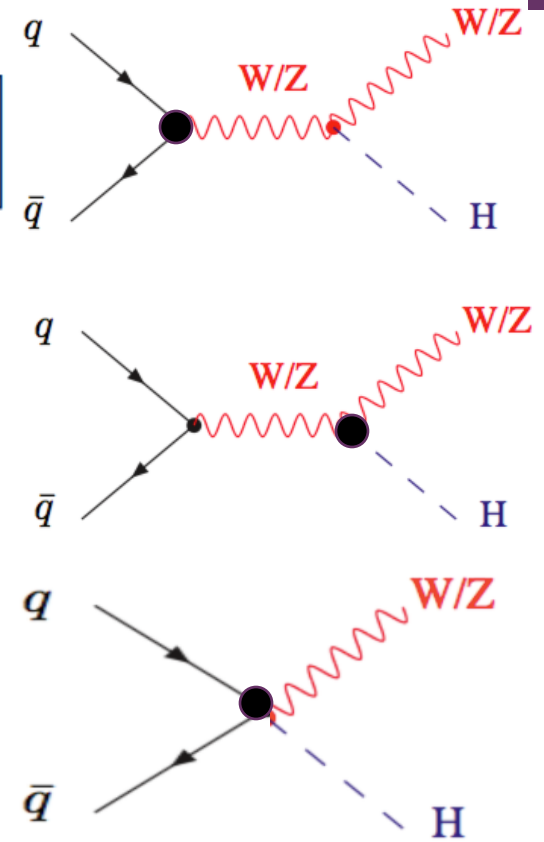
Leading effect!

+ VH production at LHC

- These vertices can be thus measured in this process. For eg. At high energies:

$$\mathcal{M}(ff \rightarrow Z_T h) = g_f^Z \frac{\epsilon^* \cdot J_f}{v} \frac{2m_Z^2}{\hat{s}} \left[1 + \left(\frac{g_{Zff}^h}{g_f^Z} - \kappa_{ZZ} \right) \frac{\hat{s}}{2m_Z^2} \right]$$

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- LEP constraint at 0.001-0.01 level. LHC needs to measure it only at 10 % level because of energy enhancement

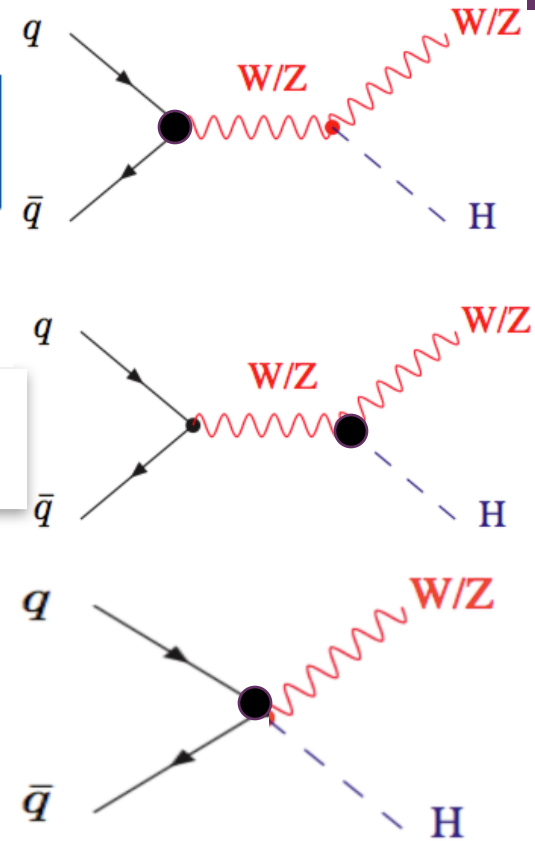
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$$g_{Zff}^h = 2\delta g_f^Z - 2\delta g_1^Z (g_f^Z c_{2\theta_W} + eQ s_{2\theta_W}) + 2\delta\kappa_\gamma g' Y \frac{s_{\theta_W}}{c_{\theta_W}^2}$$



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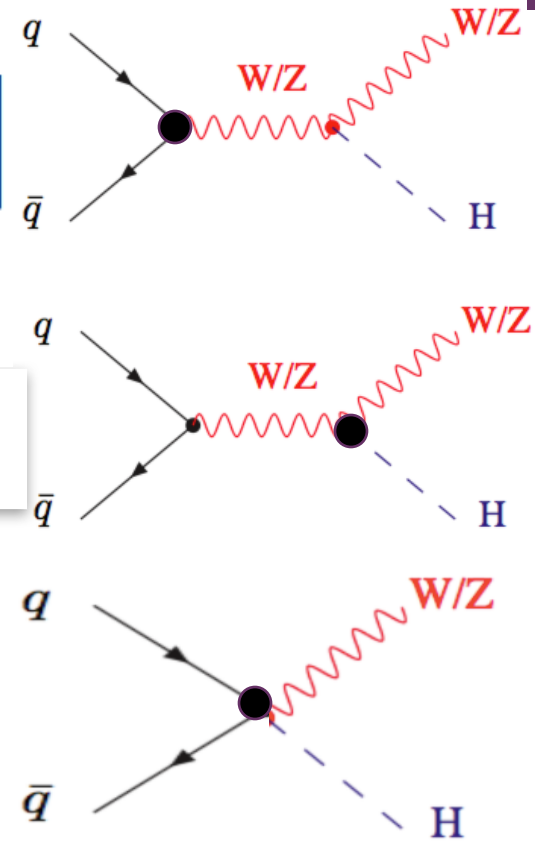
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+ VH production at LHC

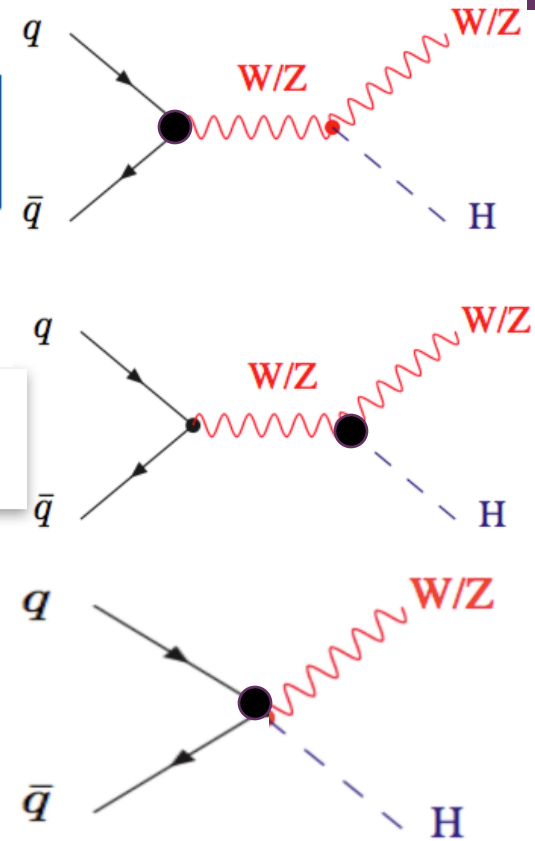
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- LEP constraint at 0.001-0.01 level.



+ VH production at LHC

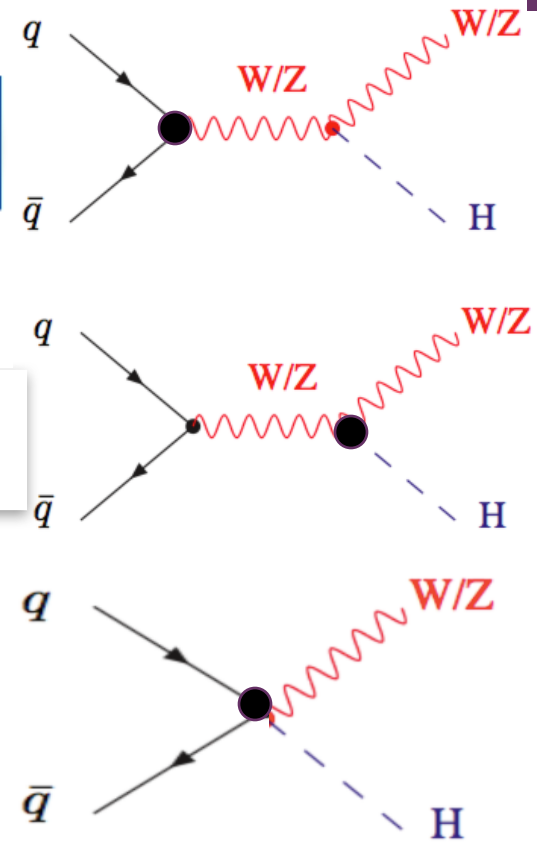
Factor of 100

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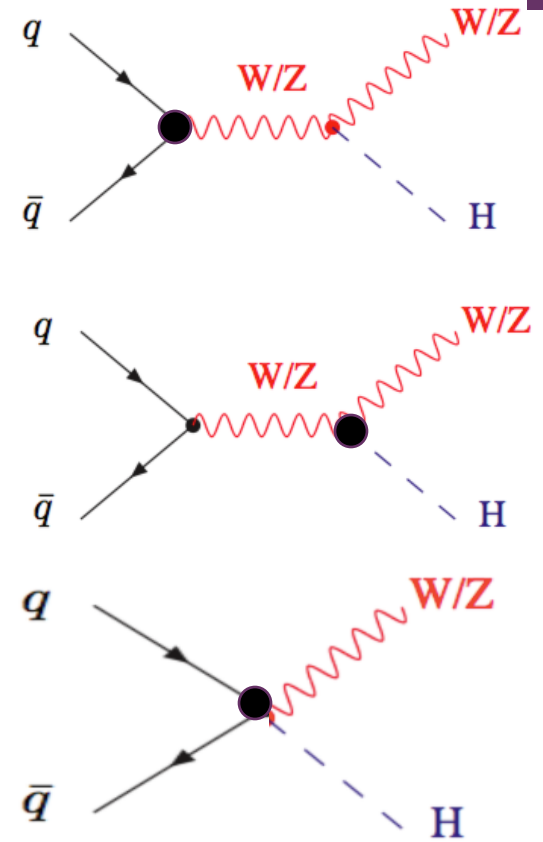


- LEP constraint at 0.001-0.01 level. To be as sensitive as LEP, LHC needs to measure this process at 10% level because of energy enhancement

+ VH production at LHC

- Can a 10% accuracy be achieved in high energy bins for this process ?
- Use of subjet techniques for boosted $h \rightarrow bb$ likely required.

Banerjee, Englert, RSG, McCullough and Spannowsky
(work in progress)



+ Diboson production at LHC

Four channels:

- $ZH \rightarrow G^0 H$
- $WH \rightarrow G^+ H$
- $WW \rightarrow G^+ G^-$
- $WZ \rightarrow G^+ G^0$

- These different final states are **connected by more than nomenclature.**
- **At high energies longitudinal W/Z production dominates.**
- Using **goldstone boson equivalence theorem** one can compute amplitudes for various components of Higgs doublet in the unbroken phase.
- **Full SU(2) symmetry manifest**

+ Diboson production at LHC

Four channels:

■ $ZH \rightarrow G^0 H$	$\bar{u}_L d_L \rightarrow W_L Z_L, W_L h$	$\sqrt{2} a_q^{(3)}$	$\sqrt{2} \frac{g^2}{m_W^2} [c_{\theta_W} (\delta g_{uL}^Z - \delta g_{dL}^Z) / g - c_{\theta_W}^2 \delta g_1^Z]$
■ $WH \rightarrow G^+ H$	$\bar{u}_L u_L \rightarrow W_L W_L$ $\bar{d}_L d_L \rightarrow Z_L h$	$a_q^{(1)} + a_q^{(3)}$	$-\frac{2g^2}{m_W^2} [Y_{Lt} t_{\theta_W}^2 \delta \kappa_\gamma + T_Z^{uL} \delta g_1^Z + c_{\theta_W} \delta g_{dL}^Z / g]$
■ $WW \rightarrow G^+ G^-$	$\bar{d}_L d_L \rightarrow W_L W_L$ $\bar{u}_L u_L \rightarrow Z_L h$	$a_q^{(1)} - a_q^{(3)}$	$-\frac{2g^2}{m_W^2} [Y_{Lt} t_{\theta_W}^2 \delta \kappa_\gamma + T_Z^{dL} \delta g_1^Z + c_{\theta_W} \delta g_{uL}^Z / g]$
■ $WZ \rightarrow G^+ G^0$	$\bar{f}_R f_R \rightarrow W_L W_L, Z_L h$	a_f	$-\frac{2g^2}{m_W^2} [Y_{fR} t_{\theta_W}^2 \delta \kappa_\gamma + T_Z^{fR} \delta g_1^Z + c_{\theta_W} \delta g_{fR}^Z / g]$

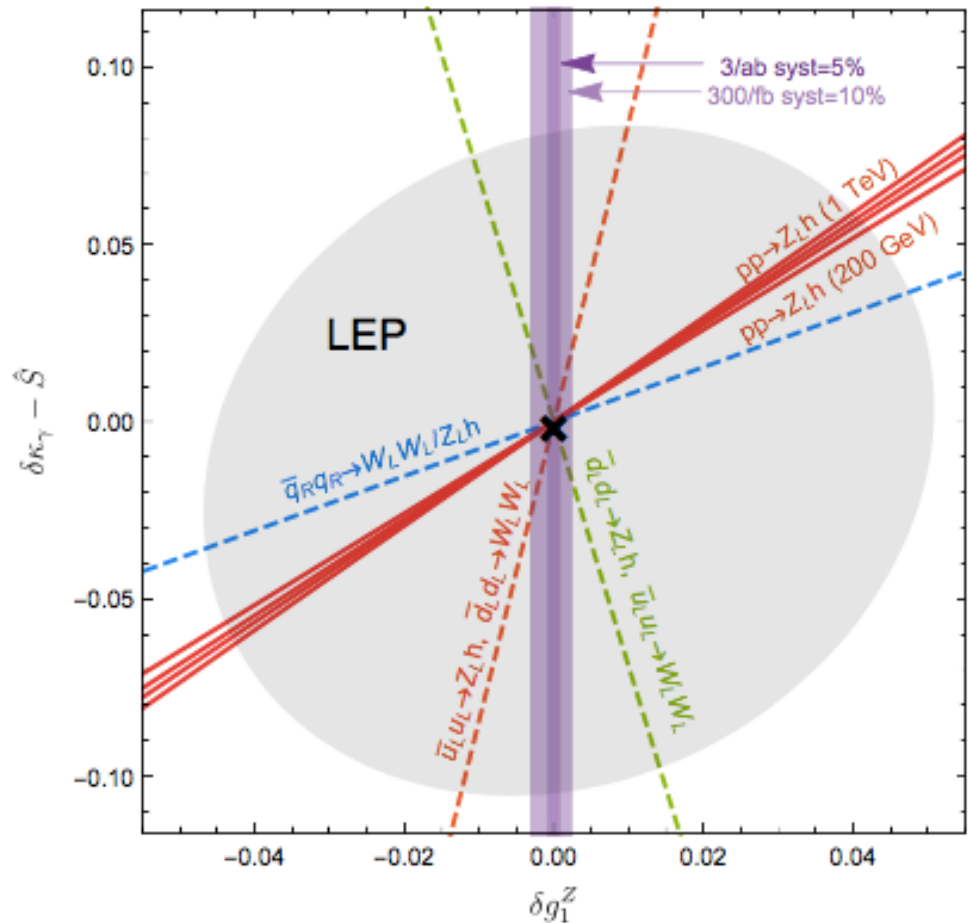
HV and *VV* processes amplitude connected by symmetry. They constrain the same set of observables at high energies

+ Diboson production at LHC

Four channels:

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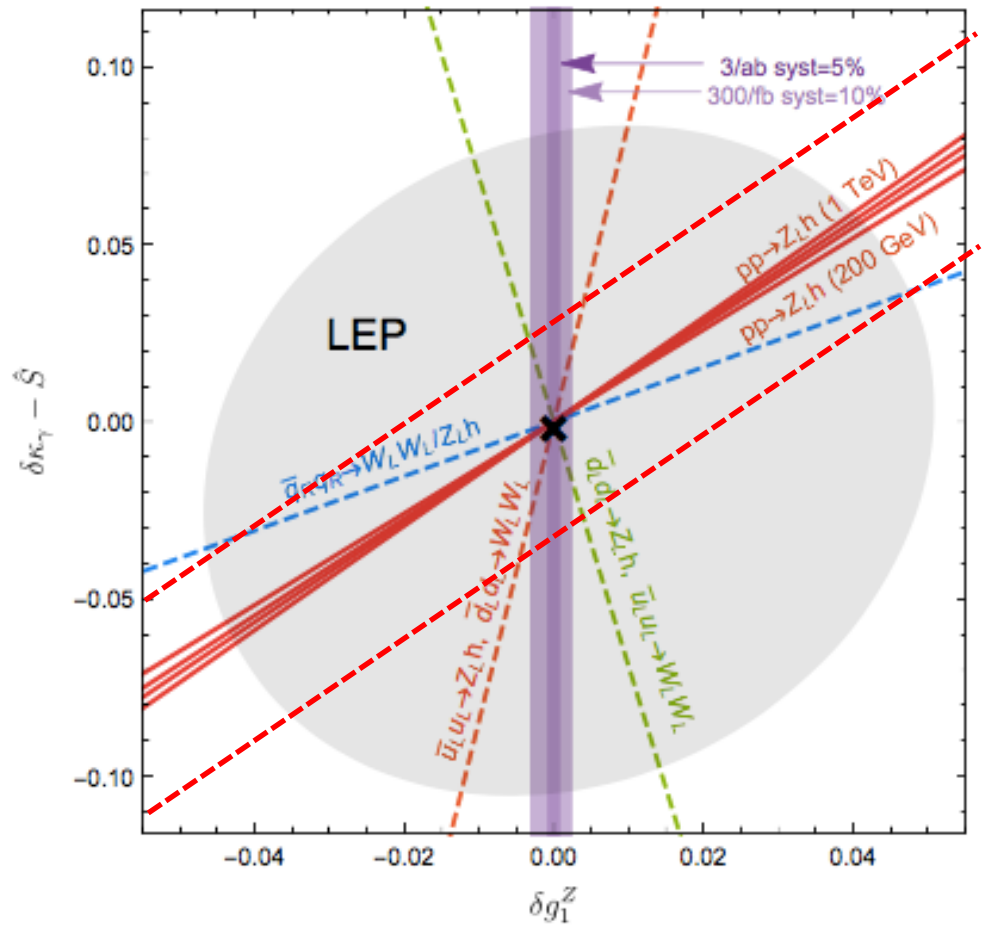
Franceschini, Panico, Pomarol, Riva & Wulzer
arxiv:712.01310

+ Diboson production at LHC

Four channels:

- $ZH \rightarrow G^0 H$
- $WH \rightarrow G^+ H$
- $WW \rightarrow G^+ G^-$
- $WZ \rightarrow G^+ G^0$

Our study $pp \rightarrow ZH(bb)$ constrains a complementary direction in the same plane.



+ Part II: RG-induced constraints



+ RG-induced Constraints (diphoton example)



BSM matching scale Λ

$c_1(\Lambda), c_2(\Lambda), \dots, c_i(\Lambda)$

Theoretically important;
To constrain these need to
know RG running.

RG running and mixing

for eg. take the diphoton operator:

$$\hat{c}_{\gamma\gamma}(m_h) = \hat{c}_{\gamma\gamma}(\Lambda) - \frac{1}{16\pi^2} \left[\left(\frac{3}{2}g^2 - 2\lambda \right) \hat{c}_{\kappa\gamma} + 3g^2 \hat{c}_{\lambda\gamma} \right] \log \left(\frac{\Lambda}{m_h} \right) < \epsilon_{h\gamma\gamma}$$

$c_1(m_W), c_2(m_W), \dots, c_i(m_W)$

**Directly constrained by
experiments**

Experimental Observable scale $m_H \sim m_W$

Jenkins, Grojean, Manohar, Trott (2013)

Elias-Miro, Espinosa, Masso, Pomarol (2013)



- But aren't these effects one loop suppressed and thus unimportant ?

+ RG-induced Constraints (diphoton example)



$$\hat{c}_{\gamma\gamma}(m_h) = \hat{c}_{\gamma\gamma}(\Lambda) - \frac{1}{16\pi^2} \left[\left(\frac{3}{2}g^2 - 2\lambda \right) \hat{c}_{\kappa\gamma} + 3g^2 \hat{c}_{\lambda\gamma} \right] \log \left(\frac{\Lambda}{m_h} \right) < \epsilon_{h\gamma\gamma}$$

One loop suppression

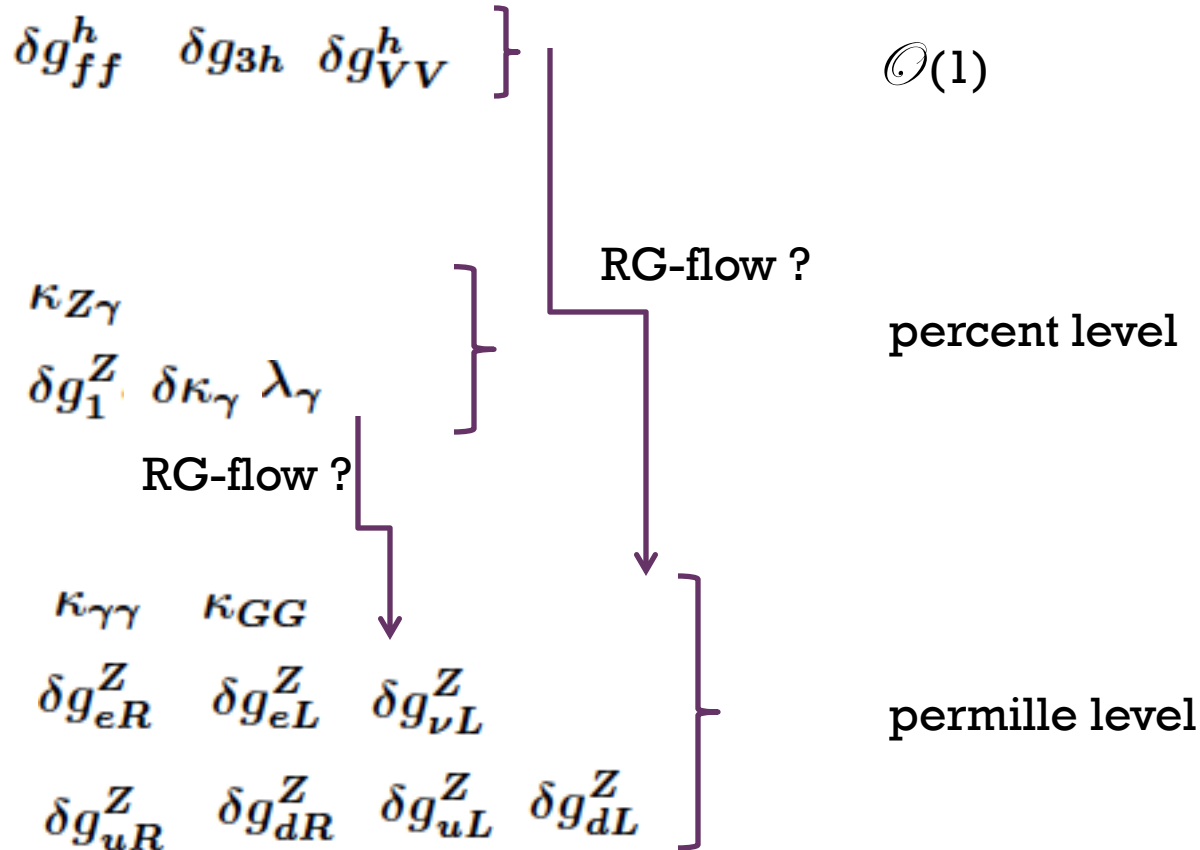
Constrained **per mille** level

Assuming **no tuning/correlation** between the RHS contributions we derive **RG-induced bounds**:

Constrained only at 10 % level thus allowed to be much larger than bound on $h\gamma\gamma$. This and the log enhancement can compensate for the loop factor.

$$|\hat{c}_{\kappa\gamma}| < \Delta_{FT} \frac{16\pi^2}{\log(\Lambda/m_h)} \left| \left(\frac{3}{2}g^2 - 2\lambda \right)^{-1} \right| \epsilon_{h\gamma\gamma}, \quad |\hat{c}_{\lambda\gamma}| < \Delta_{FT} \frac{16\pi^2}{\log(\Lambda/m_h)} \left| \frac{1}{3g^2} \right| \epsilon_{h\gamma\gamma}$$

+ A Hierarchy of Constraints



These parameters can be identified with the Wilson coefficients of dim-6 operators c_i (mw).



Anomalous Dimensional Matrix

Elias-Miro, Grojean, Gupta and Marzocca (1312.2928)

	\hat{c}_S	\hat{c}_T	\hat{c}_Y	\hat{c}_W	$\hat{c}_{\gamma\gamma}$
$\gamma_{\hat{c}_S}$	$\frac{1}{3}g'^2 + 6y_t^2$	$-\frac{g^2}{2}$	$\frac{1}{8}g'^2 \left(147 - 106\frac{g'^2}{g^2}\right)$	$\frac{1}{8}(77g^2 + 58g'^2)$	$16e^2$
$\gamma_{\hat{c}_T}$	$-9g'^2 - 24t_{\theta_W}^2 \lambda$	$\frac{9}{2}g^2 + 12y_t^2 + 12\lambda$	$\frac{9}{2}g'^2 + 12t_{\theta_W}^2(g'^2 + \lambda)$	$\frac{9}{2}g'^2$	0
$\gamma_{\hat{c}_Y}$	$-\frac{2}{3}g'^2$	0	$\frac{94}{3}g'^2$	0	0
$\gamma_{\hat{c}_W}$	0	0	$\frac{53}{12}g'^2 \left(1 - 3t_{\theta_W}^2\right)$	$\frac{331}{12}g^2 + \frac{29}{4}g'^2$	0
$\gamma_{\hat{c}_{\gamma\gamma}}$	0	0	0	0	$-\frac{9}{2}g^2 - \frac{3}{2}g'^2 + 6y_t^2 + 12\lambda$
$\gamma_{\hat{c}_{\theta_W}}$	$18g'^2 - t_{\theta_W}^2(9g'^2 + 24\lambda)$	$-9g^2 + \frac{9}{2}g'^2 + 12\lambda$	$t_{\theta_W}^2 \left(-\frac{141}{4}g'^2 + 12\lambda\right)$	$\frac{63}{2}g^2 + \frac{51}{4}g'^2 + 72\lambda$	0
$\gamma_{\hat{c}_{\gamma Z}}$	0	0	0	0	0
$\gamma_{\hat{c}_{kZ}}$	0	0	0	0	$-16e^2$
$\gamma_{\hat{c}_{gZ}}$	$-\frac{g^2}{6c_{\theta_W}^2}$	$\frac{g^2}{12c_{\theta_W}^2}$	$\frac{g^2}{8c_{\theta_W}^2}(106t_{\theta_W}^2 - 29)$	$-\frac{1}{8c_{\theta_W}^2}(79g^2 + 58g'^2)$	0
$\gamma_{\hat{c}_{\lambda\gamma}}$	0	0	0	0	0

	\hat{c}_H	$\hat{c}_{\gamma Z}$	$\hat{c}_{\kappa\gamma}$	\hat{c}_{gZ}	$\hat{c}_{\lambda\gamma}$
$\gamma_{\hat{c}_S}$	$-\frac{1}{6}g'^2$	$4(g^2 - g'^2)$	$-\frac{11}{2}g^2 - \frac{1}{6}g'^2 - 4\lambda$	$c_{\theta_W}^2 \left(9g^2 - \frac{1}{3}g'^2\right)$	$-2g^2$
$\gamma_{\hat{c}_T}$	$\frac{3}{2}g'^2$	0	$-9g'^2 - 24t_{\theta_W}^2 \lambda$	$24s_{\theta_W}^2 \lambda$	0
$\gamma_{\hat{c}_Y}$	0	0	$-\frac{2}{3}g'^2$	$\frac{2}{3}e^2$	0
$\gamma_{\hat{c}_W}$	0	0	0	$-\frac{2}{3}c_{\theta_W}^2 g^2$	0
$\gamma_{\hat{c}_{\gamma\gamma}}$	0	0	$\frac{3}{2}g^2 - 2\lambda$	0	$3g^2$
$\gamma_{\hat{c}_{\theta_W}}$	$-\frac{9}{2}g^2 - 3g'^2 + 12y_t^2 + 24\lambda$	0	$9g'^2(2 - t_{\theta_W}^2) - 24t_{\theta_W}^2 \lambda$	$9(g'^2 s_{\theta_W}^2 - g^2 c_{\theta_W}^2) - 24\lambda(6c_{\theta_W}^2 - s_{\theta_W}^2)$	0
$\gamma_{\hat{c}_{\gamma Z}}$	0	$-\frac{7}{2}g^2 - \frac{1}{2}g'^2 + 6y_t^2 + 12\lambda$	$c_{\theta_W}^2(2g^2 - 2\lambda) - s_{\theta_W}^2(g^2 - 2\lambda)$	0	$\frac{g^2}{2}(11c_{\theta_W}^2 - s_{\theta_W}^2)$
$\gamma_{\hat{c}_{\kappa\gamma}}$	0	$4(g^2 - g'^2)$	$\frac{11}{2}g^2 + \frac{g'^2}{2} + 6y_t^2 + 4\lambda$	0	$2g^2$
$\gamma_{\hat{c}_{gZ}}$	$\frac{g^2}{12c_{\theta_W}^2}$	0	$\frac{g^2}{6c_{\theta_W}^2}$	$\frac{17}{2}g^2 - \frac{g'^2}{6} + 6y_t^2$	0
$\gamma_{\hat{c}_{\lambda\gamma}}$	0	0	0	0	$\frac{53}{3}g^2$

+

Anomalous Dimensional Matrix

$$(\hat{c}_S, \hat{c}_T, \hat{c}_Y, \hat{c}_W, \hat{c}_{\gamma\gamma}, \hat{c}_{\gamma Z}, \hat{c}_{\kappa\gamma}, \hat{c}_{gz}, \hat{c}_{\lambda\gamma}, \hat{c}_H)^t (m_t) \simeq \quad (4)$$

$$\begin{array}{c}
 |Z \\
 \left(\begin{array}{cccccc}
 0.9 & 0.003 & -0.03 & -0.08 & -0.02 & -0.02 & -0.04 & 0.05 & -0.01 & 0.001 \\
 0.03 & 0.8 & -0.02 & -0.009 & 0 & 0 & -0.03 & 0.01 & 0 & -0.003 \\
 0.001 & 0 & 0.9 & 0 & 0 & 0 & -0.001 & 0.001 & 0 & 0 \\
 0 & 0 & -0.001 & 0.8 & 0 & 0 & 0 & -0.003 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0.9 & 0 & 0.006 & 0 & 0.02 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0.9 & 0.007 & 0 & 0.03 & 0 \\
 0 & 0 & 0 & 0 & -0.02 & -0.02 & 0.9 & 0 & -0.01 & 0 \\
 0.0004 & -0.0007 & -0.0004 & 0.1 & 0 & 0 & -0.0004 & 0.9 & 0 & -0.0007 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.9 & 0 \\
 -0.02 & 0.03 & 0.01 & -0.4 & 0 & 0 & 0.02 & -0.3 & 0 & 0.8
 \end{array} \right)
 \begin{array}{c}
 \hat{c}_S(\Lambda) \\
 \hat{c}_T(\Lambda) \\
 \hat{c}_Y(\Lambda) \\
 \hat{c}_W(\Lambda) \\
 \hat{c}_{\gamma\gamma}(\Lambda) \\
 \hat{c}_{\gamma Z}(\Lambda) \\
 \hat{c}_{\kappa\gamma}(\Lambda) \\
 \hat{c}_{gz}(\Lambda) \\
 \hat{c}_{\lambda\gamma}(\Lambda) \\
 \hat{c}_H(\Lambda)
 \end{array}
 \end{array}$$

- We focus on the part of the matrix, where **weakly bound couplings contribute to strongly bound couplings.**

+ Numerical Results

Coupling	Direct Constraint	RG-induced Constraint
$\hat{c}_S(m_t)$	$[-1, 2] \times 10^{-3}$ [31]	-
$\hat{c}_T(m_t)$	$[-1, 2] \times 10^{-3}$ [31]	-
$\hat{c}_Y(m_t)$	$[-3, 3] \times 10^{-3}$ [22]	-
$\hat{c}_W(m_t)$	$[-2, 2] \times 10^{-3}$ [22]	-
$\hat{c}_{\gamma\gamma}(m_t)$	$[-1, 2] \times 10^{-3}$ [18]	-
$\hat{c}_{\gamma Z}(m_t)$	$[-0.6, 1] \times 10^{-2}$ [18]	$[-2, 6] \times 10^{-2}$
$\hat{c}_{\kappa\gamma}(m_t)$	$[-10, 7] \times 10^{-2}$ [27]	$[-5, 2] \times 10^{-2}$
$\hat{c}_{gZ}(m_t)$	$[-4, 2] \times 10^{-2}$ [27]	$[-3, 1] \times 10^{-2}$
$\hat{c}_{\lambda\gamma}(m_t)$	$[-6, 2] \times 10^{-2}$ [27]	$[-2, 8] \times 10^{-2}$
$\hat{c}_H(m_t)$	$[-6, 5] \times 10^{-1}$ [32]	$[-2, 0.5] \times 10^{-1}$

- We assume that there is **no tuning** so that **each RG-induced** term in the RGE is **smaller than the bound**. This gives us new **RG-induced constraints**.
- We get bounds on some **TGC** and on **C_H** mainly from their RG-induced contribution to **{S, T, W, Y}** that are **stronger** than the direct bounds.

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+ Part IV: Explicit Models



- We consider expectations for BSM primary effects in two models:

(1) Composite Models

Giudice, Grojean, Pomarol and Rattazzi (2007)

(2) Integrating out Higgses in SUSY Models

Gupta, Montull, Riva (2012)

+ Composite Models

- **Strongly Interacting Light Higgs (SILH)** Lagrangian:

$$\begin{aligned}\mathcal{L}_{\text{SILH}} = & \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) \\ & - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left(\frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right) \\ & + \frac{ic_W g}{2m_\rho^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{ic_B g'}{2m_\rho^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu}) \\ & + \frac{ic_{HW} g}{16\pi^2 f^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{ic_{HB} g'}{16\pi^2 f^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{c_\gamma g'^2}{16\pi^2 f^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{16\pi^2 f^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}.\end{aligned}$$

(assumes **Higgs is a pseudo Nambu Goldstone Boson** of a strong sector)

+ Composite Models

$$\left. \begin{matrix} \delta g_{ff}^h & \delta g_{3h} \end{matrix} \right\}$$

$\mathcal{O}(1)$

$$\frac{g_*^2}{\Lambda^2}$$

$$\left. \begin{matrix} \kappa_{Z\gamma} & \delta g_{VV}^h \\ \delta g_1^Z & \delta \kappa_\gamma & \lambda_\gamma \end{matrix} \right\}$$

percent level
Strong RG-induced
constraint from S, T

$$\frac{1}{\Lambda^2}$$

$$\frac{g_*^2}{16\pi^2 \Lambda^2}$$

$$\left. \begin{matrix} \kappa_{\gamma\gamma} & \kappa_{GG} \\ \delta g_{eR}^Z & \delta g_{eL}^Z & \delta g_{\nu L}^Z \\ \delta g_{uR}^Z & \delta g_{dR}^Z & \delta g_{uL}^Z & \delta g_{dL}^Z \end{matrix} \right\}$$

permille level

$$\frac{g_{SM}^2}{16\pi^2 \Lambda^2}$$

$$\hat{S} \quad \hat{T}$$



+ Composite Models

$$\left. \begin{matrix} \delta g_{ff}^h & \delta g_{3h} \end{matrix} \right\}$$

$\mathcal{O}(1)$

$$\frac{g_*^2}{\Lambda^2}$$

$$\left. \begin{matrix} \kappa_{Z\gamma} & \delta g_{VV}^h \\ \delta g_1^Z & \delta \kappa_\gamma & \lambda_\gamma \end{matrix} \right\}$$

percent level

$$\frac{1}{\Lambda^2}$$

Strong RG-induced constraint from S, T

$$\left. \begin{matrix} \kappa_{\gamma\gamma} & \kappa_{GG} \\ \delta g_{eR}^Z & \delta g_{eL}^Z & \delta g_{\nu L}^Z \\ \delta g_{uR}^Z & \delta g_{dR}^Z & \delta g_{uL}^Z & \delta g_{dL}^Z \end{matrix} \right\}$$

permille level

$$\frac{g_*^2}{16\pi^2 \Lambda^2}$$

$$\frac{g_{SM}^2}{16\pi^2 \Lambda^2}$$

$$\hat{S} \quad \hat{T}$$



+ Composite Models

$$\left. \begin{array}{|c|} \hline \delta g_{ff}^h \quad \delta g_{3h} \\ \hline \end{array} \right\}$$

$\mathcal{O}(1)$

$$\frac{g_*^2}{\Lambda^2}$$

$$\left. \begin{array}{|c|} \hline \kappa_{Z\gamma} \quad \delta g_{VV}^h \\ \hline \delta g_1^Z \quad \delta \kappa_\gamma \quad \lambda_\gamma \\ \hline \end{array} \right\}$$

percent level

$$\frac{1}{\Lambda^2}$$

Strong RG-induced constraint from S, T

$$\left. \begin{array}{|c|} \hline \kappa_{\gamma\gamma} \quad \kappa_{GG} \\ \hline \delta g_{eR}^Z \quad \delta g_{eL}^Z \quad \delta g_{\nu L}^Z \\ \delta g_{uR}^Z \quad \delta g_{dR}^Z \quad \delta g_{uL}^Z \quad \delta g_{dL}^Z \\ \hline \end{array} \right\}$$

permille level

$$\frac{g_*^2}{16\pi^2 \Lambda^2}$$

$$\frac{g_{SM}^2}{16\pi^2 \Lambda^2}$$

$$\hat{S} \quad \hat{T}$$

+ Composite Models

$$\left. \begin{array}{cc} \delta g_{ff}^h & \delta g_{3h} \end{array} \right\}$$

$\mathcal{O}(1)$

$$\frac{g_*^2}{\Lambda^2}$$

Left-right symmetry

$$\left. \begin{array}{ccc} \kappa_{Z\gamma} & \delta g_{VV}^h & \\ \delta g_1^Z & \delta \kappa_\gamma & \lambda_\gamma \end{array} \right\}$$

percent level

$$\frac{1}{\Lambda^2}$$

Strong RG-induced constraint from S, T

$$\left. \begin{array}{ccc} \kappa_{\gamma\gamma} & \kappa_{GG} & \\ \delta g_{eR}^Z & \delta g_{eL}^Z & \delta g_{\nu L}^Z \\ \delta g_{uR}^Z & \delta g_{dR}^Z & \delta g_{uL}^Z & \delta g_{dL}^Z \end{array} \right\}$$

permille level

$$\frac{g_*^2}{16\pi^2 \Lambda^2}$$

$$\frac{g_{SM}^2}{16\pi^2 \Lambda^2}$$

$$\hat{S}$$

$$\hat{T}$$

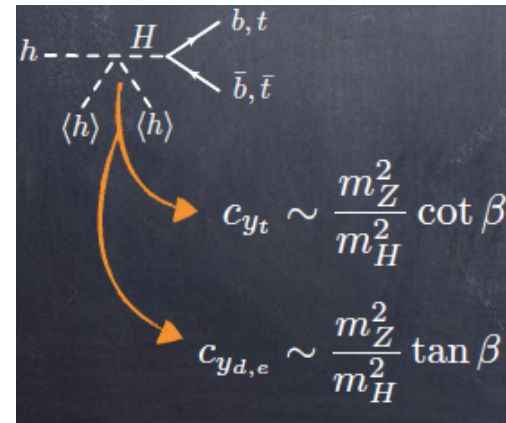
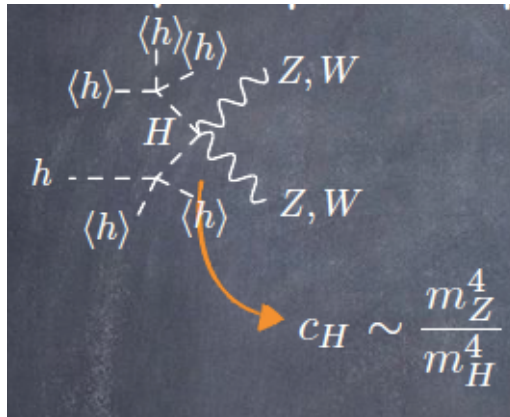
Custodial symmetry



+

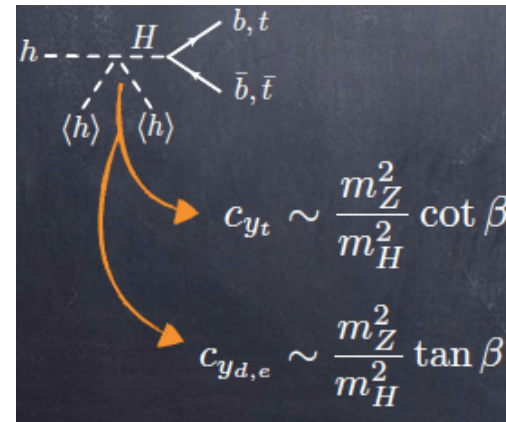
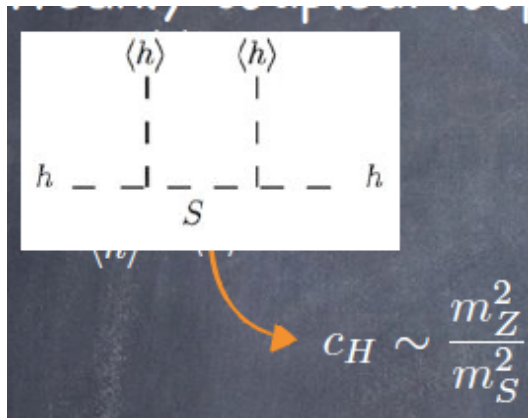
Integrating out heavy Higgses in SUSY

■ Supersymmetric models (2HDMS)



■ NMSSM

(\mathcal{O}_6 also generated)



+ Integrating out heavy Higgses in SUSY

2HDM: $\left. \begin{matrix} \delta g_{ff}^h & \delta g_{3h} \end{matrix} \right\} \mathcal{O}(1)$

$$\left. \begin{matrix} \kappa_{Z\gamma} & \delta g_{VV}^h \\ \delta g_1^Z & \delta \kappa_\gamma & \lambda_\gamma \end{matrix} \right\}$$

$$\left. \begin{matrix} \underline{\kappa_{\gamma\gamma}} & \underline{\kappa_{GG}} \\ \delta g_{eR}^Z & \delta g_{eL}^Z & \delta g_{\nu L}^Z \\ \delta g_{uR}^Z & \delta g_{dR}^Z & \delta g_{uL}^Z & \delta g_{dL}^Z \end{matrix} \right\} \text{permille level}$$

+ Integrating out heavy Higgses in SUSY

NMSSM: $\left. \begin{array}{cc} \delta g_{ff}^h & \delta g_{3h} \end{array} \right\}$

$\mathcal{O}(1)$

$\left. \begin{array}{cc} \kappa_{Z\gamma} & \delta g_{VV}^h \\ \delta g_1^Z & \delta \kappa_\gamma \lambda_\gamma \end{array} \right\}$

percent level

$\left. \begin{array}{ccc} \underline{\kappa_{\gamma\gamma}} & \underline{\kappa_{GG}} & \\ \delta g_{eR}^Z & \delta g_{eL}^Z & \delta g_{\nu L}^Z \\ \delta g_{uR}^Z & \delta g_{dR}^Z & \delta g_{uL}^Z & \delta g_{dL}^Z \end{array} \right\}$

permille level



+ Understanding SUSY Higgs coupling deviations

- Write potential in terms of h and H , where:

$$\begin{aligned}h_1^0 &= \cos \beta h + \sin \beta H \\h_2^0 &= \sin \beta h - \cos \beta H\end{aligned}$$

gets full VEV

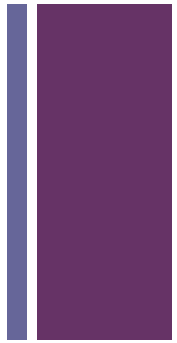
- H and h almost mass eigenstates if $\delta_i v^2 / m_H^2 \ll 1$
- h has exactly SM couplings as it gives mass to all the particles.

quartics

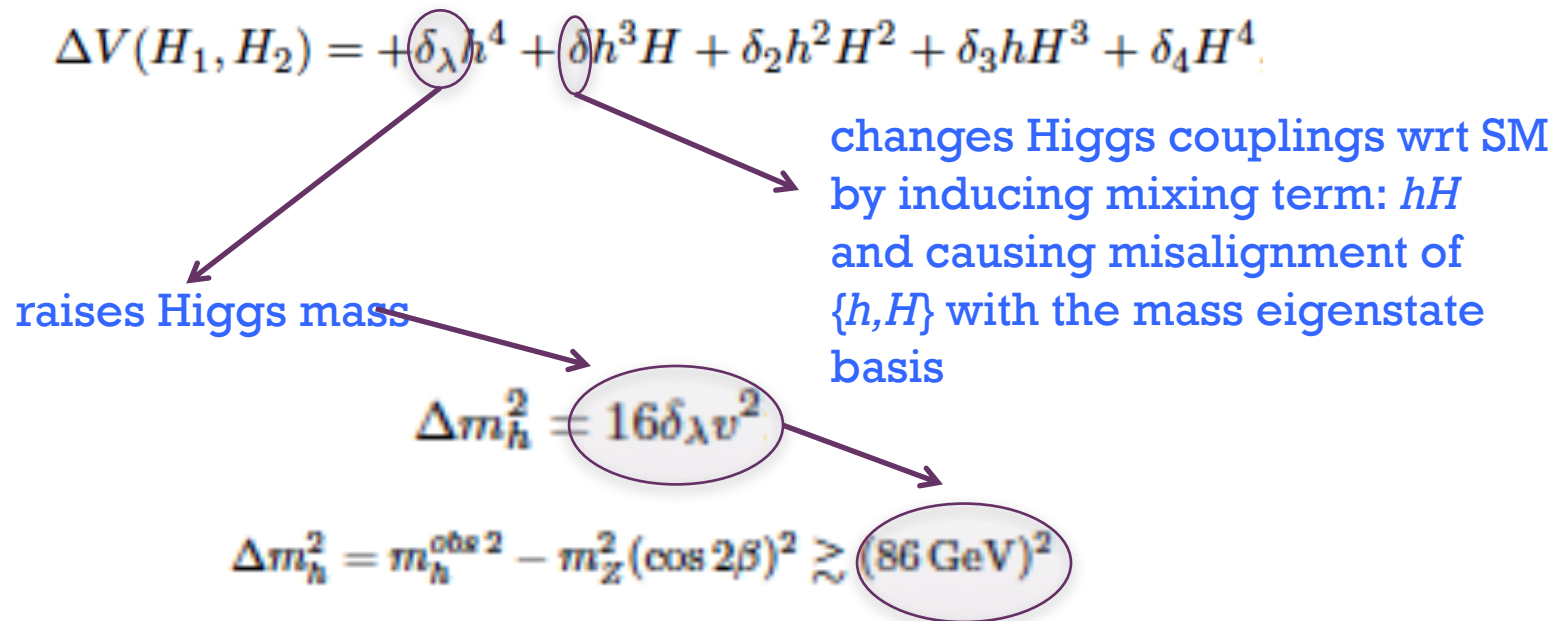


SUSY modifications to **raise the Higgs mass** would necessarily **change Higgs couplings** in a **correlated** way!

+ Understanding SUSY Higgs coupling deviations

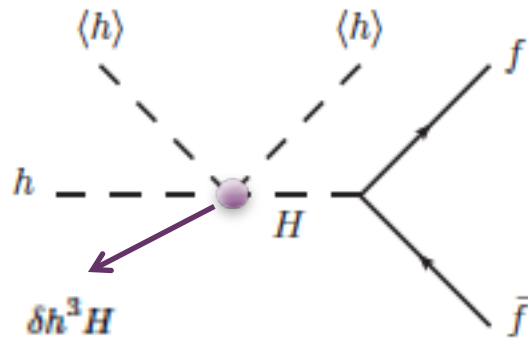


- As quartics are turned on the lightest mass eigenstate is no longer h and the misalignment causes deviations from SM couplings:



+ Understanding SUSY Higgs coupling deviations

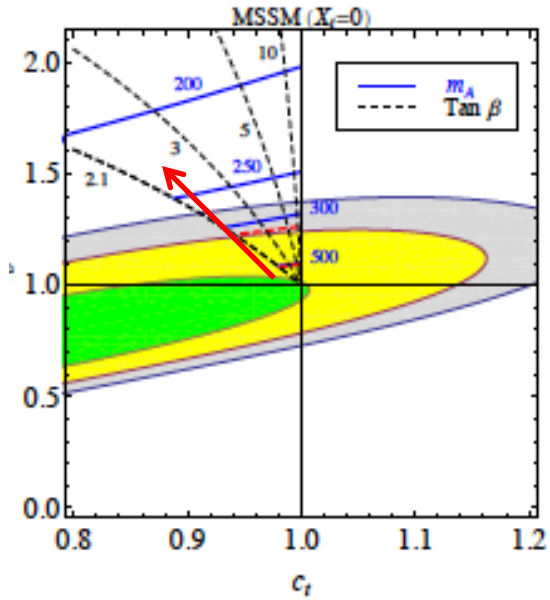
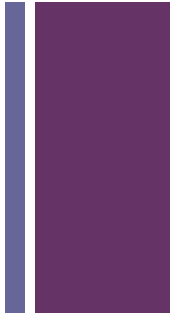
- Integrate out H to obtain:



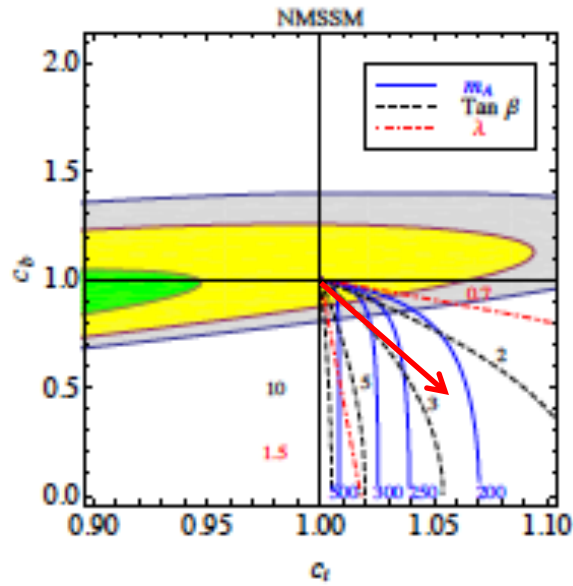
$$\begin{aligned}
 c_{b,\tau} &\approx 1 - 4 \tan \beta \delta \frac{v^2}{m_H^2} \\
 c_t &\approx 1 + 4 \cot \beta \delta \frac{v^2}{m_H^2} \\
 c_V &= 1 - \mathcal{O}\left(\delta^2 \frac{v^4}{m_H^4}\right)
 \end{aligned}$$

	ΔV	δ_λ	δ
MSSM	$\frac{g^2 + g'^2}{8} (H_1^0 ^2 - H_2^0 ^2)^2$	$\frac{m_Z^2}{16v^2} (c_\beta^2 - s_\beta^2)^2$	$\frac{m_Z^2}{2v^2} s_\beta c_\beta (c_\beta^2 - s_\beta^2)$
Stops (no mixing)	$\frac{\lambda}{2} H_2 ^4 = \frac{3y_t^4}{8\pi^2} \log[m_{\tilde{t}_1} m_{\tilde{t}_2} / M_t^2] H_2 ^4$	$s_\beta^4 \frac{\lambda_2}{8}$	$-4s_\beta^3 c_\beta \frac{\lambda_2}{8}$
D-term extension	$\kappa (H_1^0 ^2 - H_2^0 ^2)^2$	$\frac{m_Z^2}{16v^2} (c_\beta^2 - s_\beta^2)^2$	$\frac{m_Z^2}{2v^2} s_\beta c_\beta (c_\beta^2 - s_\beta^2)$
NMSSM	$\lambda^2 H_1^0 H_2^0 ^2$	$\frac{\lambda^2}{16} \sin^2 2\beta$	$-\frac{\lambda^2}{8} \sin 4\beta$

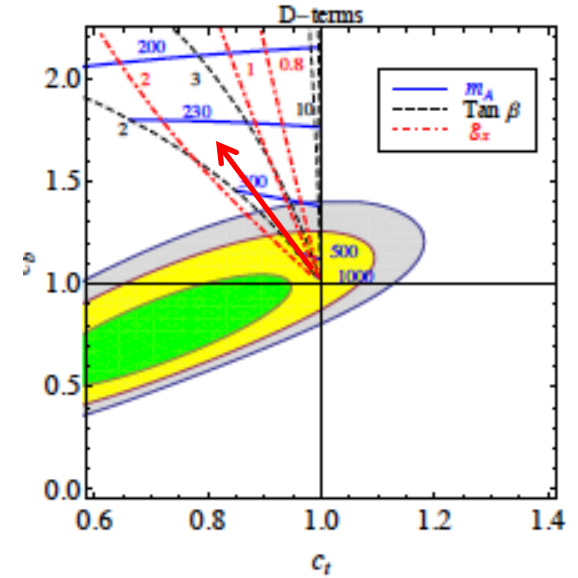
$$m_Z^2/v^2 \rightarrow 4\kappa.$$



MSSM
($\delta < 0$)



NMSSM
($\delta > 0$)



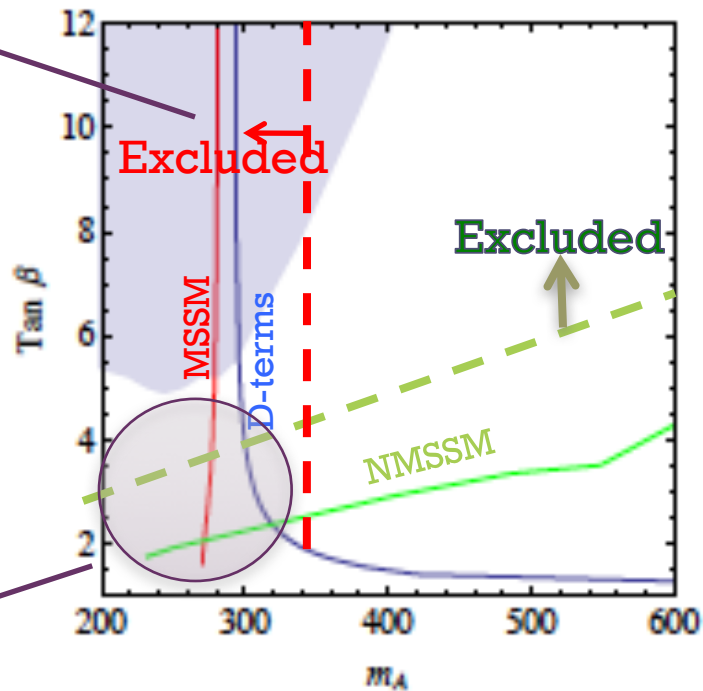
D-terms
($\delta < 0$)

- All qualitative features of the above plots can be understood using our expansion. Quantitatively it is approximate but works well if $m_A > 350$ GeV.

+ Exclusions



CMS H- \rightarrow $\tau\tau$



Higgs coupling data more competitive than direct searches in low $\tan \beta$ region

Dashed: Barbieri et al (2012)
with more recent data
Solid lines: our bounds

+ Summary

- We present an **efficient choice** of independent primary BSM deformations. All other deformations are generated in a correlated way and we derive these correlations.
- Using this approach we study the diboson process at high energies at LHC and show how it can beat LEP bounds
- We find that RG-induced constraints on the hVV and TGC primaries due to mixing with the $H\gamma\gamma$ and S -parameter primary directions can be stronger to (or of the same order as) tree level constraints.
- We show how Higgs coupling deviations can be used to infer the mechanism of raising Higgs mass in SUSY,