

# Jet substructure in heavy ion collisions



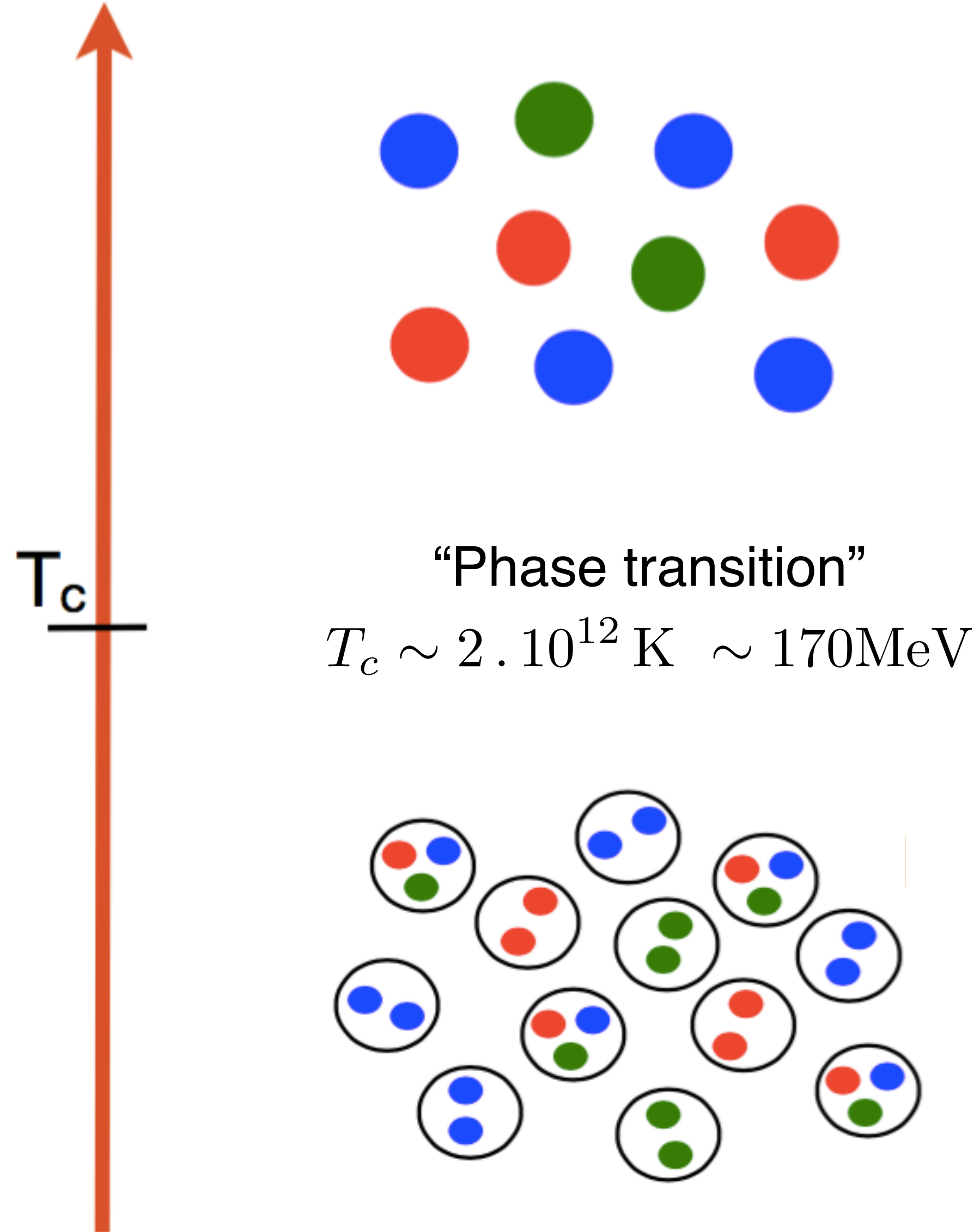
**Daniel Pablos**

Free Meson Seminar  
TIFR

15th October 2020



# QCD Matter



## A New Phase: Quark-Gluon Plasma

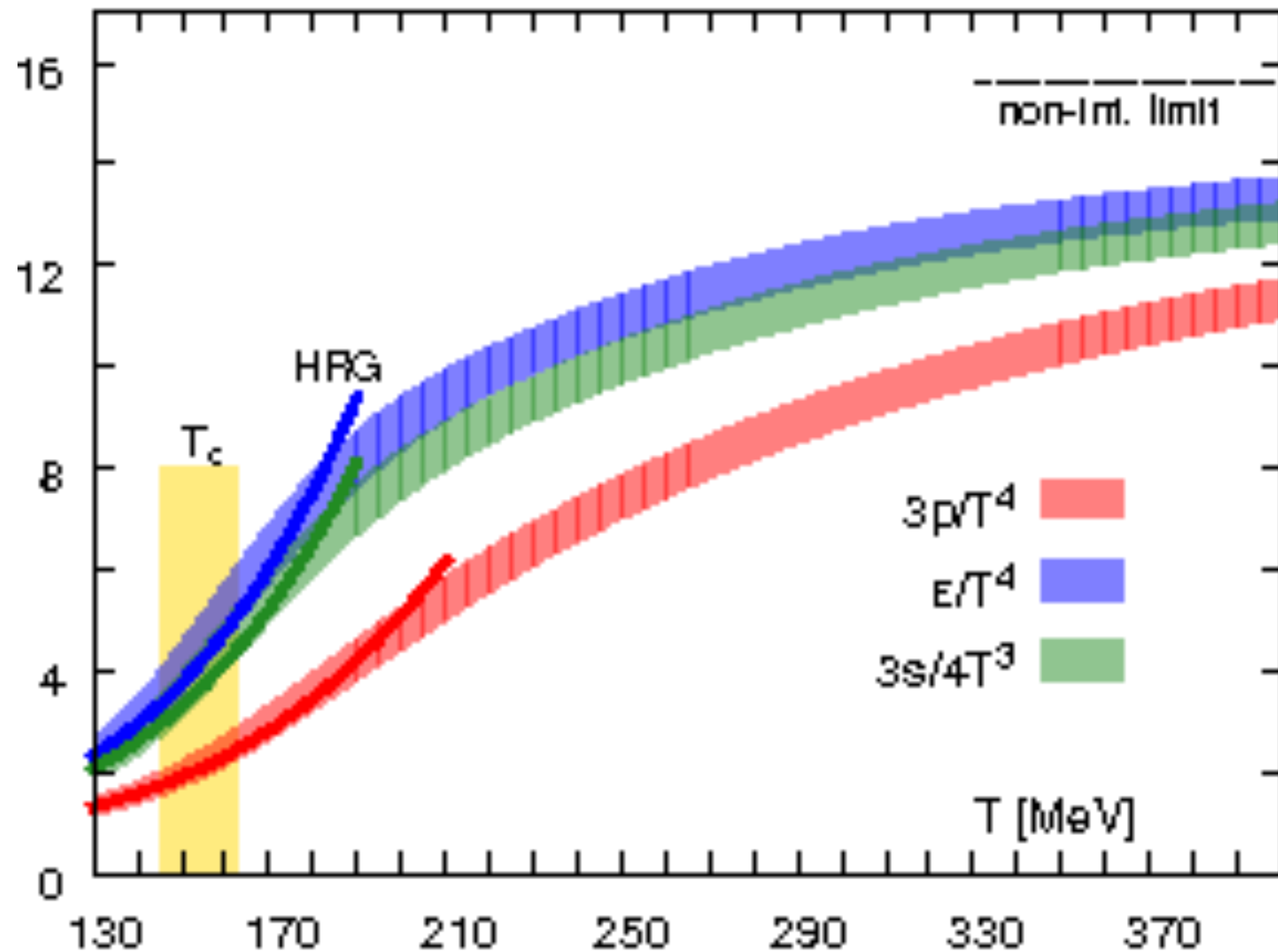
- Filled the universe  $\mu\text{s}$  after Big Bang
- Colour is liberated
- A gas of quarks and gluons

*What are the properties of the plasma close to the transition?*

## Hadron Gas

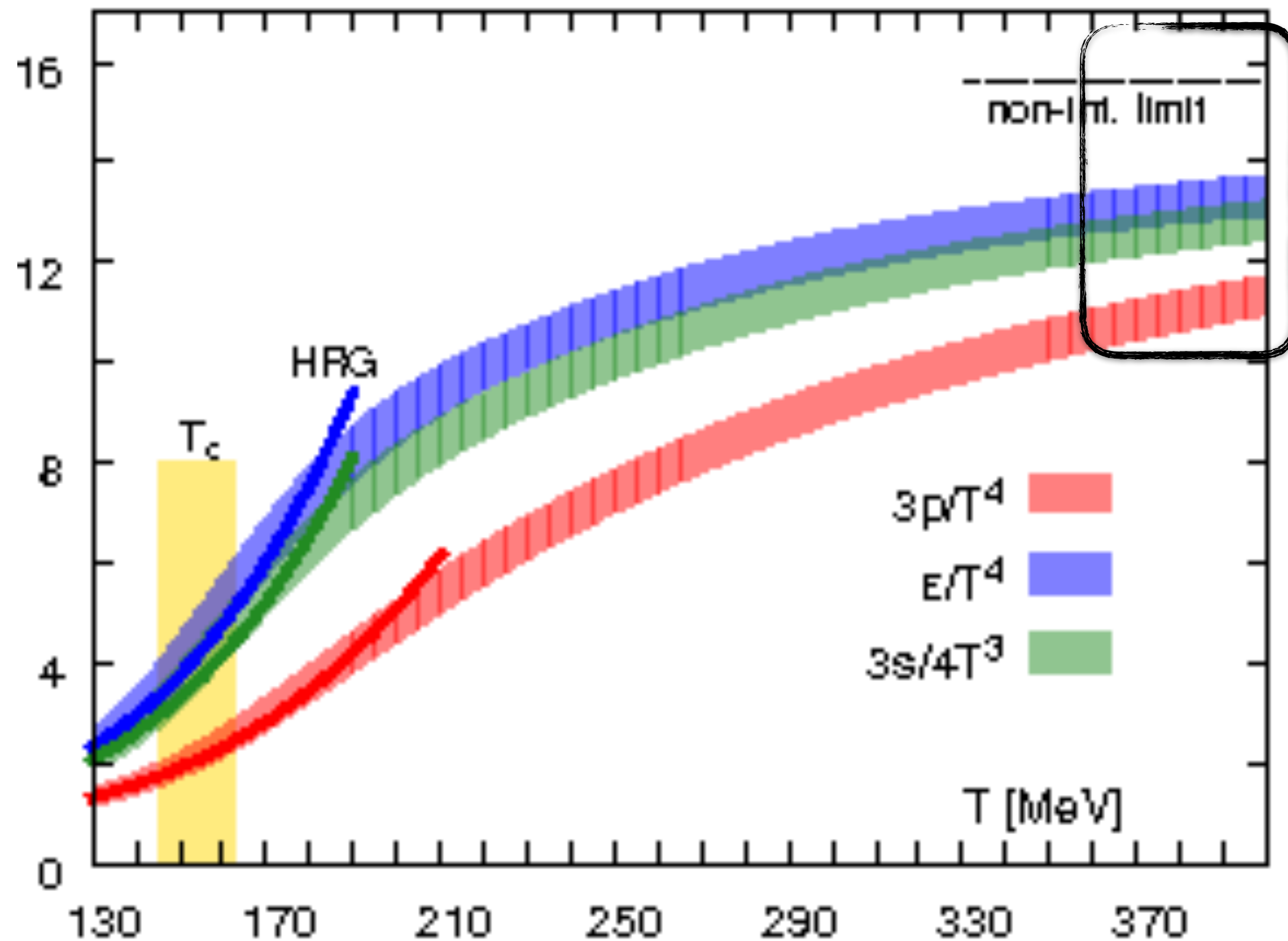
- Color is confined
- Hadrons re-scatter

# Equation of State



- Rapid crossover transition
- Deconfined matter: large increase in # d.o.f. above  $T_c$
- Asymptotically approaches non-int. limit

# Equation of State



Weakly coupled?

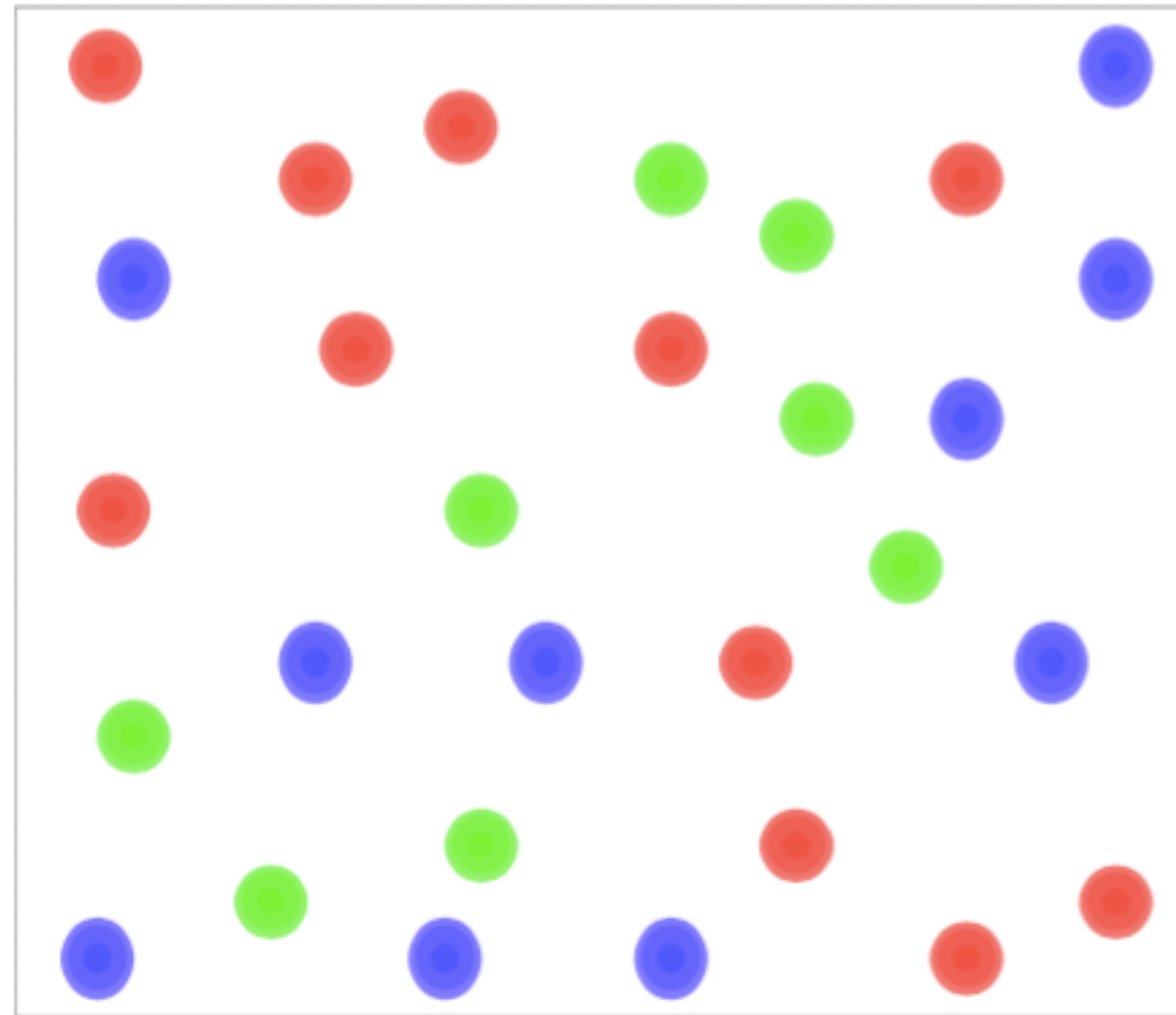
$$\frac{s_{\lambda=\infty}}{s_{\lambda=0}} = \frac{P_{\lambda=\infty}}{P_{\lambda=0}}$$

$$= \frac{\epsilon_{\lambda=\infty}}{\epsilon_{\lambda=0}} = \frac{3}{4} \quad \text{Poor indicator!}$$

- Rapid crossover transition
- Deconfined matter: large increase in # d.o.f. above  $T_c$
- Asymptotically approaches non-int. limit

# A Gas of Quarks and Gluons

$$T > 10^4 \text{ GeV}$$



$$\frac{1}{T}$$

$\ll$

$$\frac{1}{gT}$$

$\ll$

$$\frac{1}{g^2T}$$

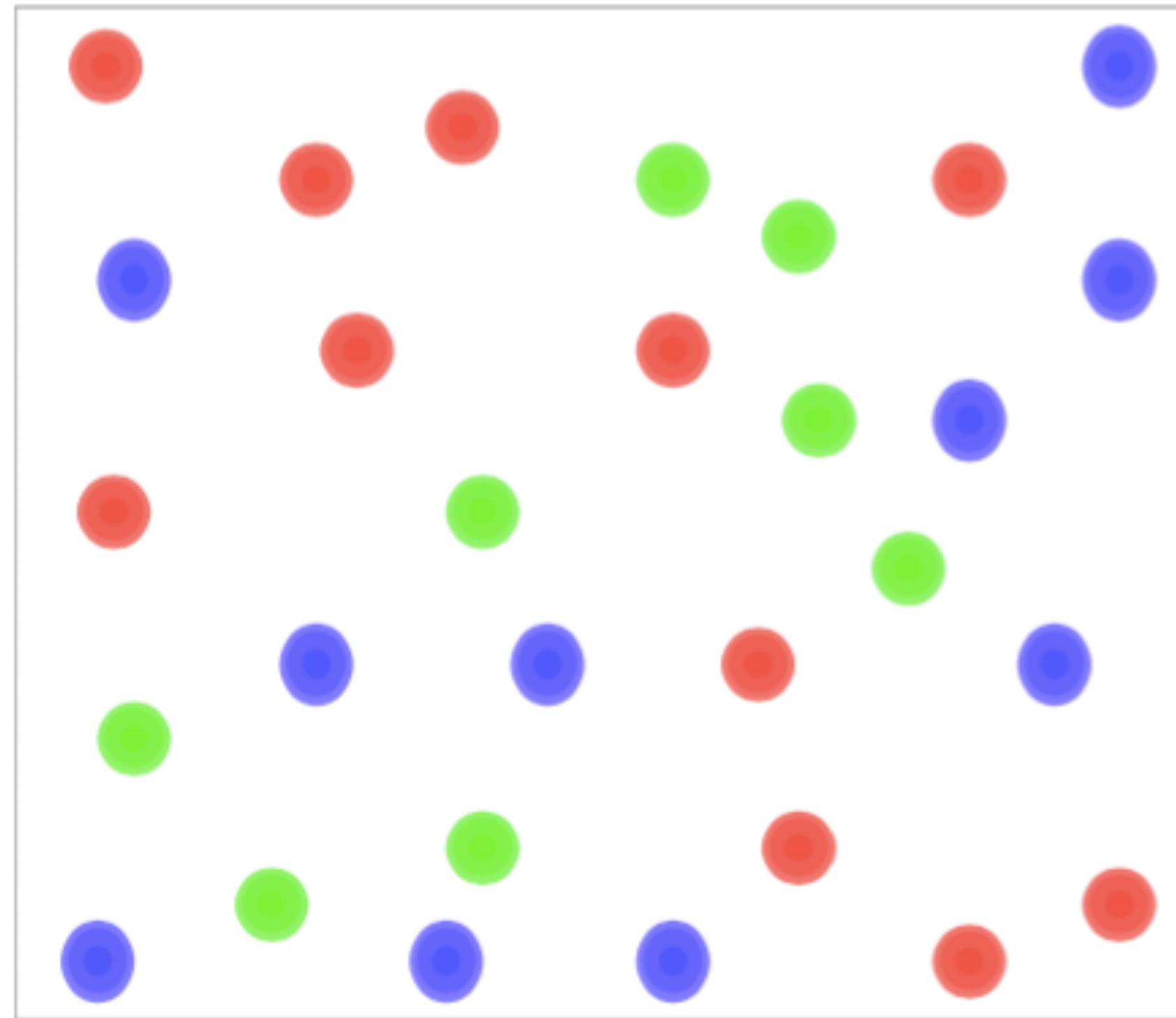
Inter-particle  
spacing

Interaction  
range

Mean free  
path

# A Gas of Quarks and Gluons

$$T > 10^4 \text{ GeV}$$



Resummation techniques can bring the validity of perturbative methods to much lower temperatures

$$\frac{1}{T}$$

$\ll$

$$\frac{1}{gT}$$

$\ll$

$$\frac{1}{g^2T}$$

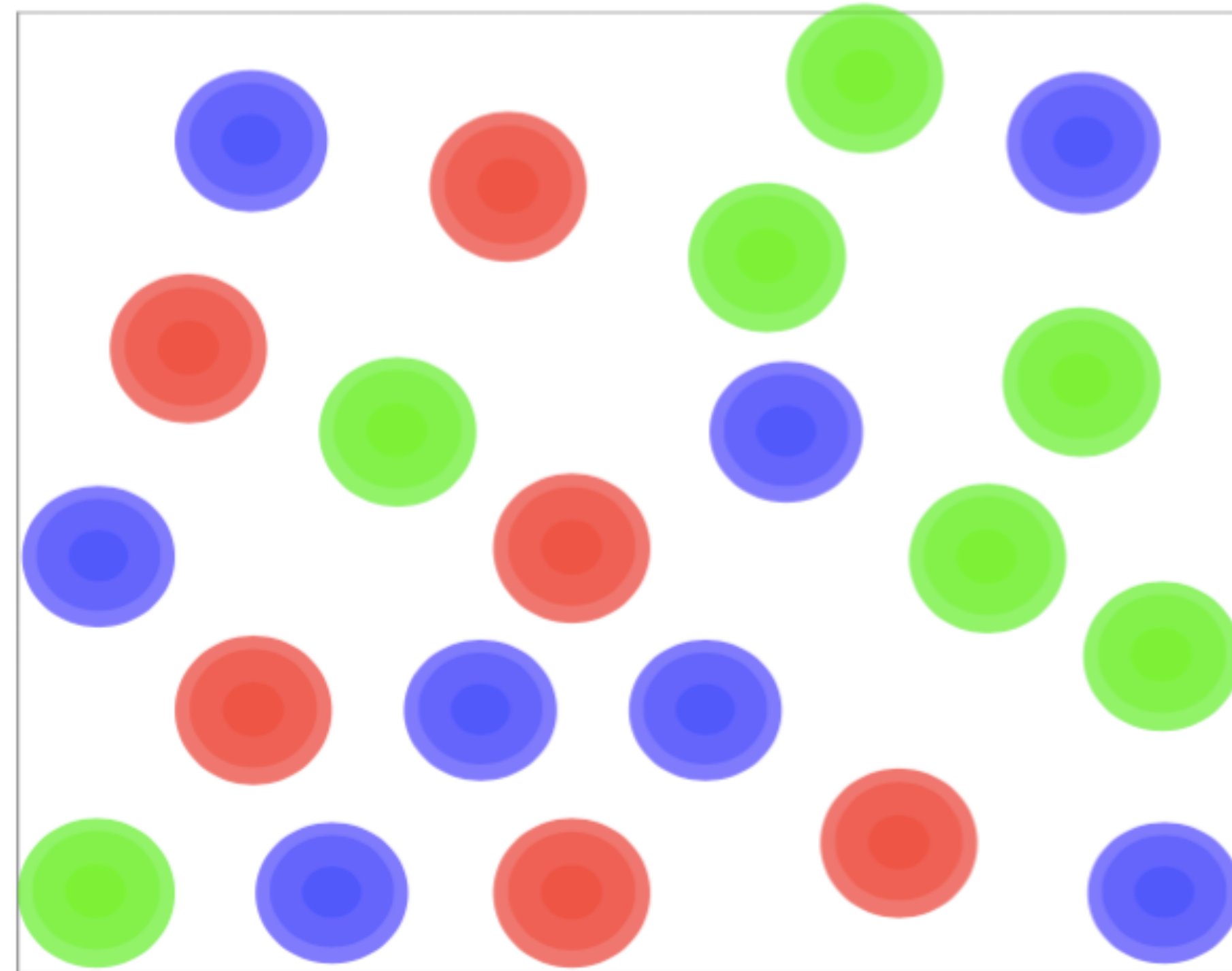
Inter-particle spacing

Interaction range

Mean free path

# Which is the correct picture of the plasma?

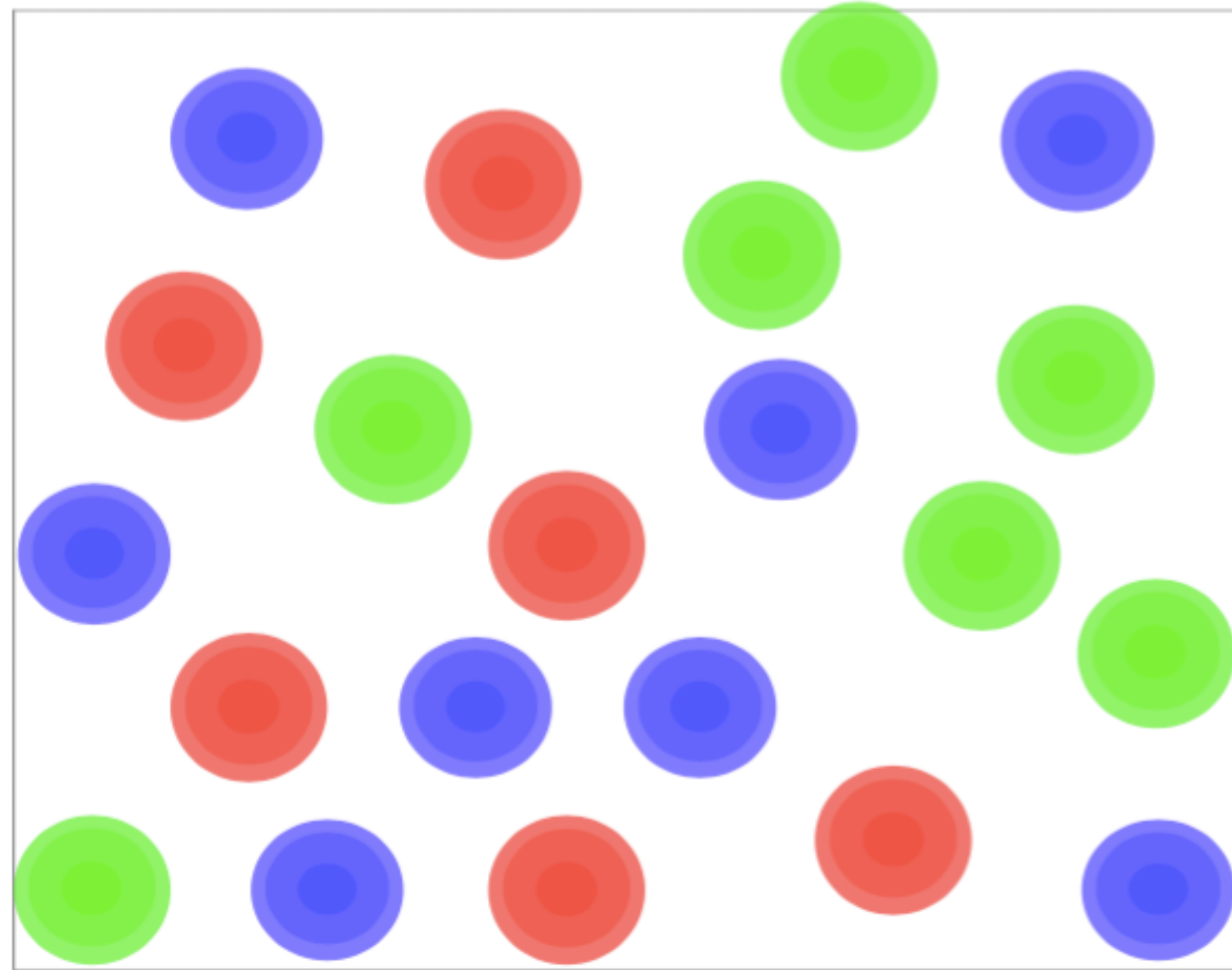
$T \sim 0.2 \text{ GeV}$



Is it a gas of quarks and gluons?

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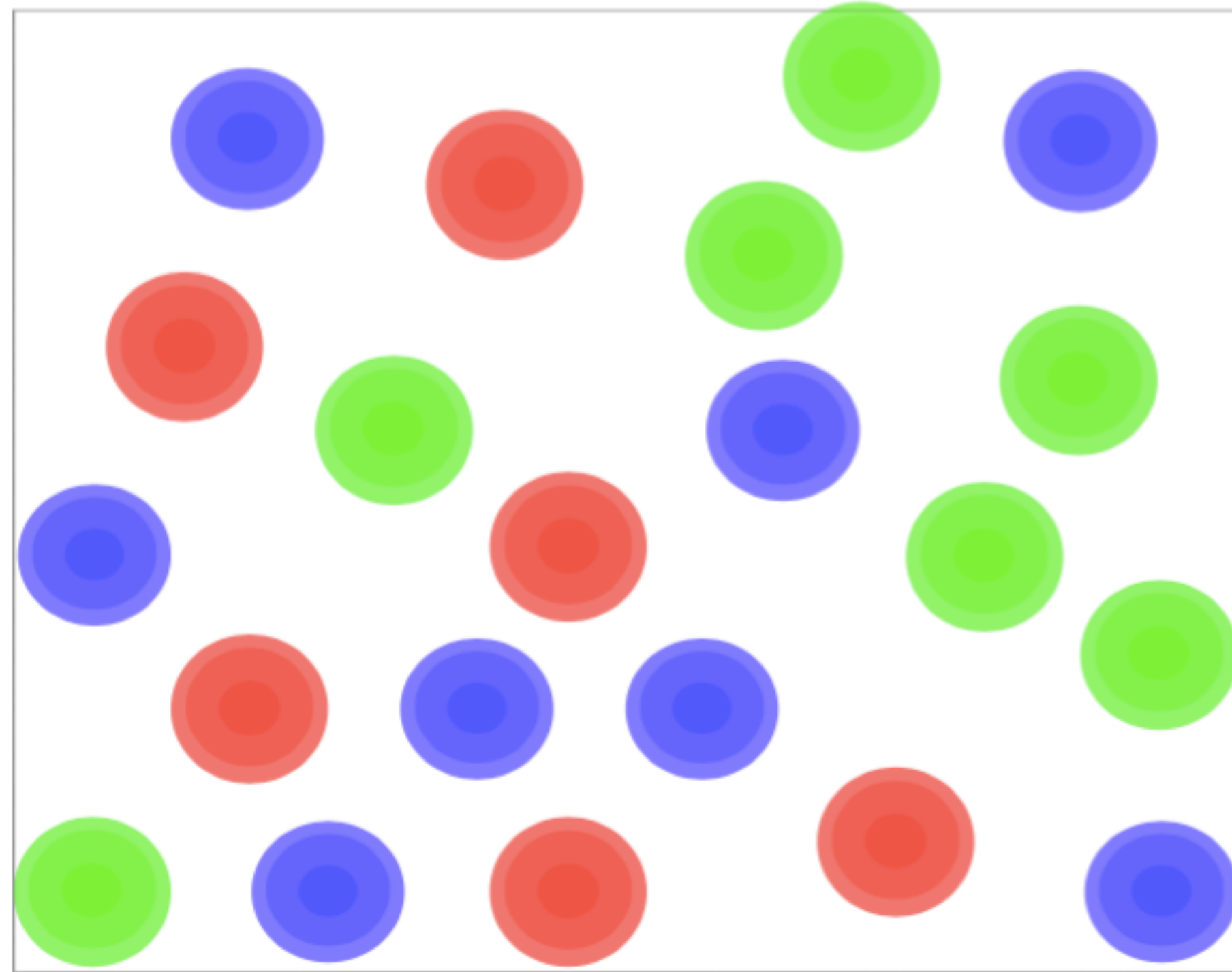
Is it a gas of quarks and gluons?

$$\alpha_s = 0.3 \rightarrow g = 2$$



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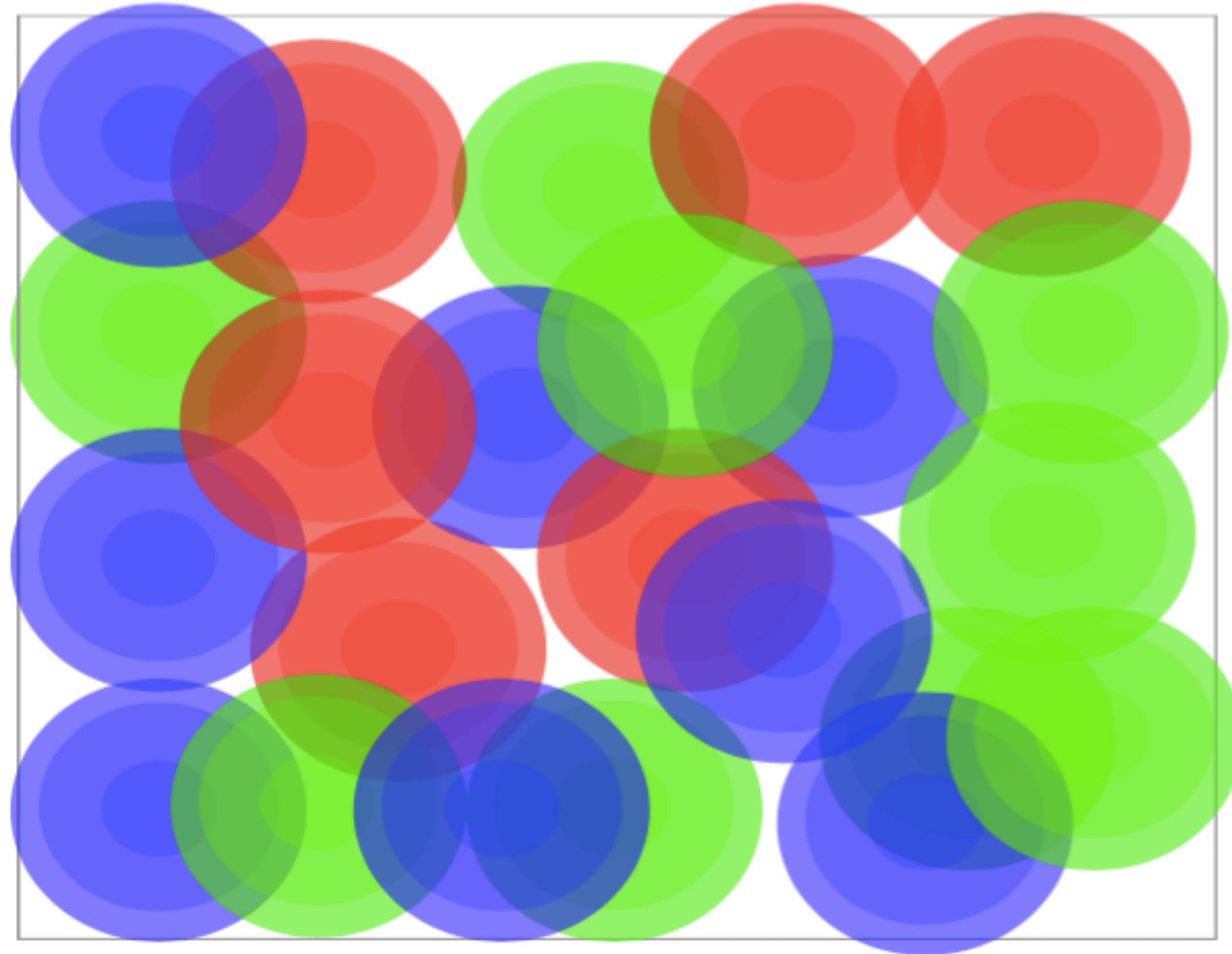
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$$T \sim gT \sim g^2 T$$

# Which is the correct picture of the plasma?

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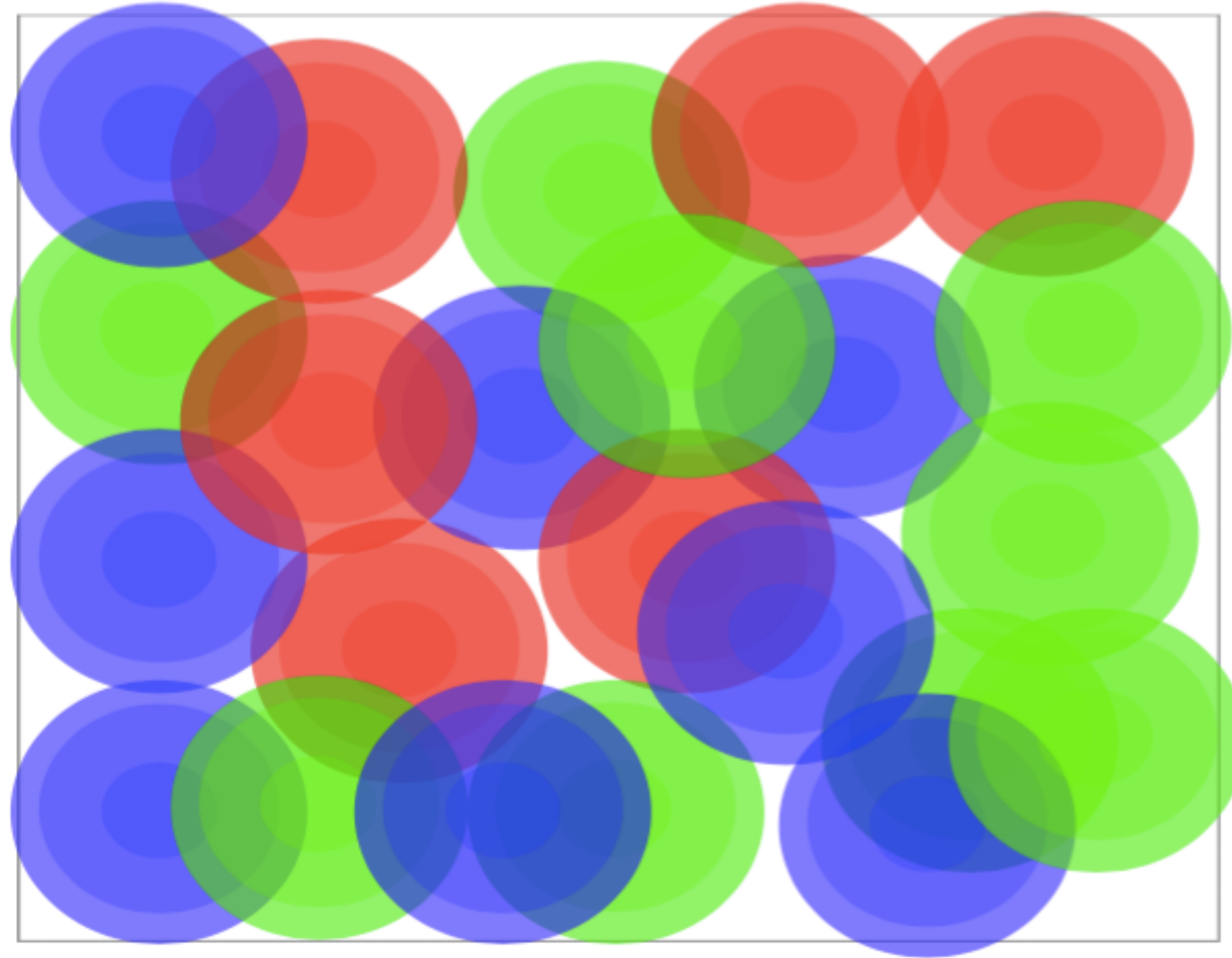
Is it a system with no long lived excitations?

$$\alpha_s = 0.3 \rightarrow g = 2$$

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# Which is the correct picture of the plasma?

$T \sim 0.2 \text{ GeV}$

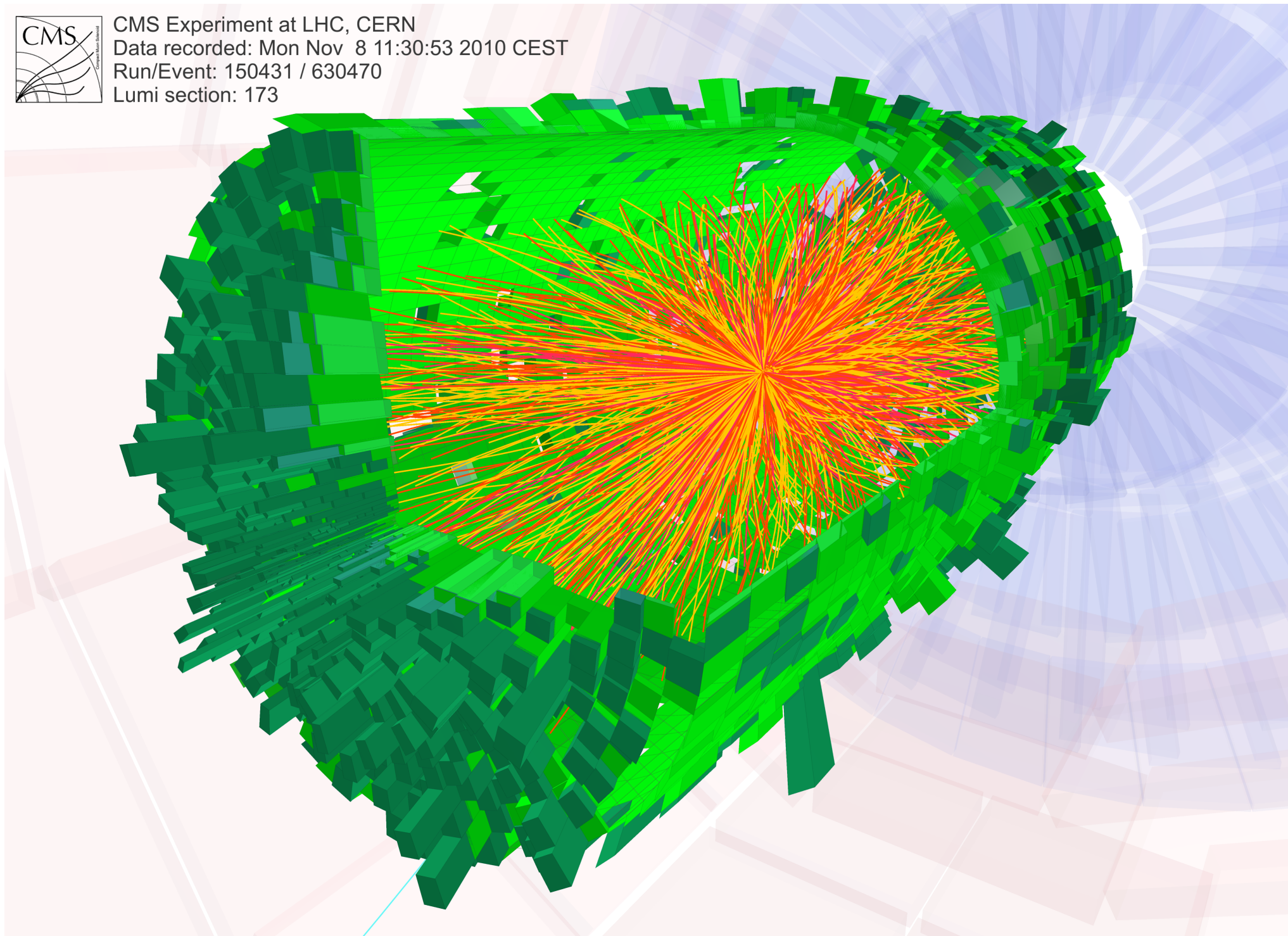


Is it a system with no **quasiparticles**?

$$\alpha_s = 0.3 \rightarrow g = 2$$

$$T \sim gT \sim g^2 T$$

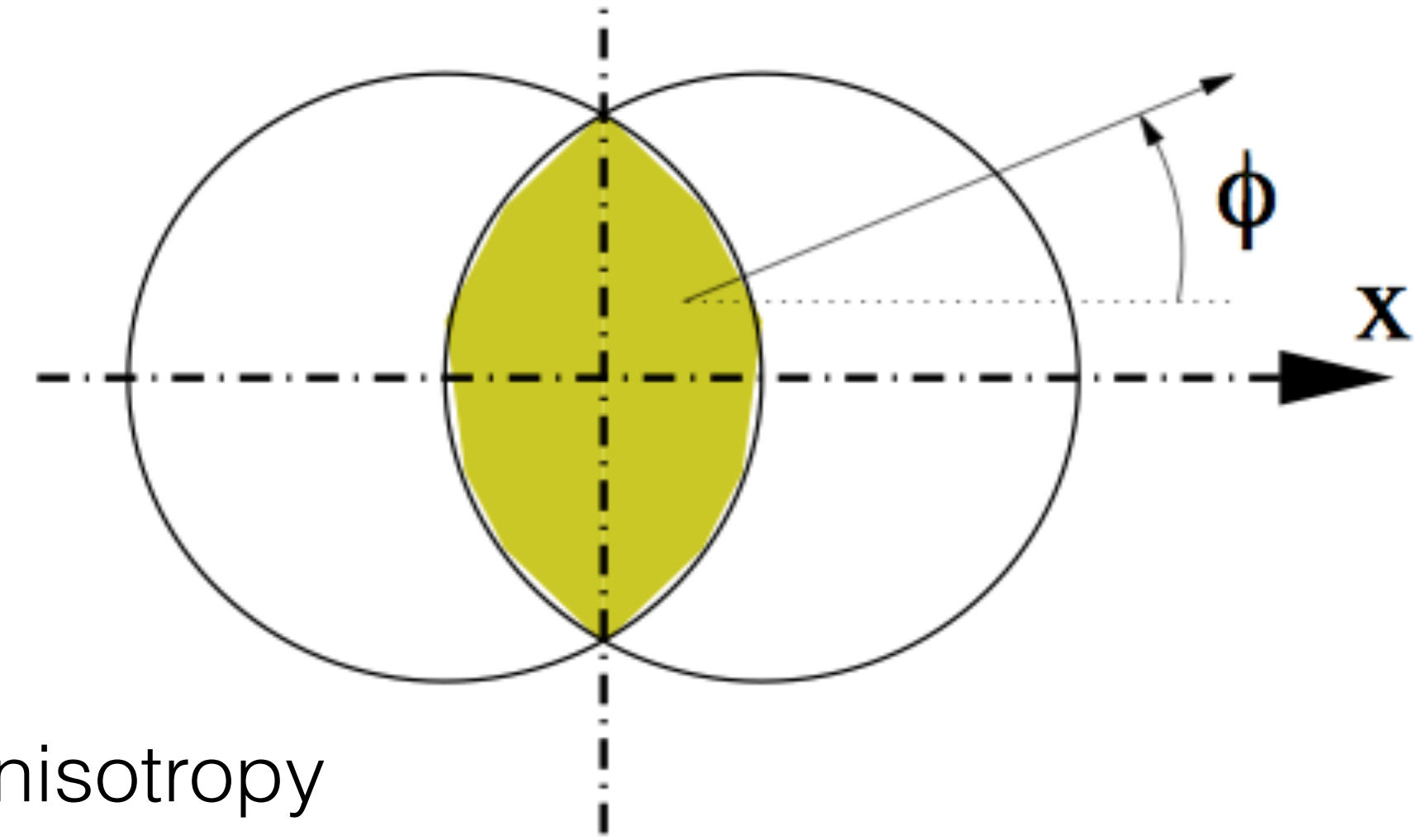
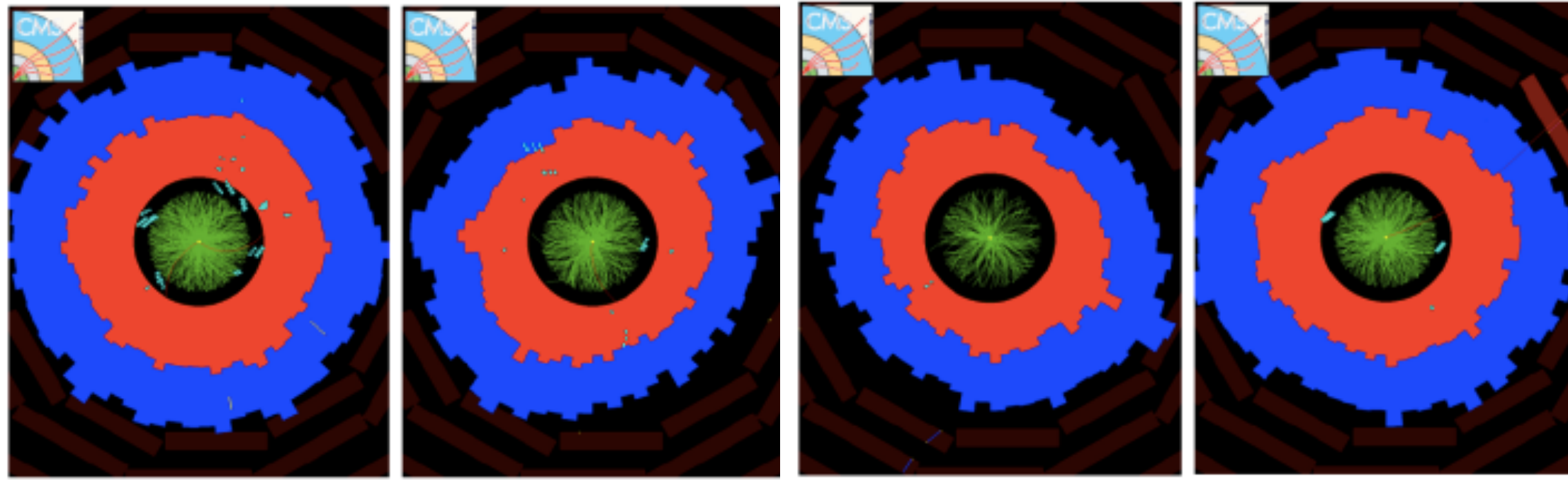
# Heavy Ion Collisions: the Little Bang



- Very strong collective effects
- 20.000 particles correlated according to collision geometry
- Hydrodynamic explosion

*The QGP is a very good fluid!*

# The QGP: Strongly Coupled Liquid



- Spatial anisotropy translates into momentum anisotropy

$$\frac{dN}{d^2\mathbf{p}_t dy} = \frac{1}{2\pi p_T} \frac{dN}{dp_T dy} [1 + 2v_1 \cos(\phi - \Phi_R) + 2v_2 \cos 2(\phi - \Phi_R) + \dots]$$

$$\left(\frac{\eta}{s}\right)_{T_c} = 0.08 \pm 0.05$$

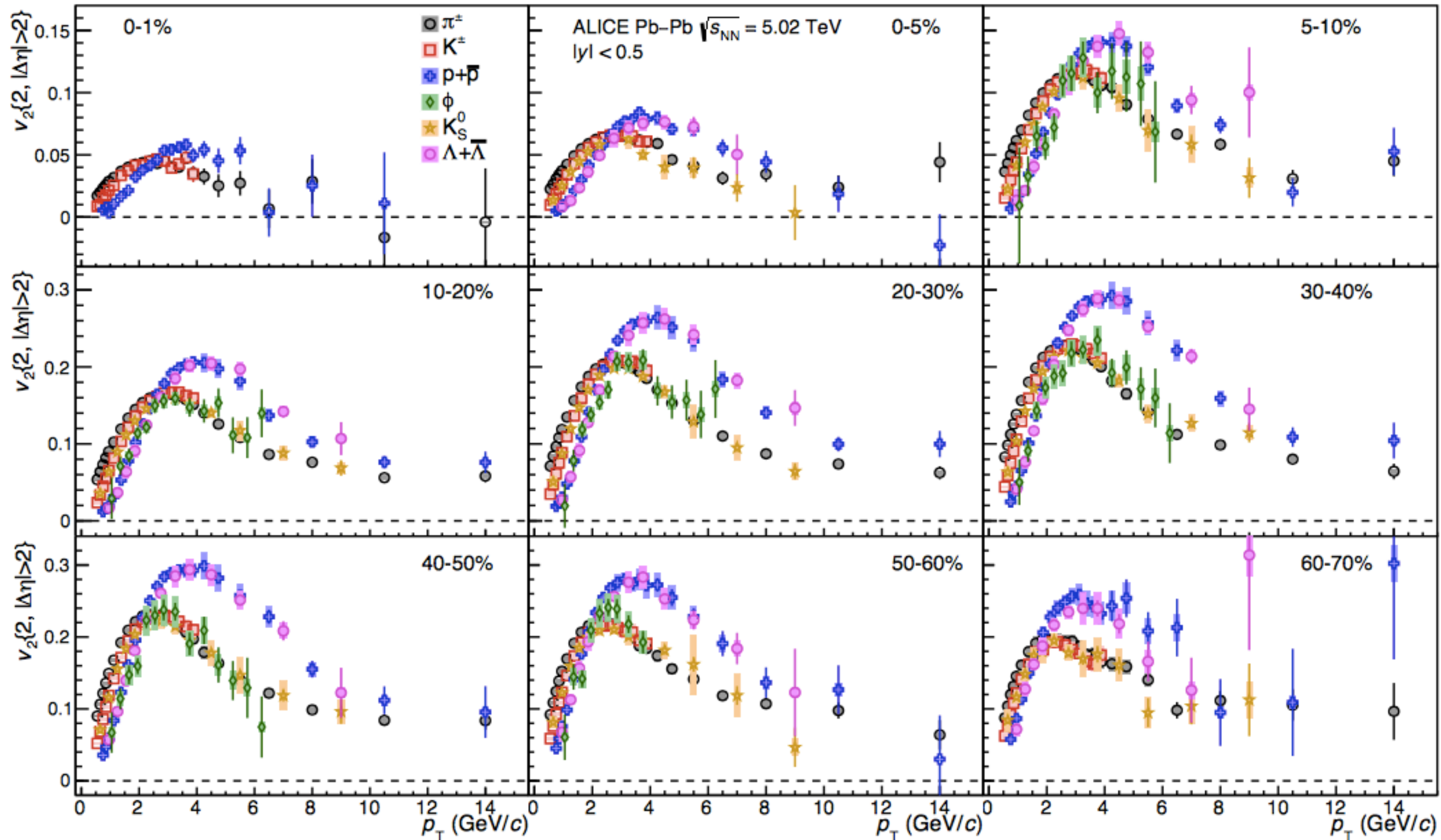
Bernhard et al. -  
PRC '16

- Data strongly favors very low shear viscosity over entropy density ratio. Characteristic of strongly coupled system (absence of weakly interacting quasiparticles)

$$\frac{\eta_{\lambda=\infty}}{s_{\lambda=\infty}} = \frac{1}{4\pi} \simeq 0.08$$

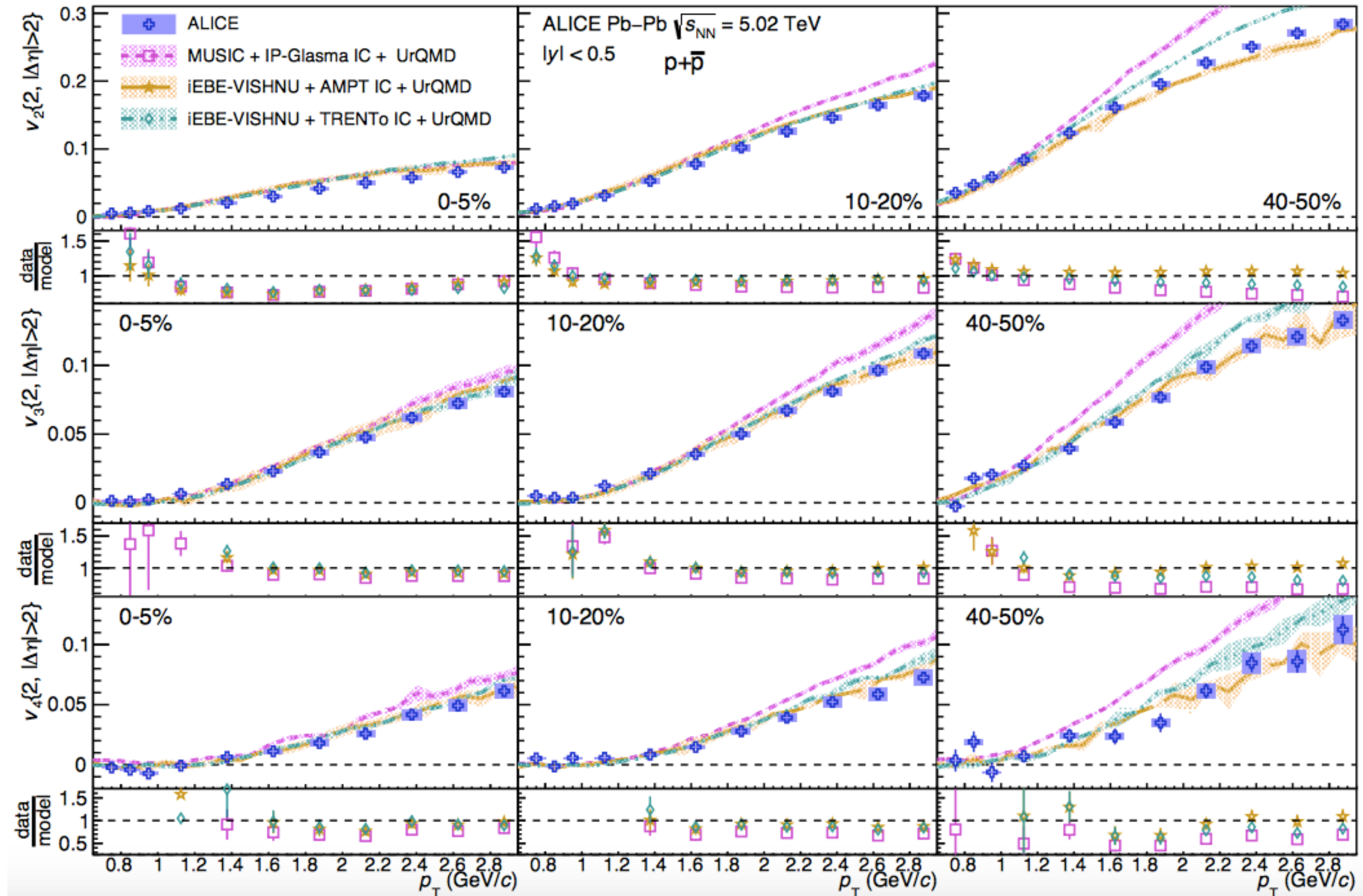
$$\frac{\eta_{\lambda \rightarrow 0}}{s_{\lambda \rightarrow 0}} = \frac{A}{\lambda^2 \log(B/\sqrt{\lambda})}$$

# Mass ordering of flow



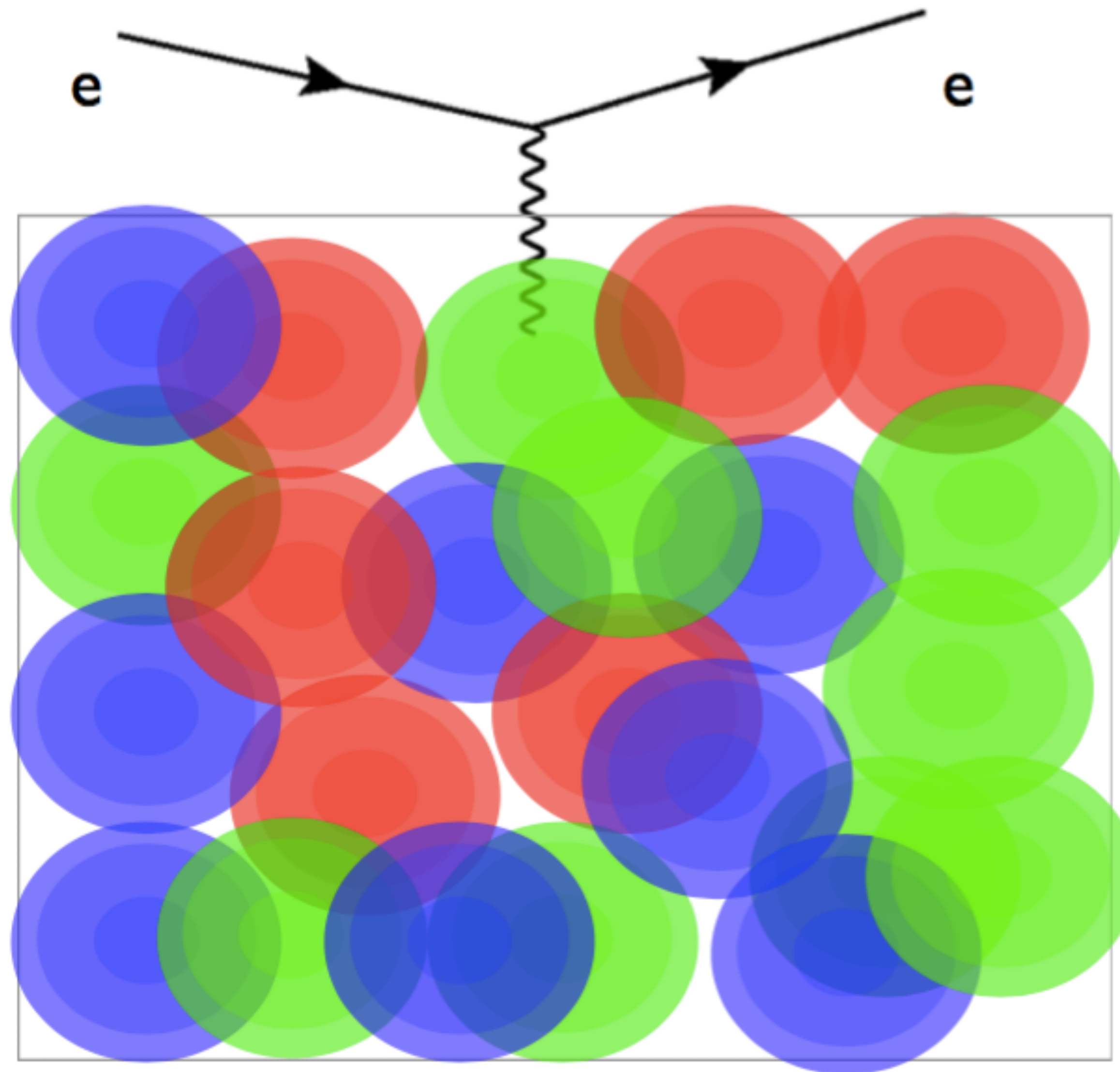
$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \Psi_n)] \right)$$

# Hydrodynamics Simulations



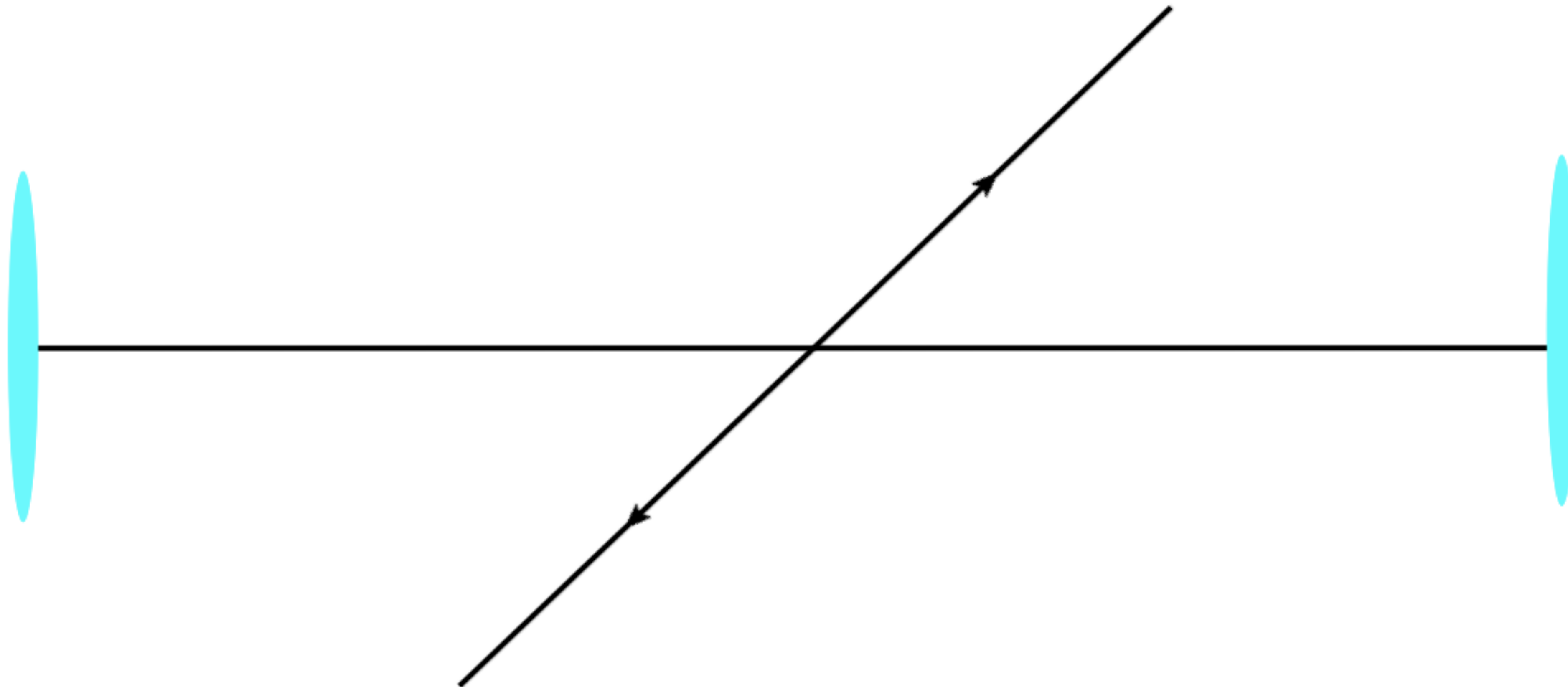
ALICE - JHEP '18

# How can we probe the QGP?

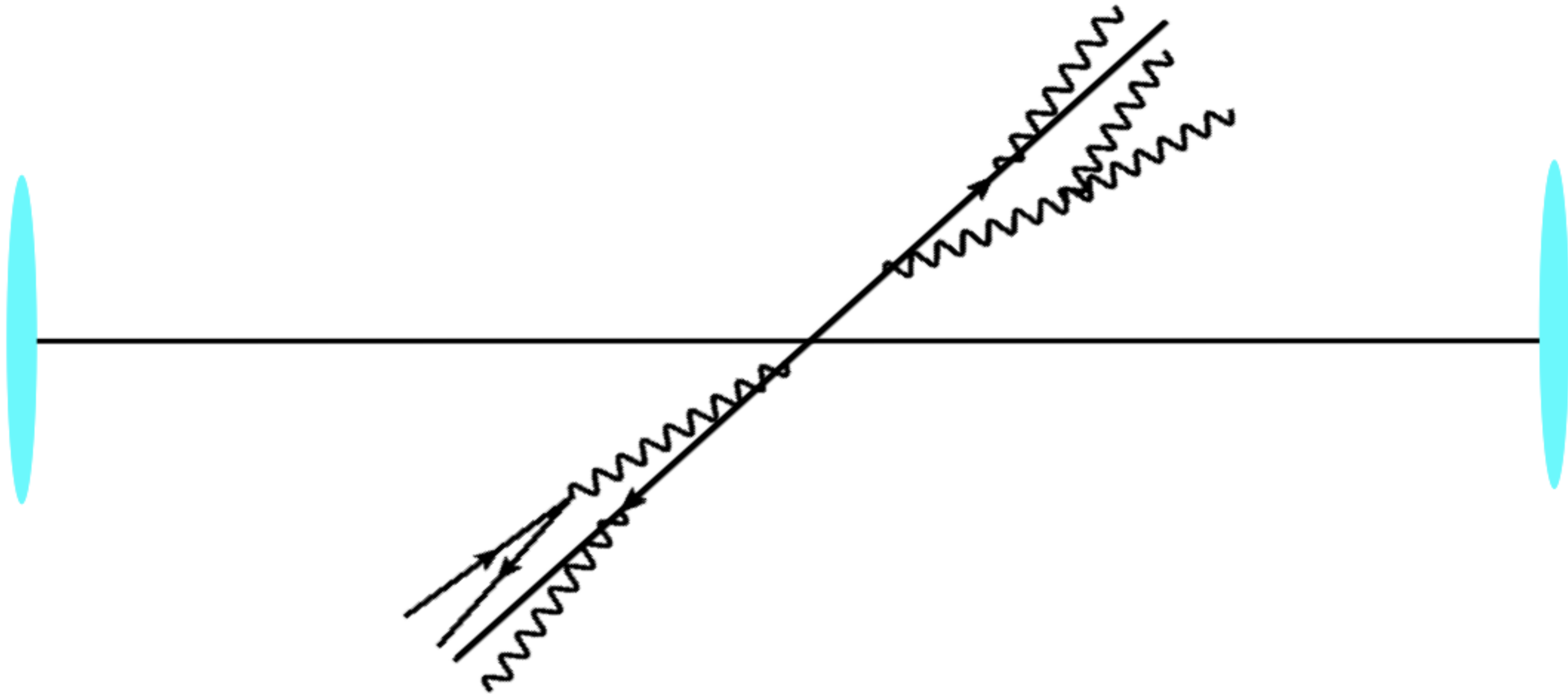




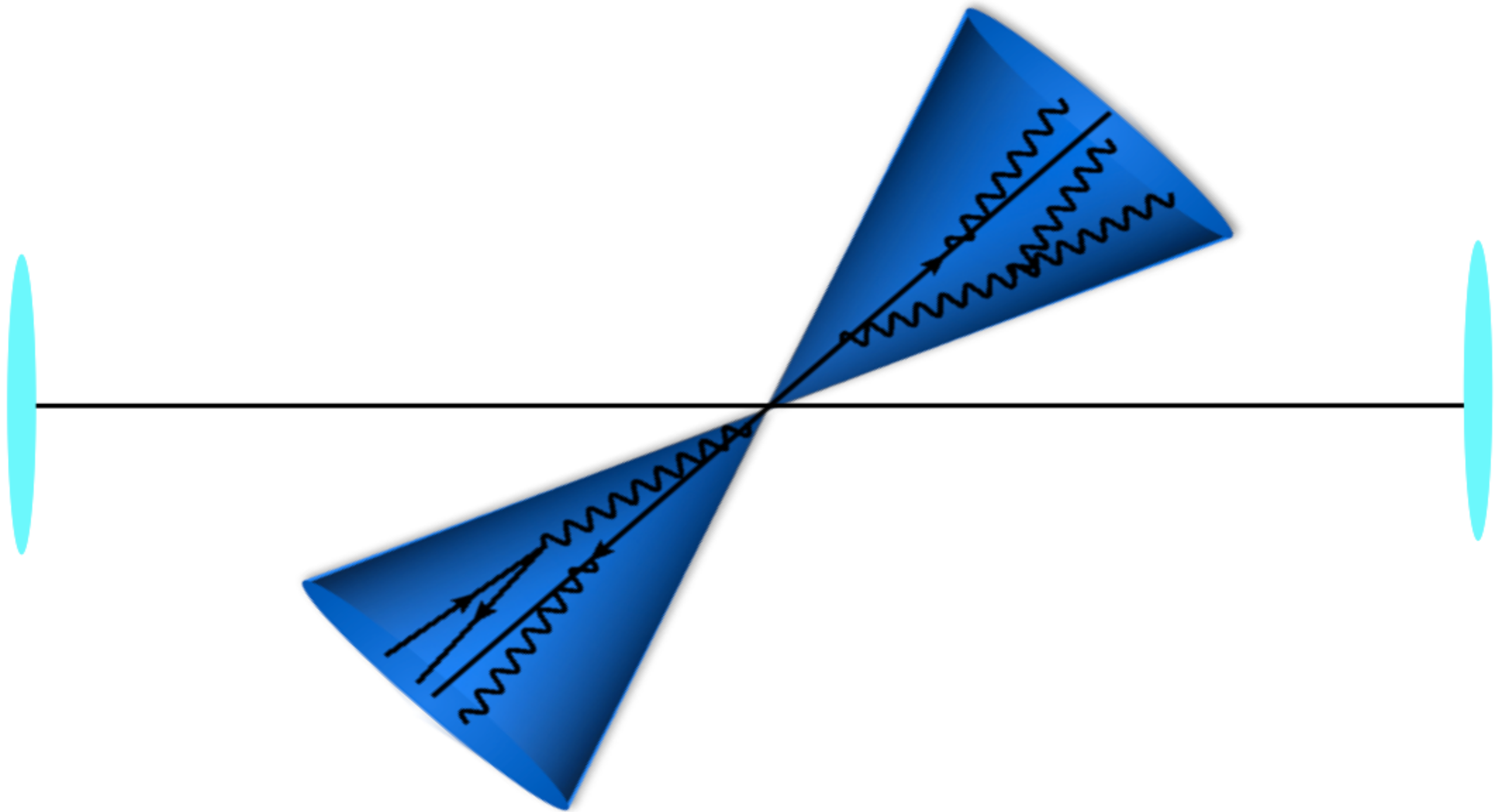
# Jets



# Jets



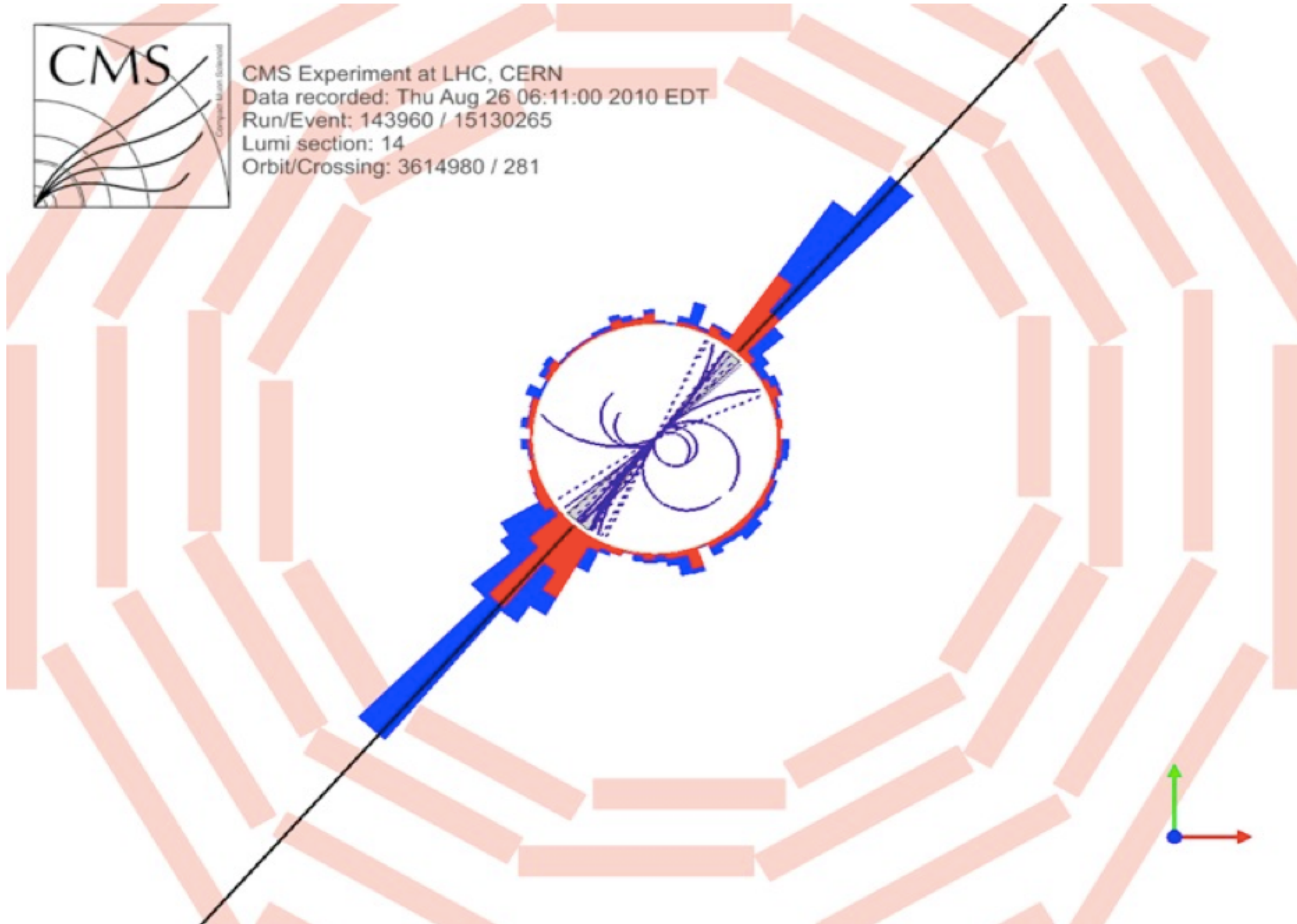
# Jets



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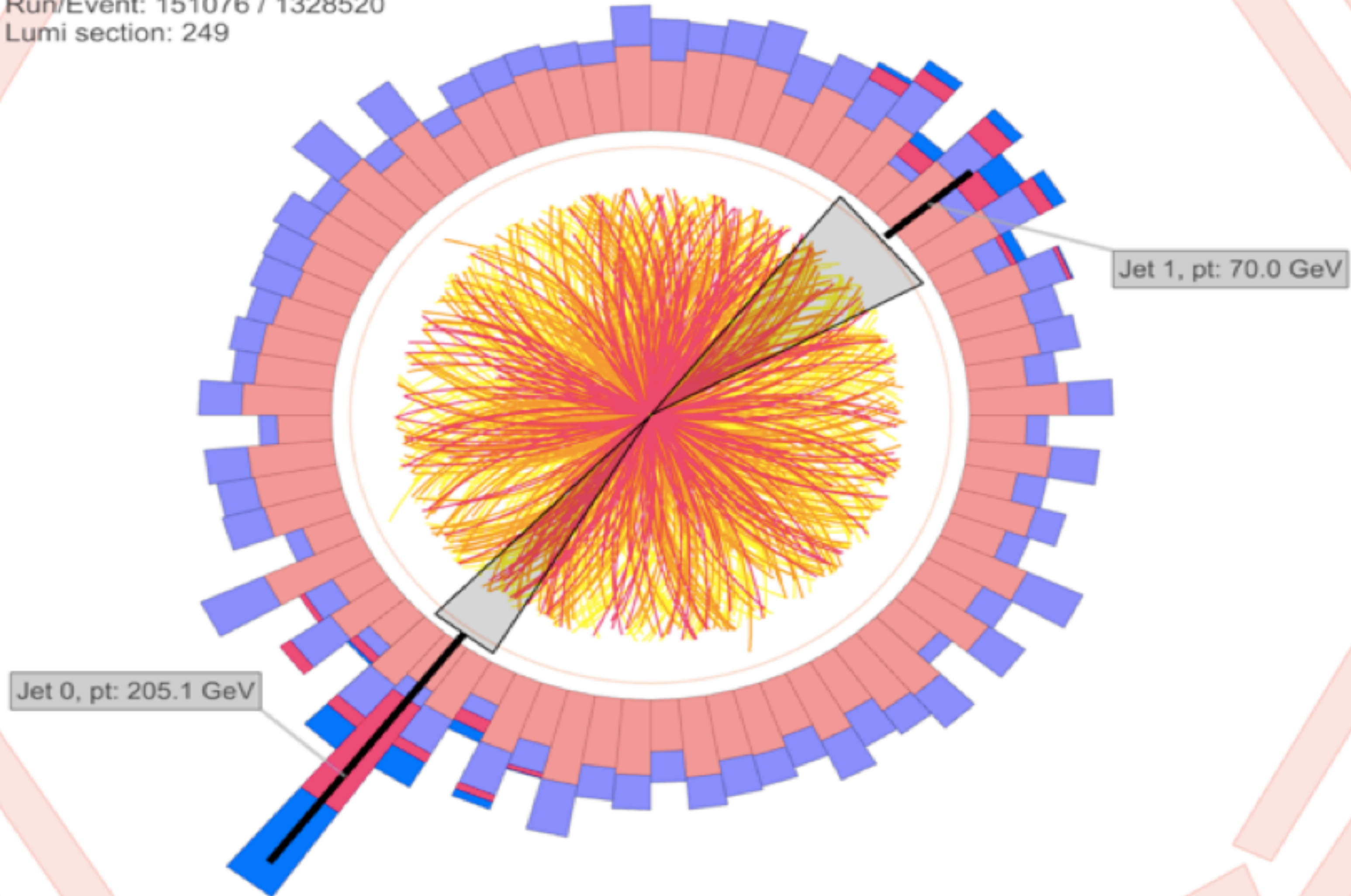
CMS Experiment at LHC, CERN  
Data recorded: Thu Aug 26 06:11:00 2010 EDT  
Run/Event: 143960 / 15130265  
Lumi section: 14  
Orbit/Crossing: 3614980 / 281



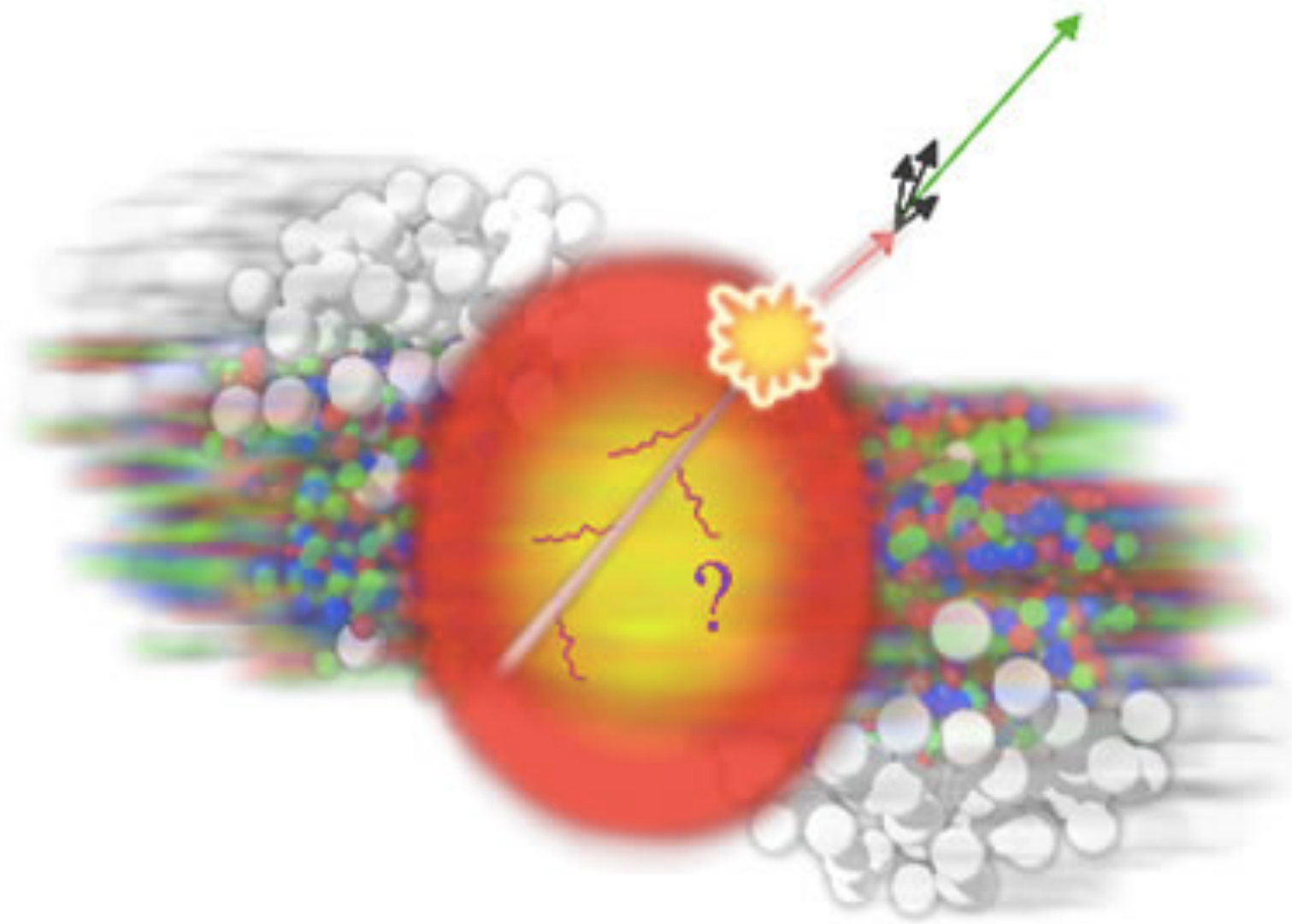
# Jets in HIC



CMS Experiment at LHC, CERN  
Data recorded: Sun Nov 14 19:31:39 2010 CEST  
Run/Event: 151076 / 1328520  
Lumi section: 249

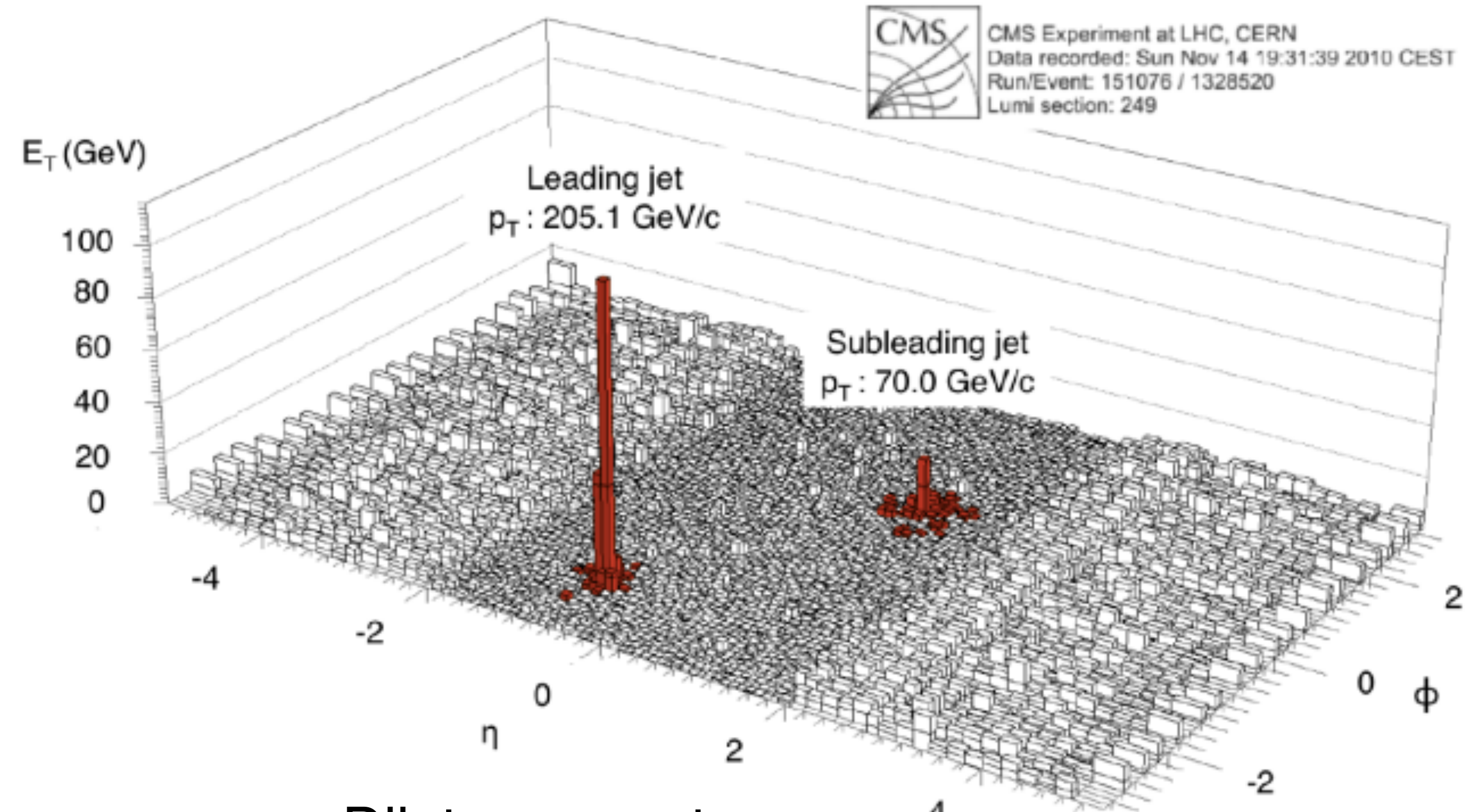


# Dijet Asymmetry



Traditional interpretation:

→ Path length difference within QGP.



Dijet asymmetry

CMS  
 CMS Experiment at LHC, CERN  
 Data recorded: Sun Nov 14 19:31:39 2010 CEST  
 Run/Event: 151076 / 1328520  
 Lumi section: 249

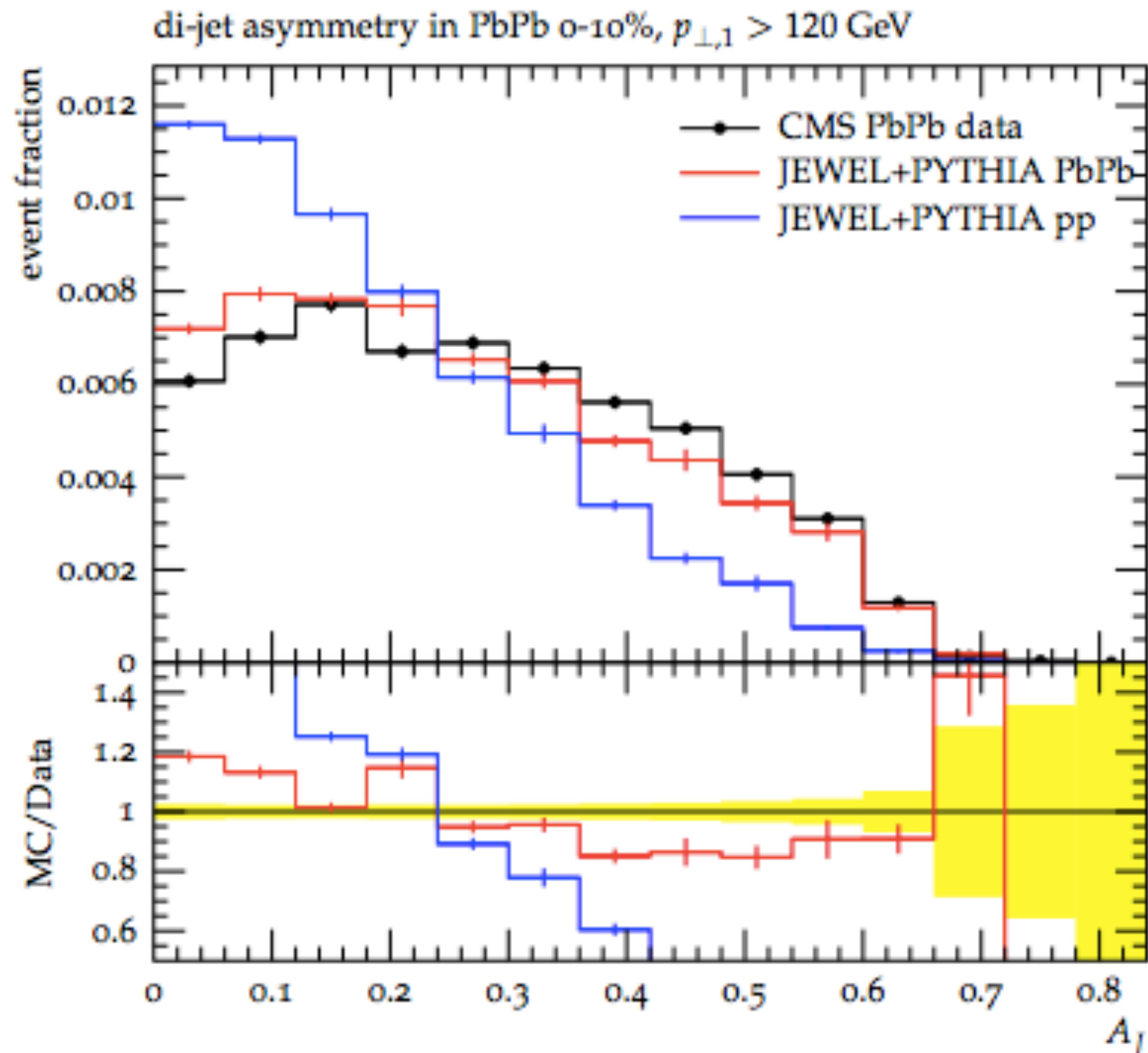
Based on single parton energy loss processes:

- Medium induced radiation
- Elastic collisions

} Controlled by transport parameter  $\hat{q}$  [GeV<sup>2</sup>/fm]

GW '94  
 BDMPS-Z '97  
 AMY '02

# Dijet Asymmetry



JEWEL jet energy loss Monte Carlo model:

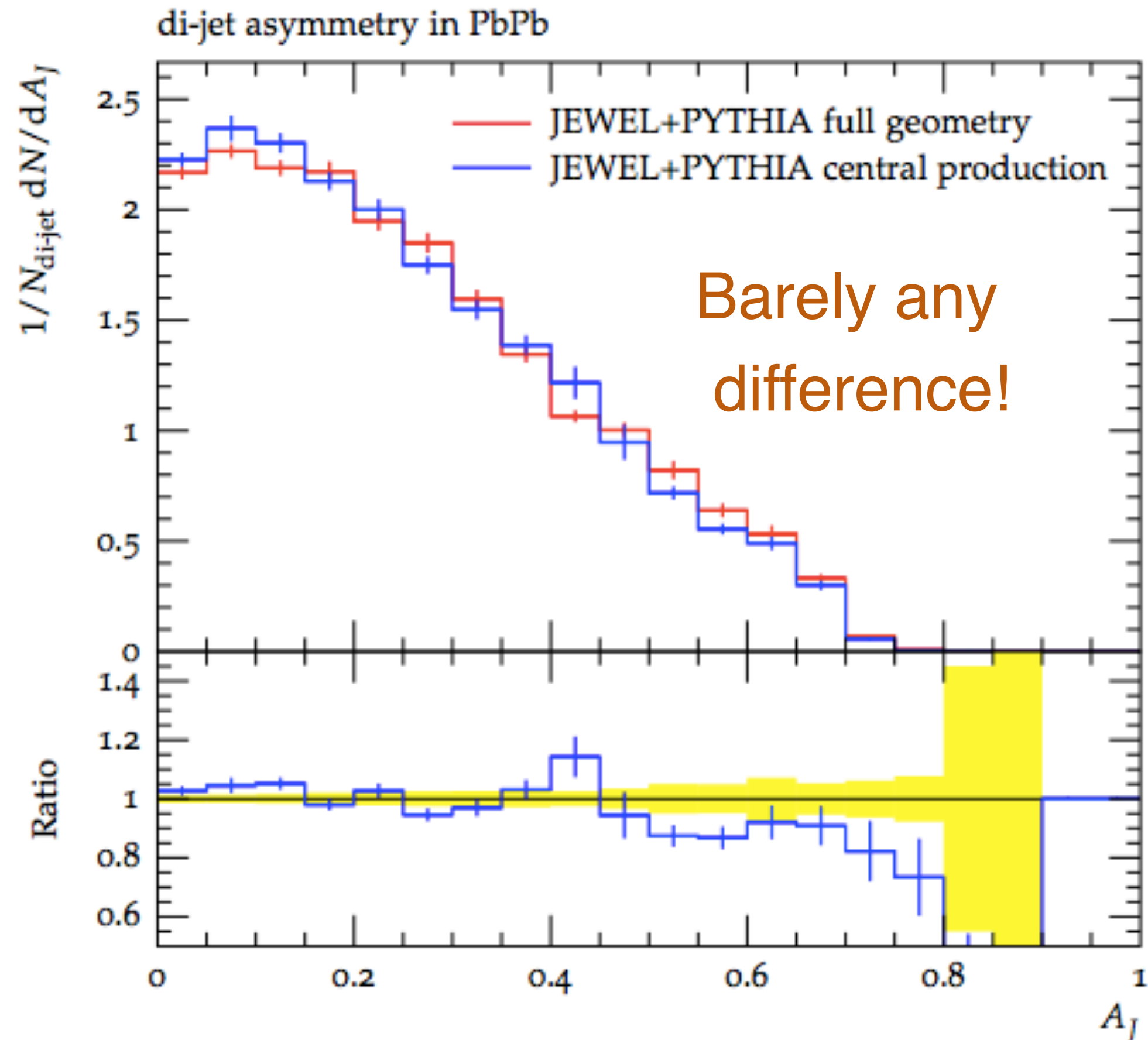
- Partons can collide with the medium scatterers.
- After-collision kinematics can alter the radiation pattern.
- Actual radiation pattern based on shortest formation time.

Good description of dijet asymmetry data.

Look under the hood...

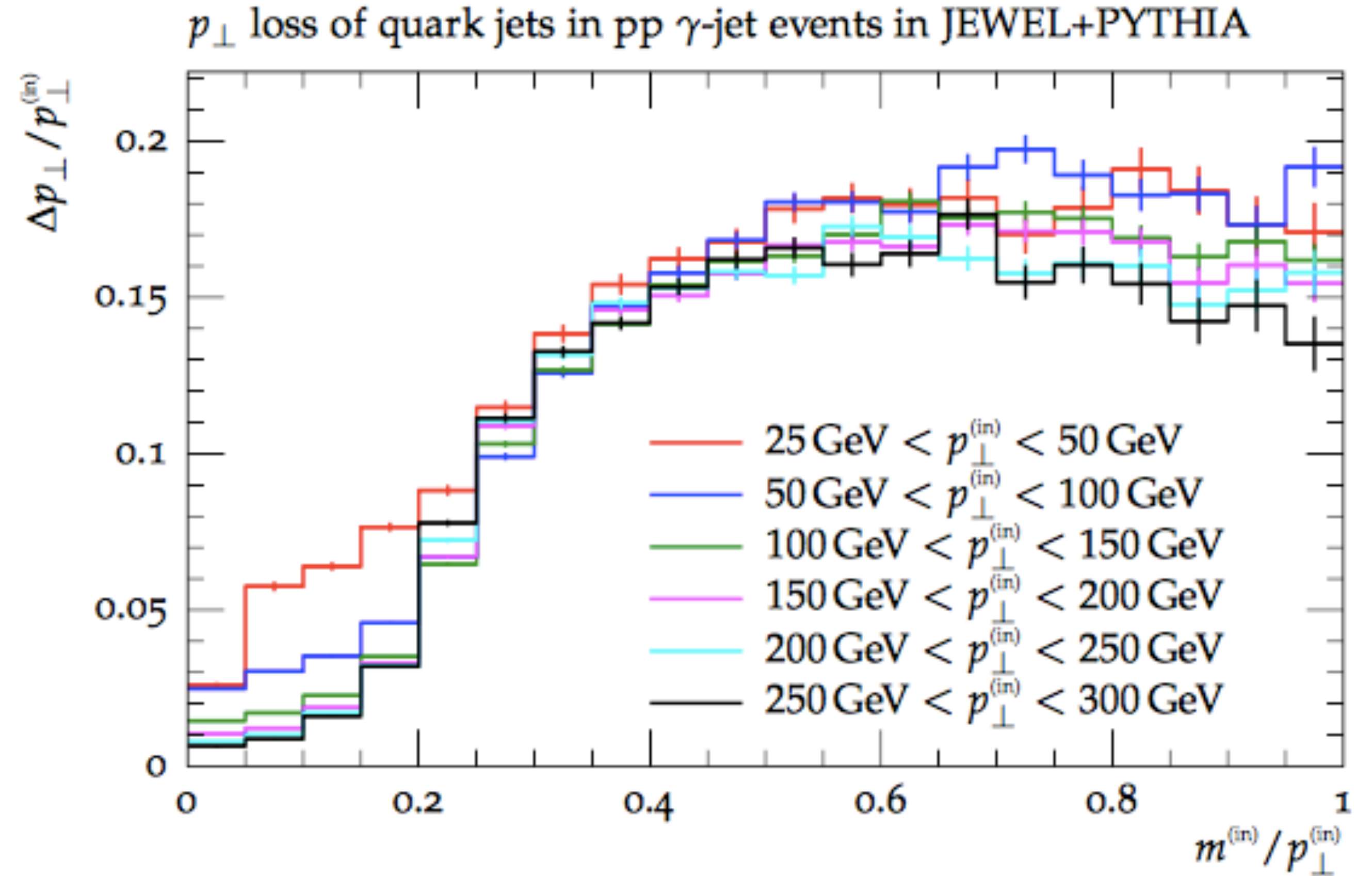
$$A_J = \frac{p_{\perp,1} - p_{\perp,2}}{p_{\perp,1} + p_{\perp,2}}$$

# Dijet Asymmetry



Full geometry  
vs  
Central production

Milhano & Zapp - EPJ '16

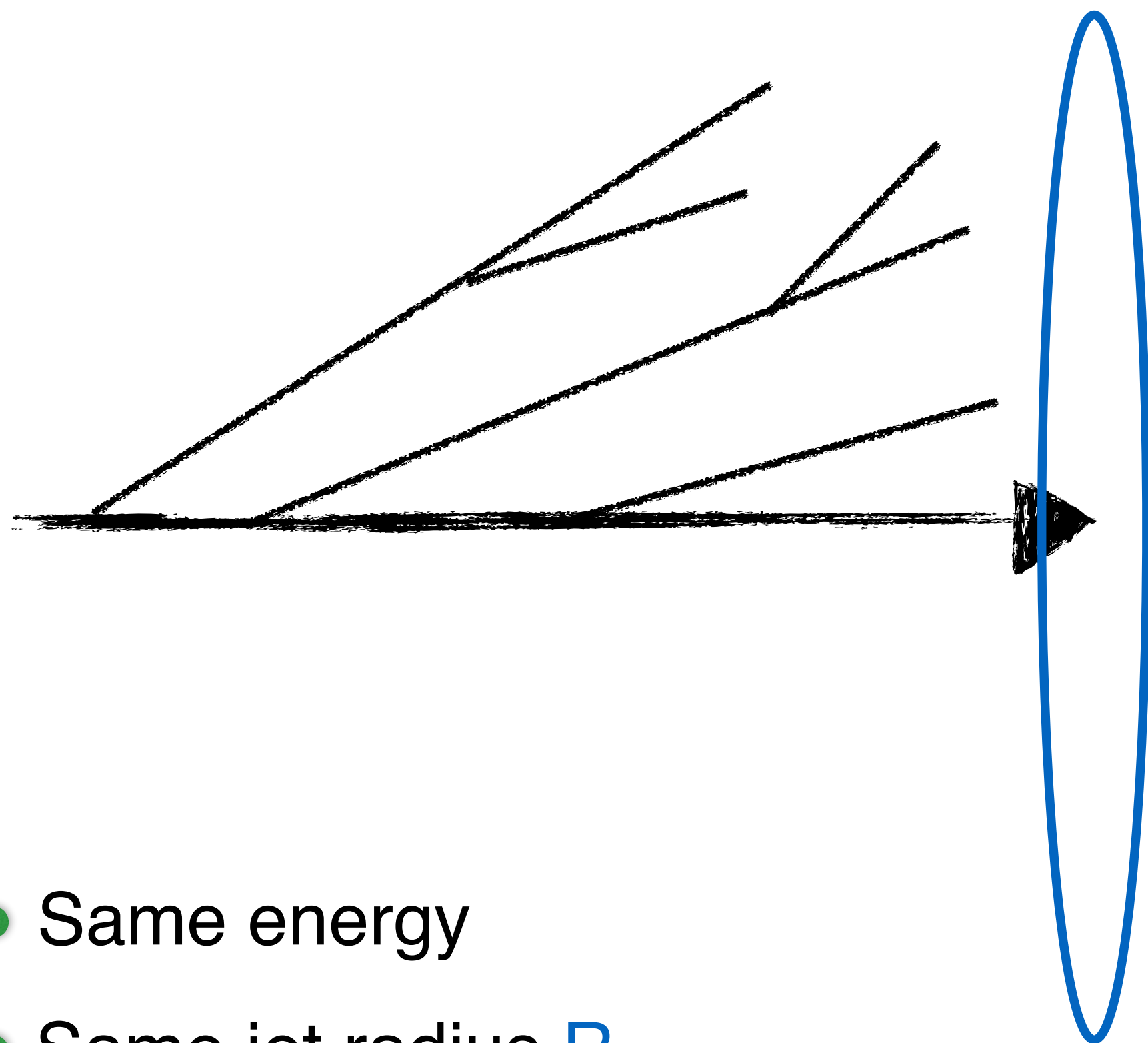


Dijet asymmetry dominated by  
mass to momentum ratio,  
proxy for # vacuum splittings



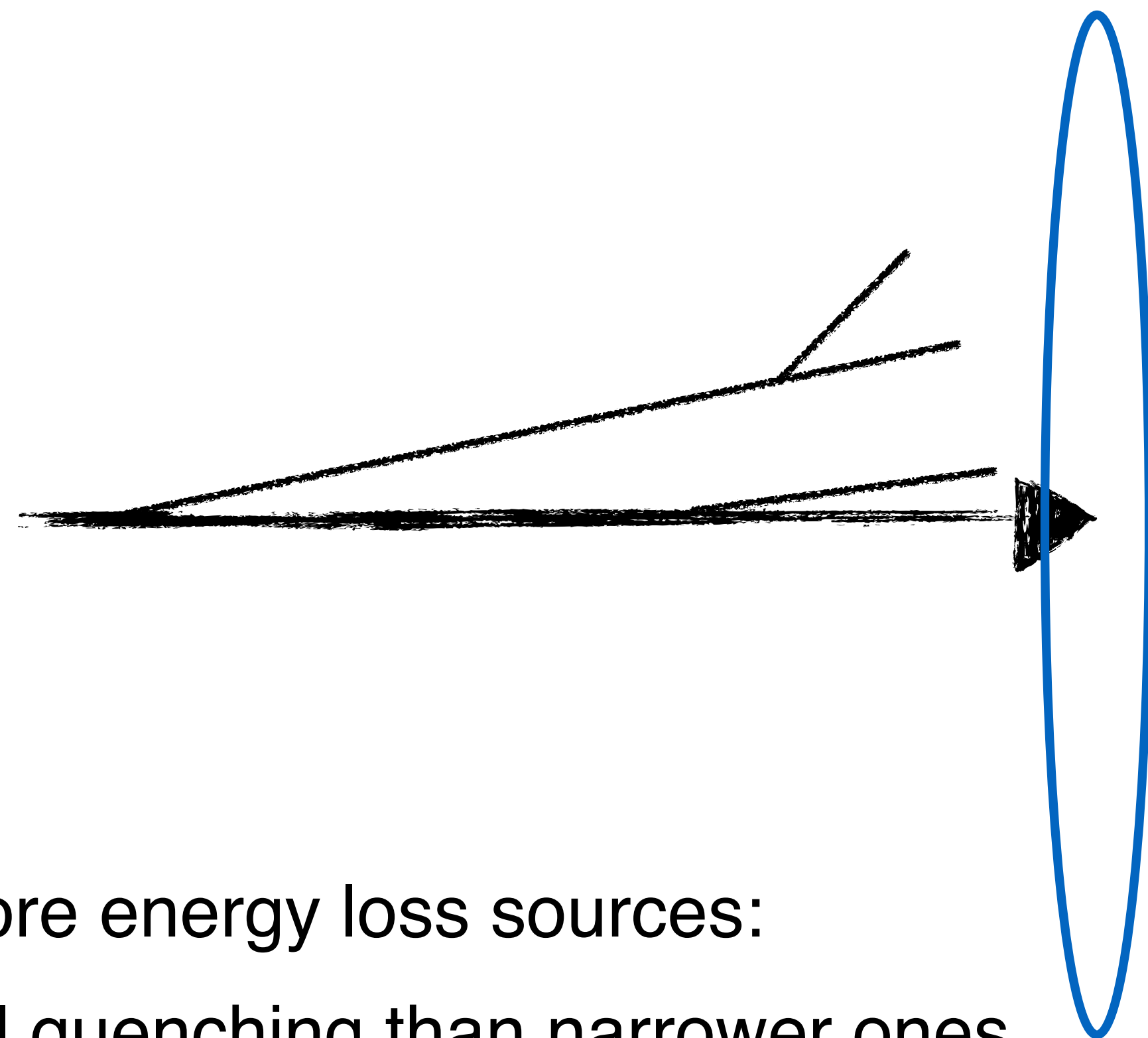
# Jets and Jets

Wide jet



- Same energy
- Same jet radius  $R$
- Different fragmentation pattern

Narrow jet



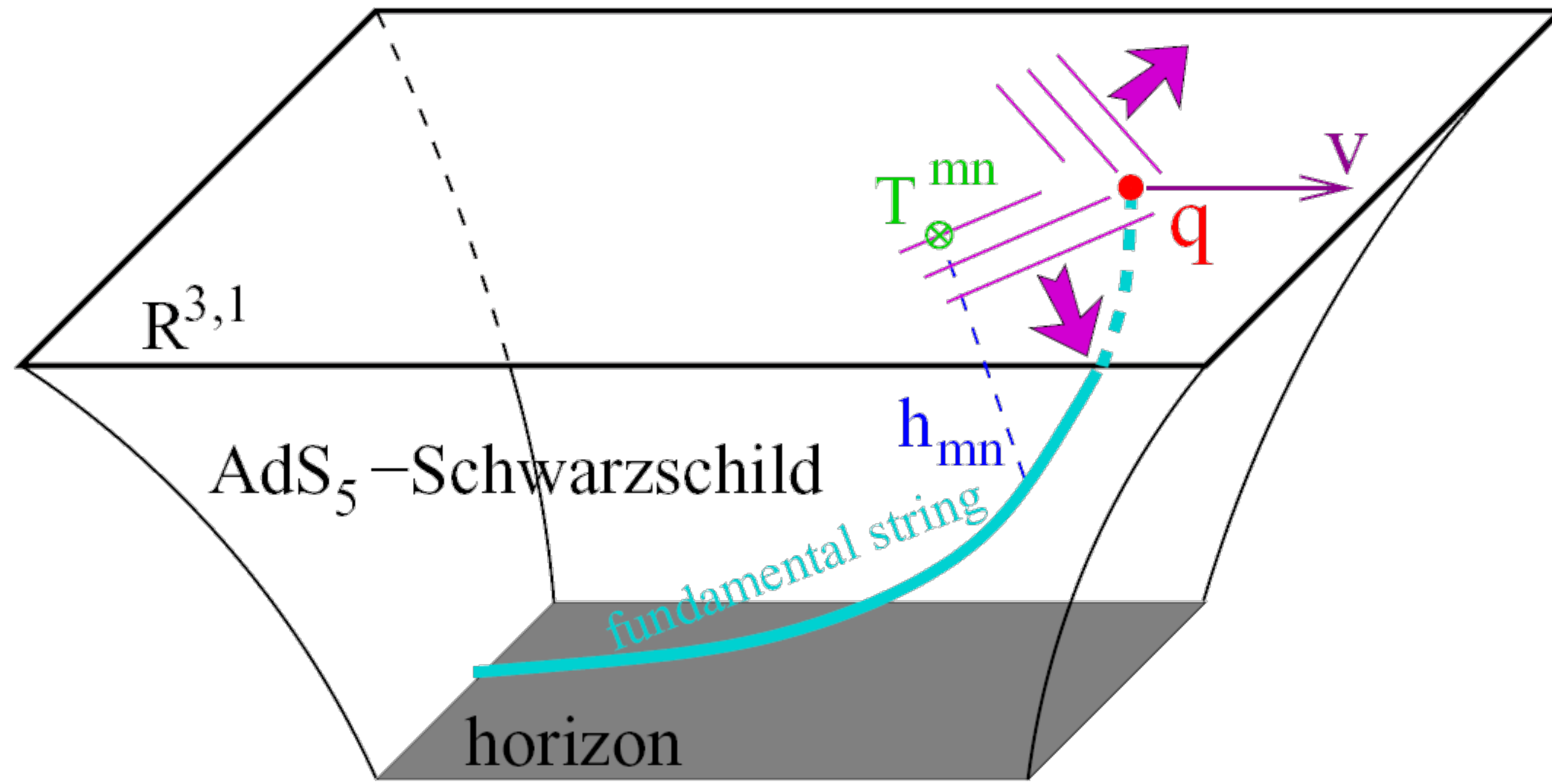
Wider jets have more energy loss sources:

→ more total quenching than narrower ones

Assuming:

- most of the energy goes out of the cone
- internal structure resolved by QGP

# Holography



J Friess, et al., PRD75 (2007)

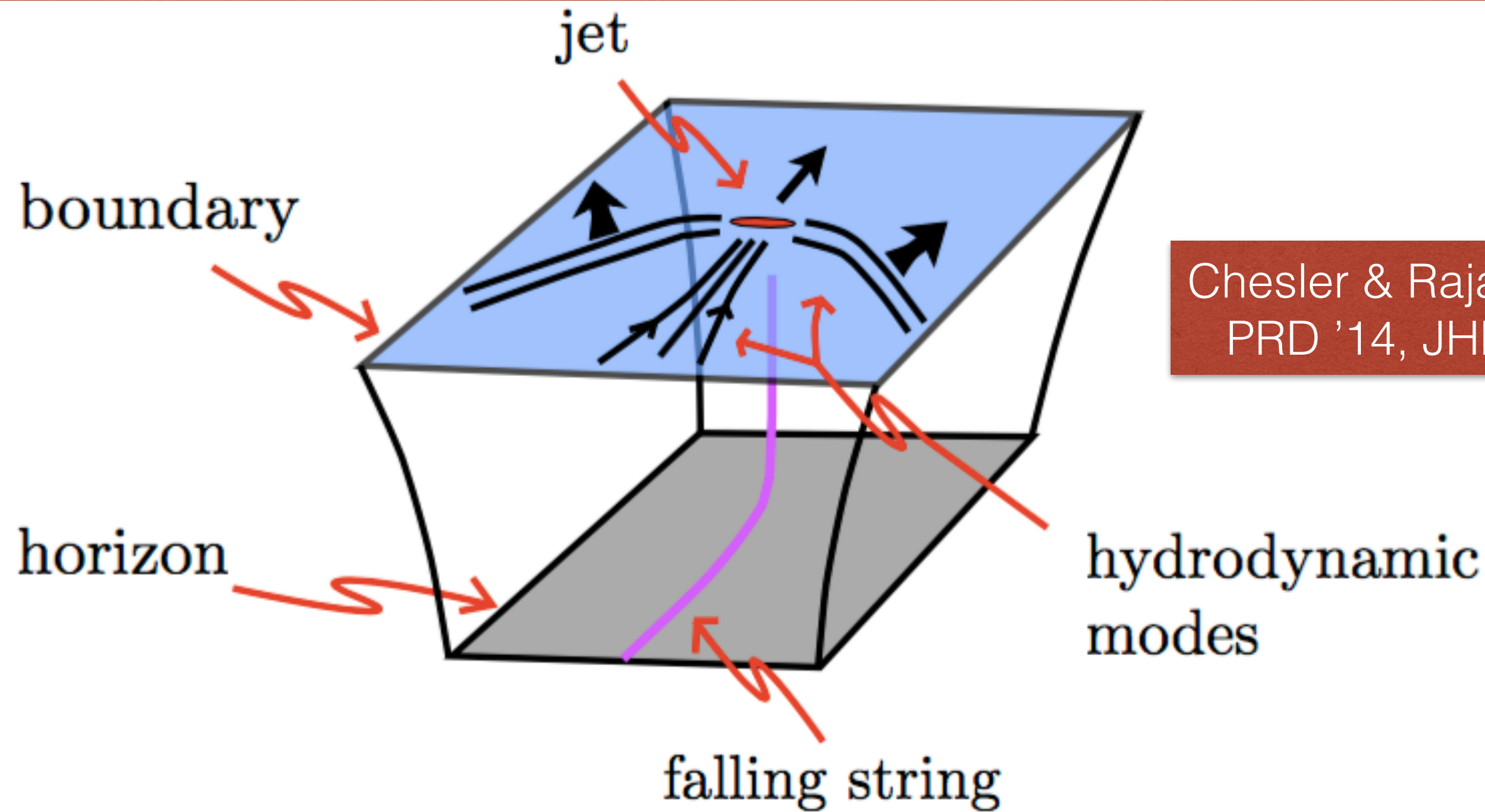
- quarks are dual to open strings attached to probe flavour branes
- having a plasma in the gauge theory is equivalent to a black hole in the bulk
- bulk metric perturbations encode boundary stress energy variations

!  $\mathcal{N} = 4$  SYM and QCD have very different vacuums

*but*

?  $\mathcal{N} = 4$   $T \neq 0$  and QCD  $T > T_c$  share similarities

# Null falling strings

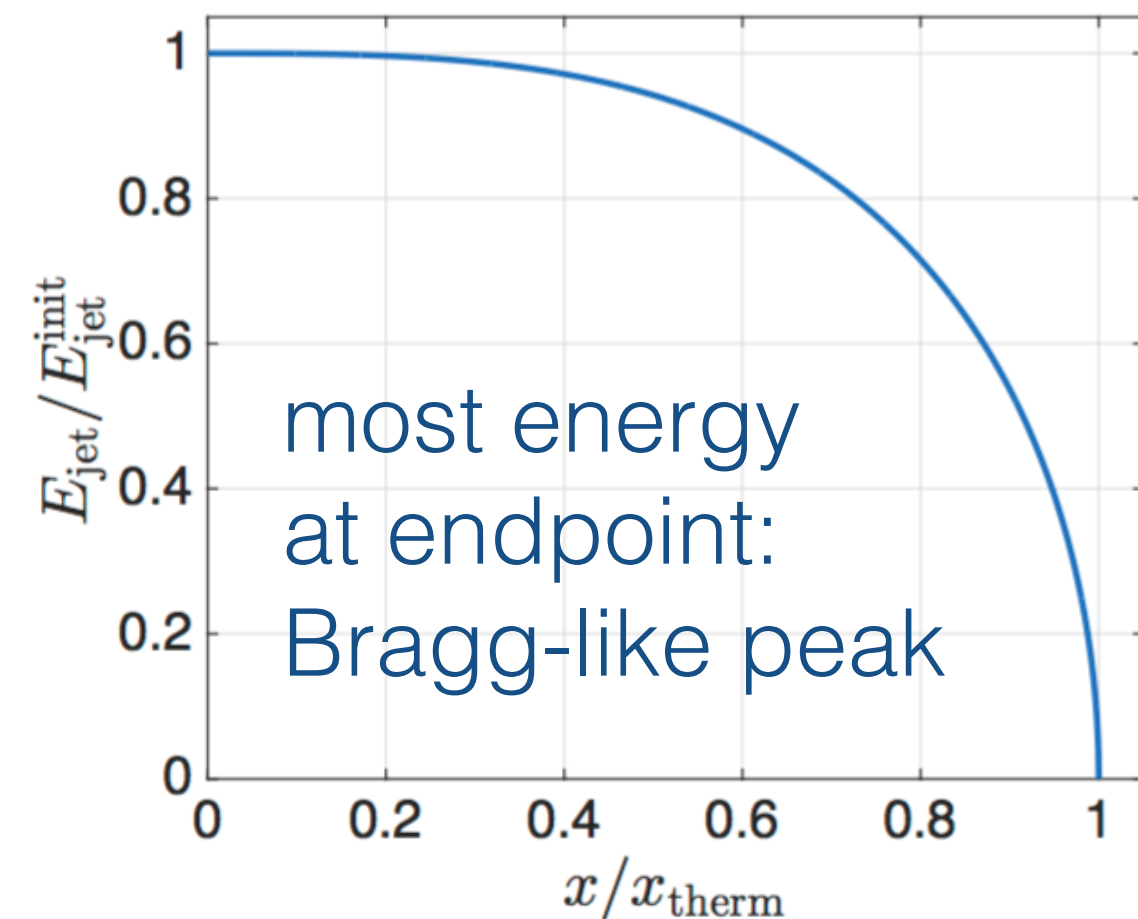


Chesler & Rajagopal -  
PRD '14, JHEP '16

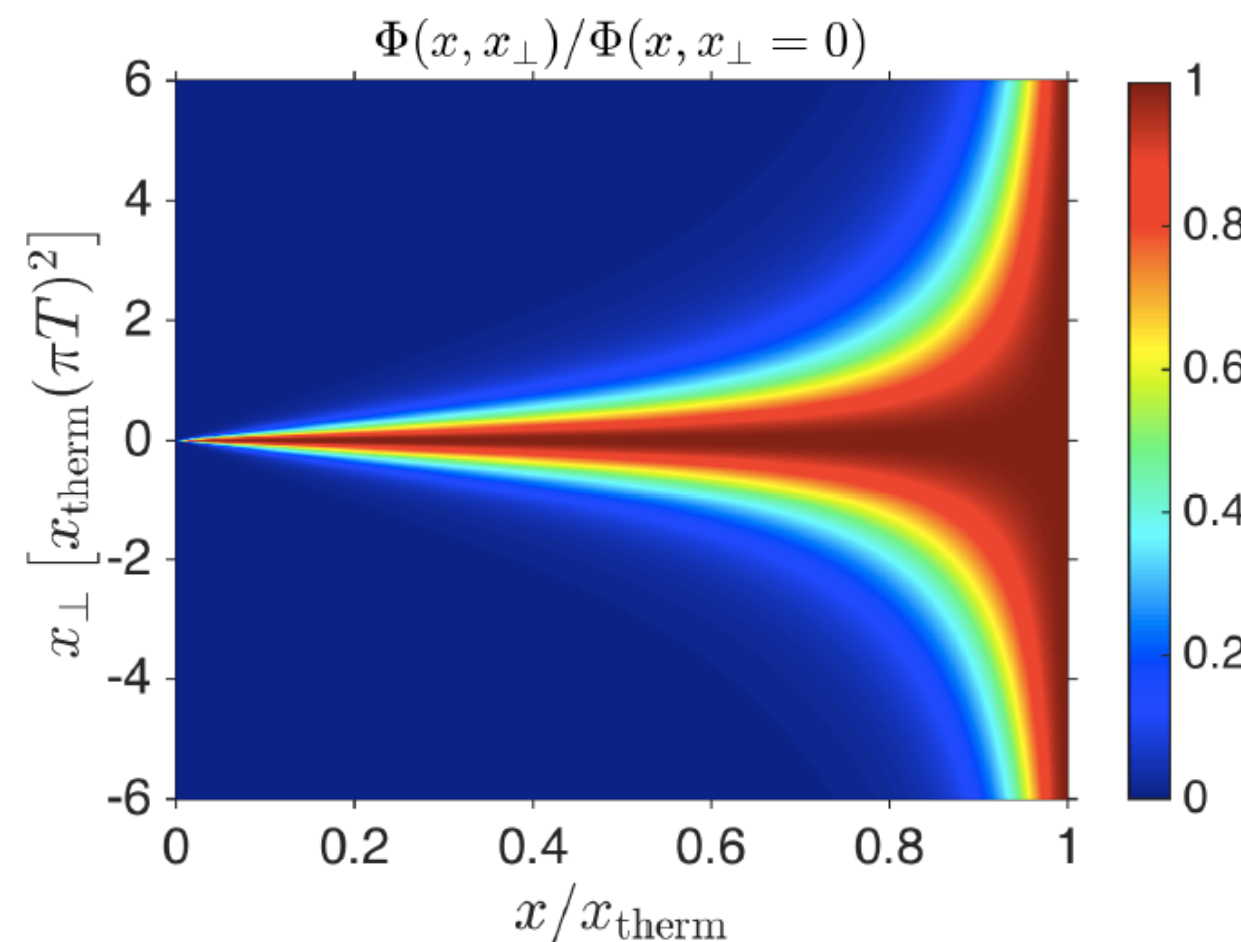
- unambiguous determination of boundary jet properties
- the rate at which energy flows into hydrodynamic modes:

$$\frac{1}{E_{\text{init}}} \frac{dE_{\text{jet}}}{dx} = - \frac{4x^2}{\pi x_{\text{therm}}^2 \sqrt{x_{\text{therm}}^2 - x^2}}$$

as the jet loses energy



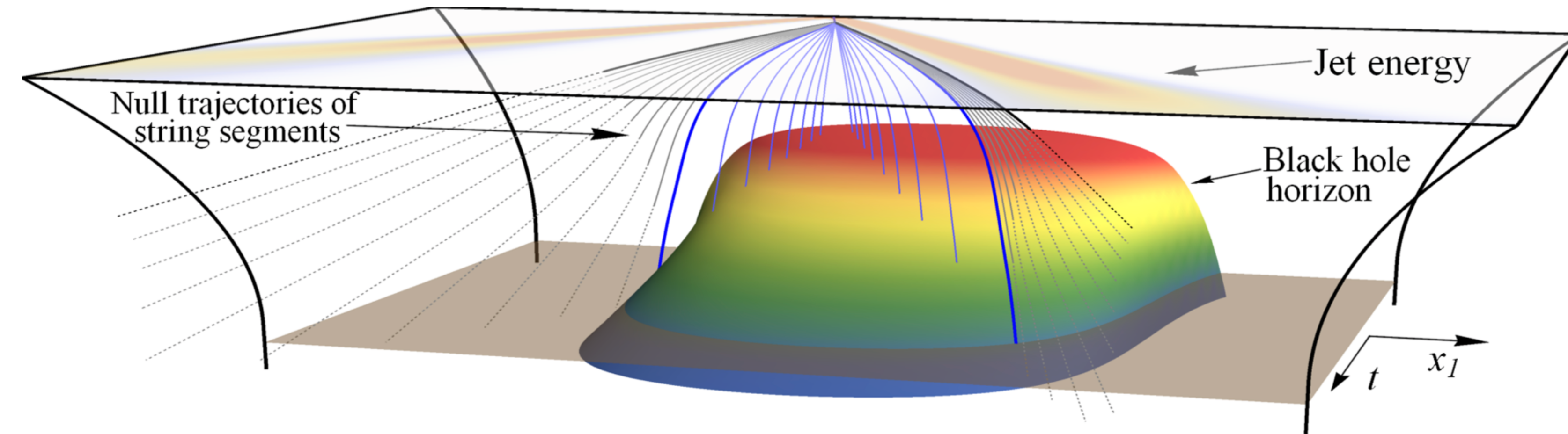
... it gets wider



Fractional energy loss  
only depends on  
initial jet opening angle

$$x_{\text{therm}} = \frac{1}{T} \sqrt{\frac{\kappa}{\theta_{\text{jet}}^{\text{init}}}}$$

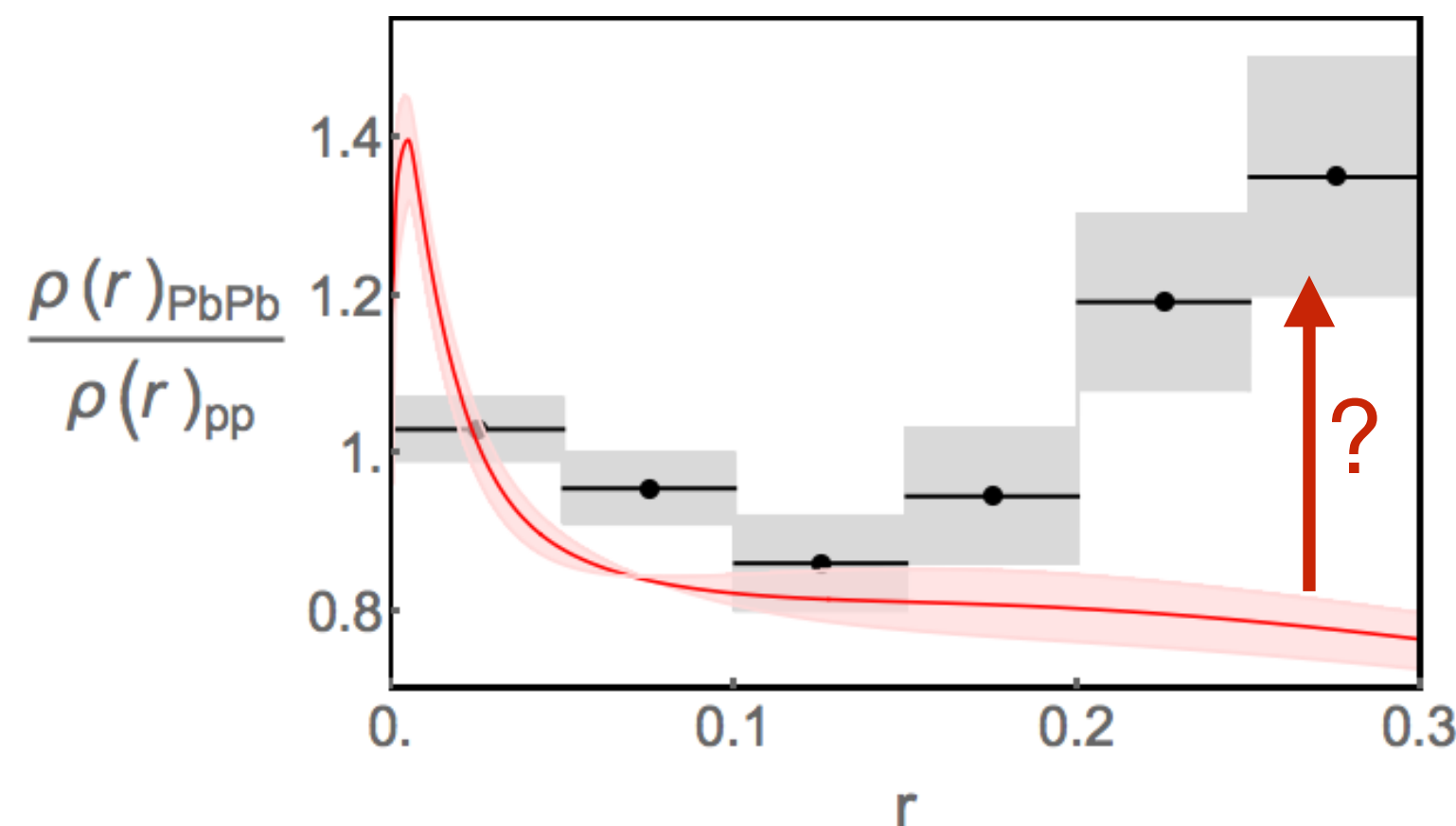
# Holographic quenching with pure strings



the *string* is treated as a model for the *jet as a whole*

Rajagopal et al. - PRL '16

- consider an *ensemble* of such jets by choosing initial distributions of energy & angle from pQCD
- competing effects: each individual jet widens, while wider jets lose more energy



Jet shapes:  
transverse jet energy  
distribution vs radial distance

*Jet narrowing due  
to selection bias!*

$$C_1^{(\alpha)} \equiv \sum_{i,j} z_i z_j \left( \frac{|\theta_{ij}|}{R} \right)^\alpha$$

measures jet angle in pQCD

$$C_1^{(1)} = a \sigma_0 \quad T_{\text{SYM}} = b T_{\text{QCD}}$$

# The hybrid strong/weak coupling model

- Evolution of **high virtuality** energetic jets dominated by **DGLAP** evolution;
- **Interaction** of partons with **QGP** of  $T \sim \Lambda_{QCD}$  is **strongly coupled**;
- Energy and momentum deposited in the QGP **hydrodynamize** quickly;

# The hybrid strong/weak coupling model

→ Evolution of **high virtuality** energetic jets dominated by **DGLAP** evolution;

- Parton shower generated with PYTHIA8.
- Formation time argument for space-time picture.

Pablos et al. - JHEP '14, '16, '17

→ Interaction of partons with **QGP** of  $T \sim \Lambda_{QCD}$  is **strongly coupled**;

- Energy loss rate from **holography**:

Chesler & Rajagopal -  
PRD '14, JHEP '16

$$\frac{1}{E_{\text{in}}} \frac{dE}{dx} = -\frac{4}{\pi} \frac{x^2}{x_{\text{stop}}^2} \frac{1}{\sqrt{x_{\text{stop}}^2 - x^2}}$$

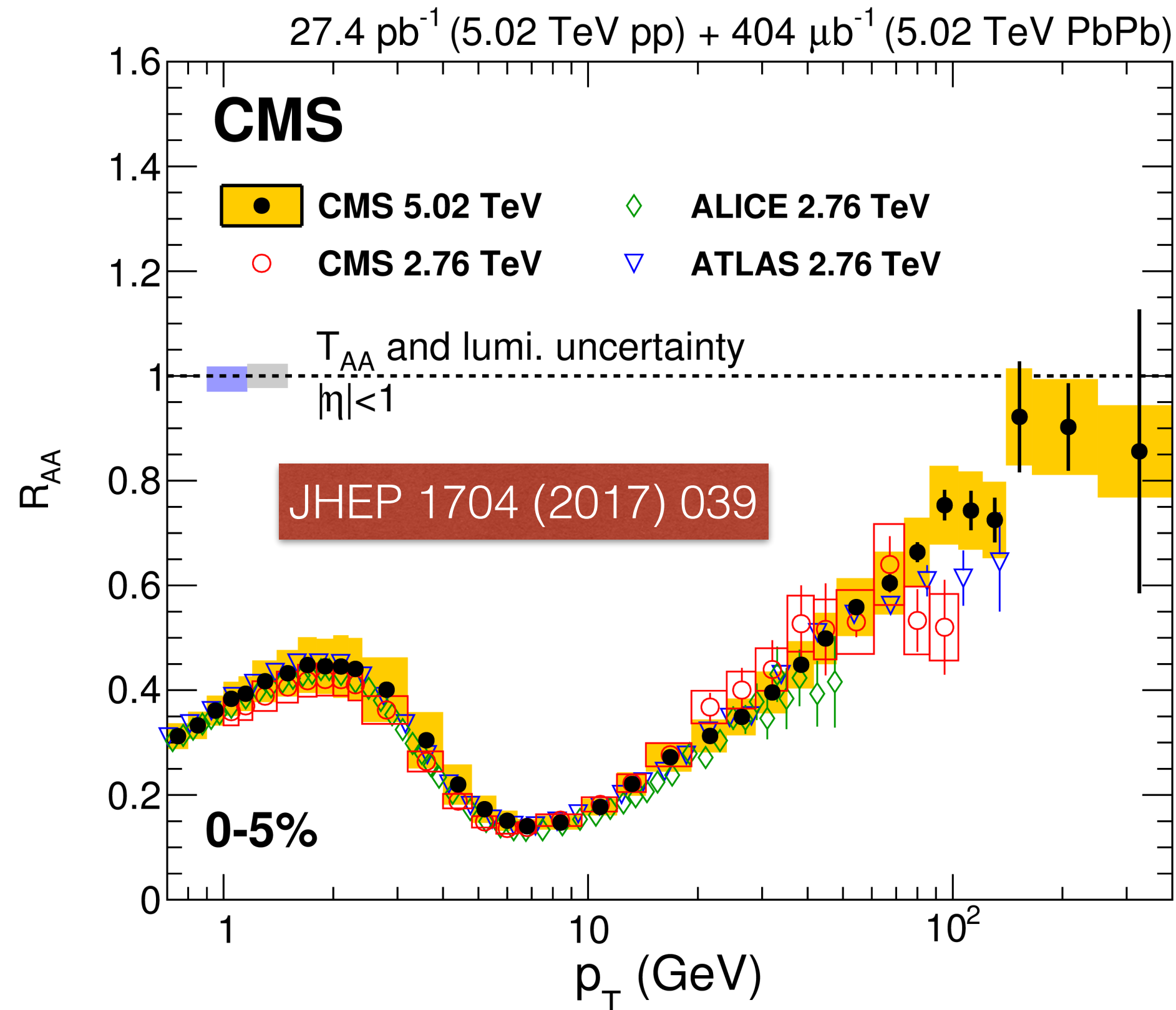
$$x_{\text{stop}} = \frac{1}{2 \kappa_{\text{SC}}} \frac{E_{\text{in}}^{1/3}}{T^{4/3}}$$

$\mathcal{O}(1)$  free parameter

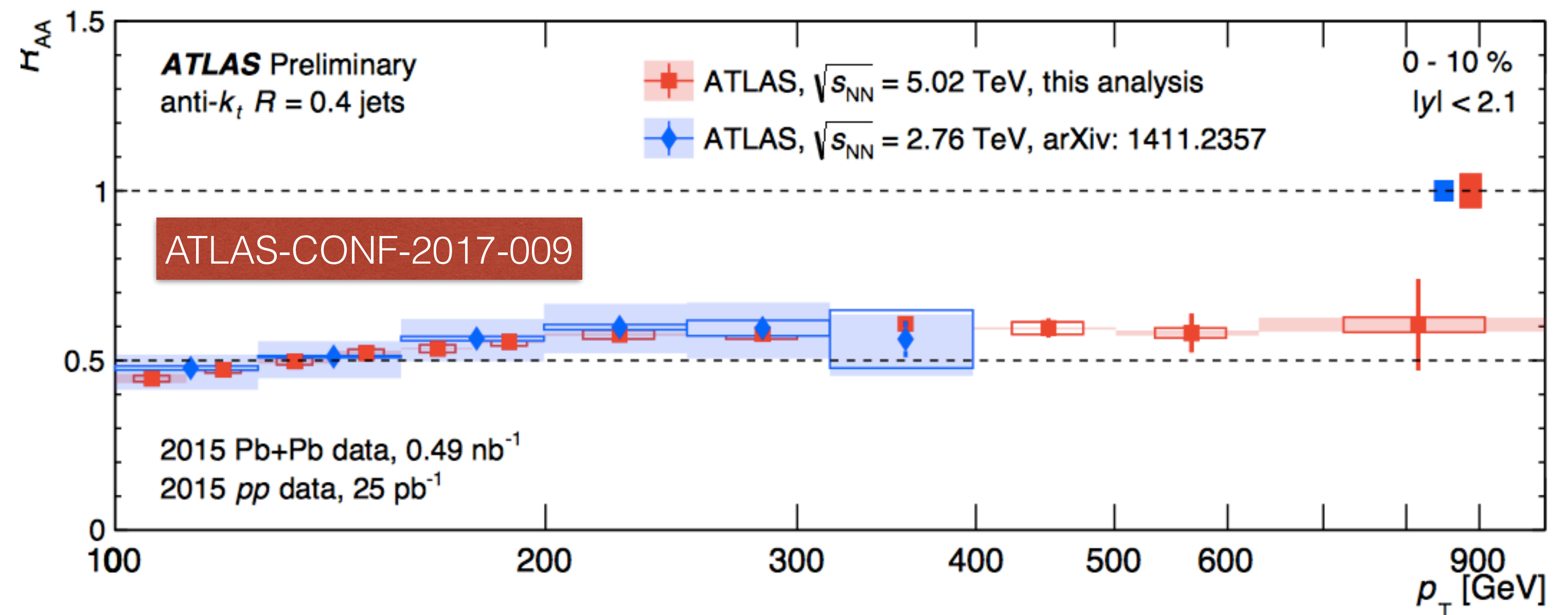
→ Energy and momentum deposited in the QGP **hydrodynamize** quickly;

- Compute modified hadron spectrum from perturbed freeze-out hyper-surface.
- Produce soft, thermal particles correlated with jet direction.

# Jet vs Hadron Suppression

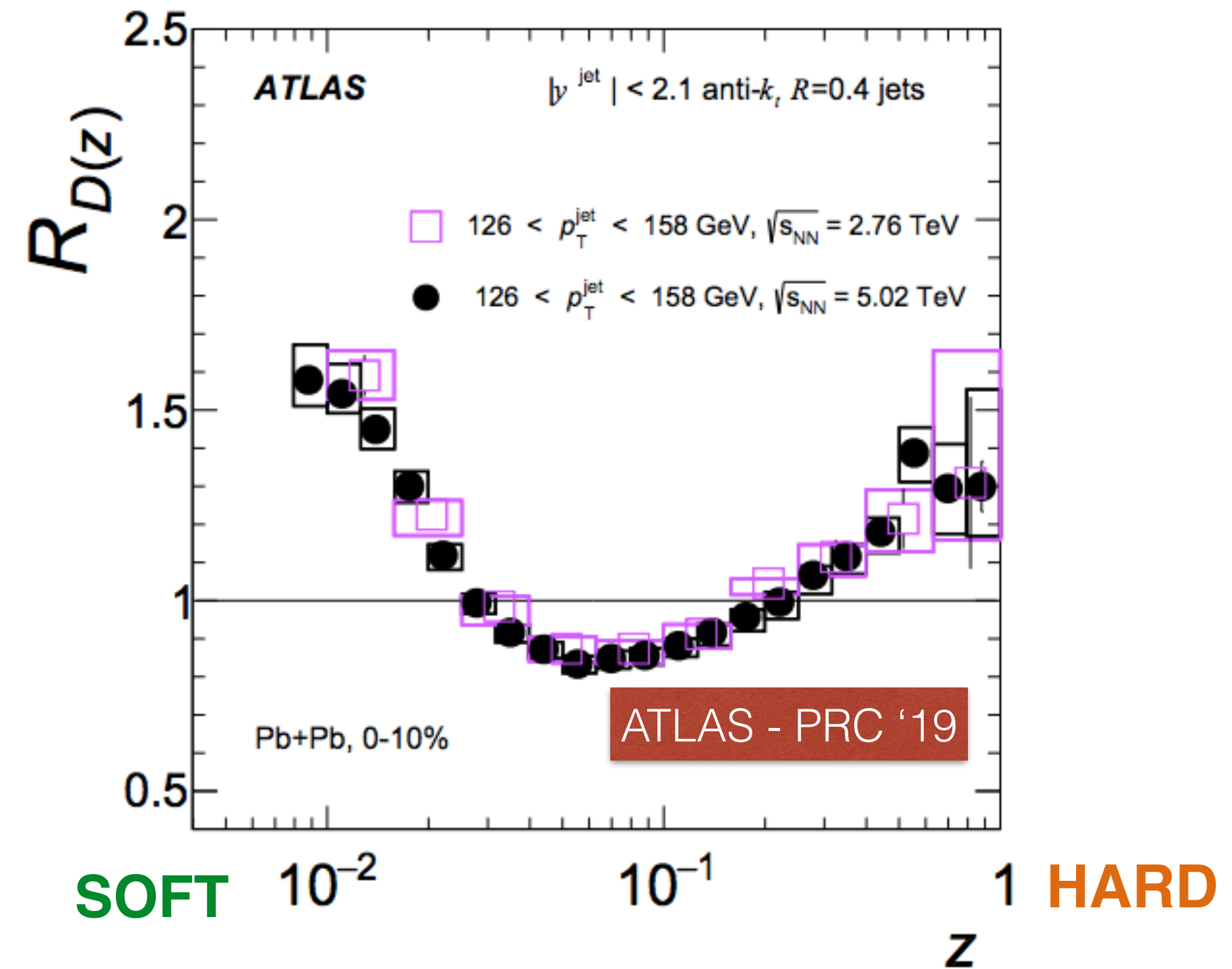
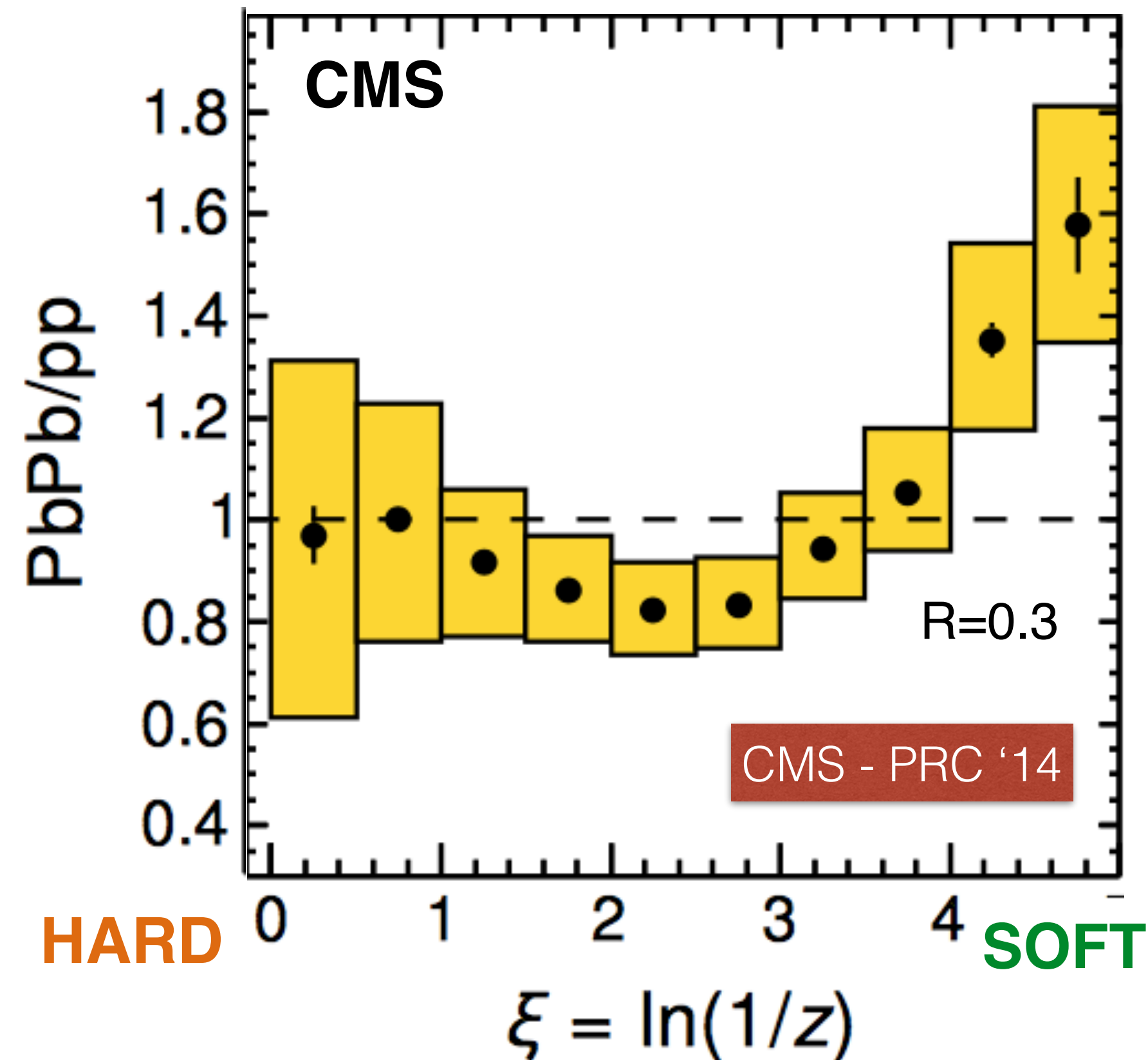


Precise data available up to very high momentum



- ➔ How to understand high momentum behaviour?
- ➔ Different asymptotic trend for jets than for hadrons?

# Jet Fragmentation Functions (FFs)



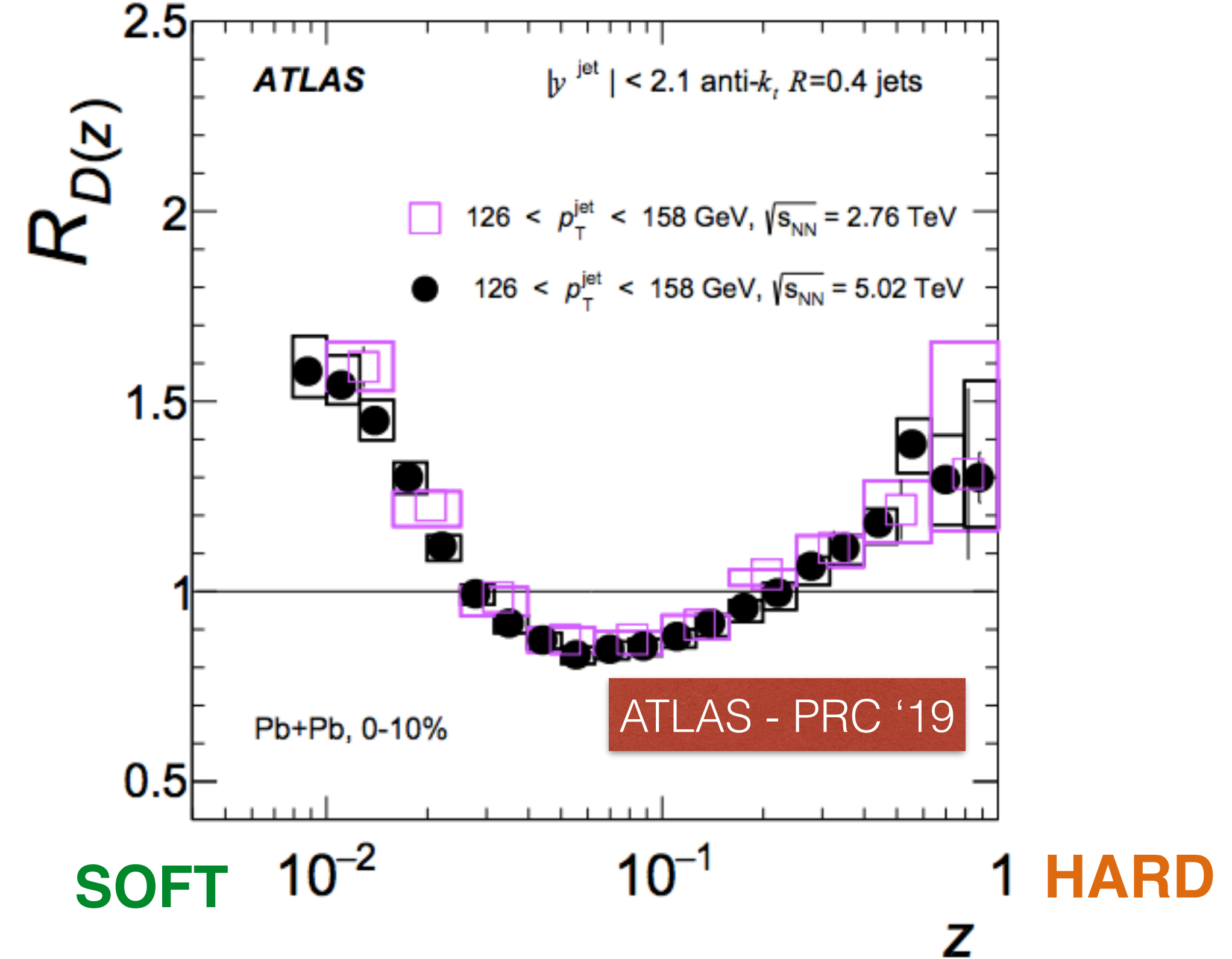
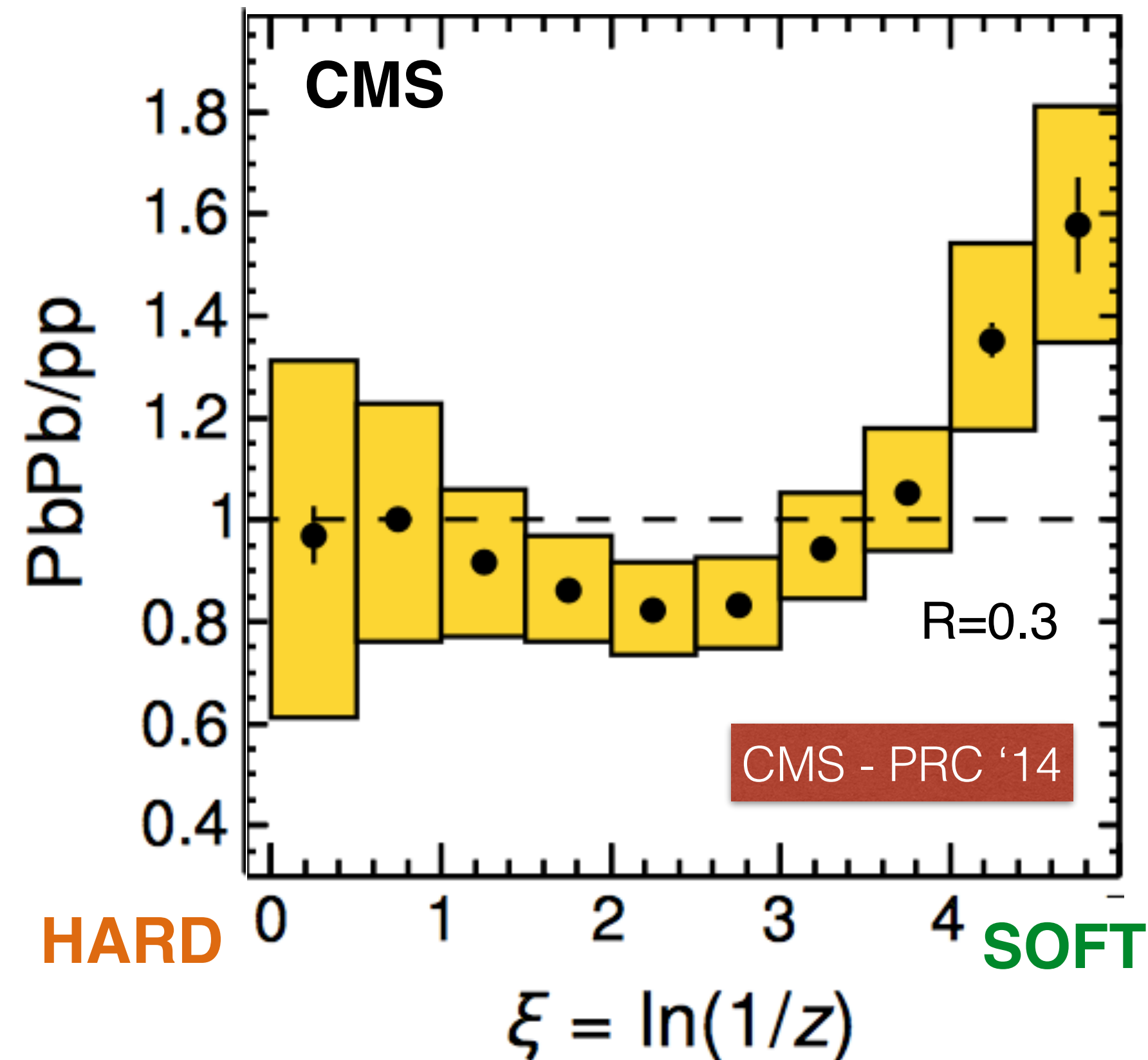
**Jet FFs count the number of hadrons, per jet, with an energy fraction  $z$**

**Soft particle enhancement w.r.t. pp jets**

- ➔ Medium back-reaction to deposited energy & momentum Pablos et al. - JHEP '17 He et al. - PRC '15
- ➔ Antenna decoherence breaks angular ordering Mehtar-Tani et al. - PLB '12 Caucal et al. - 2005.05852



# Jet Fragmentation Functions (FFs)



**Jet FFs count the number of hadrons, per jet, with an energy fraction  $z$**

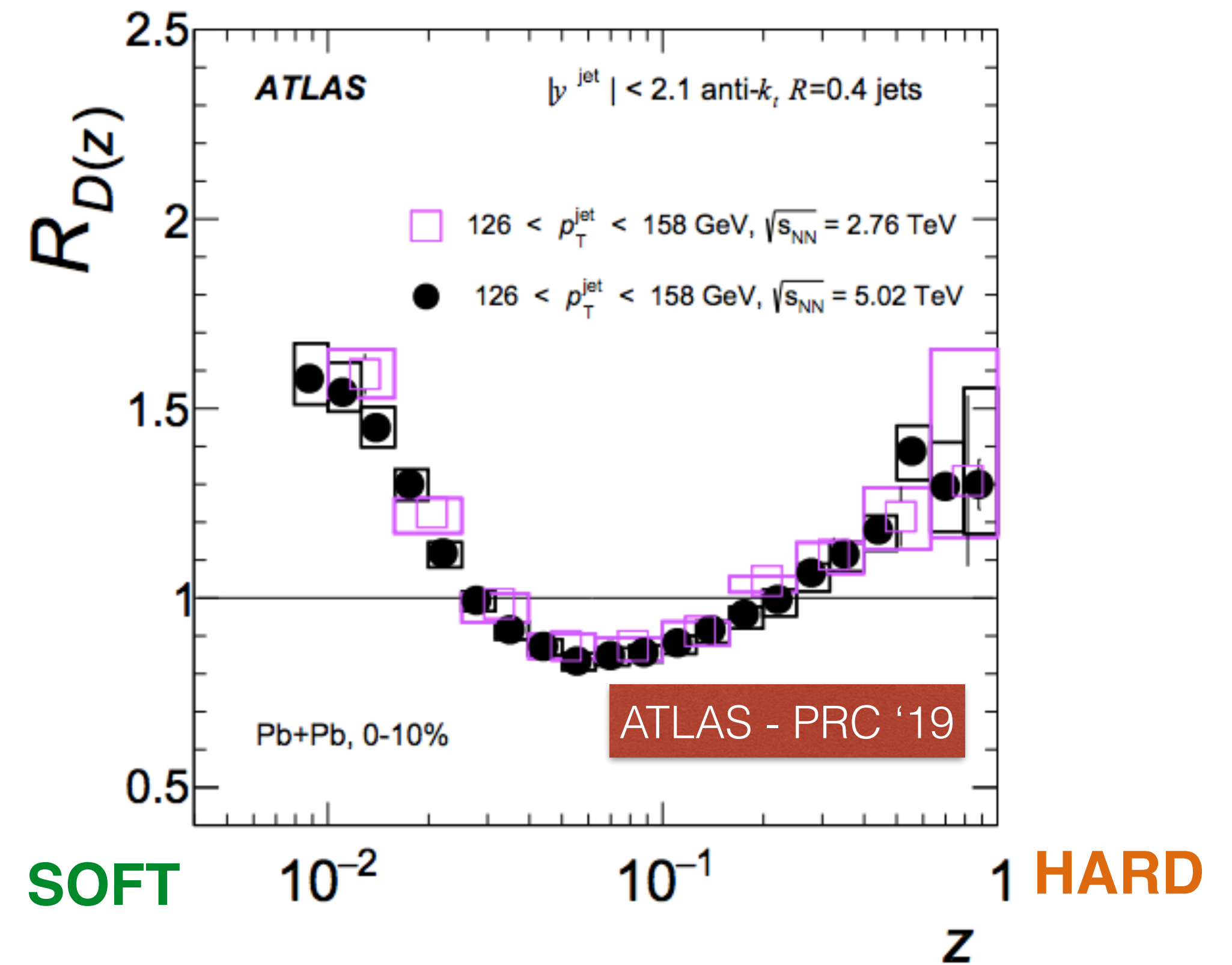
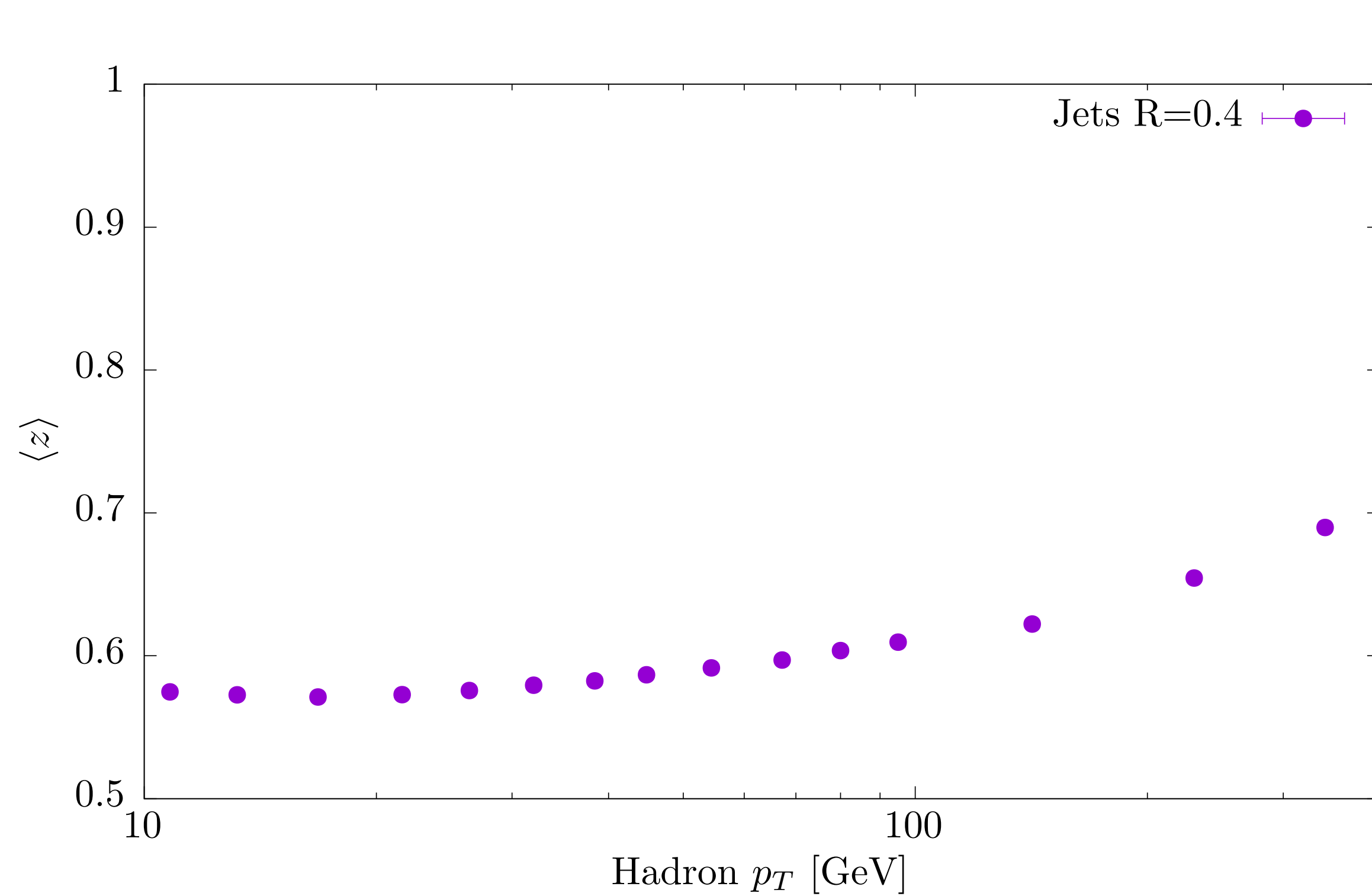
Hard particle enhancement w.r.t. pp jets

Steeply falling jet spectrum



High  $p_T$  hadron spectrum dominated by leading tracks (from hard fragmenting jets)

# Jet Fragmentation Functions (FFs)

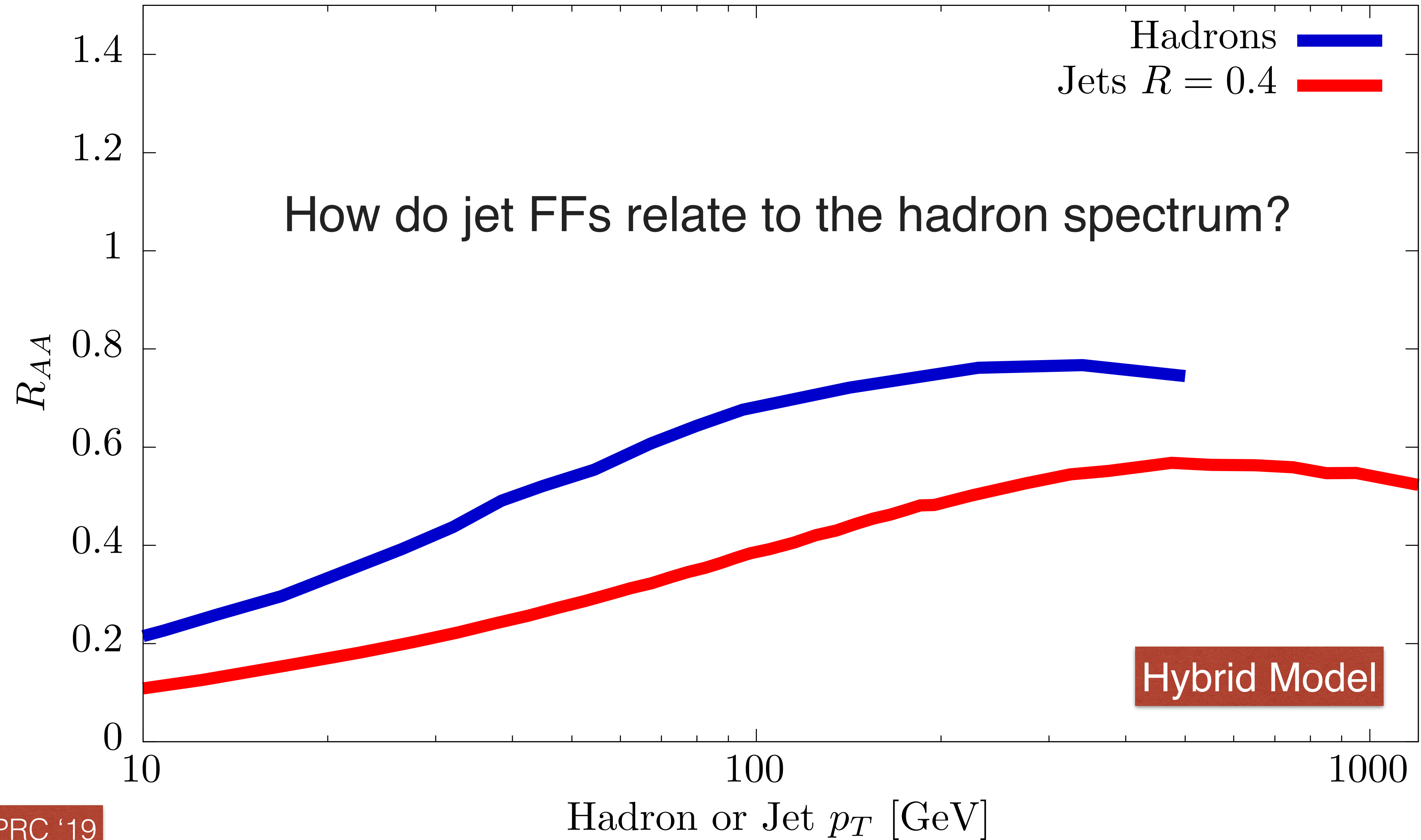


**Jet FFs count the number of hadrons, per jet, with an energy fraction  $z$**

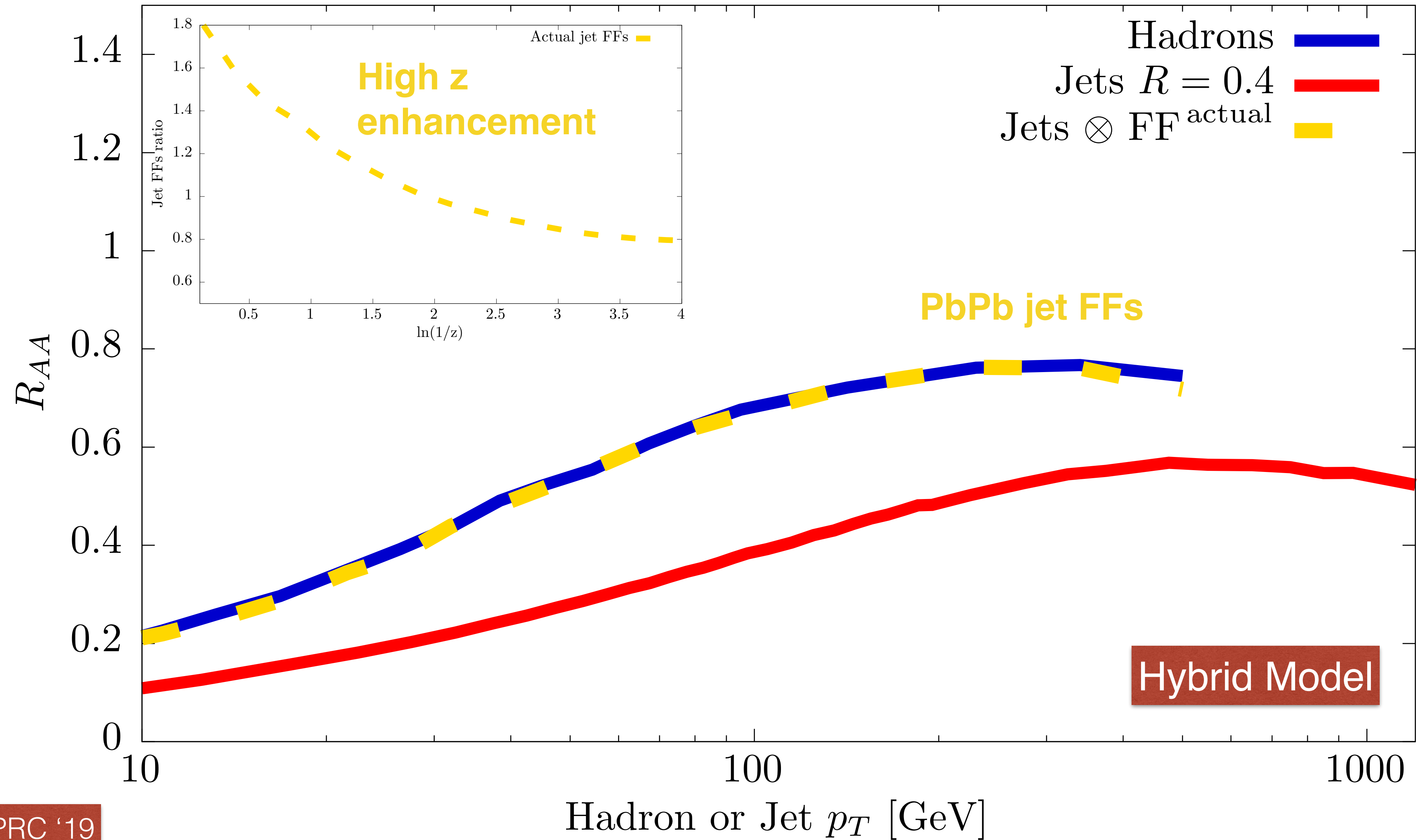
Hard particle enhancement w.r.t. pp jets

High  $z$  region of jet FFs closely related to hadronic spectrum

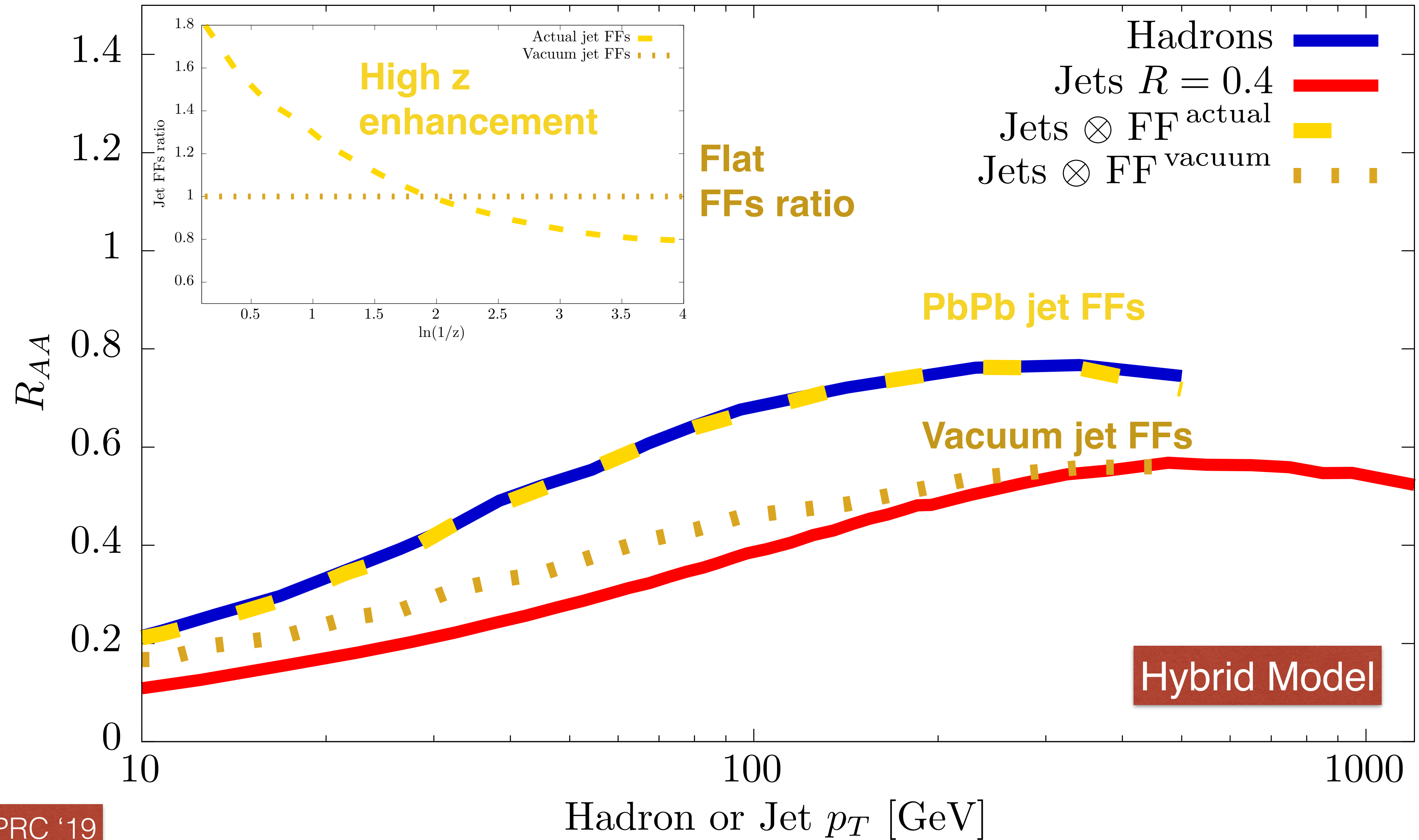
# Jets, their FFs, and hadrons



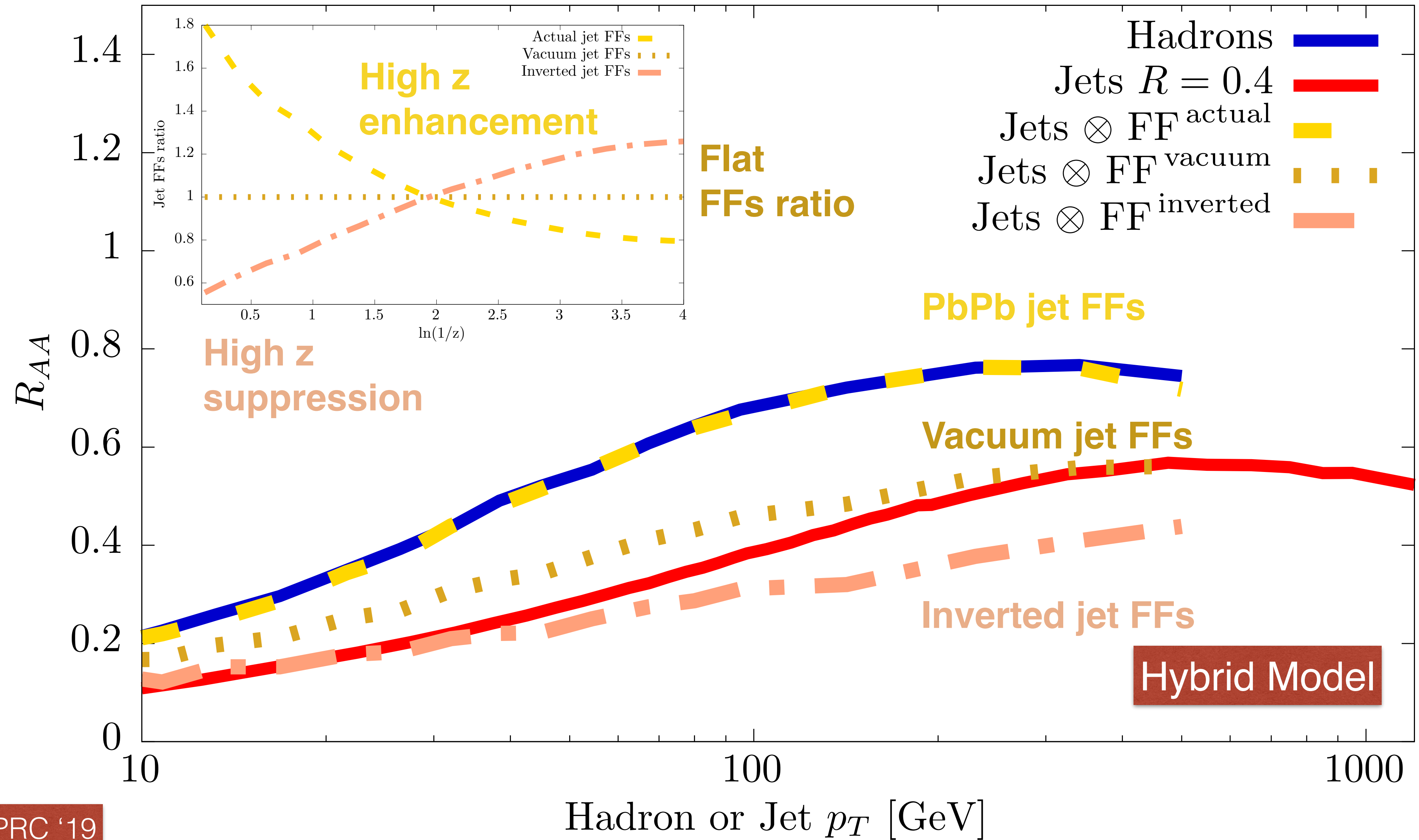
# Jets, their FFs, and hadrons



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# Jets, their FFs, and hadrons



# Jet narrowing: a selection bias

Wider, more active jets lose more energy than narrower, hard fragmenting ones

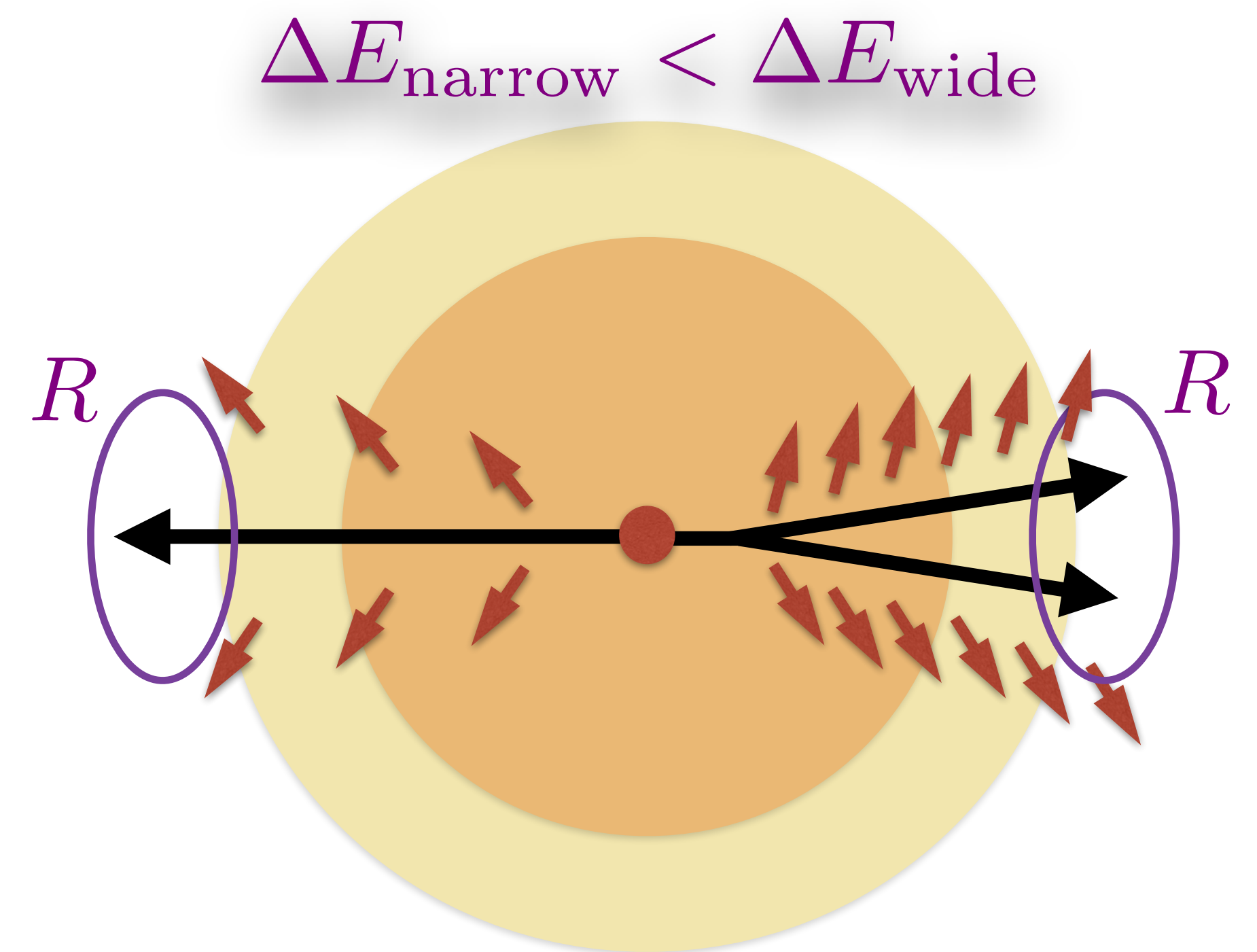
Steeply falling jet spectrum



bias inclusive jet sample to narrower ones,  
explains high z enhancement

High  $p_T$  hadrons belong to such subsample of  
narrow jets, which get less quenched,

and so  $R_{AA}^{had} > R_{AA}^{jet}$



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Steeply falling jet spectrum

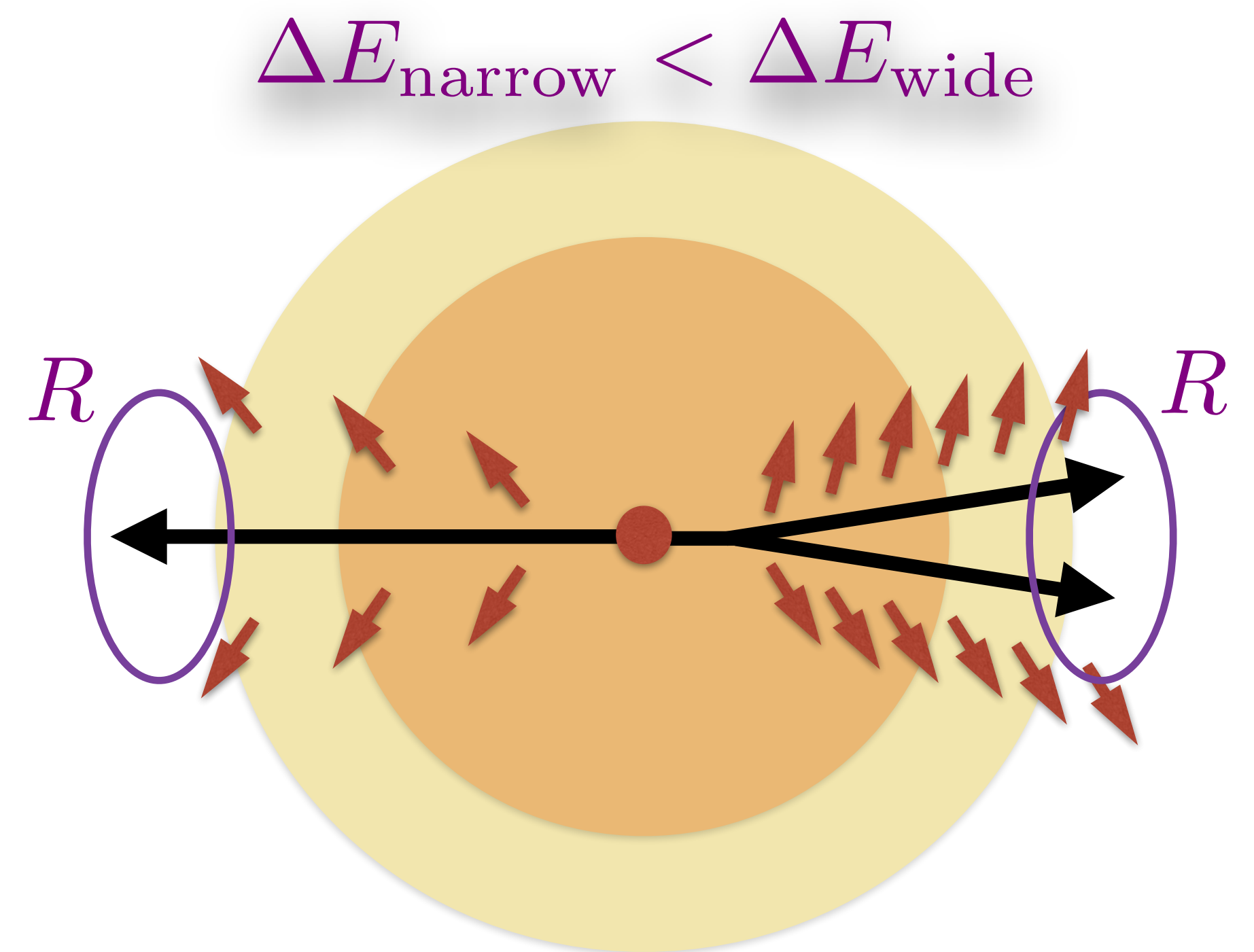


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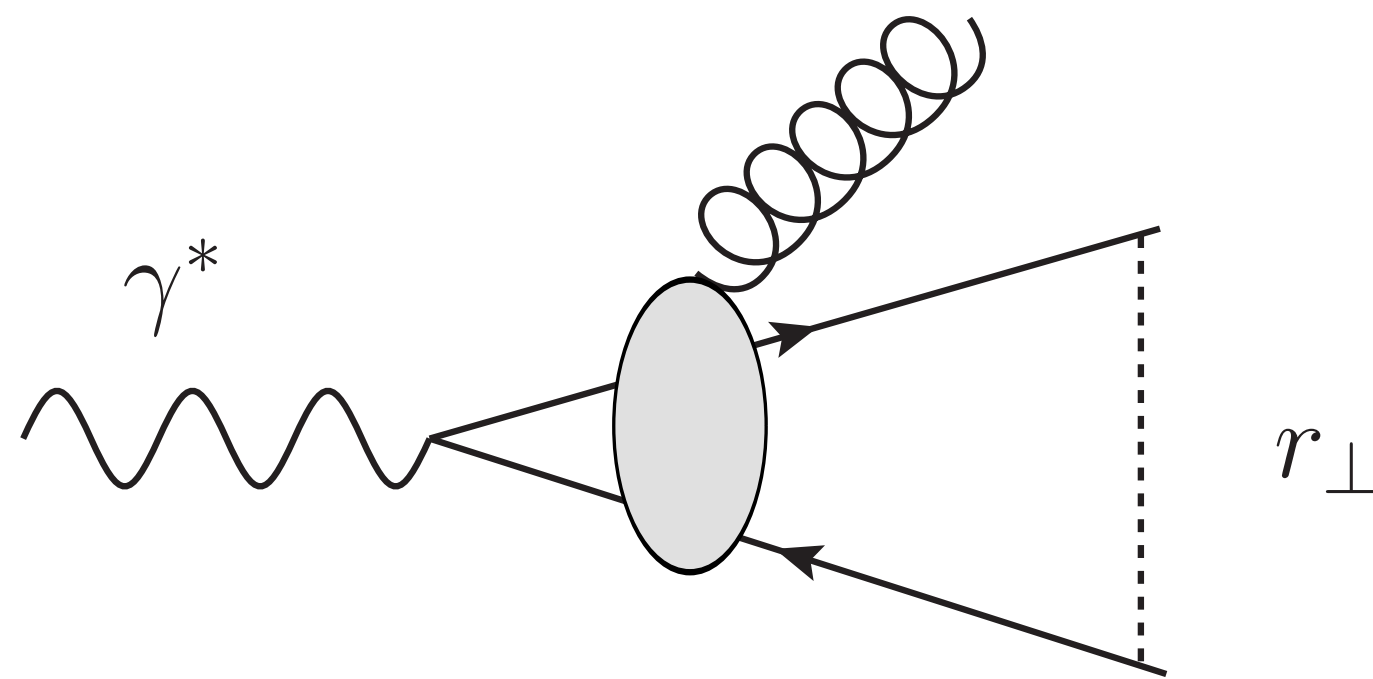
But, how well does the QGP  
resolve the internal  
structure of the jet?





# Coherence in Vacuum: Heuristic Interpretation

Need to think in terms of the *formation time*



Time at which the gluon decorrelates from the quark:

$$\tau_f = \frac{\omega}{k_{\perp}^2} = \frac{1}{\omega\theta^2}$$

- Transverse size of the gluon is
- Size of the antenna when the gluon is being emitted

$$\lambda_{\perp} \sim \frac{1}{k_{\perp}} = \frac{1}{\omega\theta}$$

$$r_{\perp} = \theta_{q\bar{q}}\tau_f = \frac{\theta_{q\bar{q}}}{\omega\theta^2}$$

Compare the two:

→ If  $r_{\perp} < \lambda_{\perp}$  the gluon cannot resolve the pair: coherent  
No emission (color singlet)

$$\frac{r_{\perp}}{\lambda_{\perp}} < 1 \rightarrow \theta_{q\bar{q}} < \theta_q$$

→ If  $r_{\perp} > \lambda_{\perp}$  independent emission by quark and antiquark

$$\frac{r_{\perp}}{\lambda_{\perp}} > 1 \rightarrow \theta_{q\bar{q}} > \theta_q$$

# Coherence in Vacuum: Heuristic Interpretation

Need to think in terms

Time at which the gluon decorrelates from the quark:

For medium induced emissions:

- Typical wavelength determined by interaction potential:

- Dilute medium: Debye mass

- Dense medium: Accumulated momentum  $\hat{q}L$

- Color correlation can be lost through multiple scatterings.

→ If  $r_{\perp} > \lambda_{\perp}$  independent emission by quark and antiquark  $\frac{r_{\perp}}{\lambda_{\perp}} > 1 \rightarrow \theta_{q\bar{q}} > \theta_q$

# The QGP Resolution Length

QGP resolution length:

minimal distance between two coloured charges such that they engage with the plasma independently.



The medium perceives a parton shower as a **collection of effective probes**.

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The medium perceives a parton shower as a **collection of effective probes**.

## At weak coupling:

connection between resolution length and energy loss.

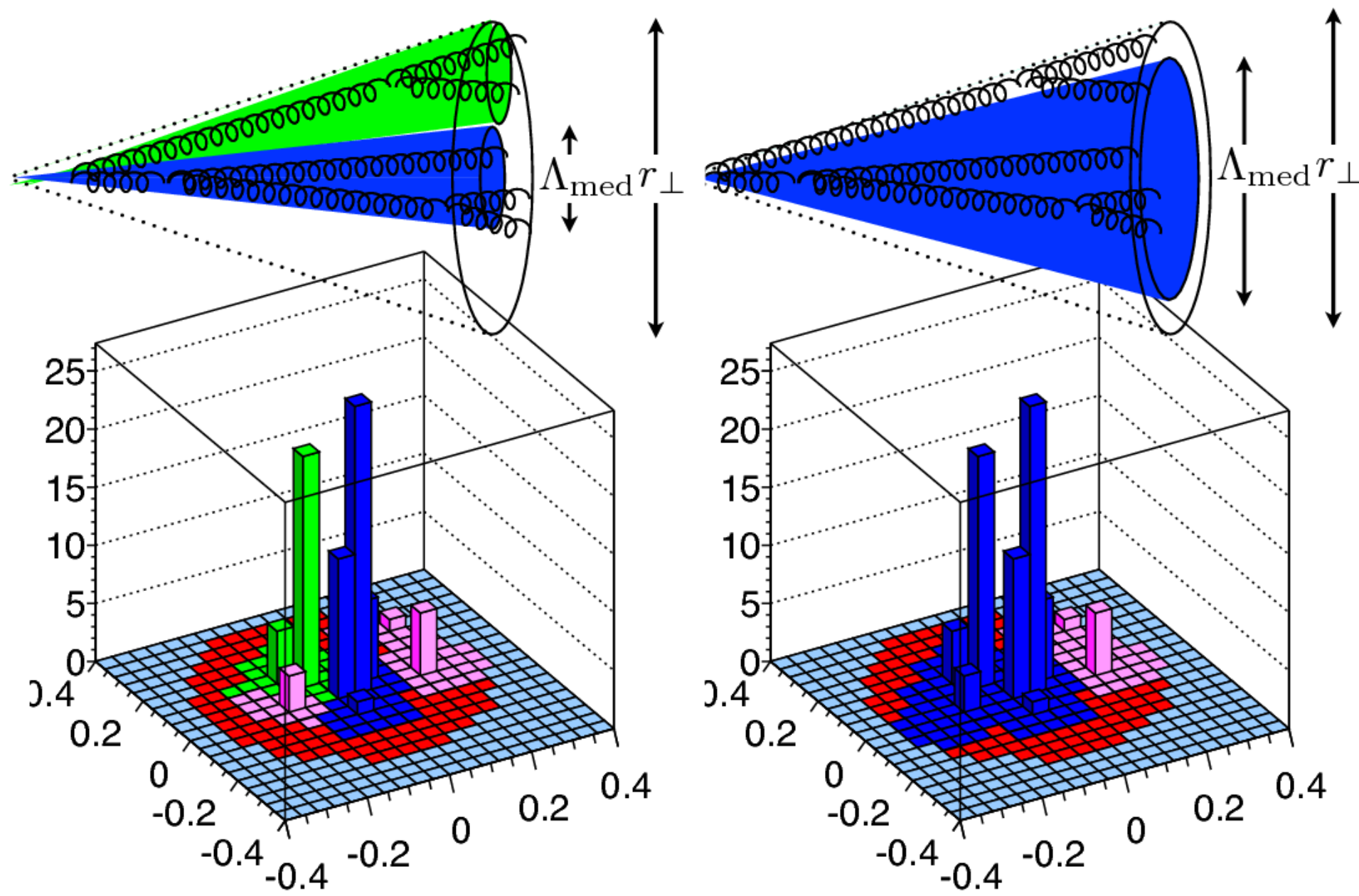
## At strong coupling:

no such connection (yet).

## In the hybrid model:

resolution length proportional to the Debye screening length of QGP.

$$L_{\text{res}} \sim \lambda_D$$



# Two extreme scenarios

Look for sensitivity of observables to  $L_{\text{res}}$  :

Take two extreme values for  $L_{\text{res}}$

(explore realistic values later on)

- $L_{\text{res}} = 0$  fully **resolved** case
- $L_{\text{res}} = \infty$  fully **unresolved** case

# Two extreme scenarios

Look for sensitivity of observables to  $L_{\text{res}}$ :

Take two extreme values for  $L_{\text{res}}$   
(explore realistic values later on)

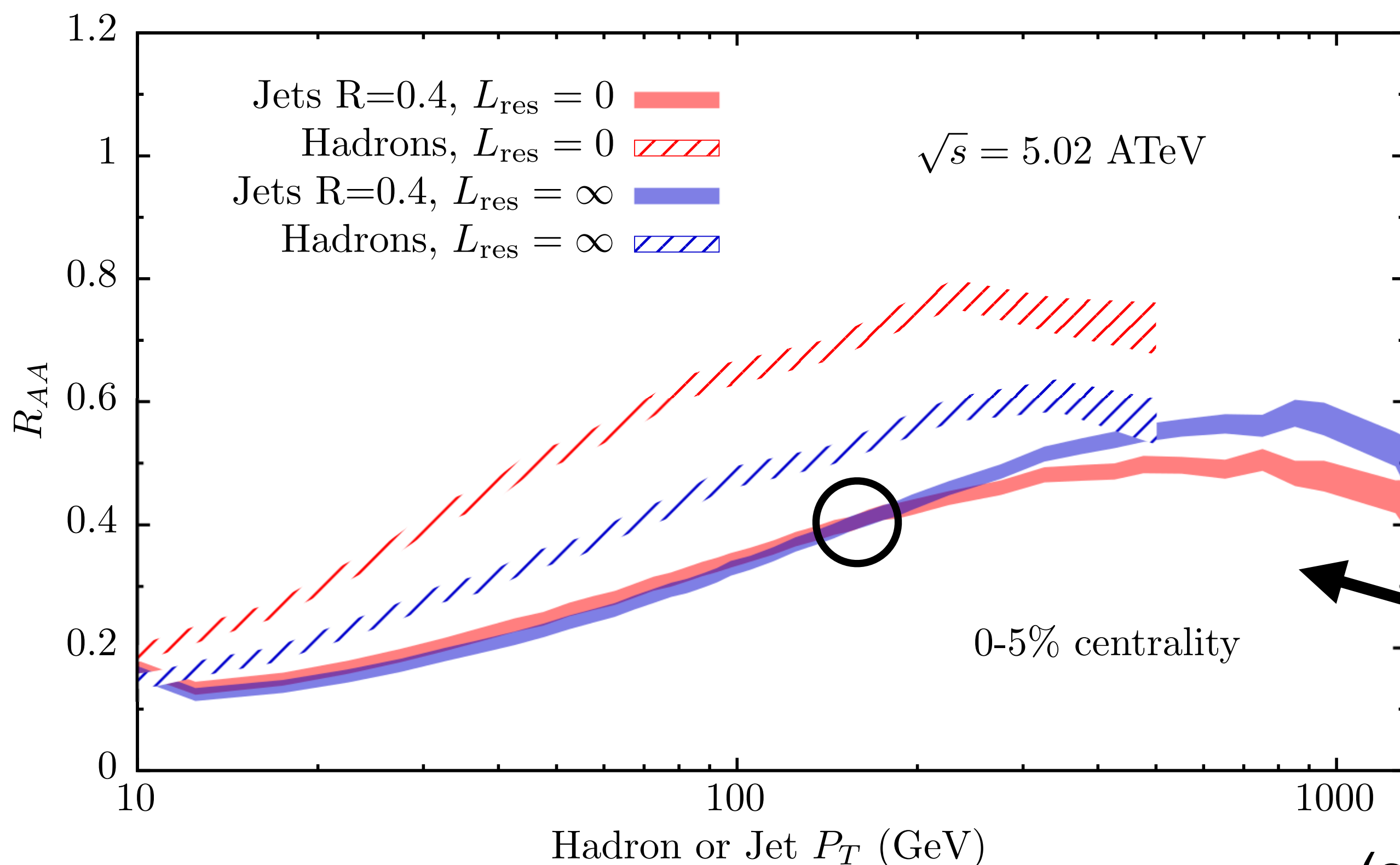
- $L_{\text{res}} = 0$  fully **resolved** case
- $L_{\text{res}} = \infty$  fully **unresolved** case

Amount of *jet* quenching depends on  $L_{\text{res}}$

→ Adjust value of  $\kappa_{\text{SC}}$  to compare results at the same value of jet RAA

$L_{\text{res}} = 0$ (global fit)	$L_{\text{res}} = \infty$ (adjusted)
$0.404 < \kappa_{\text{SC}} < 0.423$	$0.5 < \kappa_{\text{SC}} < 0.52$

Relative suppression of hadrons vs jets strongly depends on QGP resolution length.



(see [Pablos et al. - PRC '19](#) and [Mehtar-Tani & Tywoniuk - PRD '18](#))

# Soft Drop

Soft Drop (SD) procedure in a nutshell:

1. Reconstruct jet with anti- $k_T$ .
2. Recluster jet with **Cambridge-Aachen**.
3. Go back **clustering history**, store  $\mathbf{z}$  and  $\Delta\mathbf{R}$  of each pair of branches.

# Soft Drop

Soft Drop (SD) procedure in a nutshell:

Larkoski et al. - JHEP '14, PRD '15

1. Reconstruct jet with anti- $k_T$ .
2. Recluster jet with **Cambridge-Aachen**.
3. Go back **clustering history**, store  $\mathbf{z}$  and  $\Delta\mathbf{R}$  of each pair of branches.

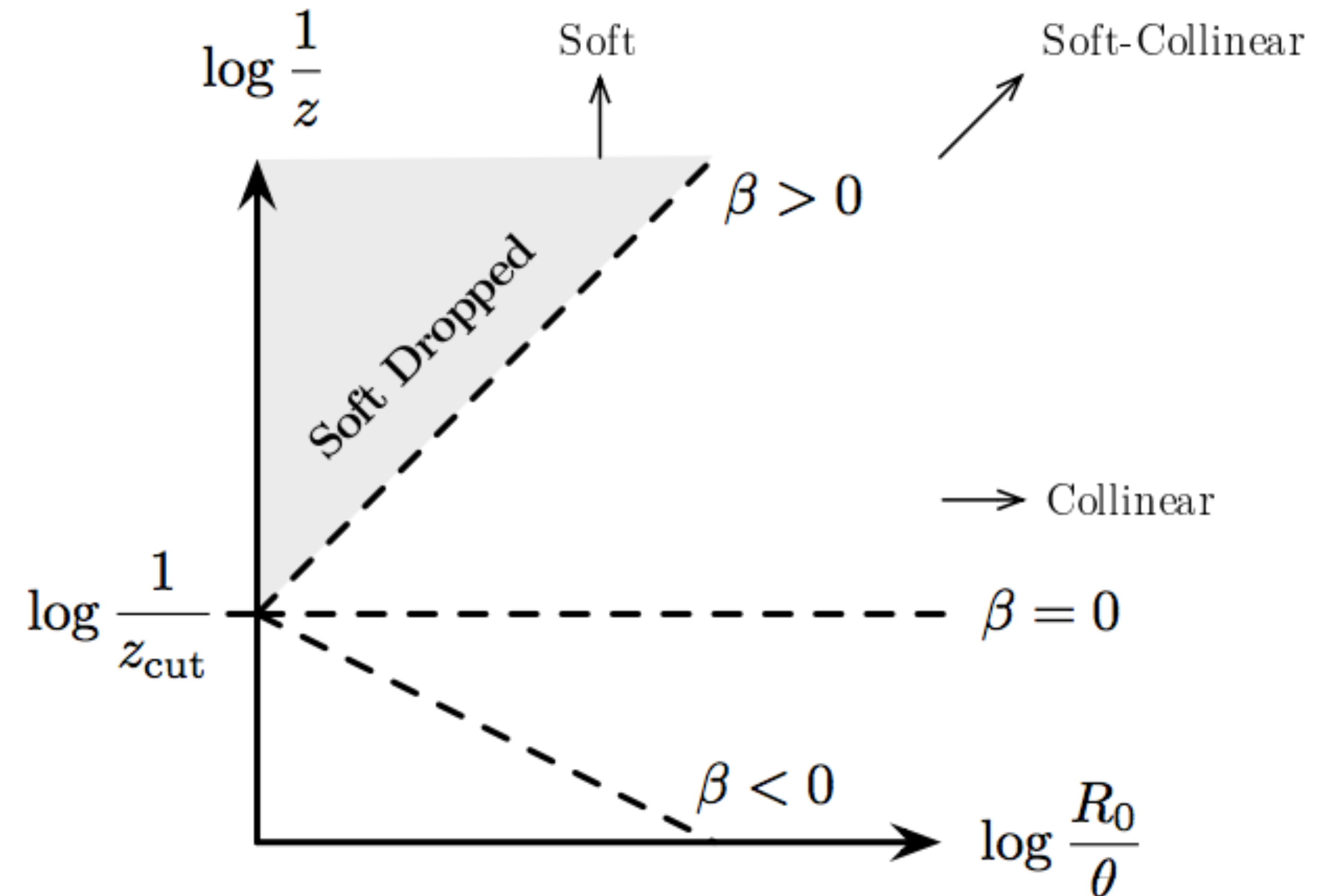
➔ If stop at first step that satisfies SD condition:

## 1st SD “splitting”

- study such 1st “splitting”
- study groomed jet properties

Soft Drop condition:

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} > z_{\text{cut}} \left( \frac{R_{12}}{R_0} \right)^\beta$$





# Soft Drop

Soft Drop (SD) procedure in a nutshell:

1. Reconstruct jet with anti- $k_T$ .
2. Recluster jet with **Cambridge-Aachen**.
3. Go back **clustering history**, store  $\mathbf{z}$  and  $\Delta R$  of each pair of branches.

→ If stop at first step that satisfies SD condition:

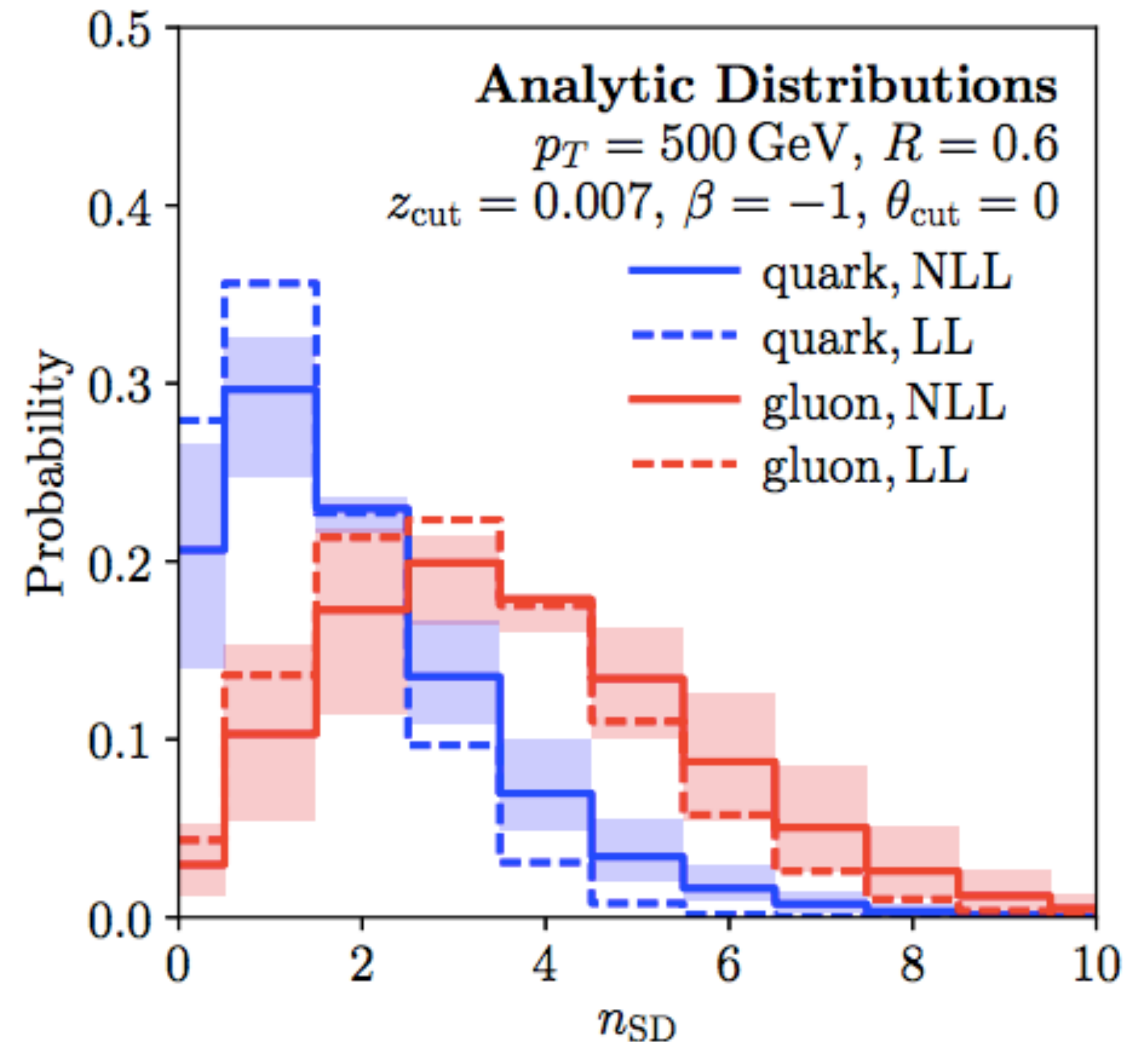
## 1st SD “splitting”

- study such 1st “splitting”
- study groomed jet properties

→ If count all “splittings” that satisfy SD condition:  
(following the hardest branch, i.e. Iterative SD)

**# SD “splittings”,  $n_{SD}$**

Frye et al. - JHEP '17



# # SD Splittings

**Flat** grooming setup:

$$z_{\text{cut}} = 0.1 \quad \beta = 0$$

$$L_{\text{res}} = 0$$

reduction of  $n_{\text{SD}}$

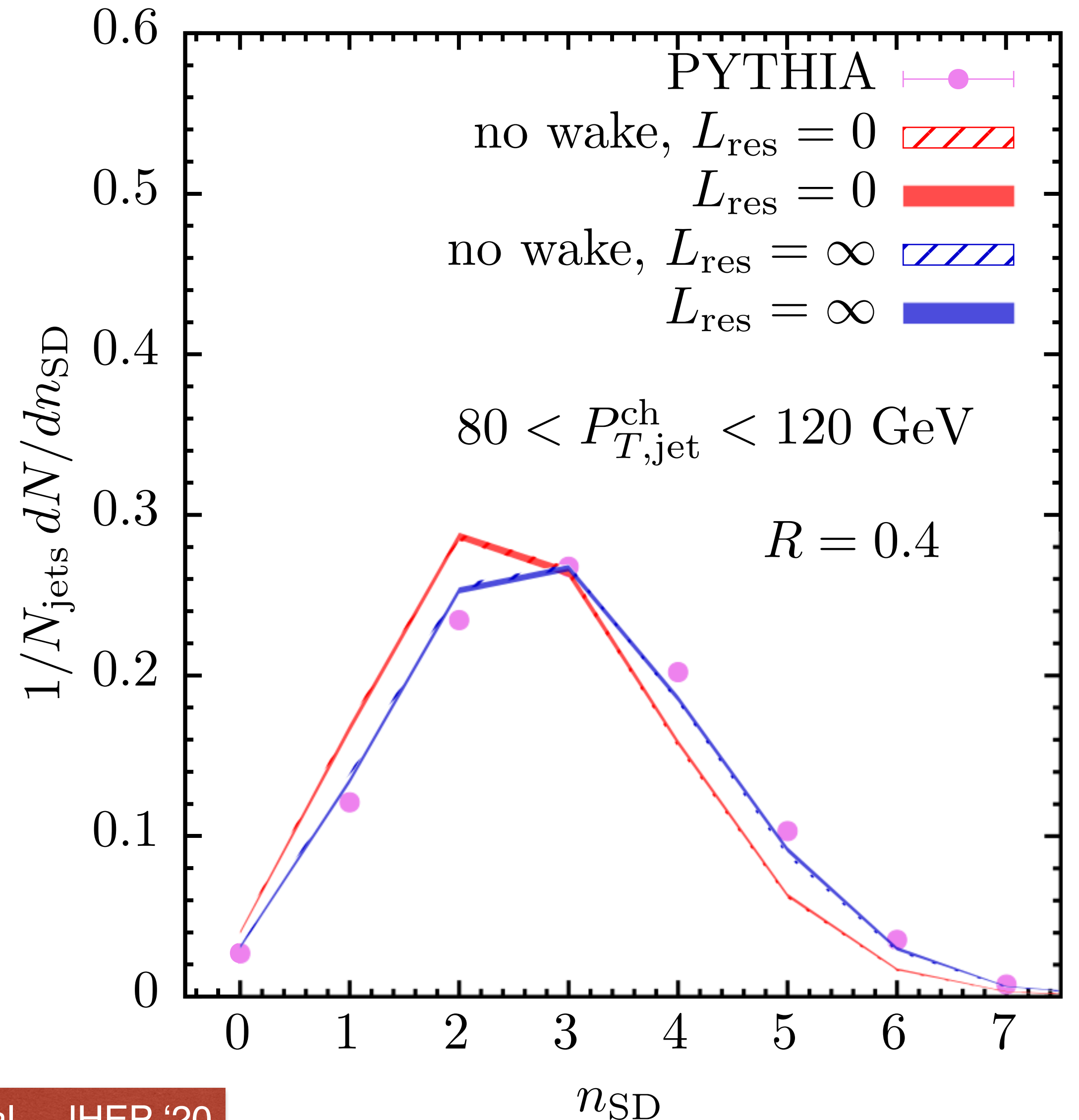
$$L_{\text{res}} = \infty$$

barely any modification

Remove soft &  
soft-collinear

Wake negligible.

Jets with higher multiplicity  
are more suppressed, ensemble  
biased towards less active ones if  
substructure is resolved.

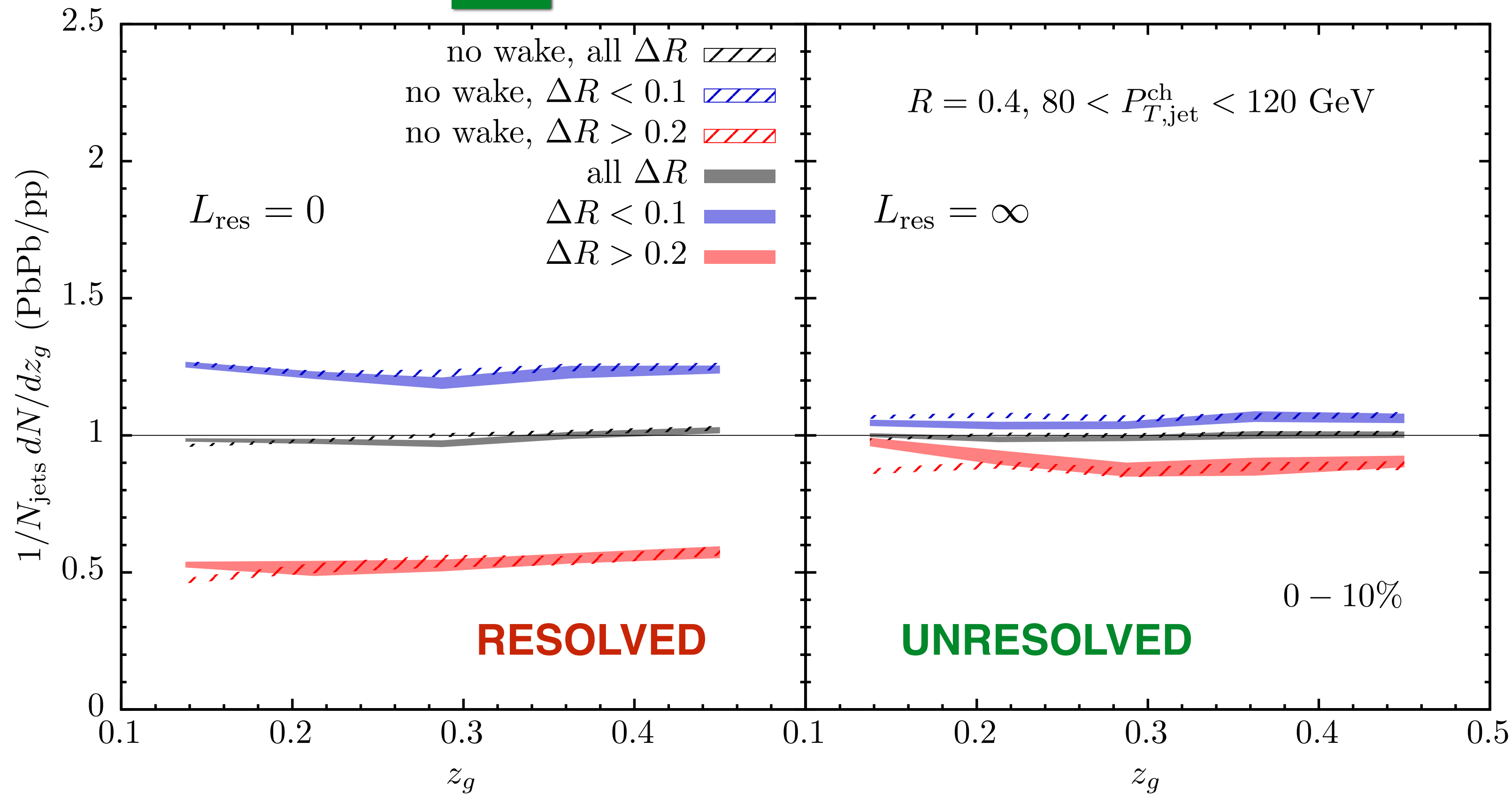


(also a subleading effect from “per jet” energy loss, see back-up)

Pablos et al. - JHEP '20

# 1st SD splitting $z_g$ vs $\Delta R$

**Flat**  $z_{\text{cut}} = 0.1$   $\beta = 0$



Strong ordering in  $\Delta R$   
(if parton shower resolved).

Larger  $\Delta R$ ;



Larger phase-space  
for emissions;



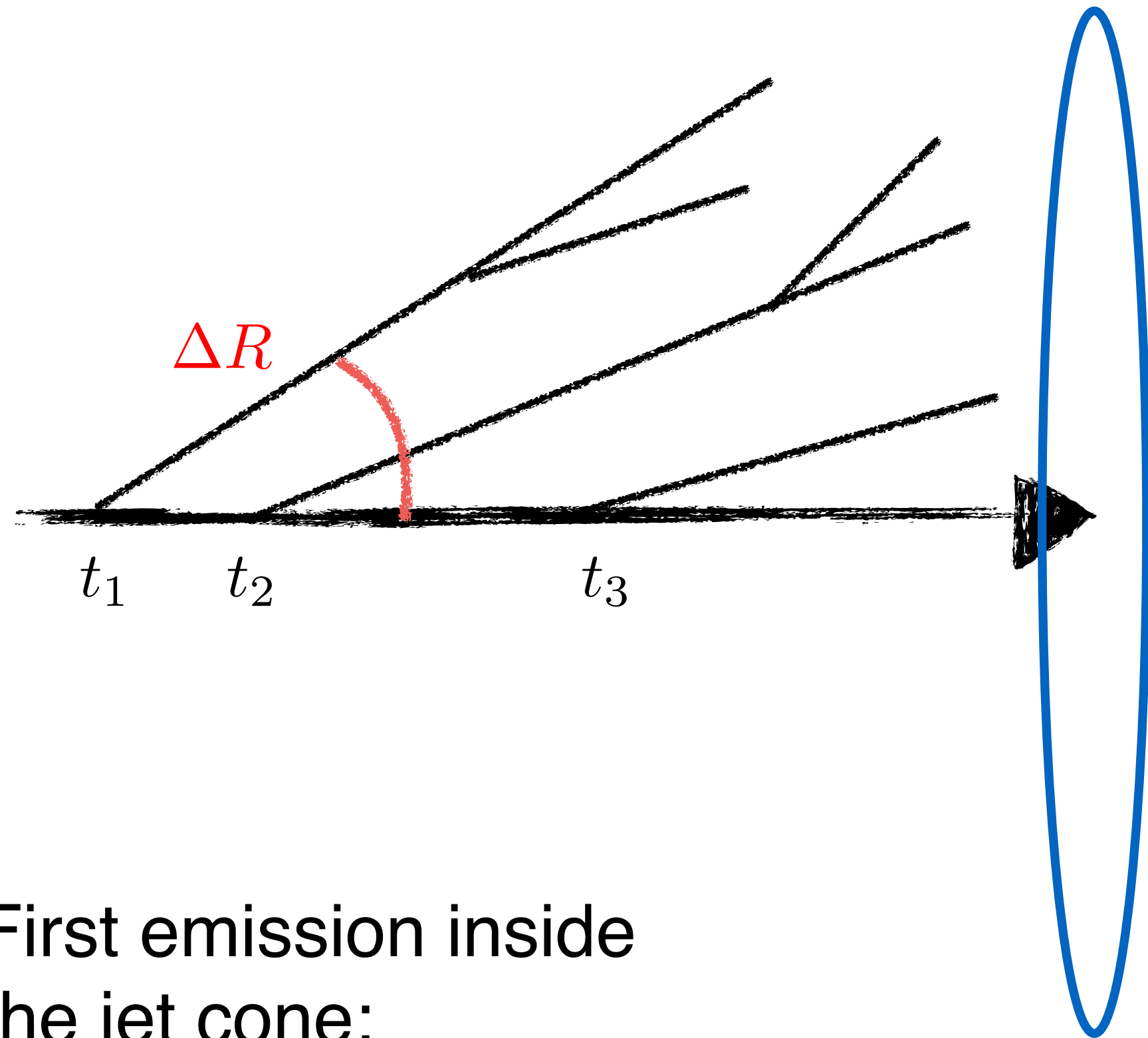
Larger quenching,  
smaller survival rate;

(almost NO effect from “per jet”  
energy loss, see back-up)

normalised to  $N_{\text{jets}}$

# Jets and Jets (again)

Wide jet



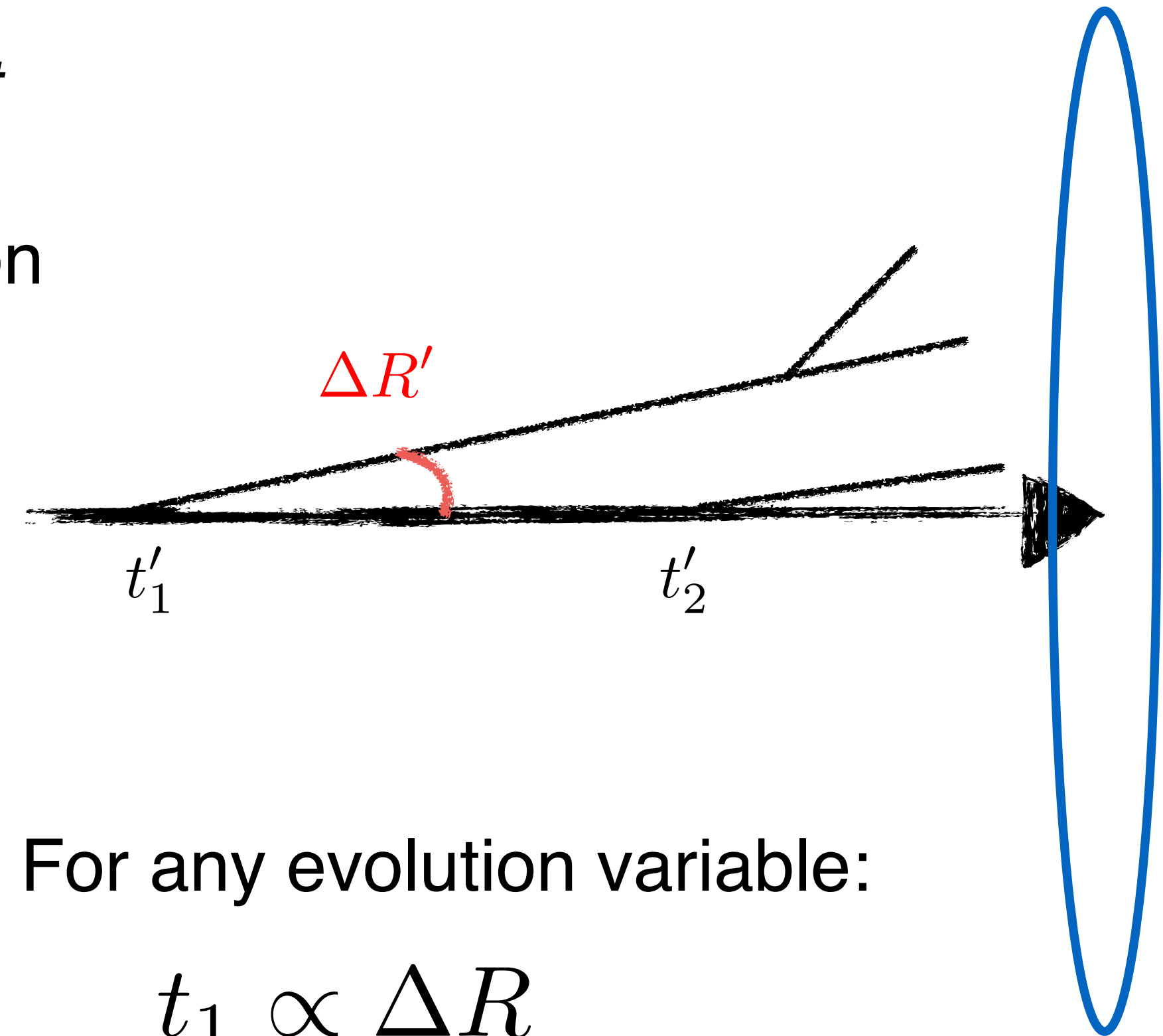
First emission inside the jet cone:

- If high, increased probability for further emissions
- If low, decreased probability for further emissions

Scale of emission  $t$  sampled from Sudakov distribution

$$t_1 > t'_1$$

Narrow jet



For any evolution variable:

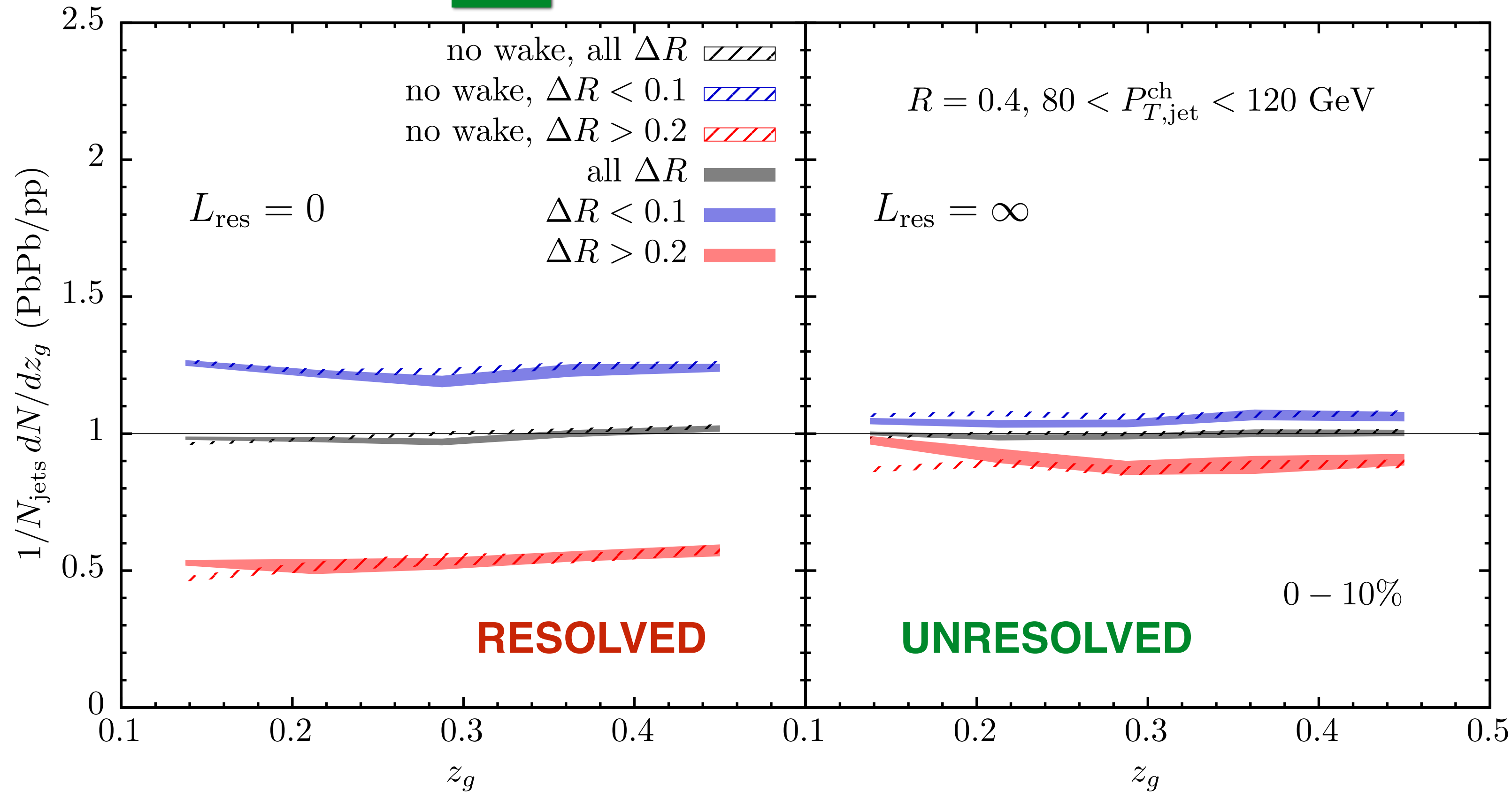
$$t_1 \propto \Delta R$$

$$t'_1 \propto \Delta R'$$

Groomed angle is proxy for jet activity

# 1st SD splitting $z_g$ vs $\Delta R$

**Flat**  $z_{\text{cut}} = 0.1$   $\beta = 0$



Strong ordering in  $\Delta R$   
(if parton shower resolved).

Larger  $\Delta R$ ;



Larger phase-space  
for emissions;



Larger quenching,  
smaller survival rate;

(almost NO effect from “per jet”  
energy loss, see back-up)

normalised to  $N_{\text{jets}}$

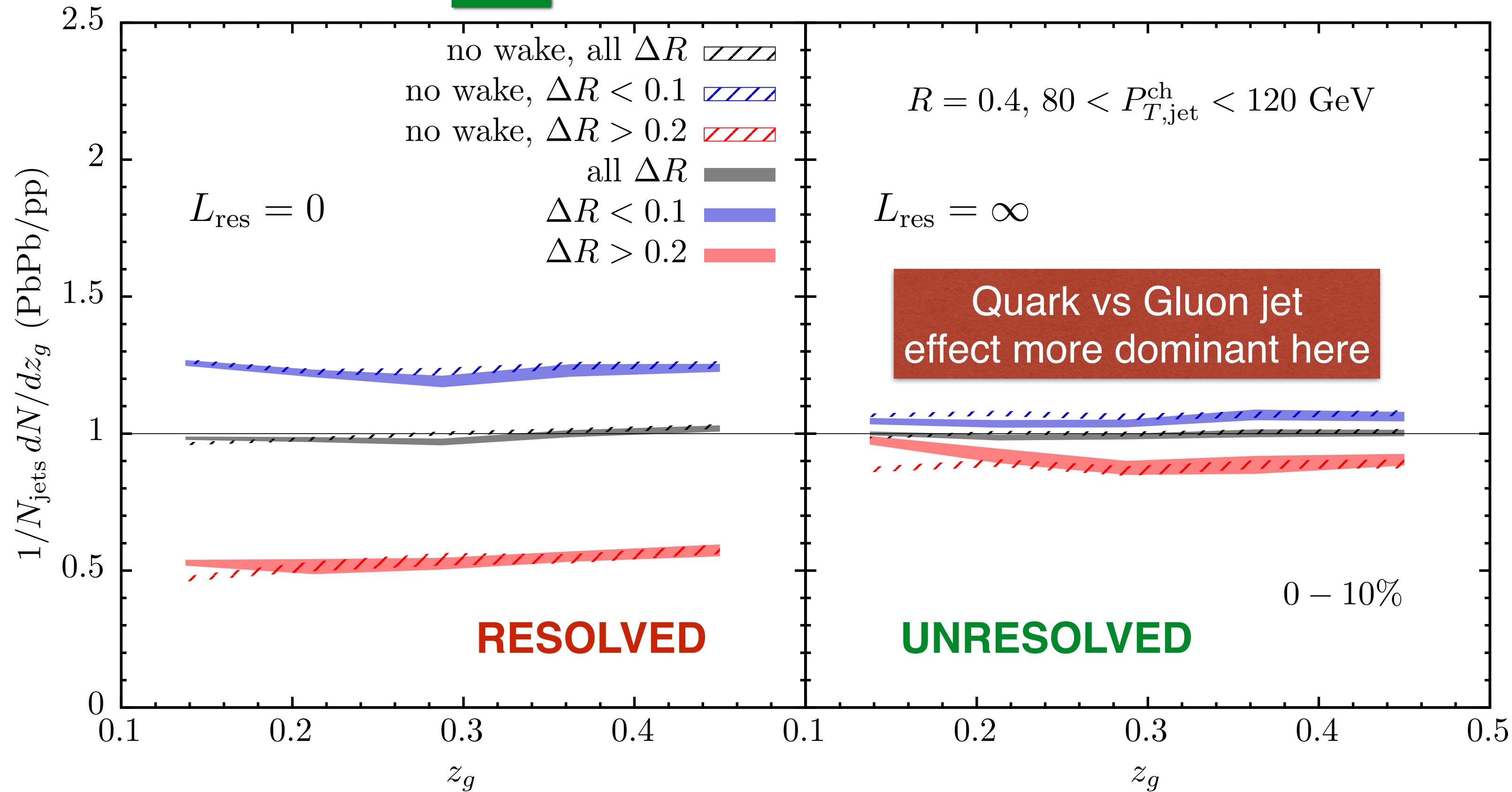
- Wake almost no effect.
- Negligible modification  $z_g$  shape.

(small incoherent energy loss  
effect visible at partonic level, see back-up)

Pablos et al. - JHEP '20

# 1st SD splitting $z_g$ vs $\Delta R$

**Flat**  $z_{\text{cut}} = 0.1$   $\beta = 0$



Strong ordering in  $\Delta R$   
(if parton shower resolved).

Larger  $\Delta R$ ;



Larger phase-space  
for emissions;



Larger quenching,  
smaller survival rate;

(almost NO effect from “per jet”  
energy loss, see back-up)

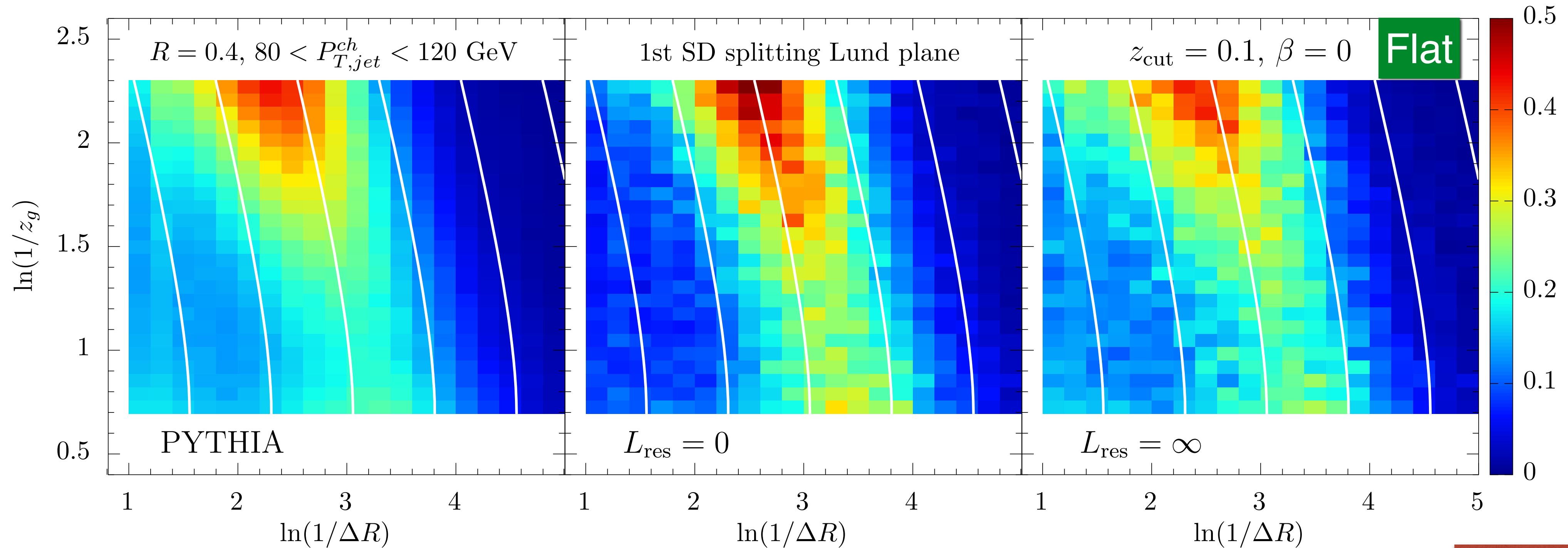
normalised to  $N_{\text{jets}}$

- Wake almost no effect.
- Negligible modification  $z_g$  shape.

(small incoherent energy loss  
effect visible at partonic level, see back-up)

Pablos et al. - JHEP '20

# 1st SD splitting Lund Plane



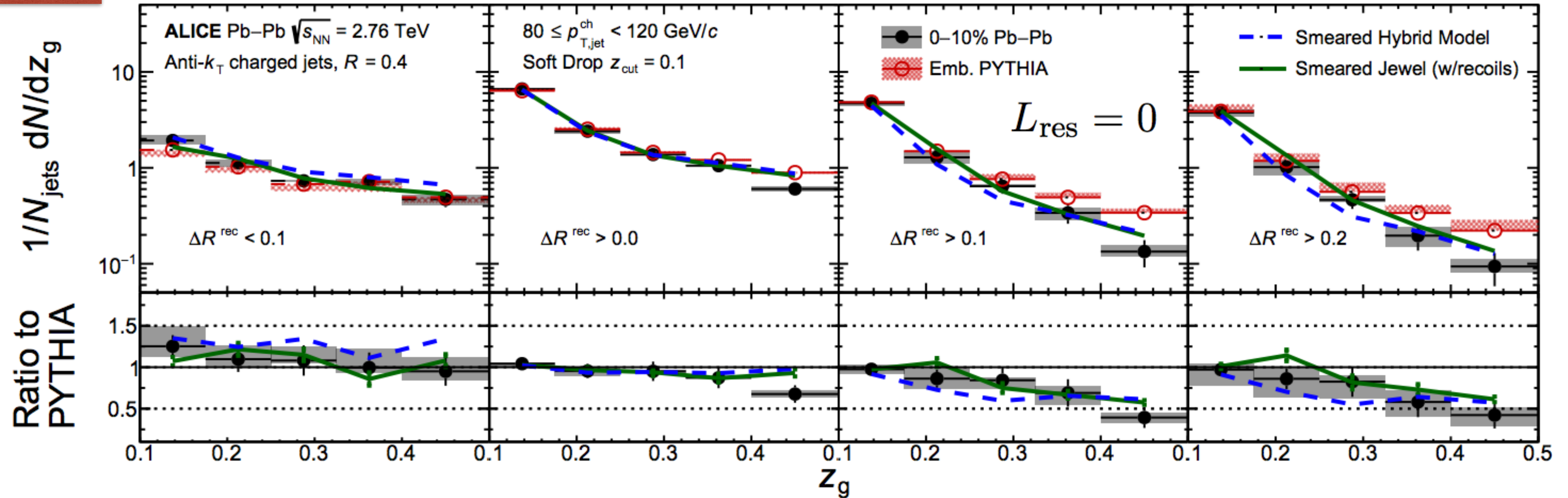
Pablos et al. - JHEP '20

If shower resolved  $\longrightarrow$  increased weight of jets with smaller (groomed) mass.

**White curves:** lines of constant  $\log(1/(M_g/p_{T,g}))$ , where  $\frac{M_g^2}{p_{T,g}^2} \simeq z_g(1 - z_g)\Delta R^2$

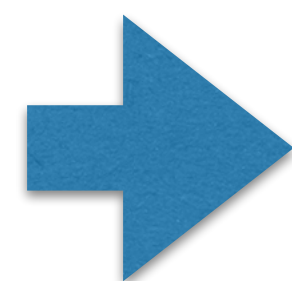
# Comparison with (not unfolded) data

ALICE - PLB '20



Low  $z_g$  enhancement arises in our model from smearing effects.

Strong ordering in  $\Delta R$  is robust under smearing effects.



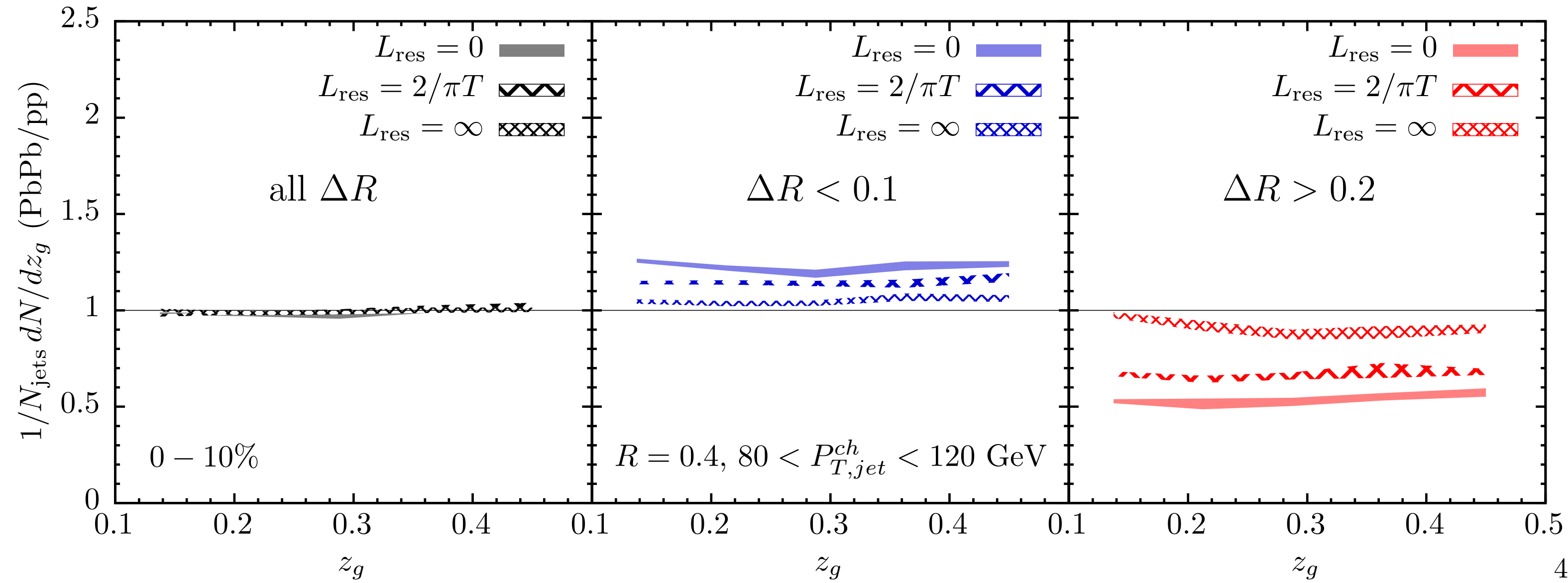
$L_{\text{res}} = \infty$  is disfavoured by data.

$z_g$  distribution, differential in  $\Delta R$ , successfully described by the Hybrid Model.





# Sensitivity to $L_{\text{res}}$

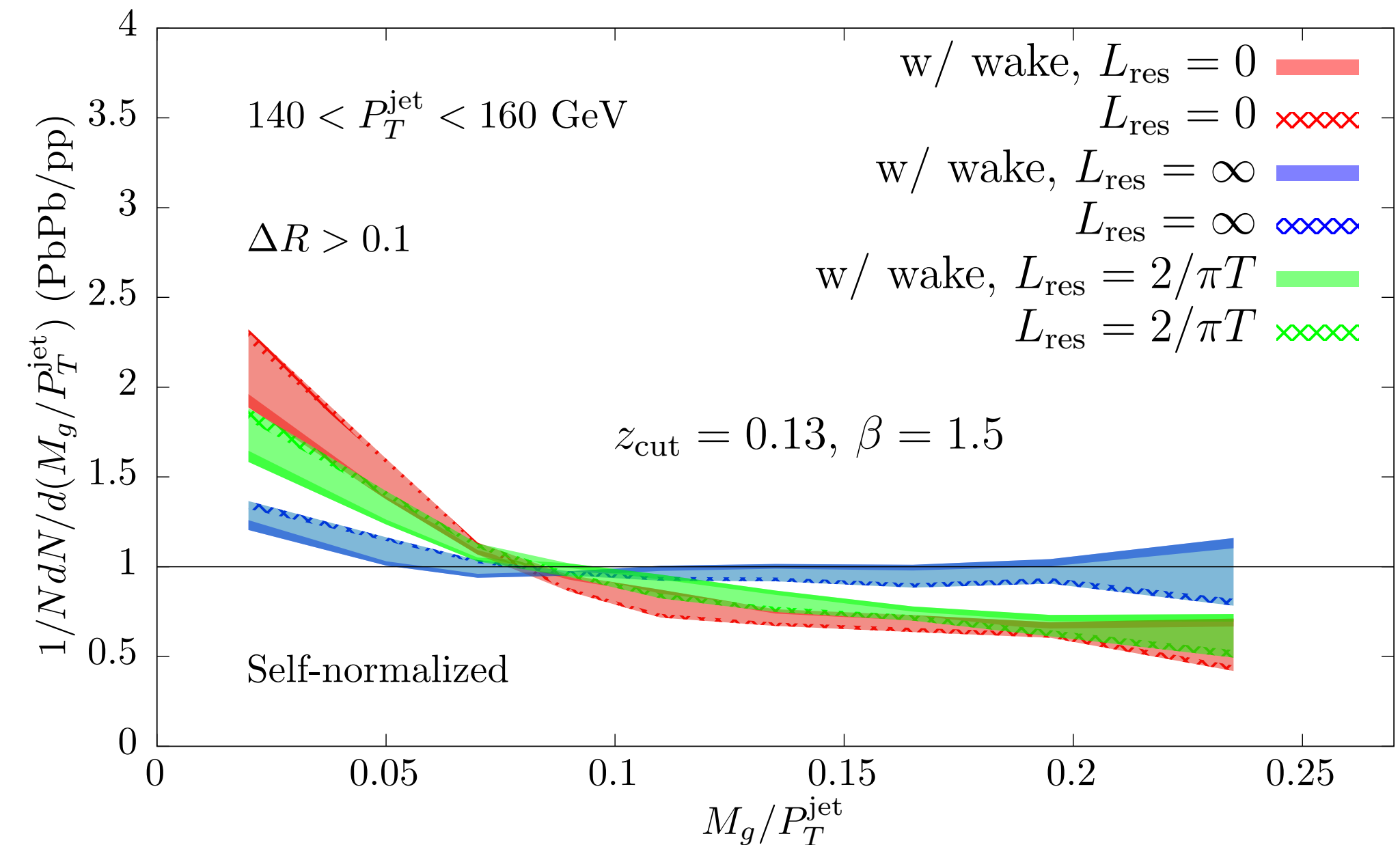


$\Delta R$  ordering of  $z_g$  dist.  
closely correlated with value of  
QGP resolution length.

Results for  $L_{\text{res}} = 2/\pi T$   
closer to  $L_{\text{res}} = 0$  than to  $L_{\text{res}} = \infty$

Tagged rate (# selected jets)

	$\Delta R > 0.0$	$\Delta R < 0.1$	$\Delta R > 0.2$
PYTHIA	0.9729(2)	0.5757(7)	0.1730(4)
$L_{\text{res}} = 0$	0.9599(8)	0.710(4)	0.092(2)
$L_{\text{res}} = 2/\pi T$	0.9633(8)	0.660(3)	0.115(2)
$L_{\text{res}} = \infty$	0.969(1)	0.603(3)	0.161(2)



# Diagnosing jet energy loss with deep learning

Selection bias is a dominant effect for many jet observables:

- Common to all calculations, jet MCs, that include jet substructure fluctuations.
- Obscures the interpretation of data: how do quenched jets really look like?

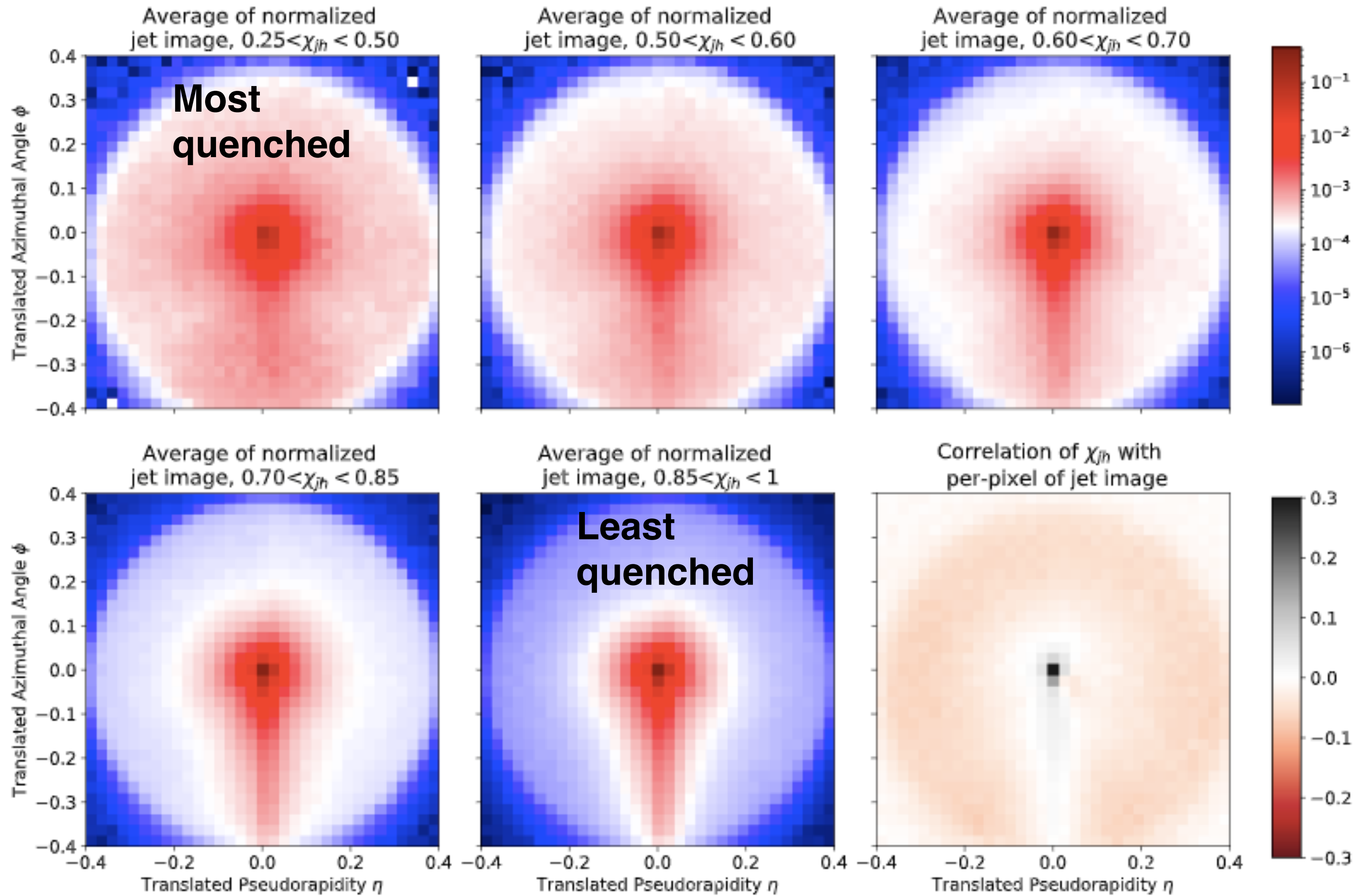
→ Use deep learning techniques to determine amount of energy loss jet-by-jet:

Energy loss ratio:  $\chi_{jh} \equiv \frac{E_f}{E_i}$

Final, measurable jet energy

Vacuum energy (had there been no medium)

# Jet Images

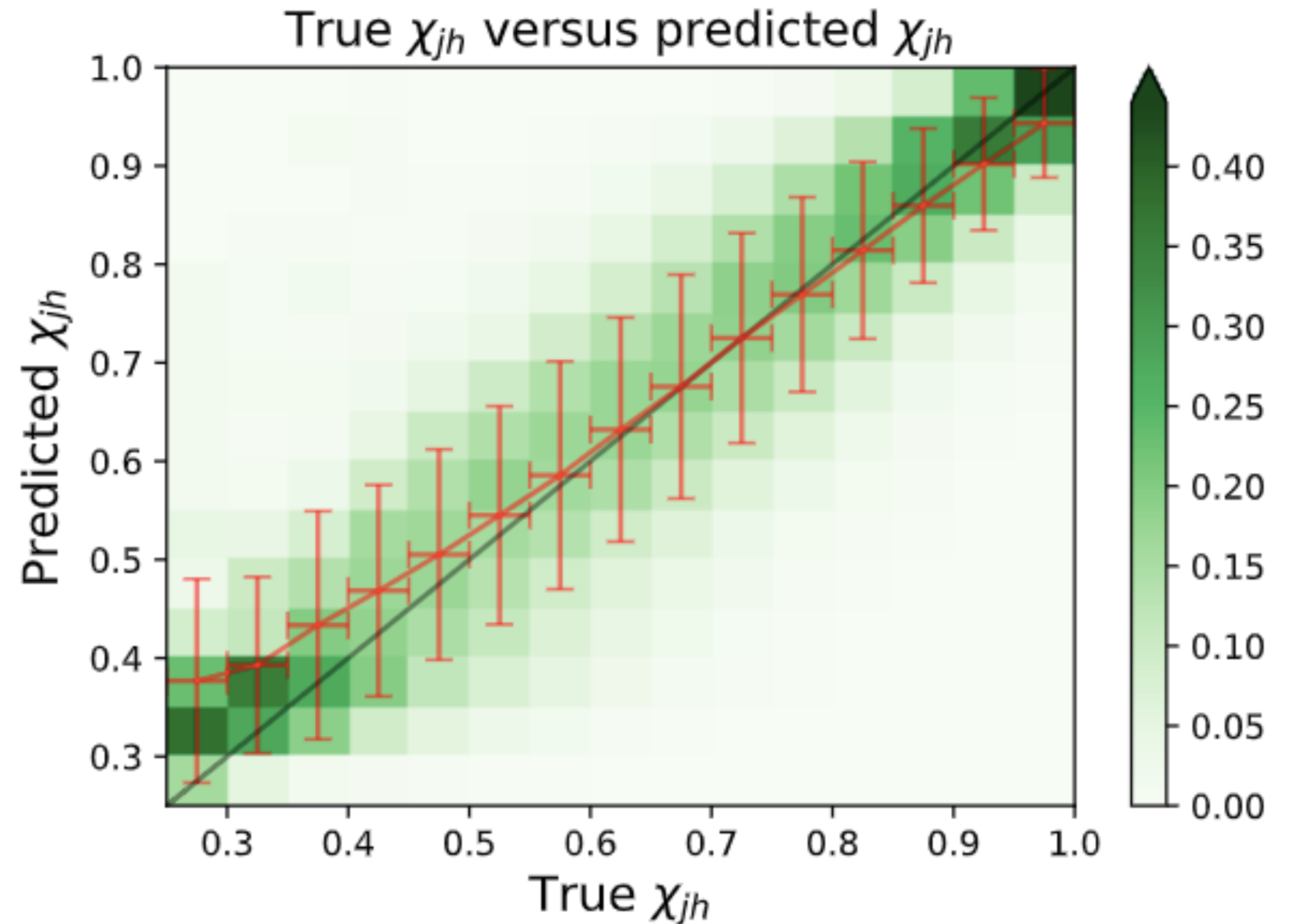


- Image rotated jet-by-jet to have subleading branch at  $-\pi/2$
- Quenching increases # of soft particles, specially at the periphery

→ Use images as input for CNN

# Performance of neural network

- Good performance across a wide range in  $\chi_{jh}$
- Consistency check: pp jets get  $\chi_{jh} \simeq 1$  (after training on medium jets only)
- Interpretability: jet shape (lower dimensional projection of jet image) contains greatest discriminating power



Du et al. - 2010.XXXX

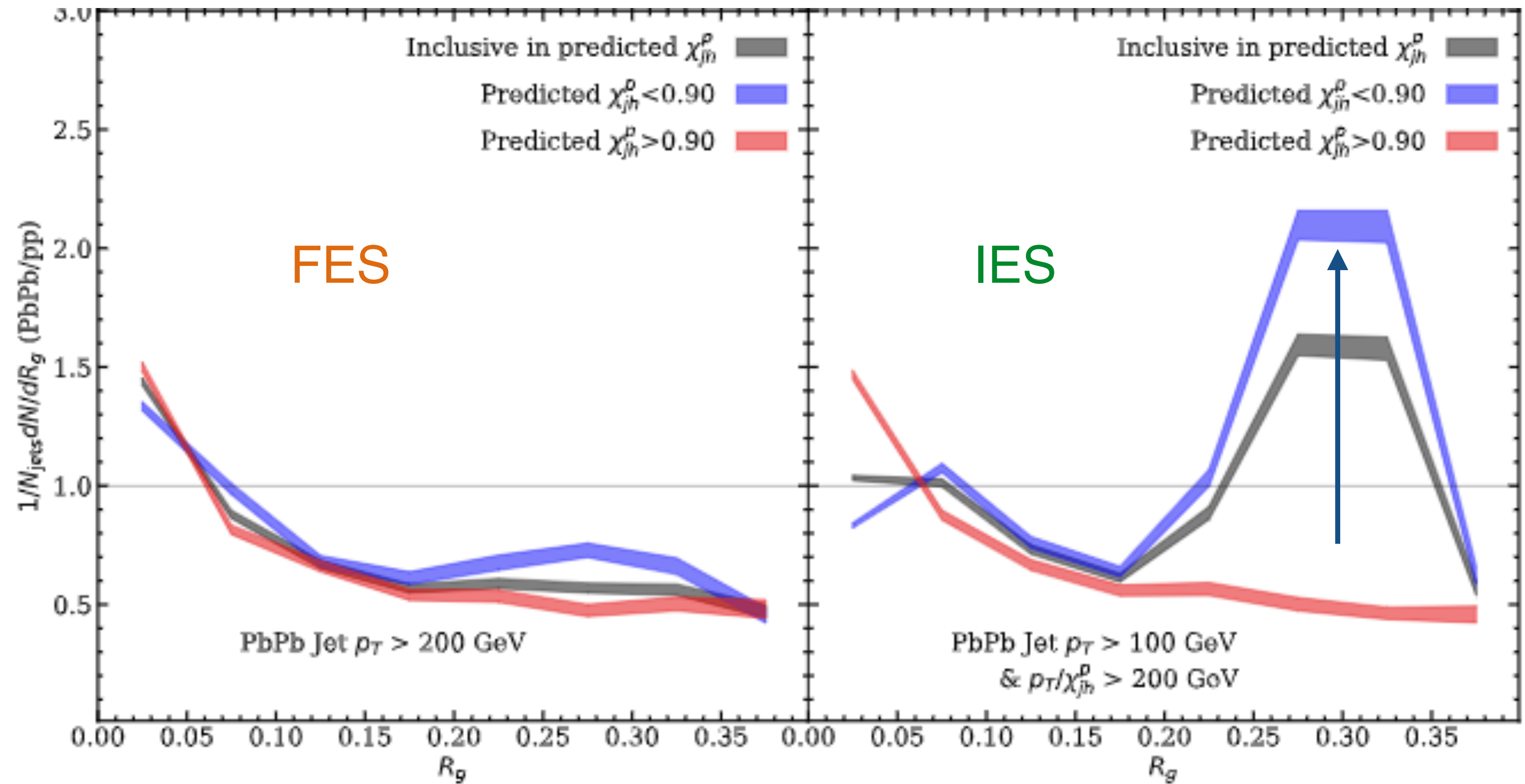
# Applications to jet observables

- **FES** (Final Energy Selection): select jets according to measured energy (usual)

➔ Mostly unquenched jets due to selection bias

- **IES** (Initial Energy Selection): select jets according to initial energy (new)

➔ Observe true effects of energy loss!



Modification of groomed radius

Du et al. - 2010.XXXX , see also Brodsky et al. - 2009.03316

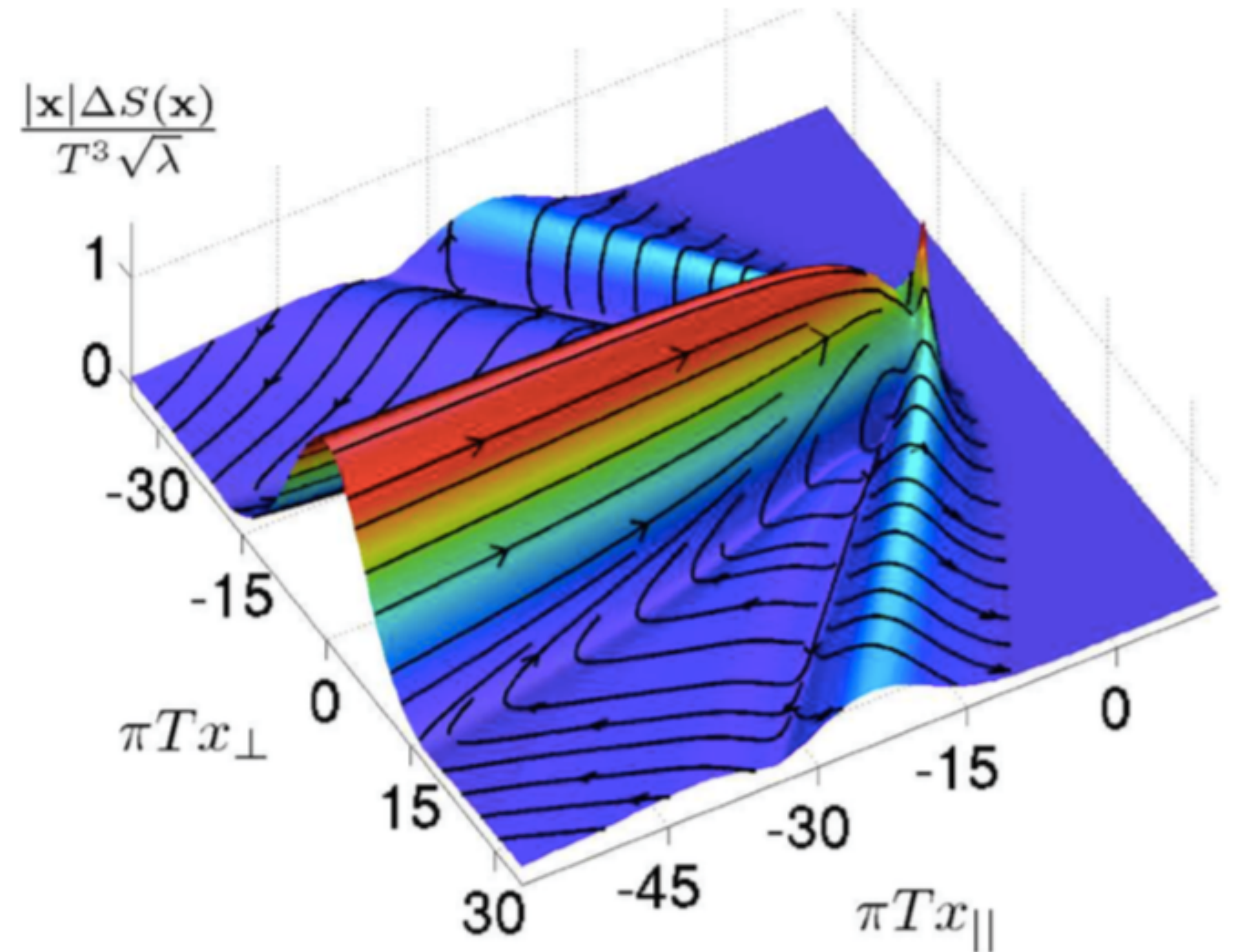
# The Wake of the Jet

Chesler & Yaffe - PRL '07

At strong coupling:

- String acts as a perturbation in the large  $N_c$  limit.
- Agreement between hydrodynamics & wake of a quark in gauge/gravity duality.

*energy-momentum  
conservation in the  
jet+plasma interplay*



# The hadrons from the wake

Pablos et al. - JHEP '17

- Assuming small perturbations on top of Bjorken flow:
  - ➔ Expand Cooper-Frye spectrum to first order in perturbations:

Fully constrained by energy-momentum conservation.

$$E \frac{d\Delta N}{d^3p} = \frac{1}{32\pi} \frac{m_T}{T^5} \cosh(y - y_j) \exp \left[ -\frac{m_T}{T} \cosh(y - y_j) \right]$$

$$\left\{ p_T \Delta P_T \cos(\phi - \phi_j) + \frac{1}{3} m_T \Delta M_T \cosh(y - y_j) \right\}$$

$$\Delta P_{\perp}^i = w \tau \int d^2x_{\perp} d\eta \delta u_{\perp}^i$$

velocity pert.

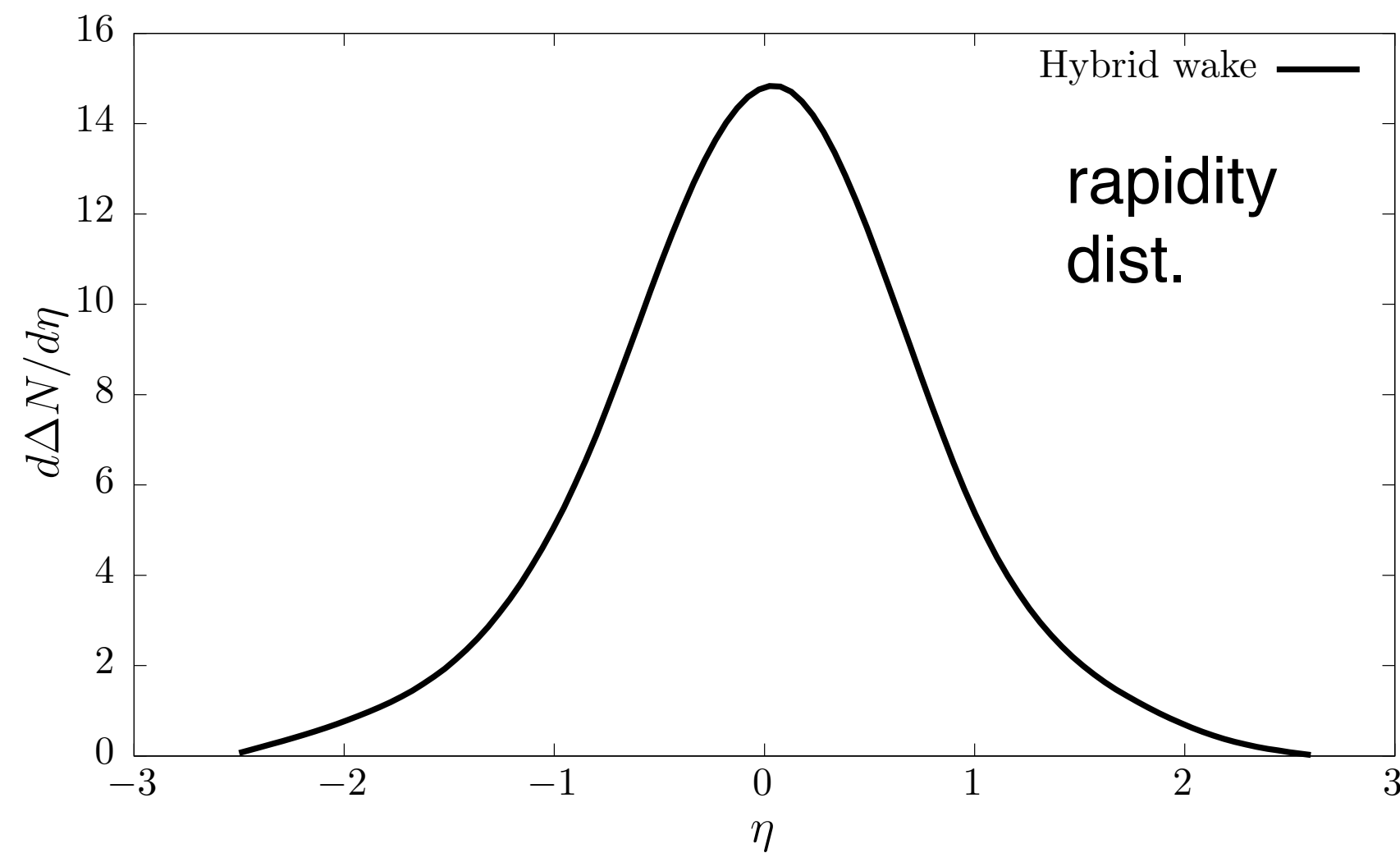
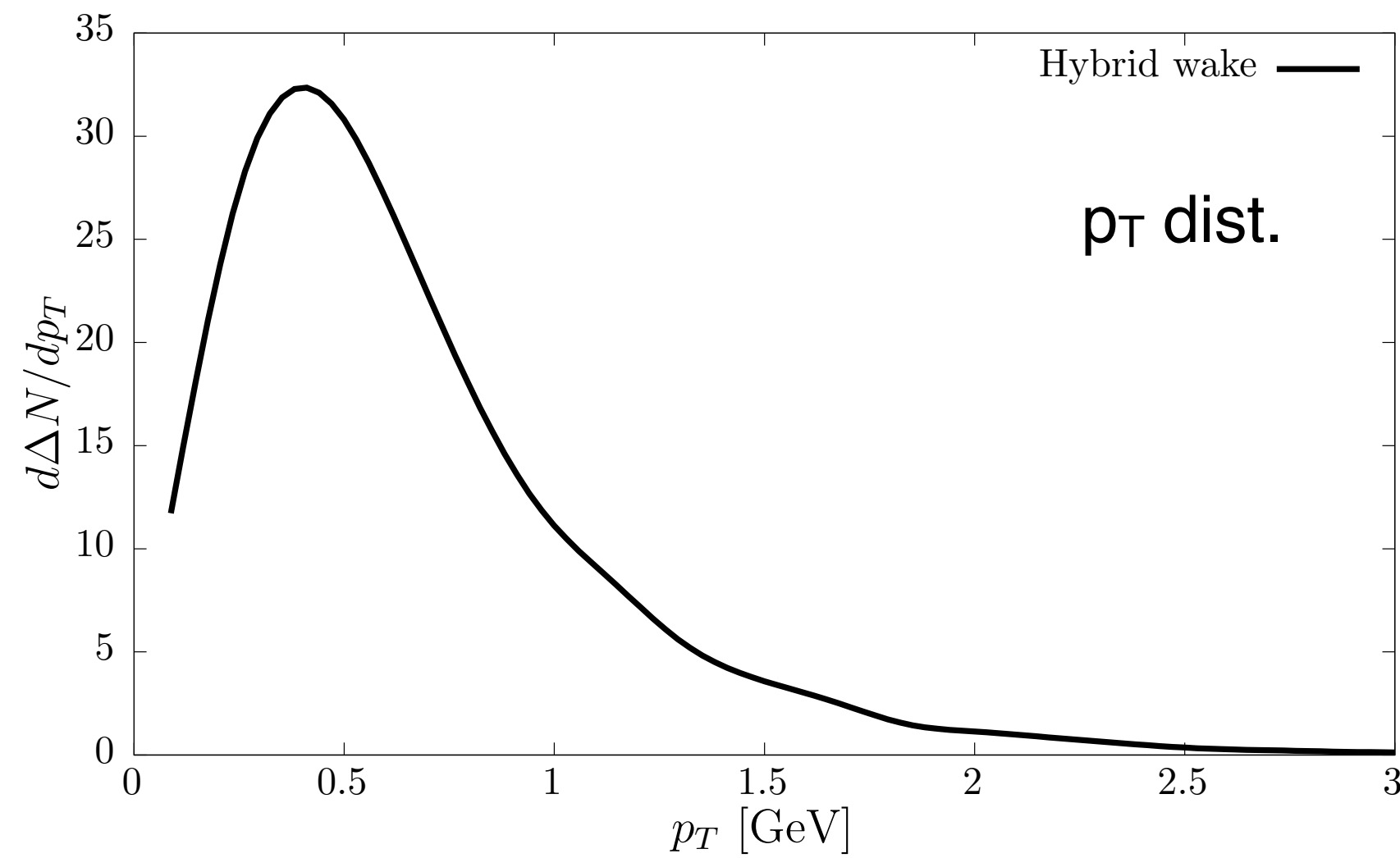
$$\Delta S = \frac{s \tau}{c_s^2} \int d\eta d^2x_{\perp} \frac{\delta T}{T}$$

temperature pert.

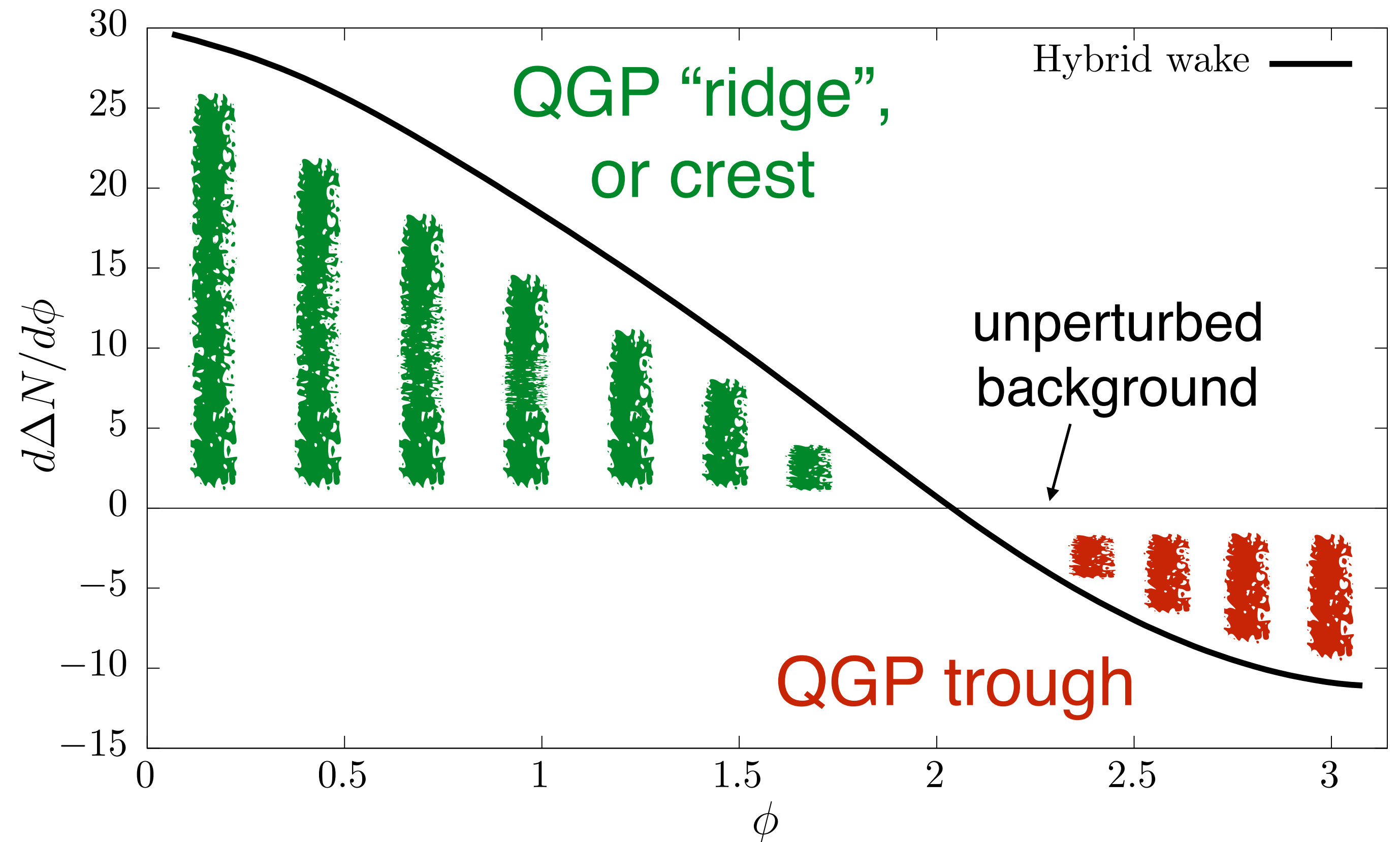
- ! Only valid for soft particles.
- ! Effect from background flow not included.



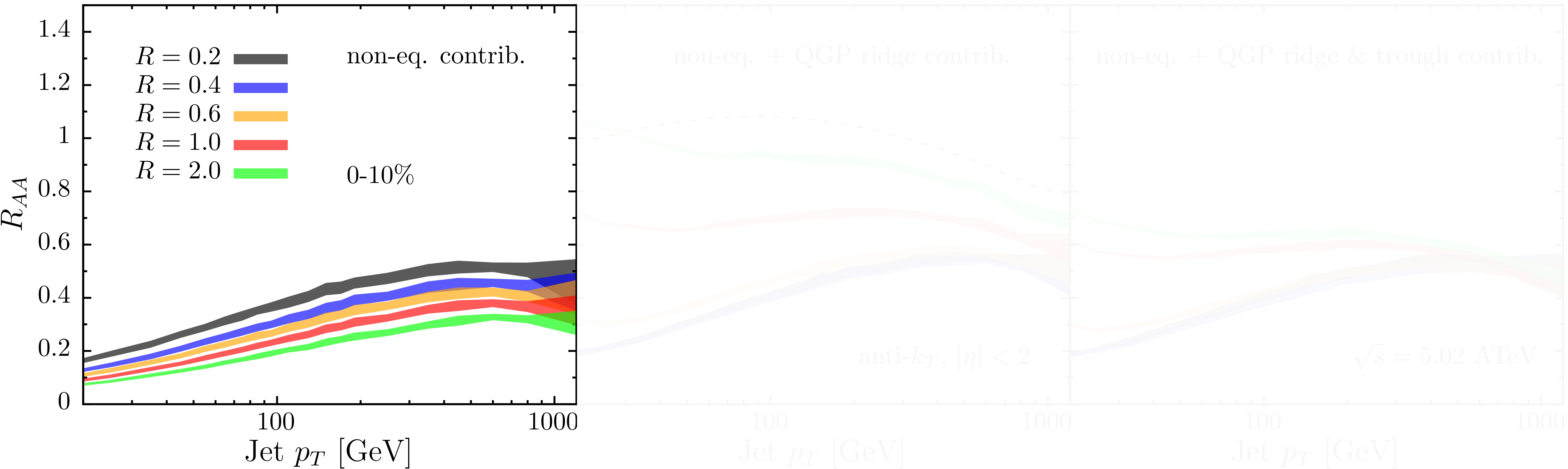
# The hadrons from the wake



- Sample hadrons from one body dist.
- Energy-momentum cons. through Metropolis.



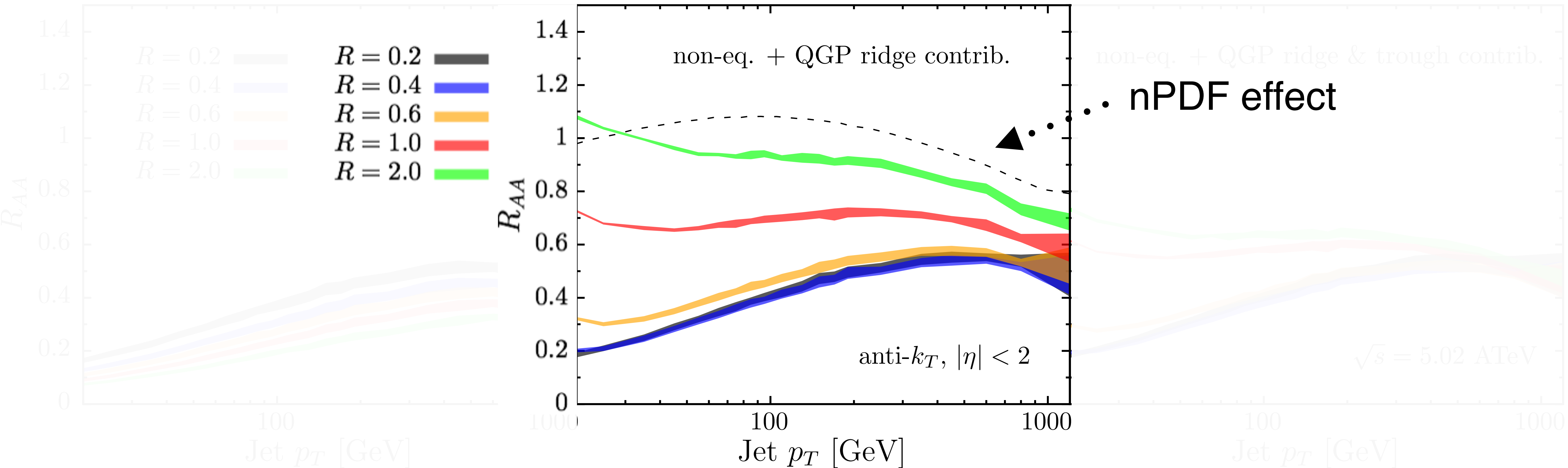
# Jet $R_{AA}$ at LHC



Include **non-eq. contribution** only, i.e. jet particles that did not hydrodynamize:

- Jet suppression increases with increasing  $R$ .
- ➔ Wider jets “lose” more energy, more energy loss sources.

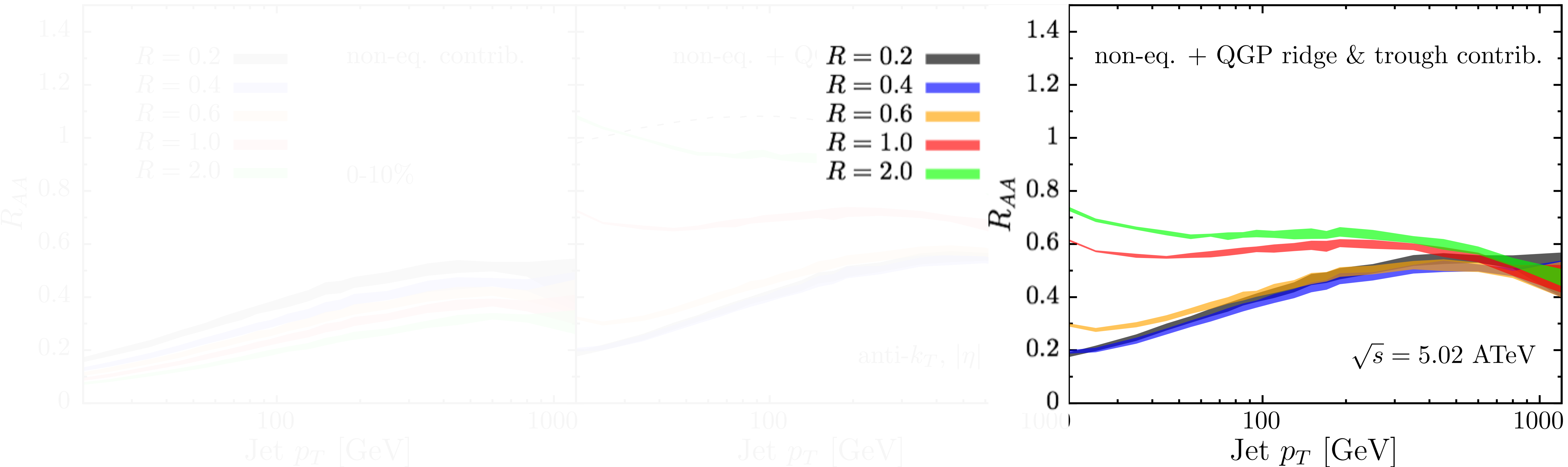
# Jet $R_{AA}$ at LHC



Include both **non-eq.** and **QGP “ridge”** contributions:

- Energy is progressively recovered with increasing  $R$ .
- ! nPDF effect sets an upper limit on  $R_{AA}$  at very high  $p_T$ .

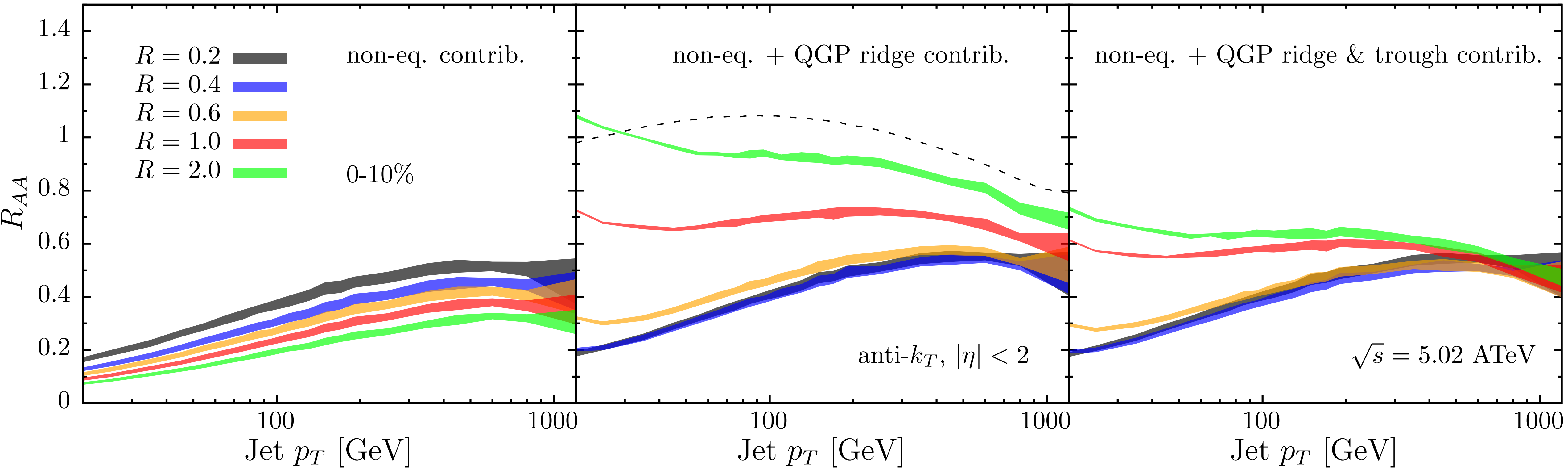
# Jet $R_{AA}$ at LHC



Include non-eq., QGP “ridge” and QGP trough contribution:

- QGP trough amounts to jet suppression; over-subtraction effect.
- Effect increases with increasing  $R$ .

# Jet $R_{AA}$ at LHC

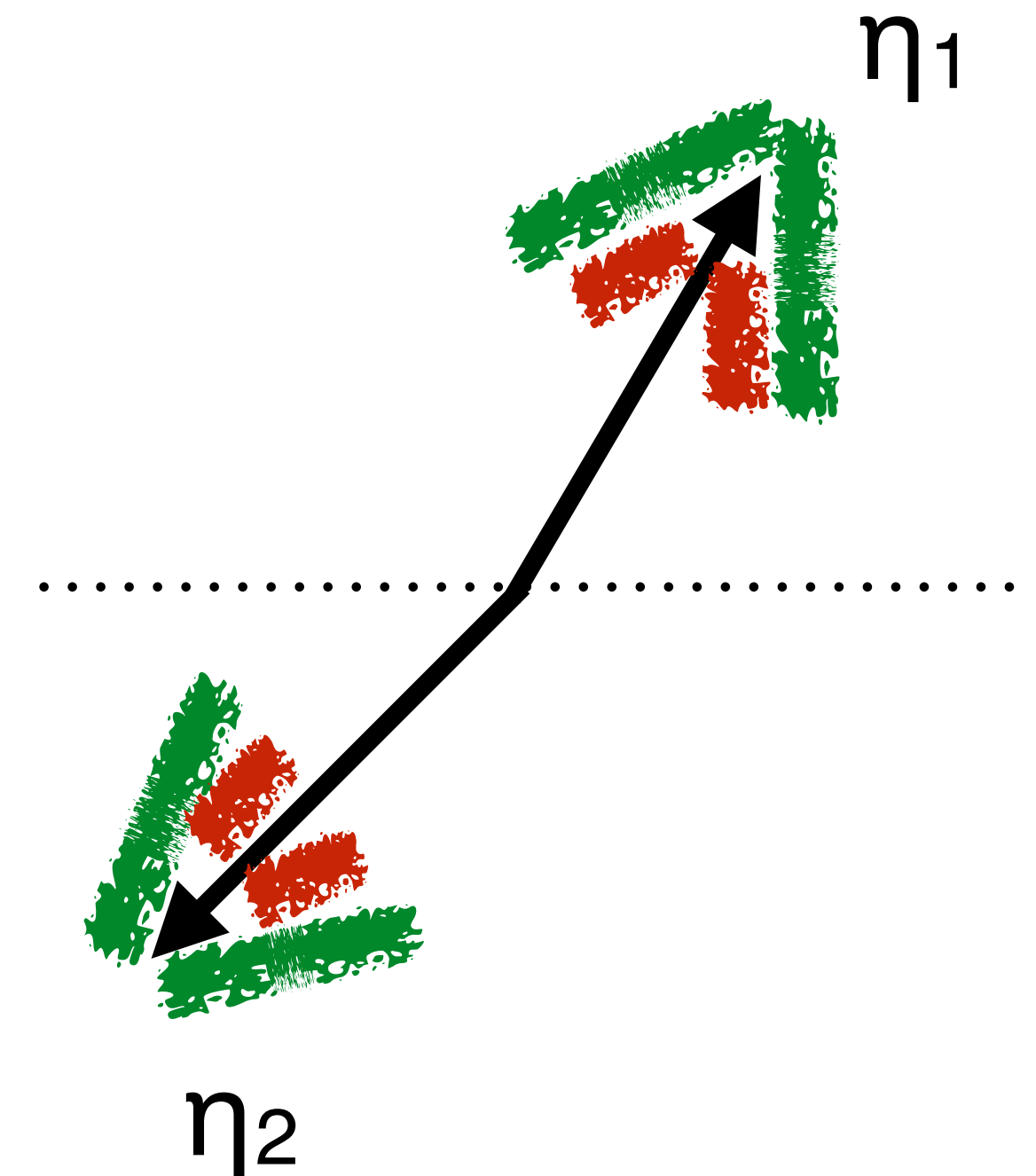


Competition of effects that yield, overall,  
a very mild evolution from small to large  $R$ .

# The effect of the recoiling jet

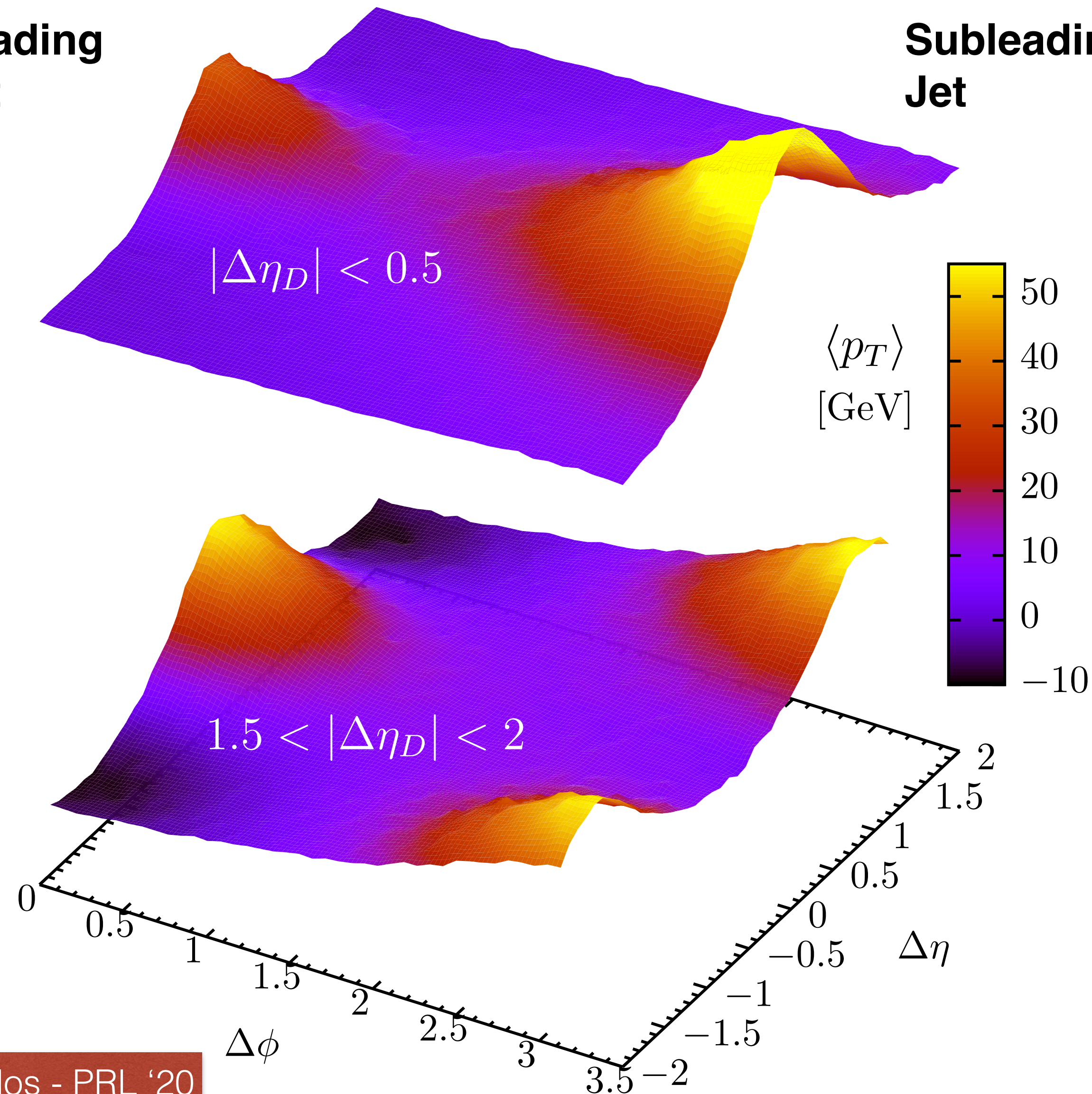
Jet suppression due to **QGP trough** comes from the wake of the *recoiling* jet.

- Rapidity dist. from the wake hadrons relatively **narrow**.
- Rapidity gap dist. between dijet system relatively **wide**.



Study dijet systems with different rapidity gaps.

# The effect of the recoiling jet



$\langle p_T \rangle$  density of wake hadrons  
w.r.t leading jet axis.

*Aligned in rapidity*

Subleading jet's **QGP trough**  
**hits leading jet.**

*Separated in rapidity*

Subleading jet's **QGP trough**  
**misses leading jet.**

$$p_T^L > 250 \text{ GeV}$$

$$p_T^S > 80 \text{ GeV}$$

$$\Delta\phi_D > 2\pi/3$$

differential in

$$|\eta_D| \equiv |\eta_L - \eta_S|$$

# Leading jet suppression vs. $|\eta_D|$

Pablos - PRL '20

*A new observable*

**R=0.4**

leading jet area easy to miss;  
small effect from QGP trough.

**R=1.0**

strong dependence on  $|\eta_D|$ ;  
knee visible when  $|\eta_D| \sim R$ .

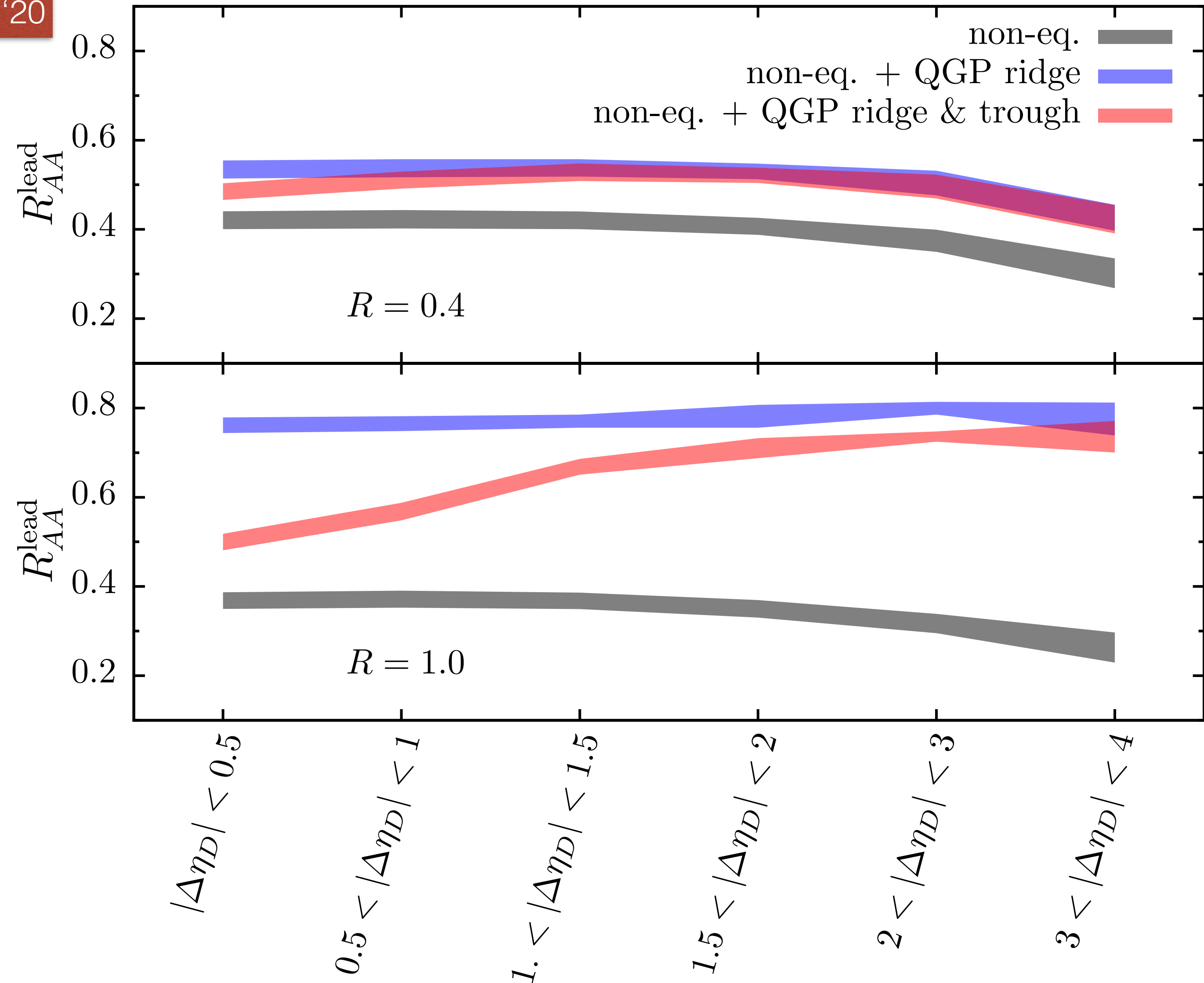
$$p_T^L > 250 \text{ GeV}$$

$$p_T^S > 80 \text{ GeV}$$

$$\Delta\phi_D > 2\pi/3$$

differential in

$$|\eta_D| \equiv |\eta_L - \eta_S|$$





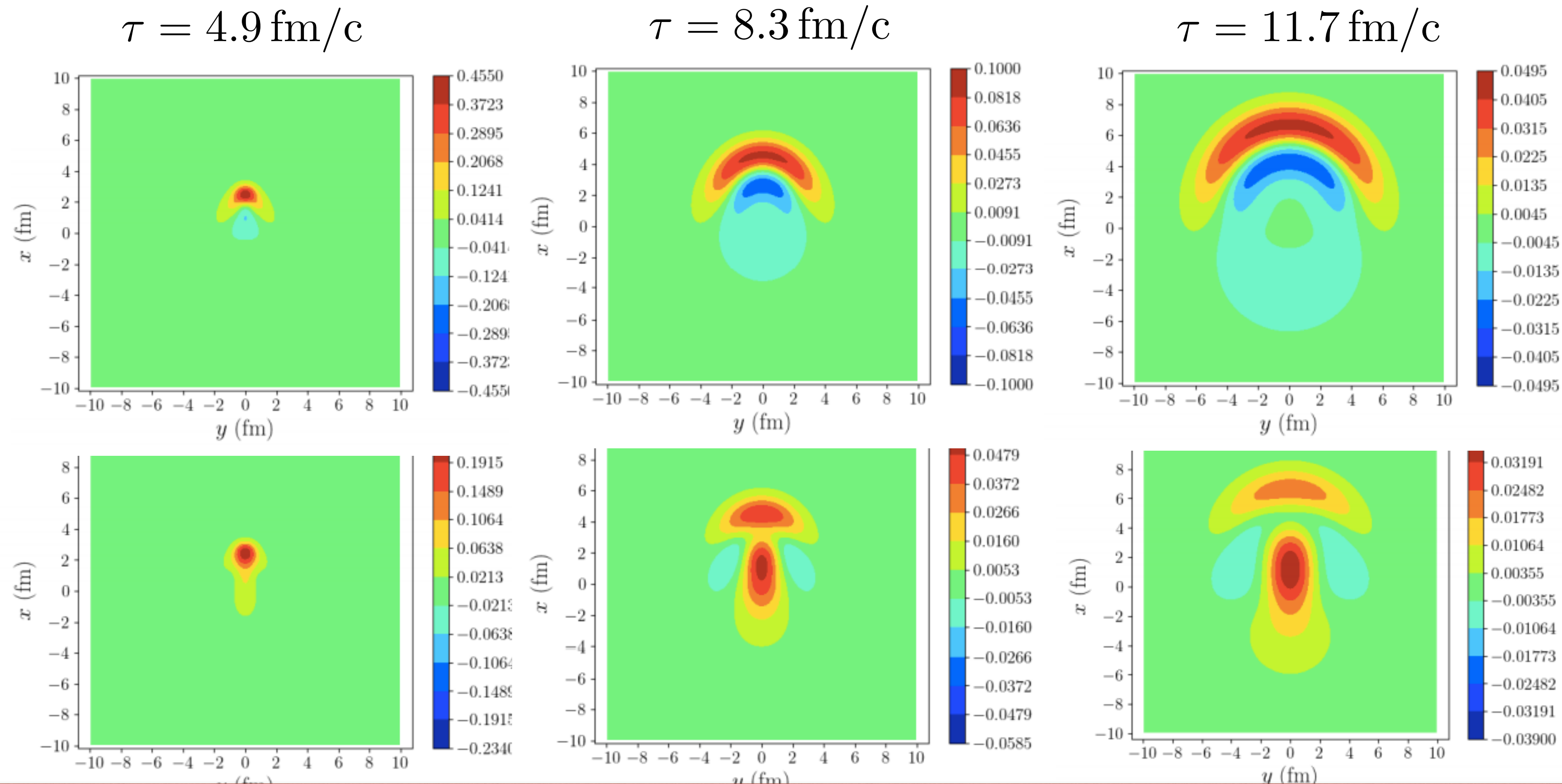
# Improving the wake description

Efficient, but over-simplified medium response needs to be improved:

- Extend kinematical validity: requires knowledge of spacetime evolution of hydro perturbations.

→ Linearised hydro eqs. for perturbations on top of viscous Bjorken flow:  $\nabla_{\mu} T_{(0)}^{\mu\nu} = 0$

$$\nabla_{\mu} \delta T^{\mu\nu} = J^{\nu}$$



$\frac{\delta \epsilon}{\epsilon_0}(\eta_s = 0)$   
energy perturbation

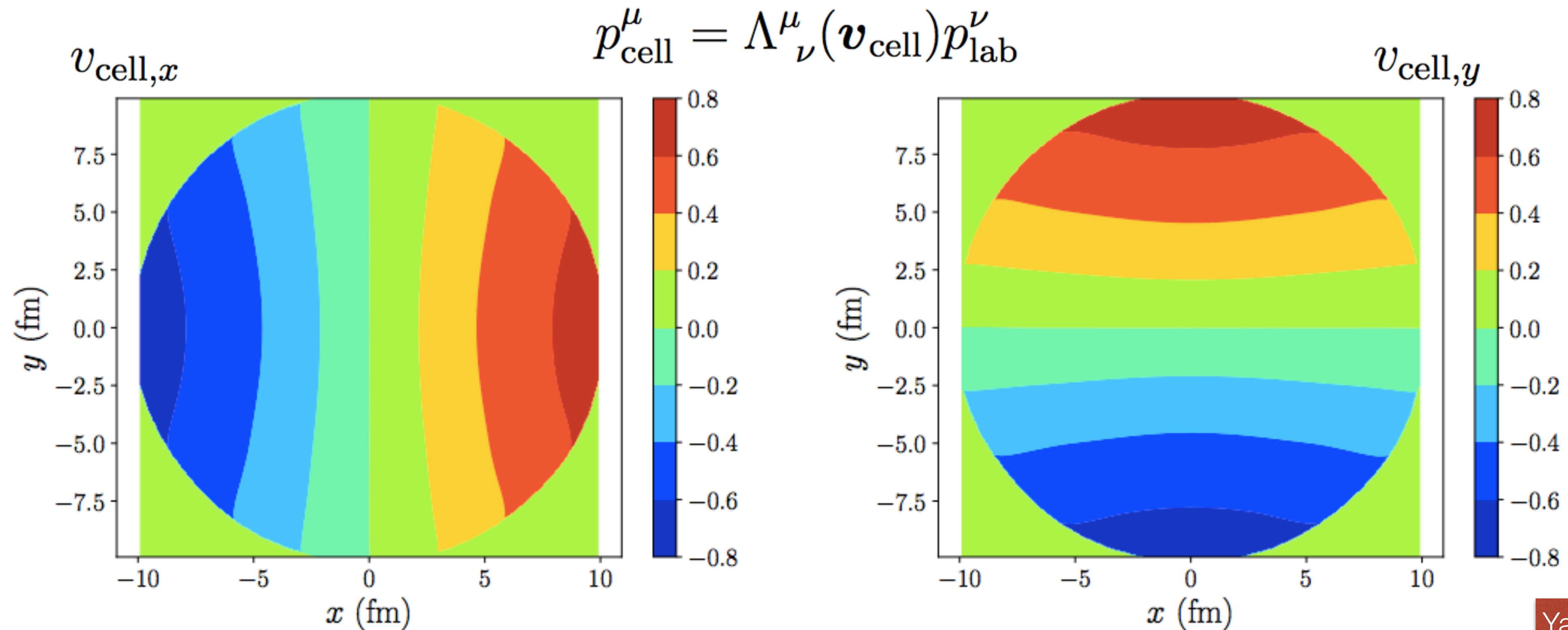
$\delta u^x(\eta_s = 0)$   
velocity perturbation

# Improving the wake description

Efficient, but over-simplified medium response needs to be improved:

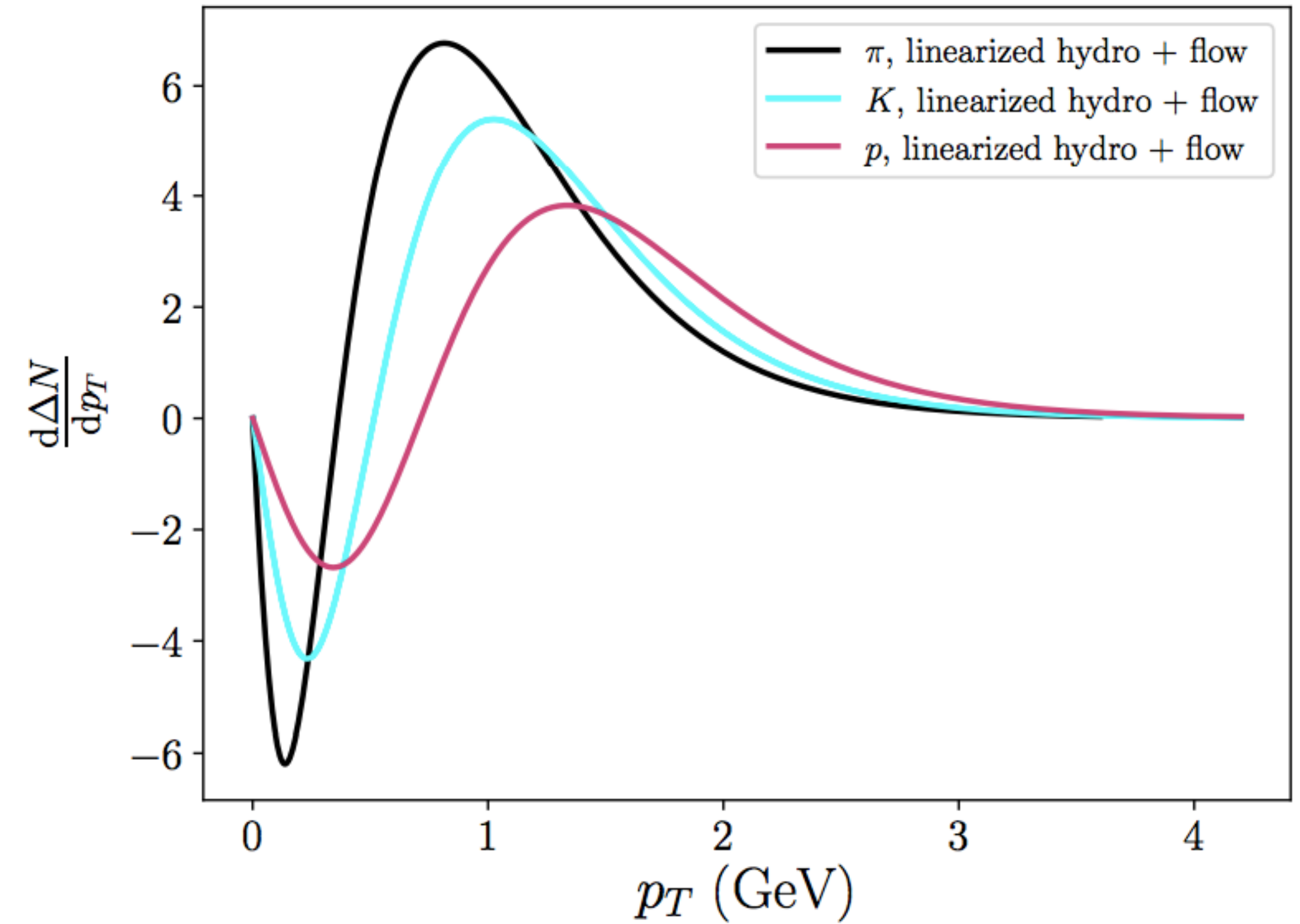
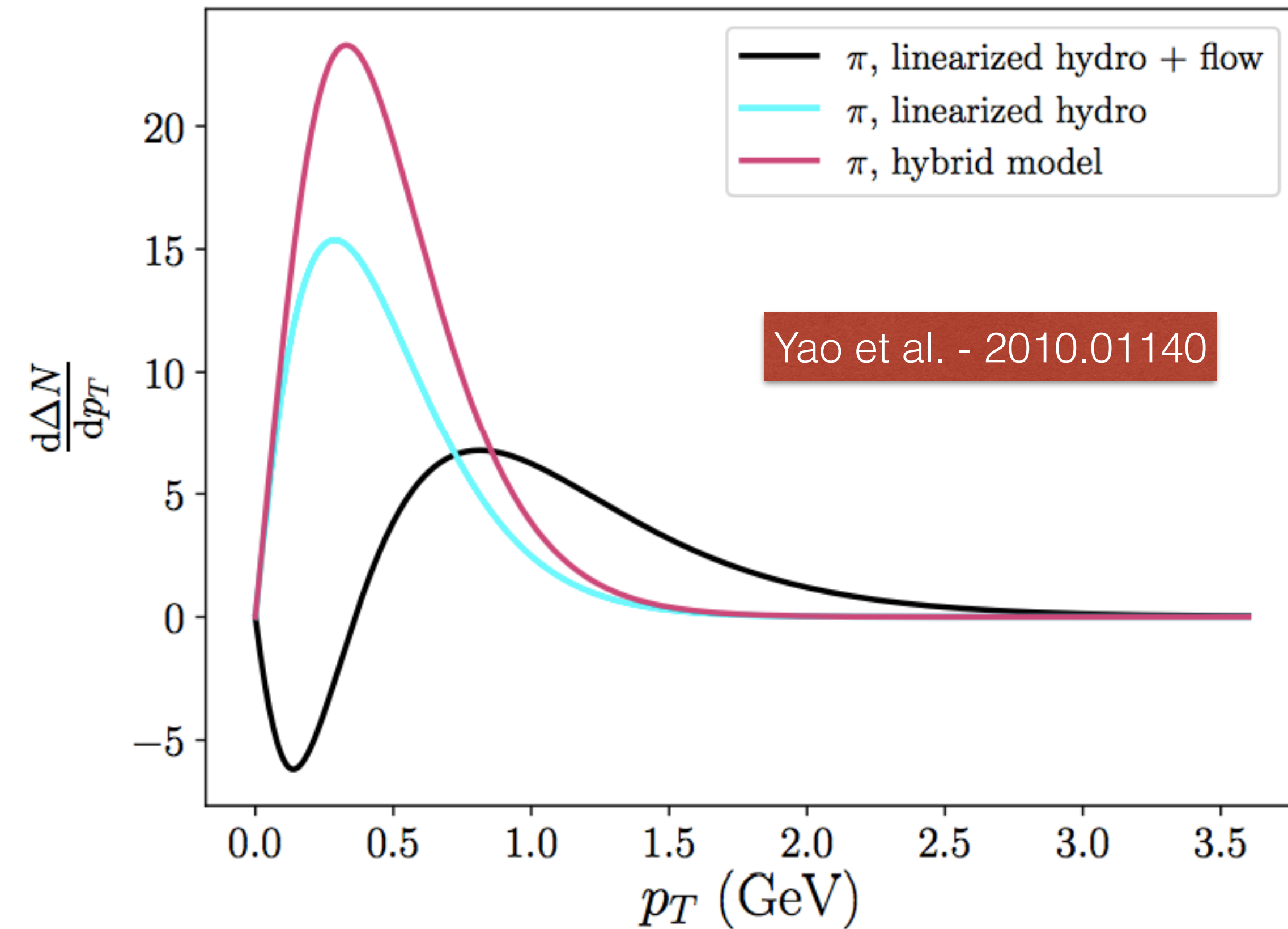
- Include the effects of realistic background flow.

➔ Boost fluid cell of the perturbation according to local radial flow at freeze-out hyper surface:



Yao et al. - 2010.01140

# Linearised Wake: effects on observables



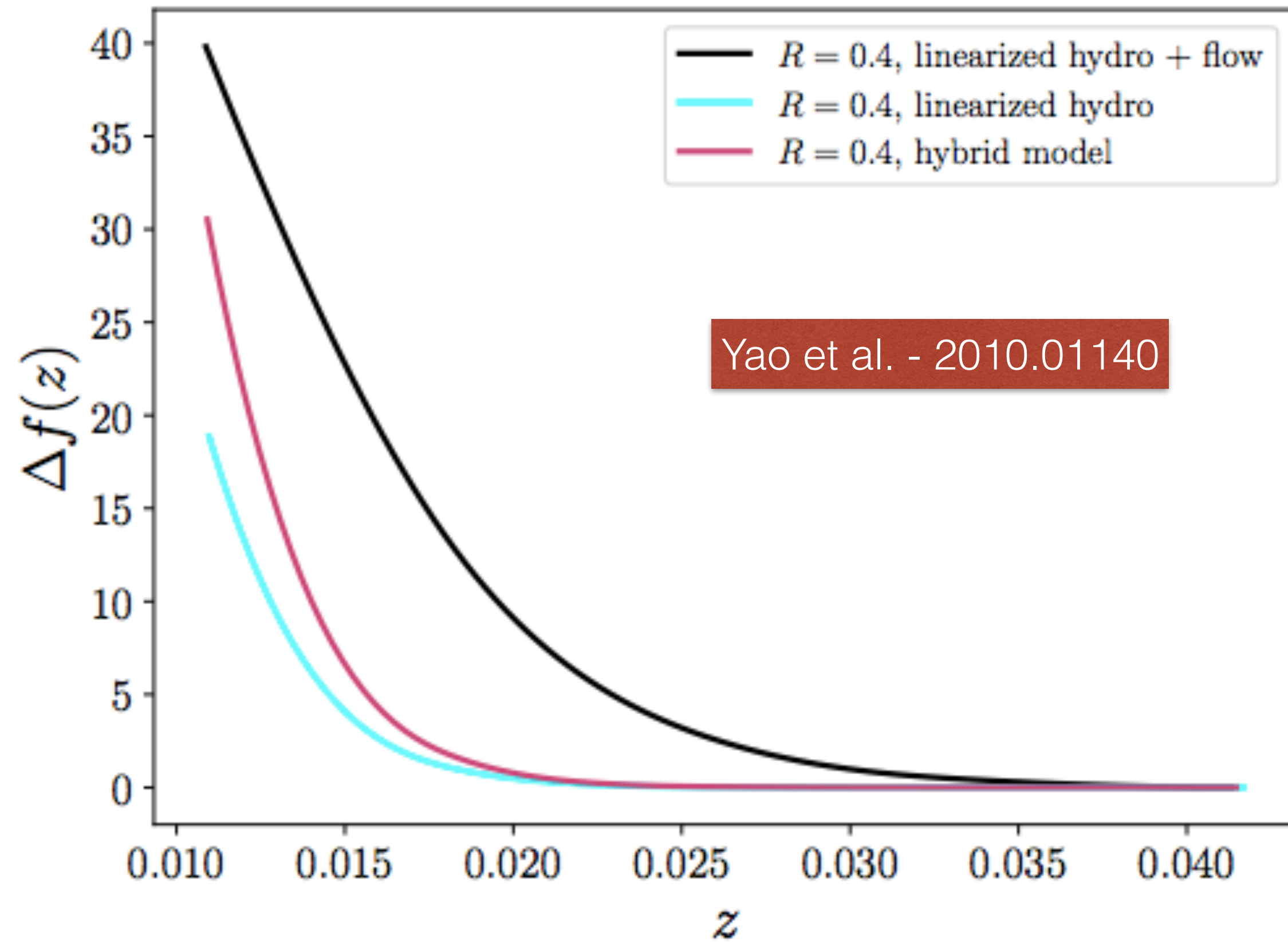
Strongest new effect comes from radial flow:

- Important hardening of hadrons  $p_T$  spectrum.

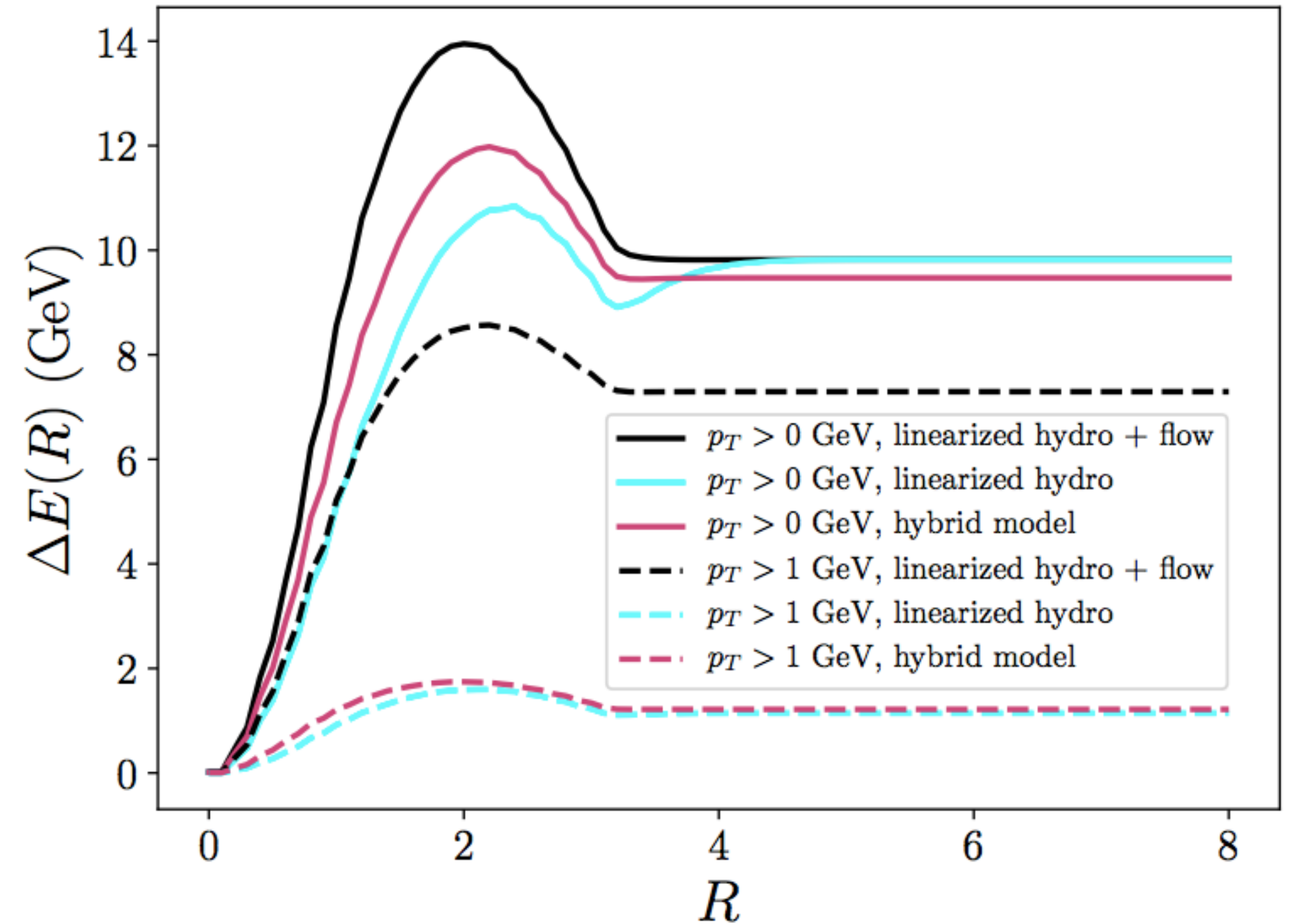
As expected from hydrodynamics:

- Hadrons from the wake display mass ordering.

# Linearised Wake: effects on observables

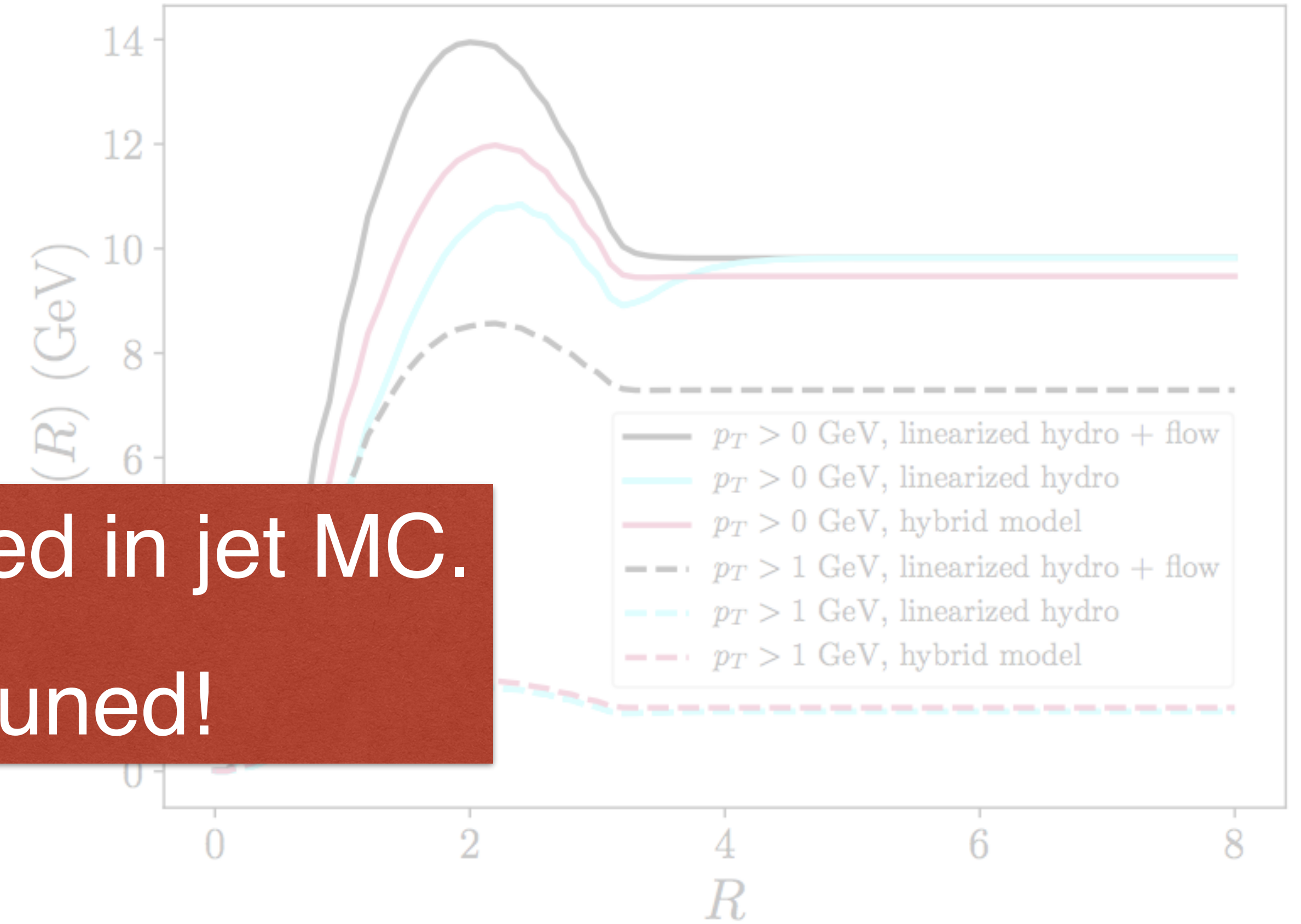
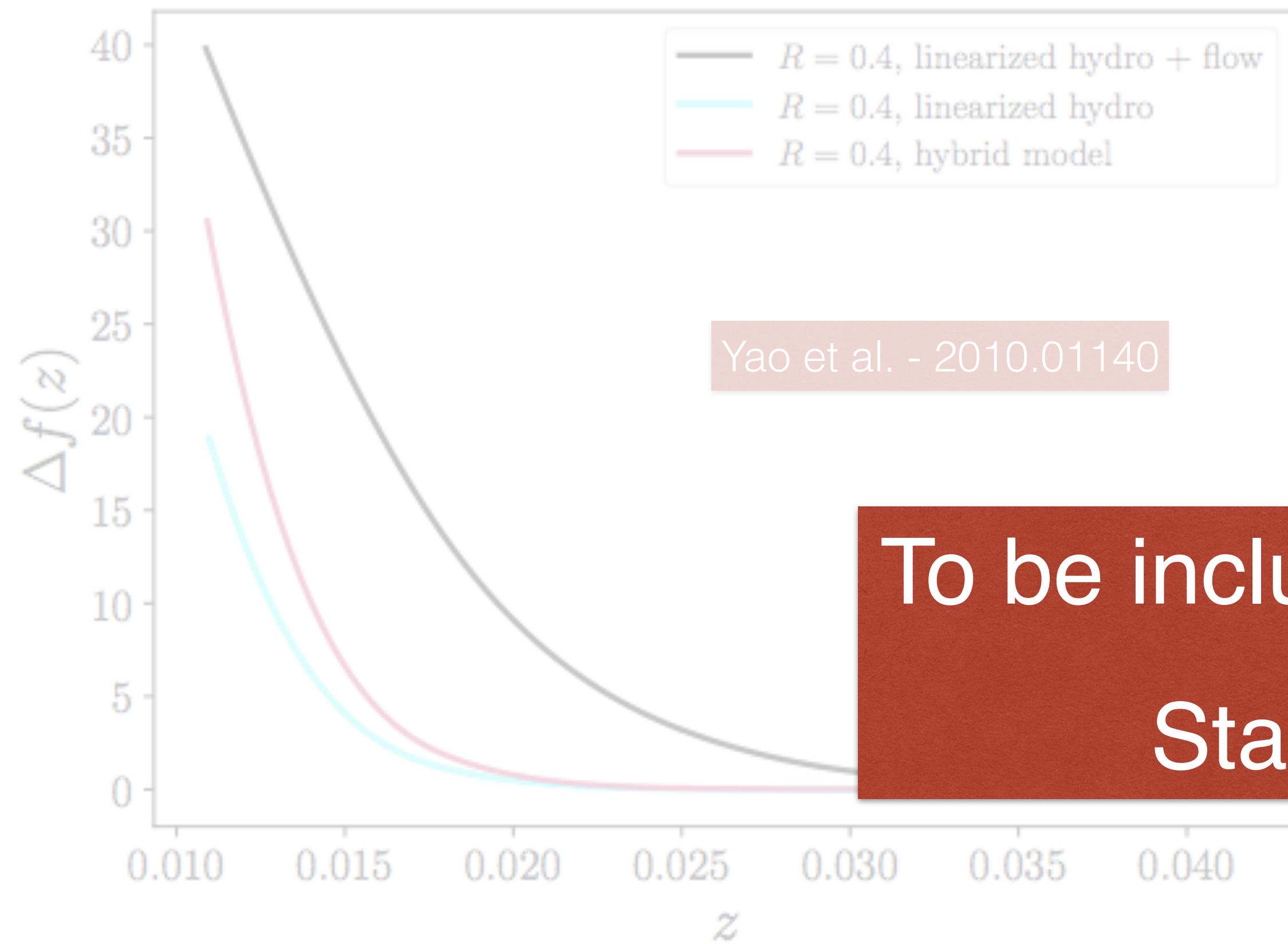


- Increase in # fragments with higher  $z$  inside the jet (jet FFs)



- Modified recovery of energy as a function of radial distance (jet shapes,  $R_{AA}$  vs  $R$ )

# Linearised Wake: effects on observables



To be included in jet MC.  
Stay tuned!

Increase in # fragments  
with higher  $z$  inside the jet  
(jet FFs)

Modified recovery of energy as a  
function of radial distance  
(jet shapes,  $R_{AA}$  vs  $R$ )

# Jet Suppression: Analytics

- Great deal of jet observables are understood through consideration of jet substructure fluctuations within the medium:
  - Jet MC quenching models naturally include these effects, although with many uncontrolled modelling assumptions.
- Want to extend these concepts to phenomenologically relevant perturbative, analytic calculations in QCD. We need to:
  - Resum quenching effects from multi-prong nature of jets.
  - Take into account color coherence effects.
  - Gauge uncertainties on non-perturbative components (e.g. the wake).
  - Embed into realistic heavy ion environment to account for in-medium path flucs.

# Jet Suppression: Analytics

- Cross-section of jet with radius  $R$  in the medium:

$$\sigma_{AA}(p_T, R) = f_{\text{jet}/k}^{(n-1)}(R|p_T, R_0) \hat{\sigma}_k(p_T, R_0)$$

$$f_{\text{jet}/k}^{(n-1)} = \sum_{i=q,g} Q_i(p_T, R) f_{i/k}^{(n-1)}$$

← moment of jet frag. function

↑ quenching factor

Dasgupta et al. - JHEP '15

- Resummation of bare quenching factor through DGLAP:

$$\frac{\partial Q_i(p, \theta)}{\partial \ln \theta} = \int_0^1 dz \frac{\alpha_s(k_\perp)}{2\pi} p_{ji}^{(k)}(z) \Theta_{\text{in}}(z, \theta) \times [Q_j(zp, \theta) Q_k((1-z)p, \theta) - Q_i(p, \theta)]$$

Mehtar-Tani & Tywoniuk - PRD '18

with quenched phase space:

$$\Theta_{\text{in}}(p, R) = \Theta(t_f < t_d < L)$$

Quench resolved emission inside the medium only

with initial condition:

$$Q_i(p, 0) = Q_{\text{rad},i}^{(0)}(\nu) Q_{\text{el},i}^{(0)}(\nu)$$

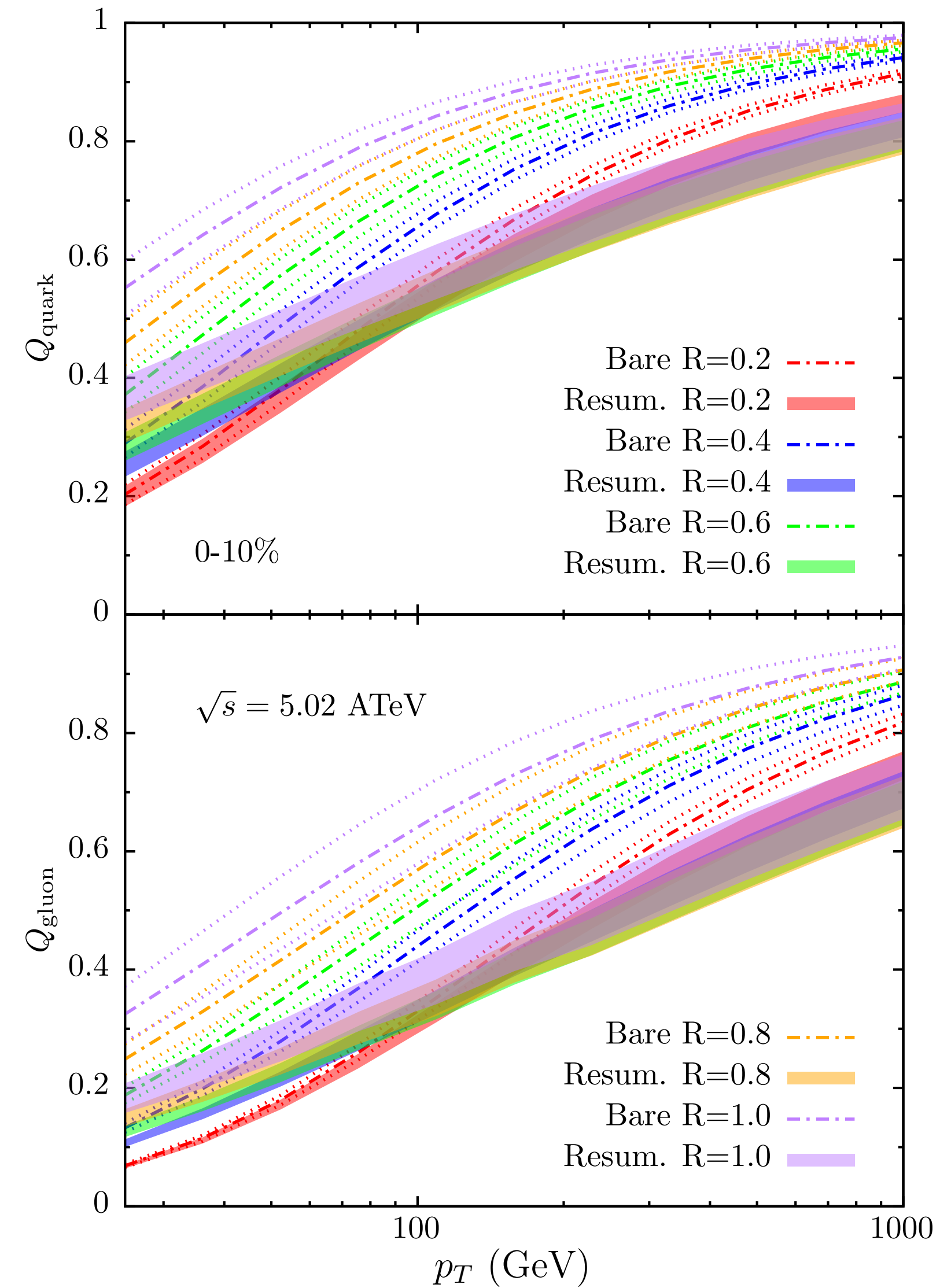
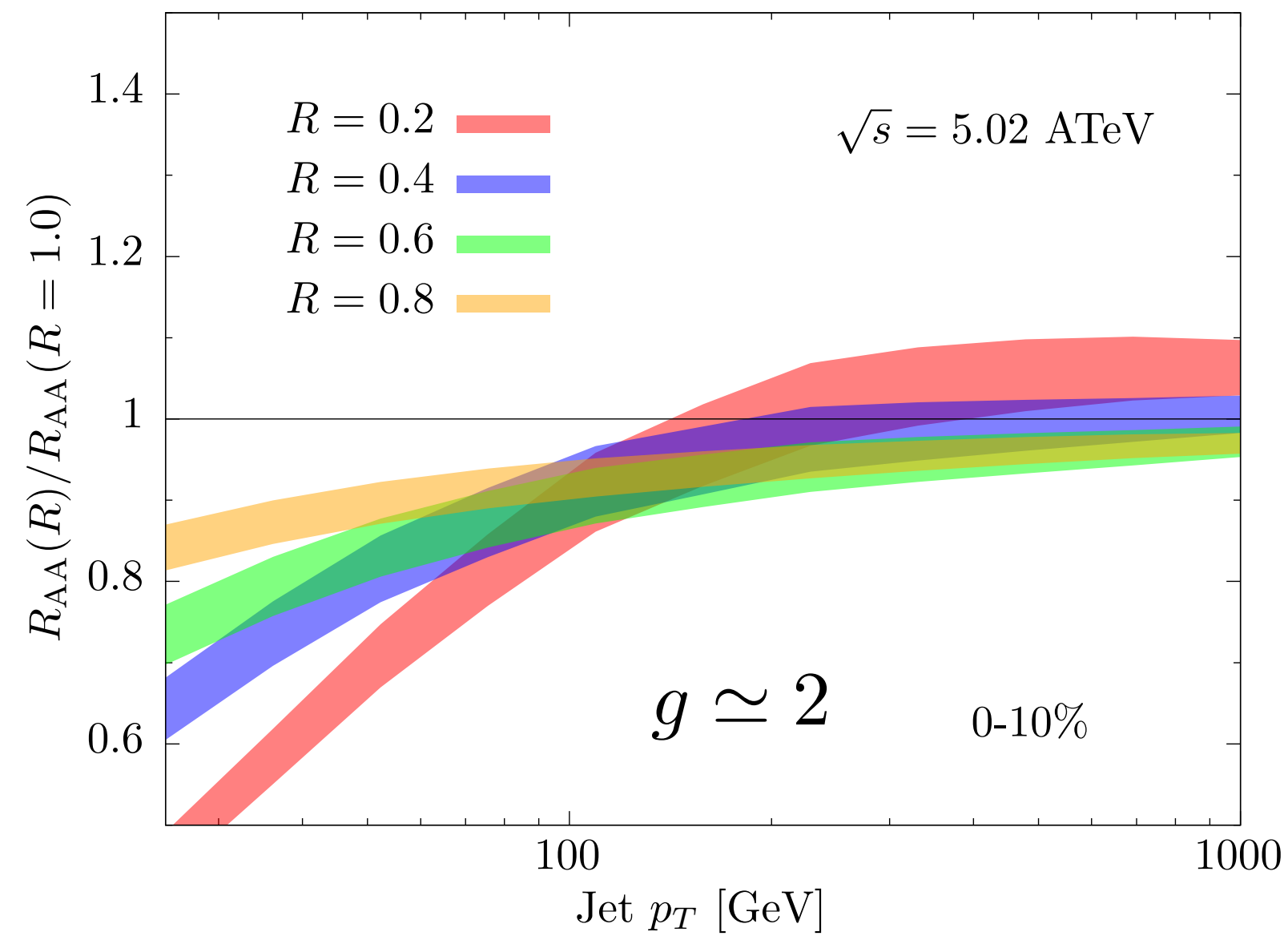
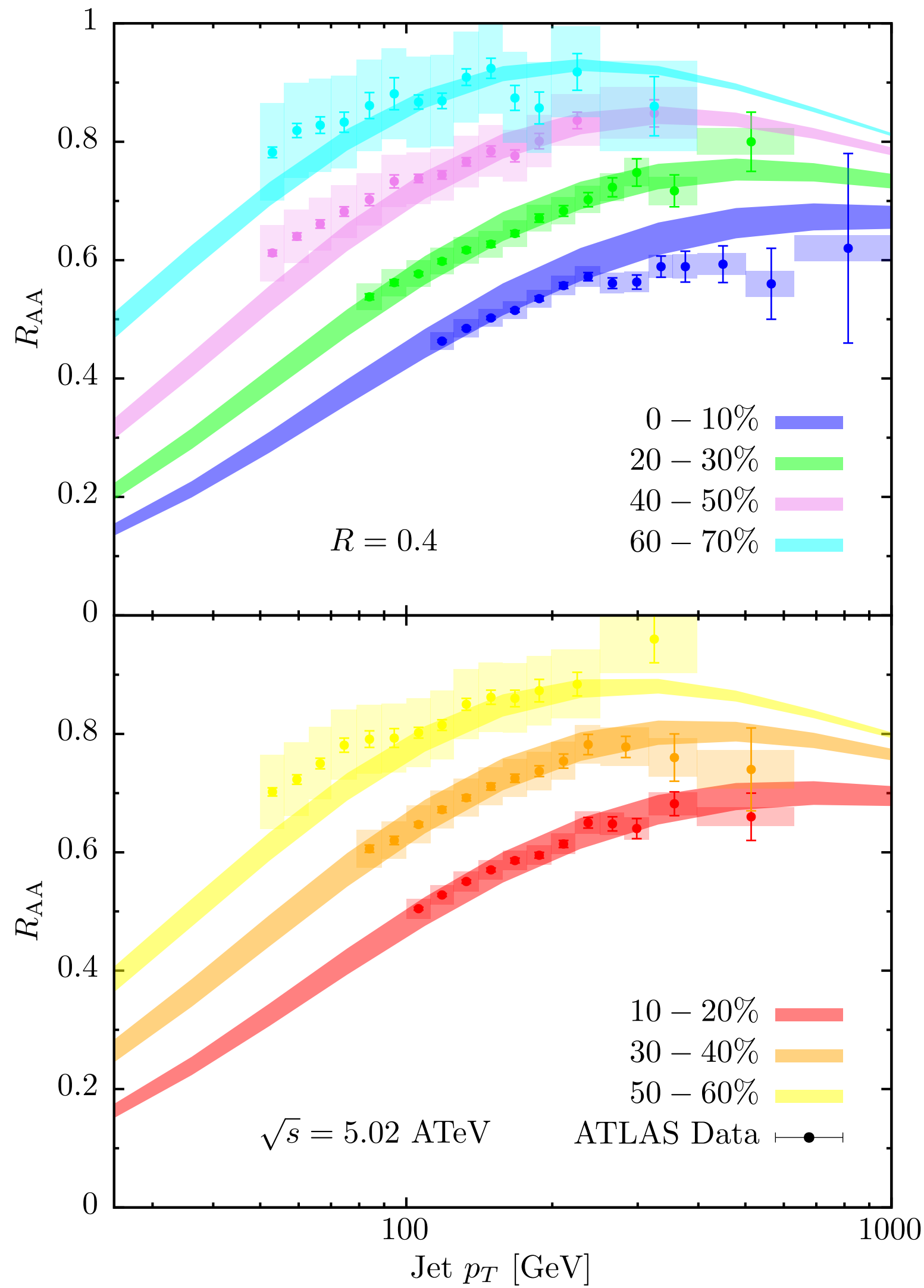
Radiative component at NLO in improved opacity expansion

Include  $R_{\text{rec}}$  parameter for energy recovery vs  $R$

Barata & Mehtar-Tani - 2004.02323

Mehtar-Tani et al. - 2010.XXXX

# Jet Suppression: Analytics



● Excellent description of  $p_T$  and centrality evolution

ATLAS - PLB '18

● Mild  $R$  dependence of jet suppression in agreement with recent CMS data

CMS-PAS-HIN-18-014

Mehtar-Tani et al. - 2010.XXXX



# Summary

- Jet substructure fluctuations are key to our understanding of jet quenching phenomenology.

Early fragmentation pattern of the jet (mostly dominated by vacuum physics) controls amount of quenching:

- Selection bias towards narrower jets due to steeply falling spectrum, provided that the medium resolves the internal structure of the jet.
- Can use machine learning to select jets with a certain amount of energy loss, study observables based on initial jet energy, getting rid of the selection bias.

- Hydrodynamization of jet energy can be studied through jet substructure observables.

Soft particles from the wake enter the jet cone:

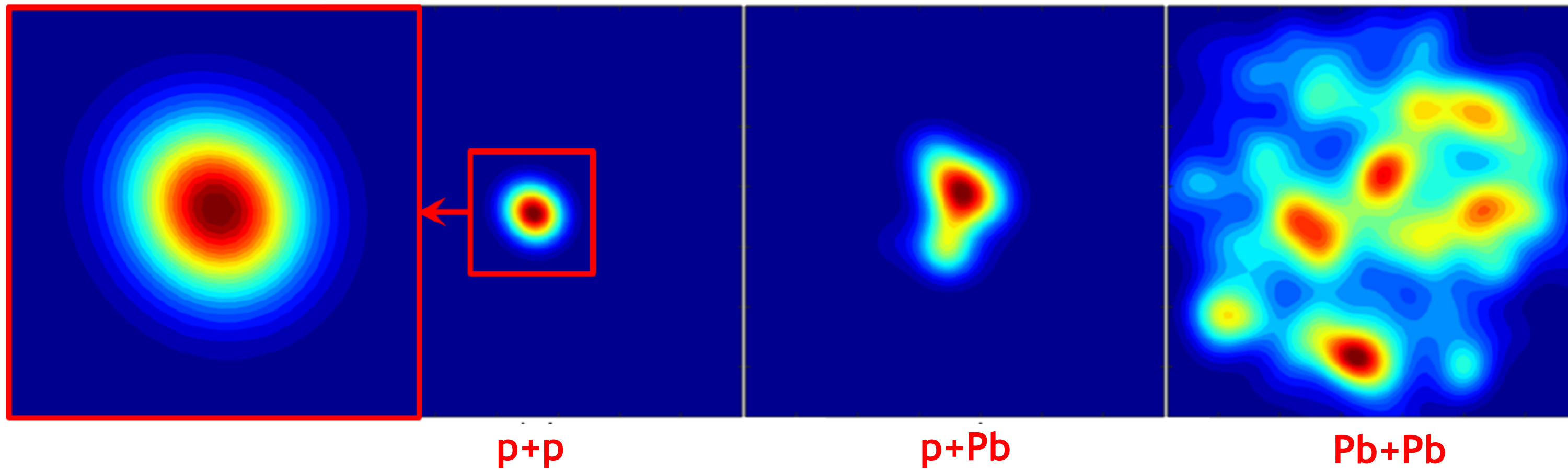
- Sensitive to background flow, display mass ordering.
  - Long range correlations between dijet system vs R.
- } Crucial elements of fluid QGP paradigm!

# Backup Slides

# Hydro in Small Systems

“One fluid to rule them all”

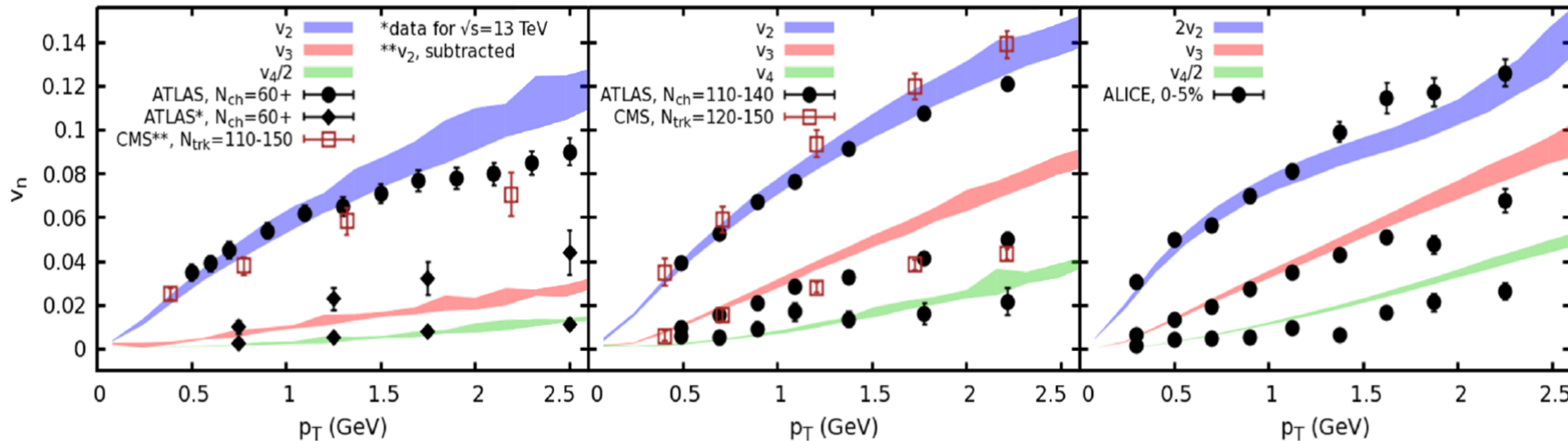
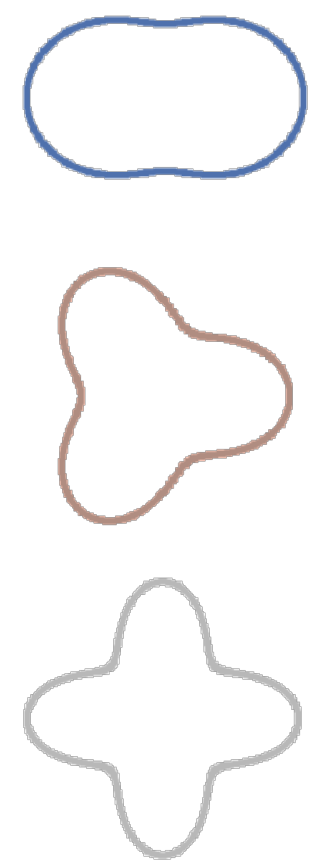
Weller & Romatschke -  
PLB '17



superSONIC for p+p,  $\sqrt{s}=5.02$  TeV, 0-1%

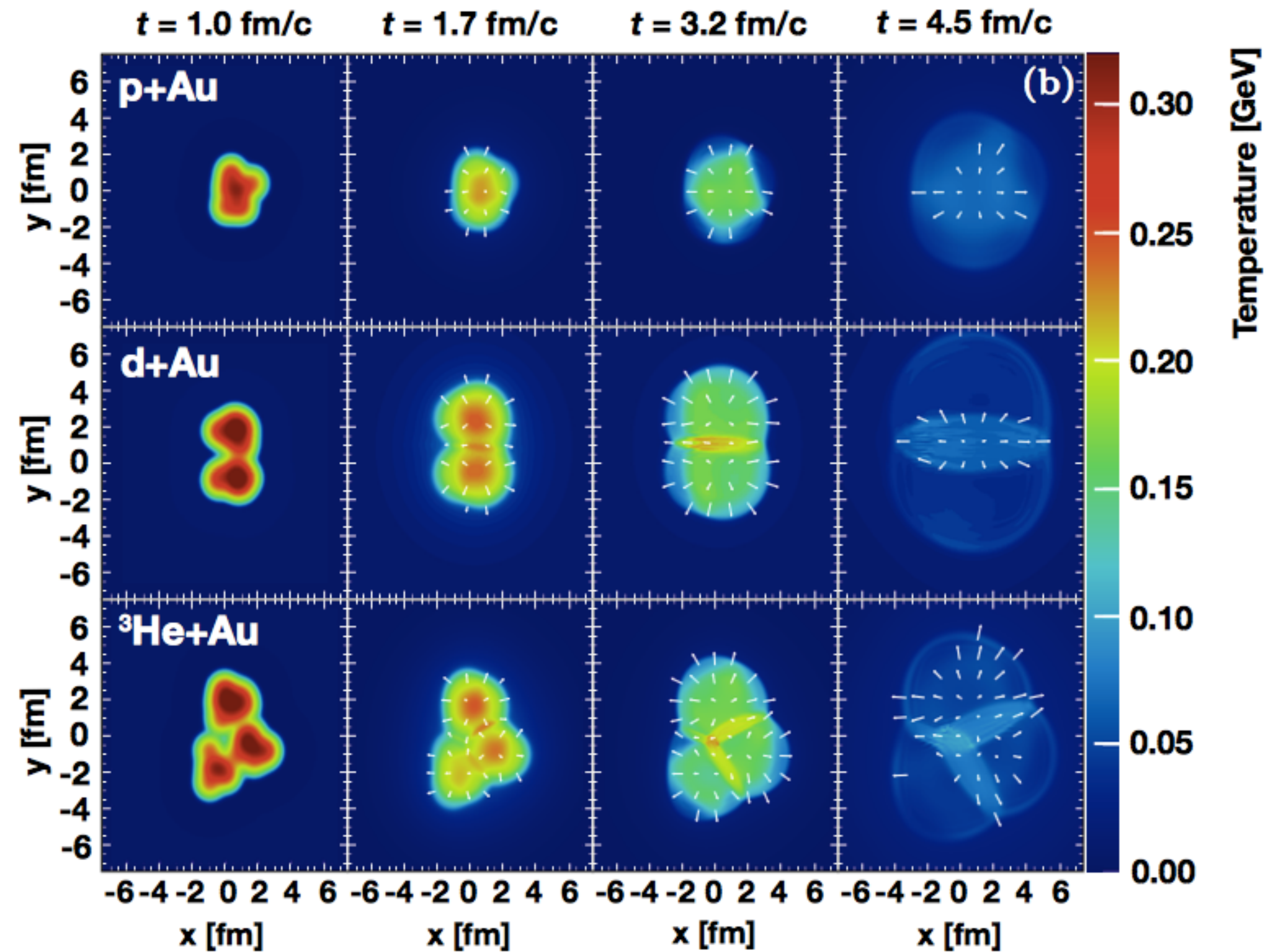
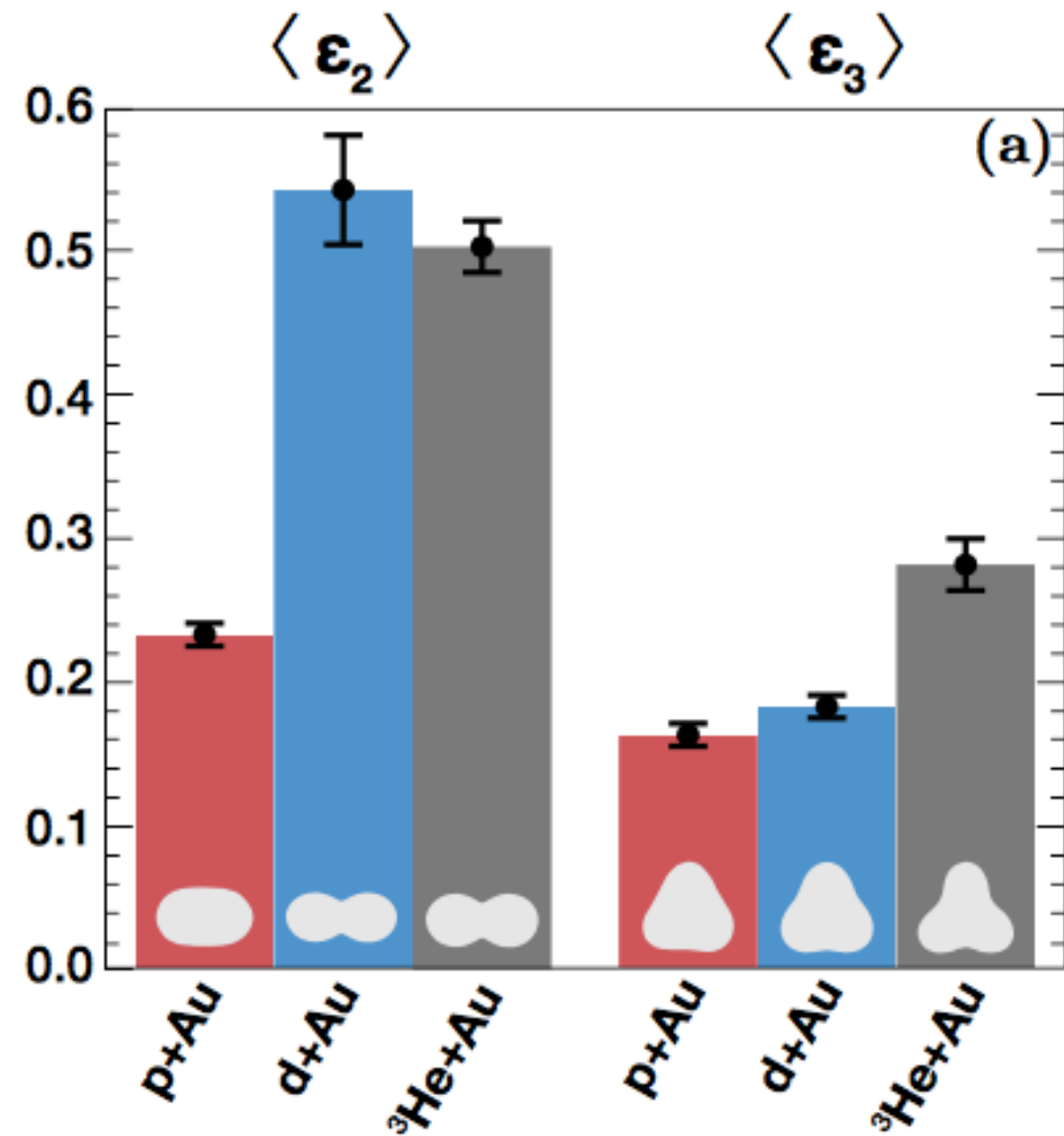
superSONIC for p+Pb,  $\sqrt{s}=5.02$  TeV, 0-5%

superSONIC for Pb+Pb,  $\sqrt{s}=5.02$  TeV, 0-5%



# Hydro in Small Systems

*Nature Physics* **15**, 214–220 (2019)  
 PHENIX collaboration

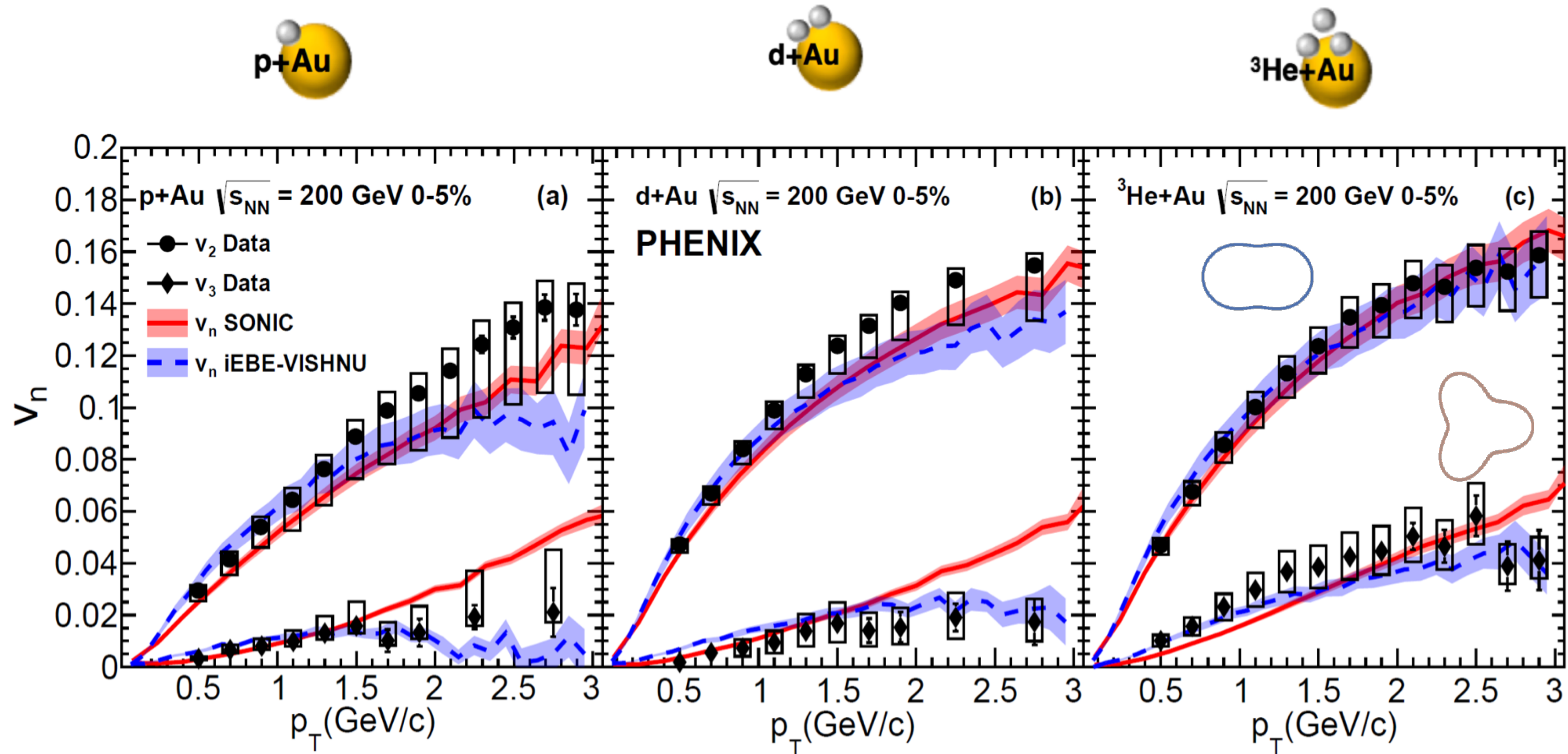


Expectation from hydro arguments:  

$$v_2^{p+Au} < v_2^{d+Au} \approx v_2^{^3\text{He}+Au},$$

$$v_3^{p+Au} \approx v_3^{d+Au} < v_3^{^3\text{He}+Au}.$$

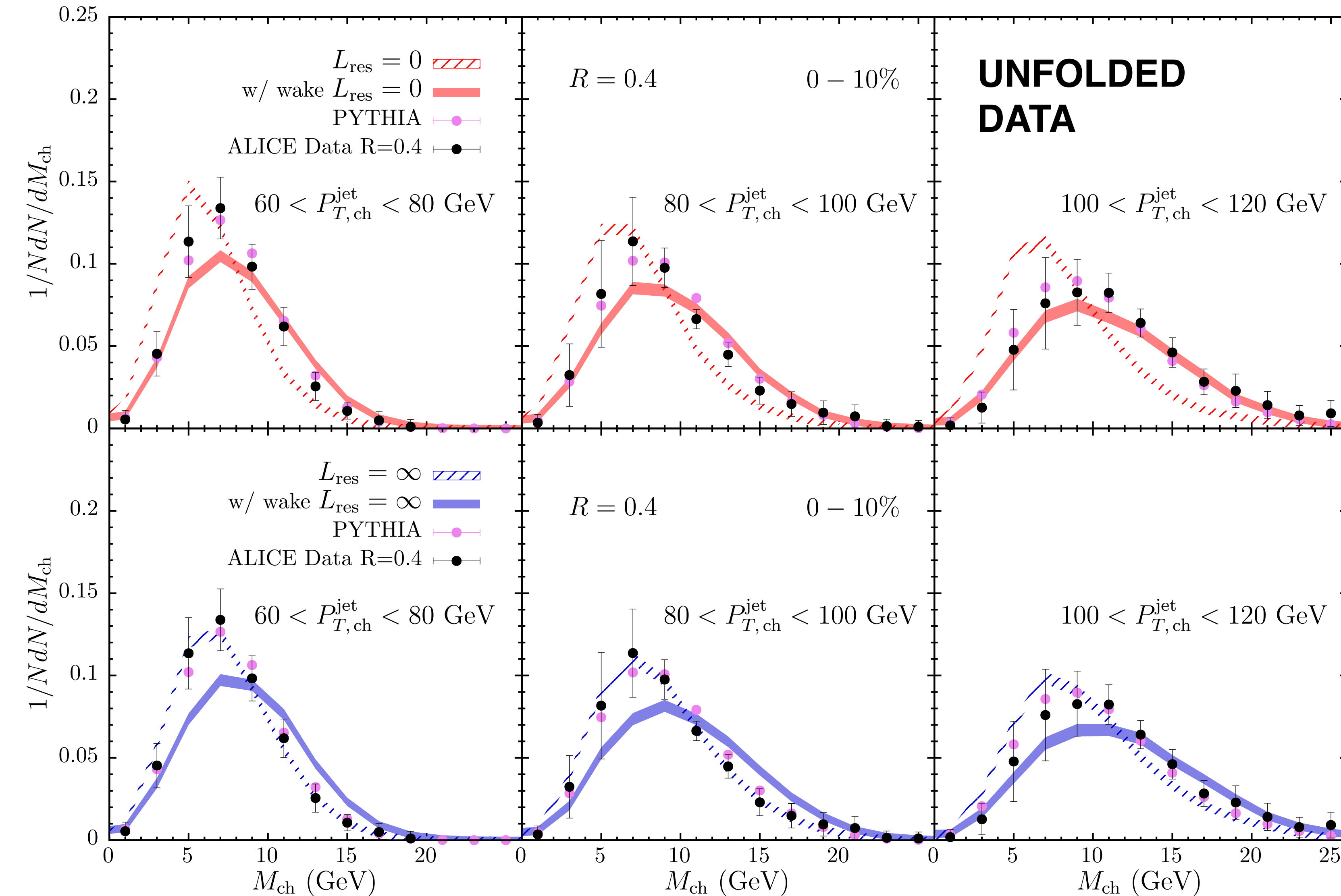
# Hydro in Small Systems



Expectation from hydro arguments:  
 $v_2^{p+Au} < v_2^{d+Au} \approx v_2^{3\text{He}+Au}$ ,  
 $v_3^{p+Au} \approx v_3^{d+Au} < v_3^{3\text{He}+Au}$ .

*Nature Physics* **15**, 214–220 (2019)  
 PHENIX collaboration

# A frustrating observable: charged jet mass



**Without wake:**

$$L_{\text{res}} = 0$$

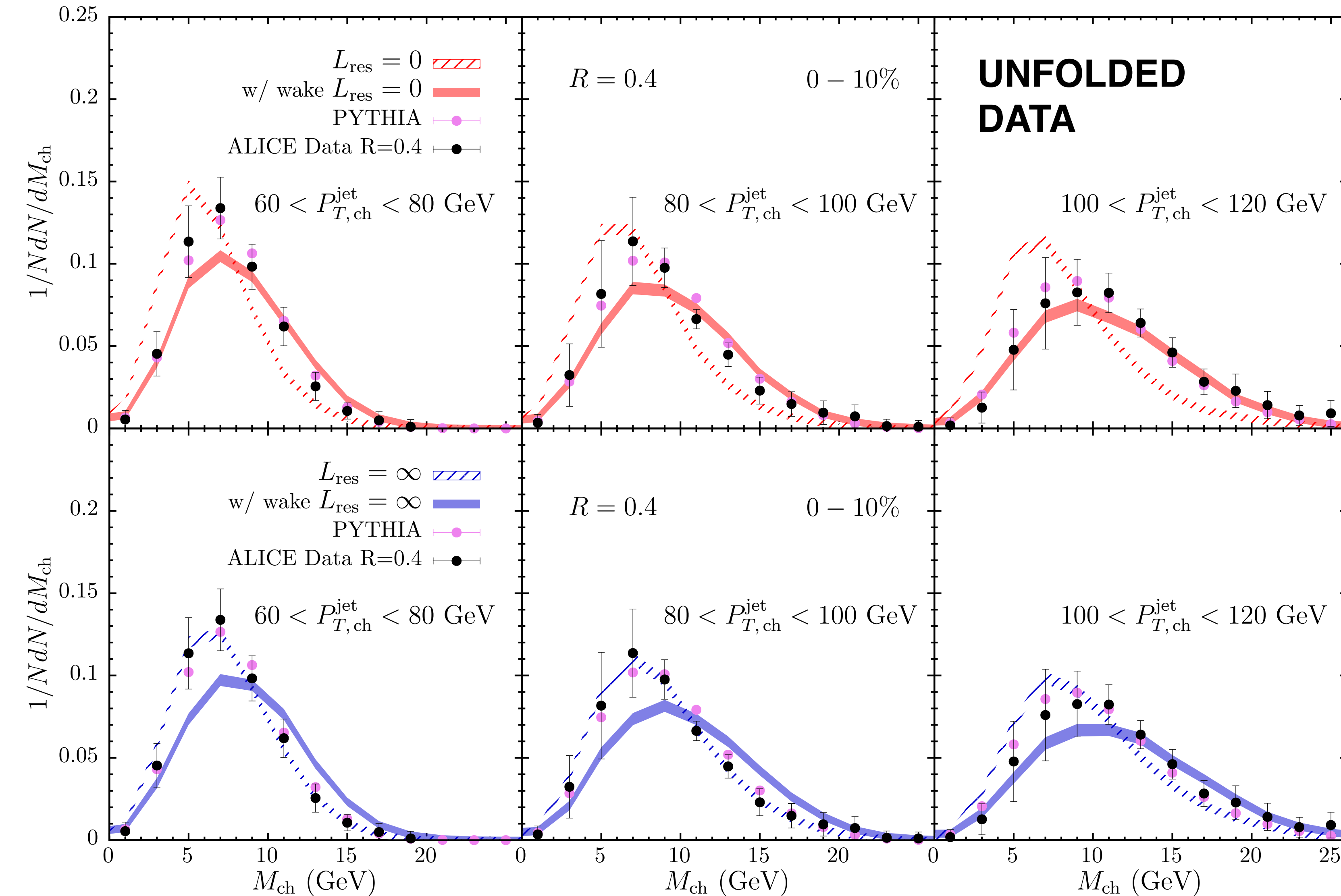
shift towards smaller masses

$$L_{\text{res}} = \infty$$

barely any modification

Larger mass jets  
are more active;  
*more suppressed if  
substructure resolved.*

# A frustrating observable: charged jet mass



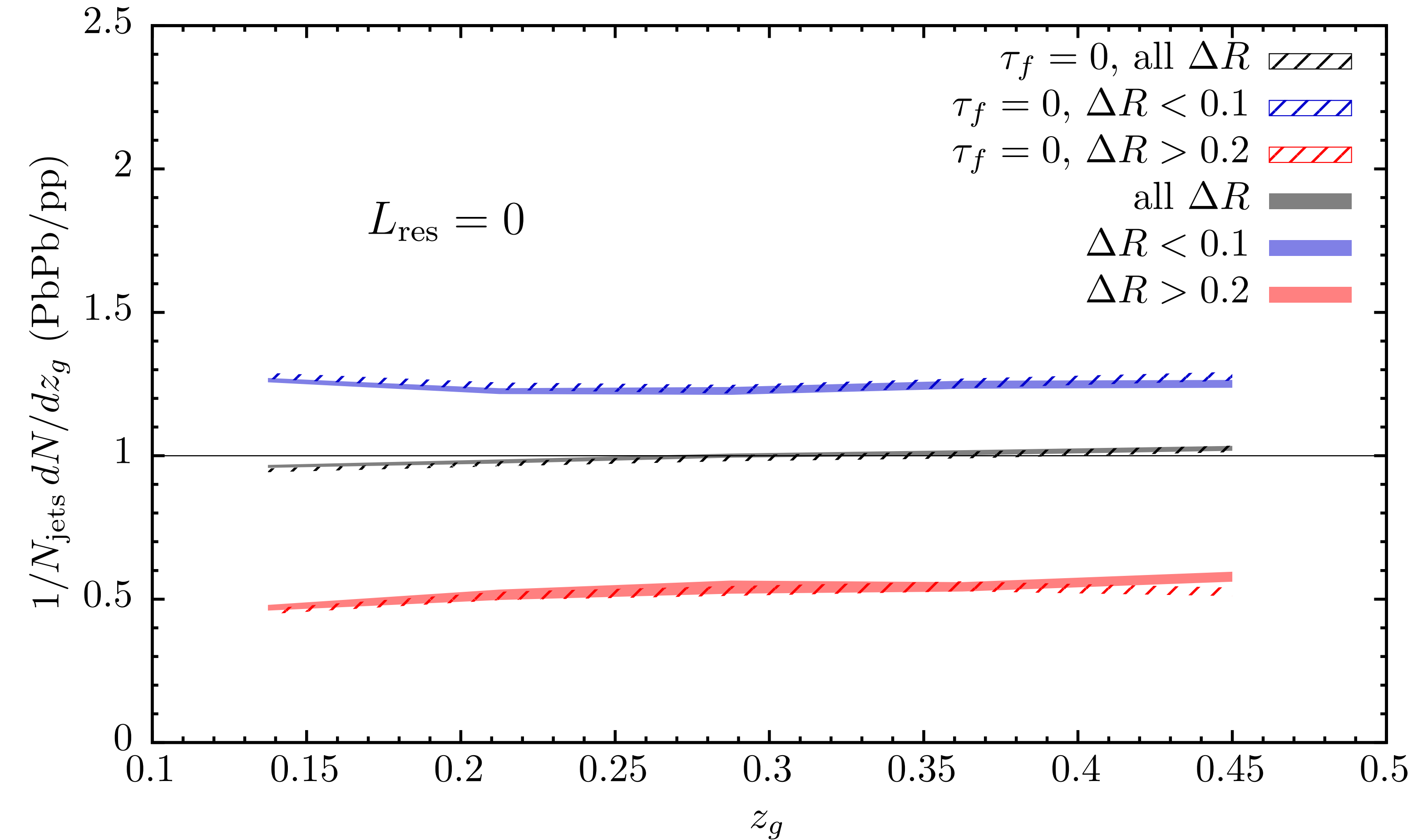
**With wake:**

Soft particles from the wake increase the mass, compensating quenching.

$L_{\text{res}} = 0$  and  $L_{\text{res}} = \infty$  barely distinguishable!

Surprisingly good description of data across three  $p_T$  ranges, after cancellation of effects...

# The role of formation time



Is wide configuration suppressed because formed early?

Radical test:

Assume all formation times are zero.

→ Small adjustment of kappa.

→ Almost no change in  $\Delta R$  ordering.

**Observable dominated by correlation between  $\Delta R$  and multiplicity.**



# Cutting the Lund Plane

Difference PbPb-pp  
of 1st SD splitting Lund plane

Flat

Removes soft & soft-collinear

Core

Removes soft-wide

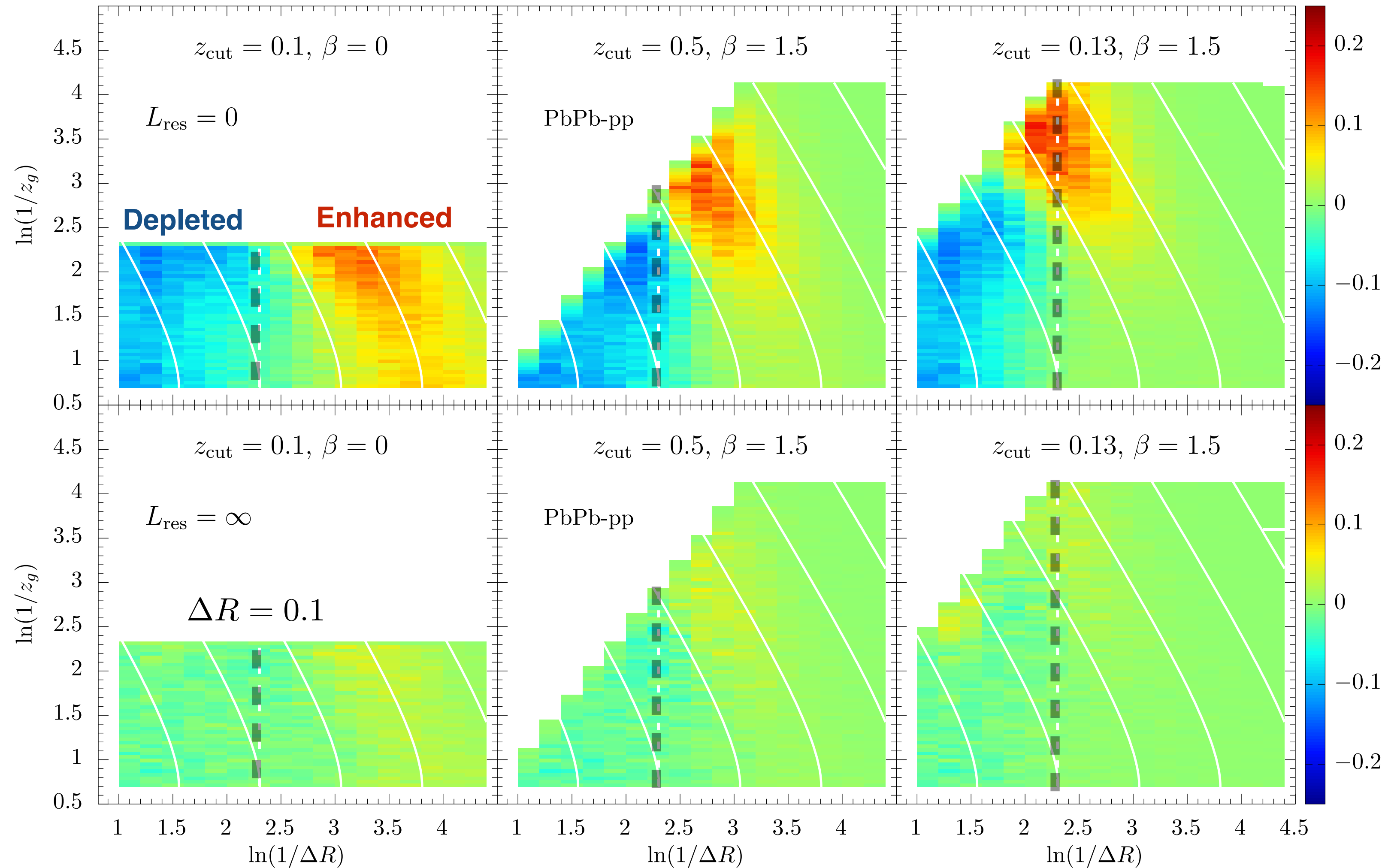
Soft-core

Extends soft-collinear region

Flat

Core

Soft-core



CMS angularity limit:  $\Delta R > 0.1$

# Cutting the Lund Plane

**Difference PbPb-pp  
of 1st SD splitting Lund plane**

**Flat**

Removes soft & soft-collinear

**Core**

Removes soft-wide

**Soft-core**

Extends soft-collinear region

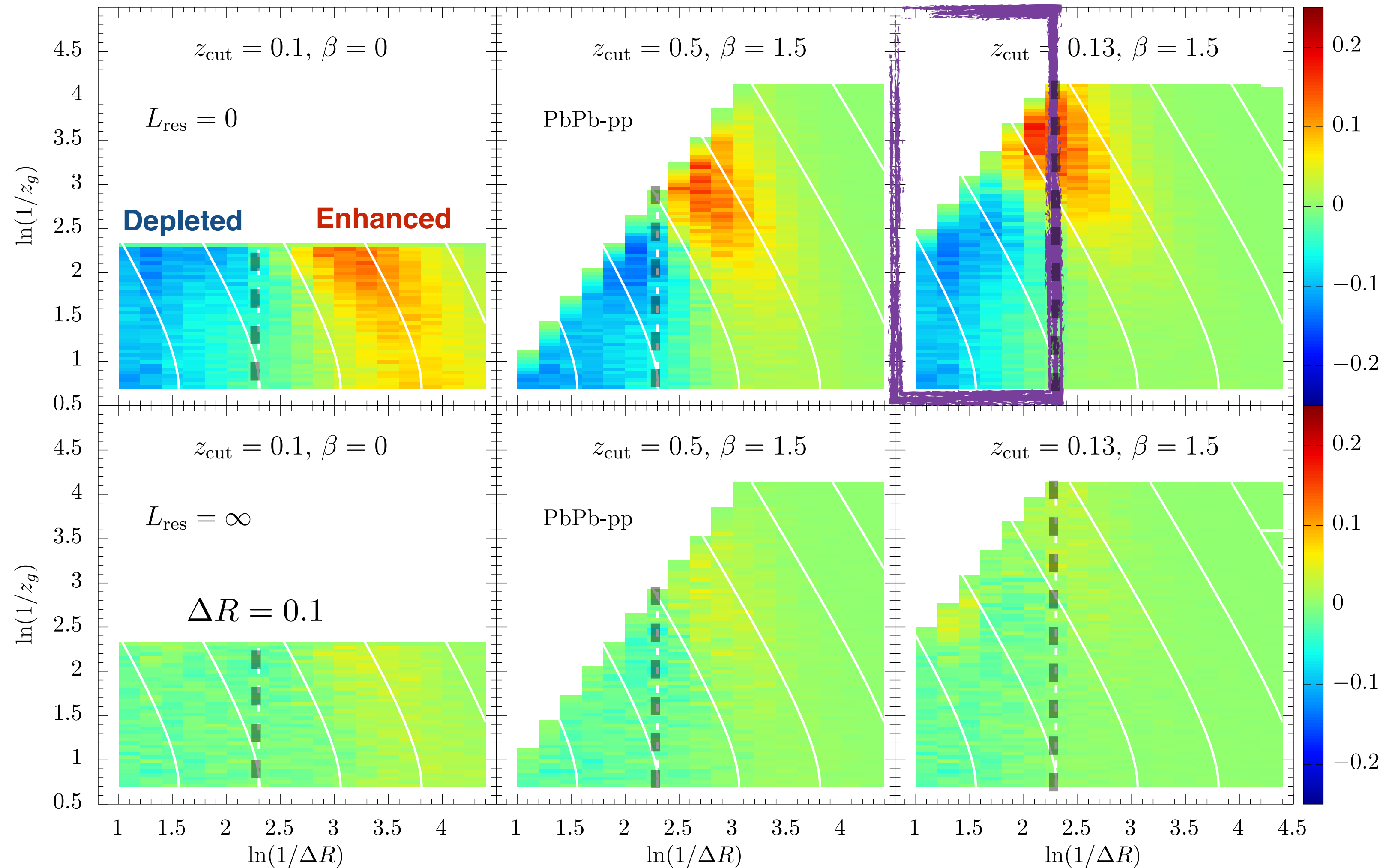
*Enhances Lund plane  
structure above  $\Delta R > 0.1$*

CMS angularity limit:  $\Delta R > 0.1$

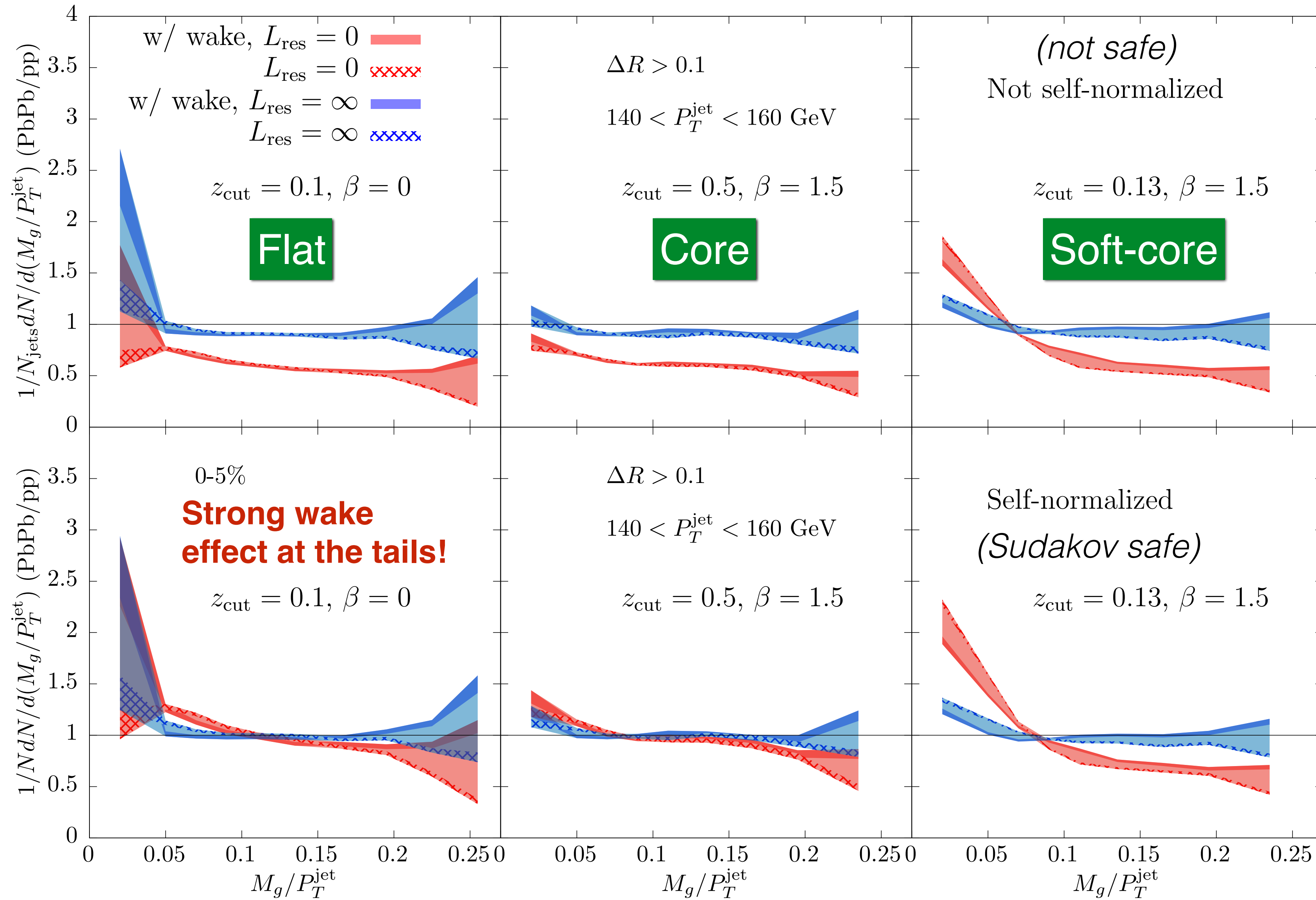
**Flat**

**Core**

**Soft-core**



# Groomed jet mass



Flat

Core

**Not self-normalized:**

merely reflect absence of wide angle configurations

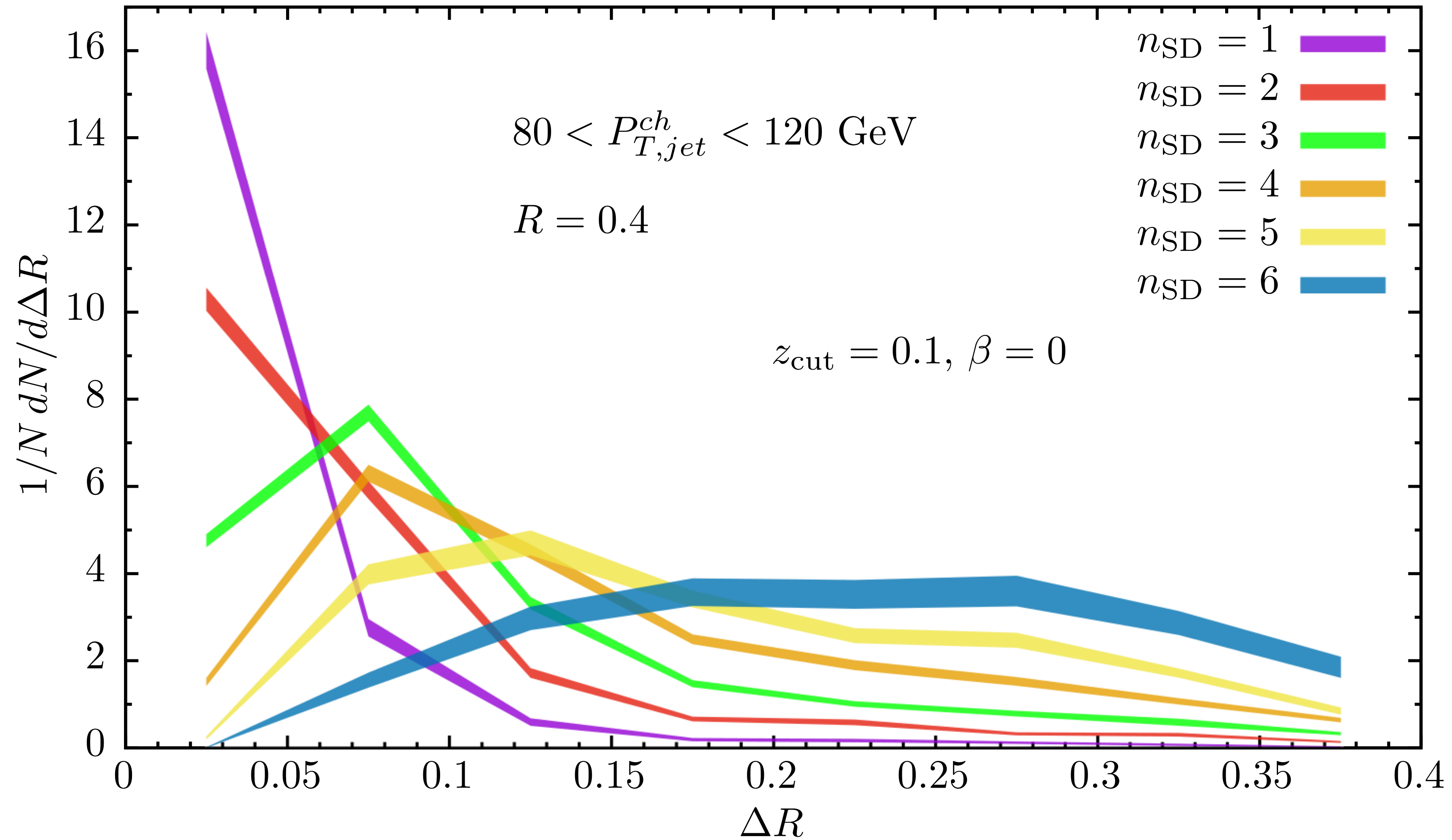
**Self-normalized:**

differences due to  $L_{\text{res}}$  of the size of the wake effect

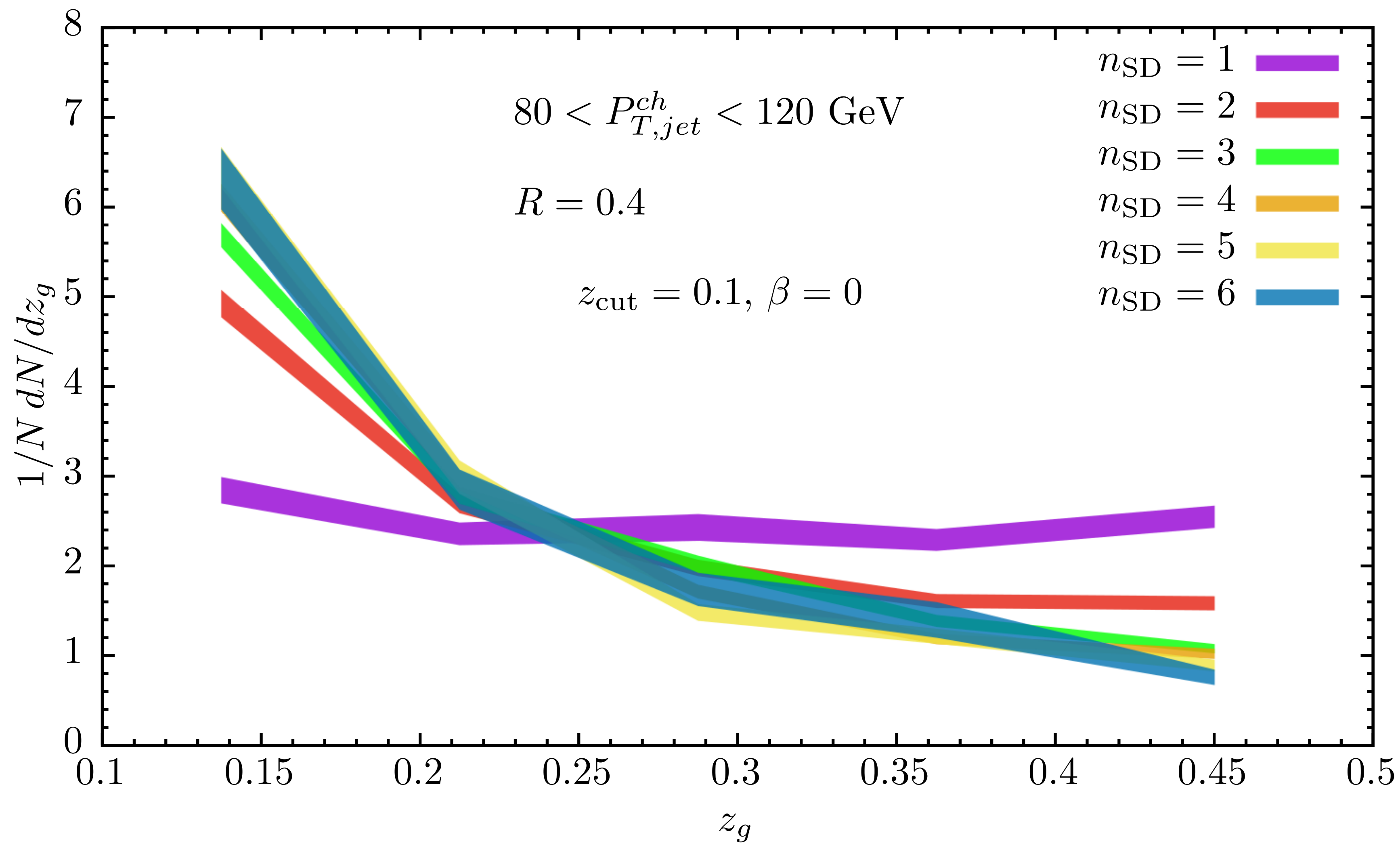
Soft-core

**Strong discriminating power, not relying on the norm.**

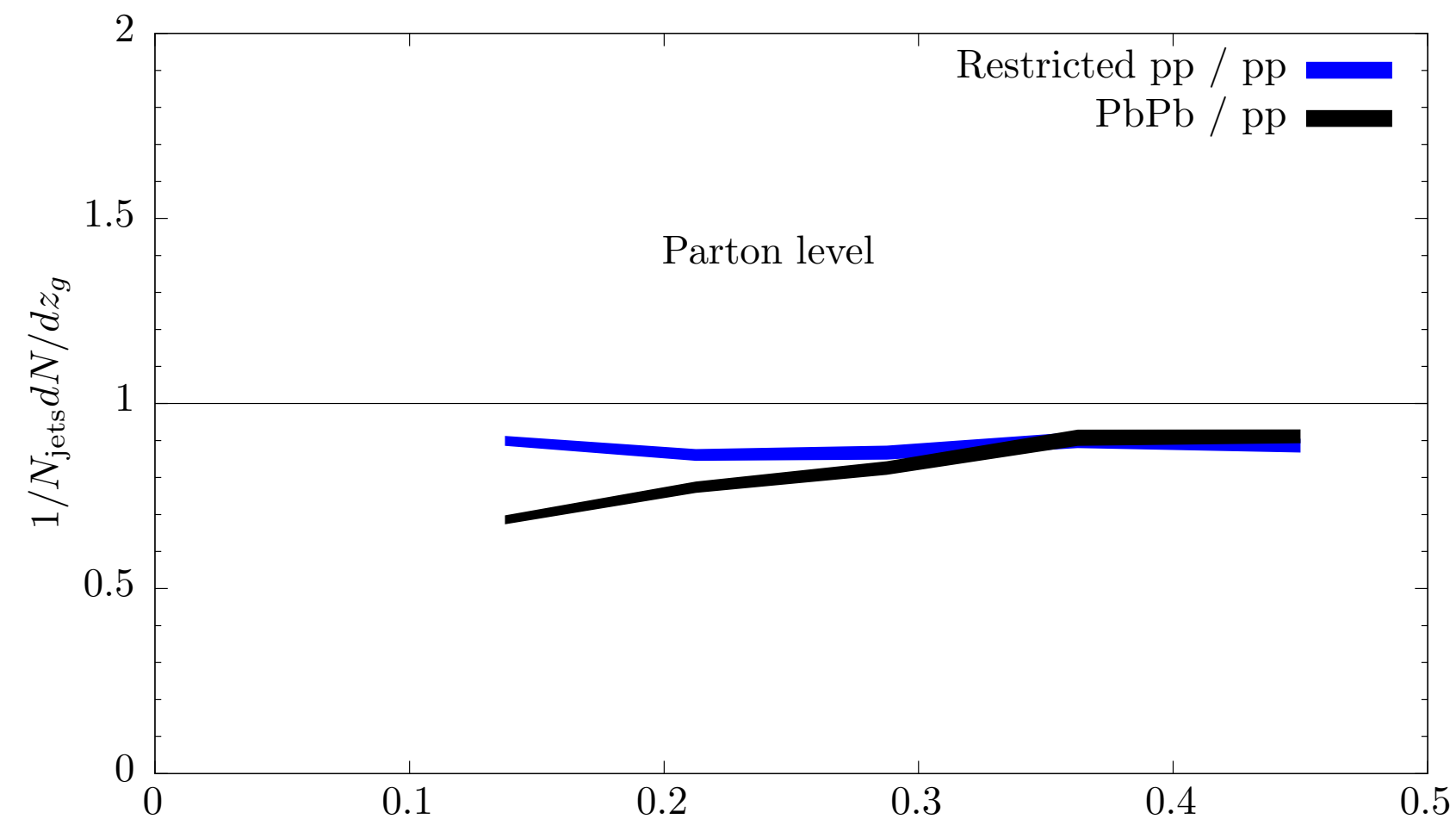
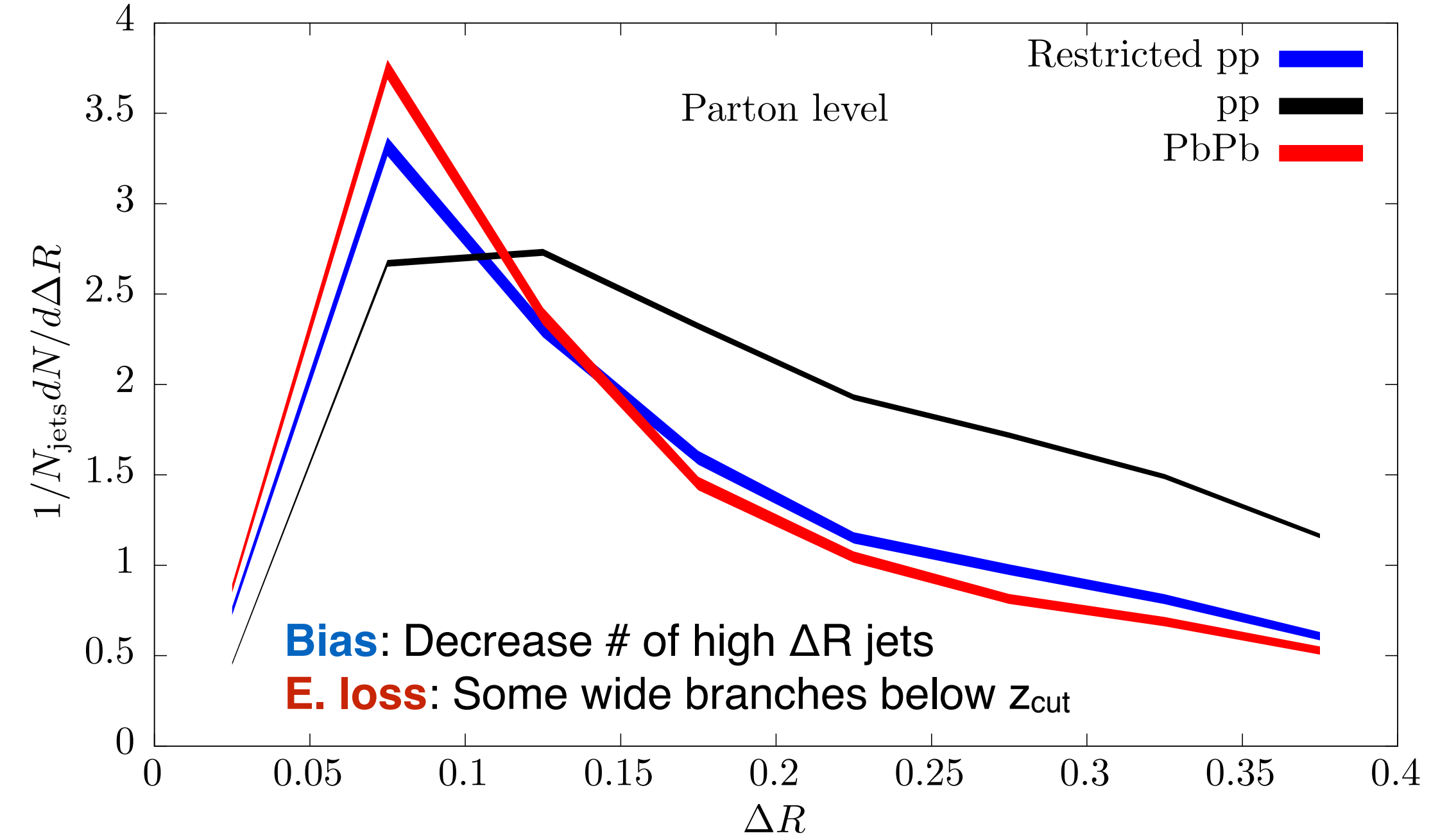
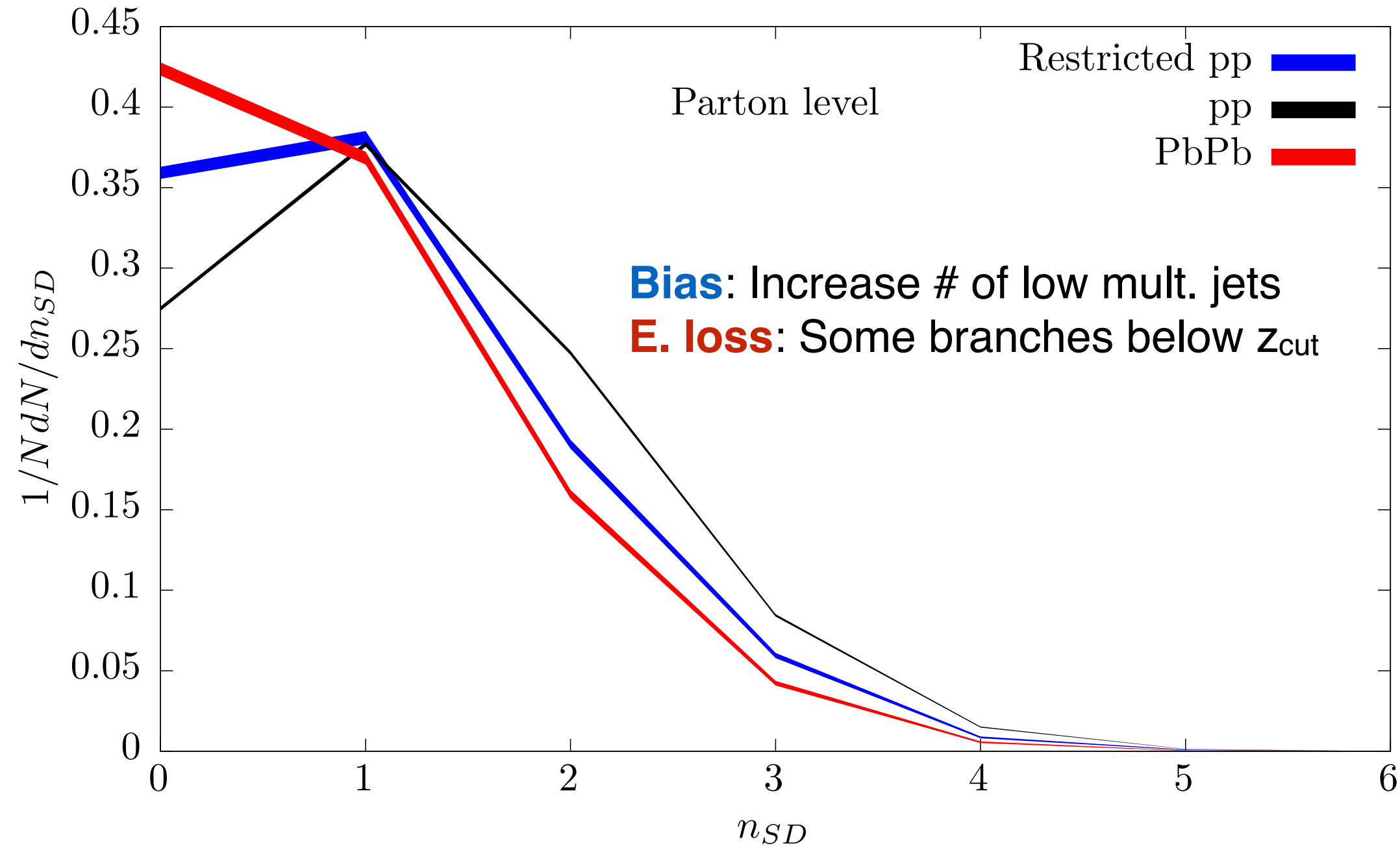
# Correlation between $n_{SD}$ and $\Delta R$



# Correlation between $n_{SD}$ and $z_g$

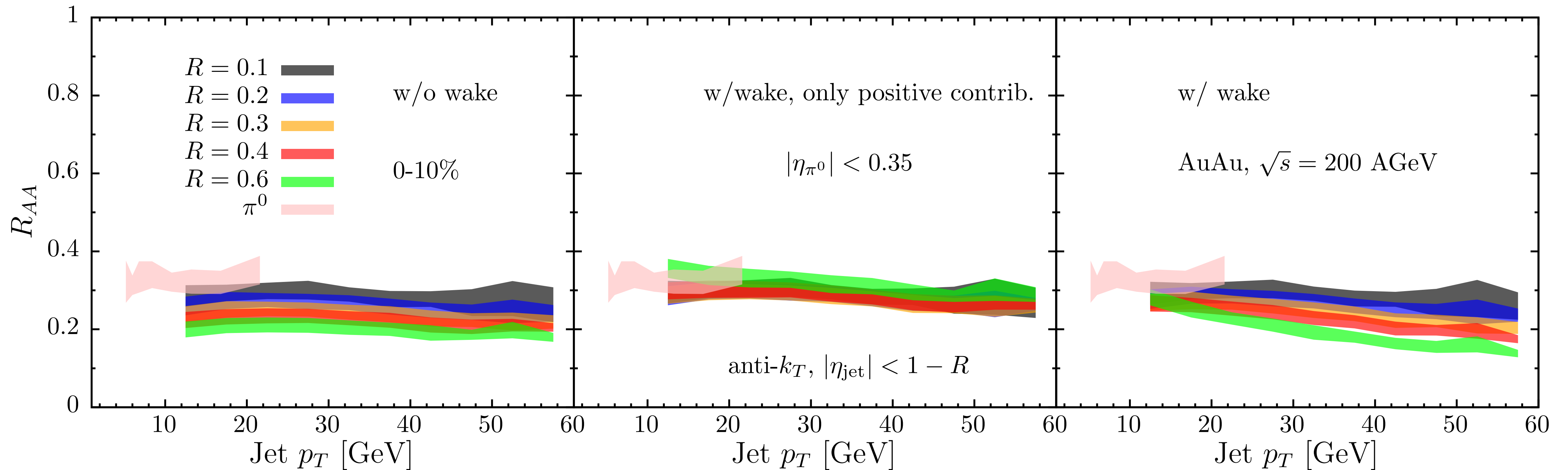


# A careful look into the selection bias



**Restricted pp:** sample of pp jets from which the “surviving” sample of PbPb jets come from

# Jet suppression vs. $R$ at RHIC



- QGP trough effect more pronounced at RHIC than at LHC; effect increases with jet  $p_T$ .

→ steeper spectrum

reduced dijet rapidity gap.

$R_{AA}$  more sensitive to  $\Delta E$ .