

Water Cherenkov ν -Detectors & GEANT4

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Cherenkov photon emission

If the velocity of a particle is such that

$$v_p > c/n(\lambda)$$

where $n(\lambda)$ → the index of refraction of the material,

a pulse of light is emitted around the particle direction with an opening angle (θ_c)

Cherenkov photon emission

- A charged particle moves faster than the phase velocity of light in a medium →

electrons interacting with the particle can emit coherent photons while conserving energy and momentum

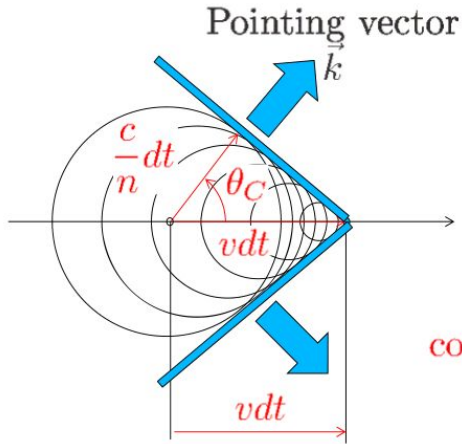
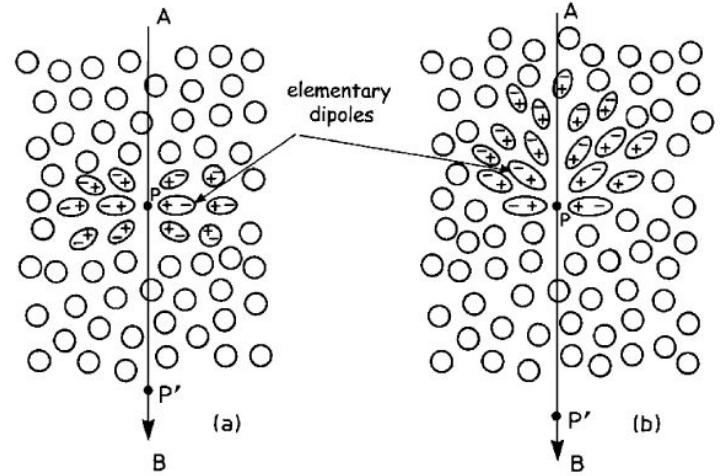
- It is actually not the particle that emits light, but the bounded (dielectric) electrons of the immediately surrounding medium
- Emission is coherent →

in phase with the particle velocity

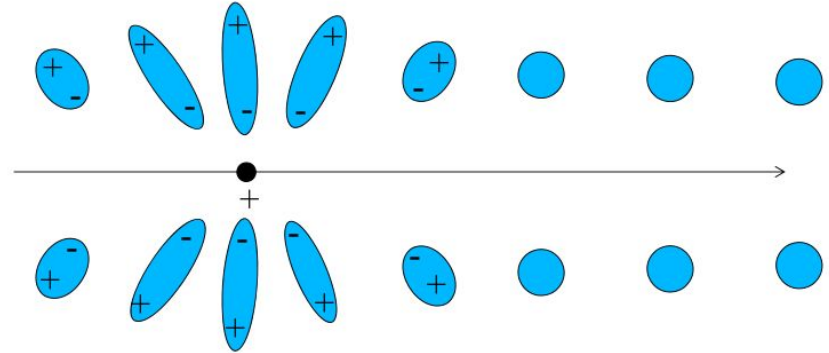
- Discovery: Cerenkov and Vavilov in 1934
- Explanation: Tamm and Frank in 1937

Cherenkov photon emission

- Dielectric medium electrons polarized by a moving charged particle
- De-excitation gives rise to a coherent radiation
- Same basic process as energy loss (Bethe, Fermi)



$$\cos \theta_C = \frac{c}{nv} = \frac{1}{n\beta}$$



Cherenkov photon emission

The energy emitted per unit length dx travelled by the particle per unit of angular frequency $d\omega$ is:

$$dE = \frac{q^2}{4\pi} \mu(\omega) \omega \left(1 - \frac{c^2}{v^2 n^2(\omega)} \right) dx d\omega$$

provided that $\beta = \frac{v}{c} > \frac{1}{n(\omega)}$. Here $\mu(\omega)$ and $n(\omega)$ are the frequency-dependent permeability and index of refraction of the medium, q is the electric charge of the particle, v is the speed of the particle, and c is the speed of light in vacuum.

Consequences:

- the **yield** of photons is **flat** versus these photons energy ($h\nu$).
- the **yield** of photons is $\propto \lambda^{-2} \Rightarrow$ prominent at small wavelengths (UV)
- the spectrum is continuous \neq fluorescence

Cherenkov photon emission

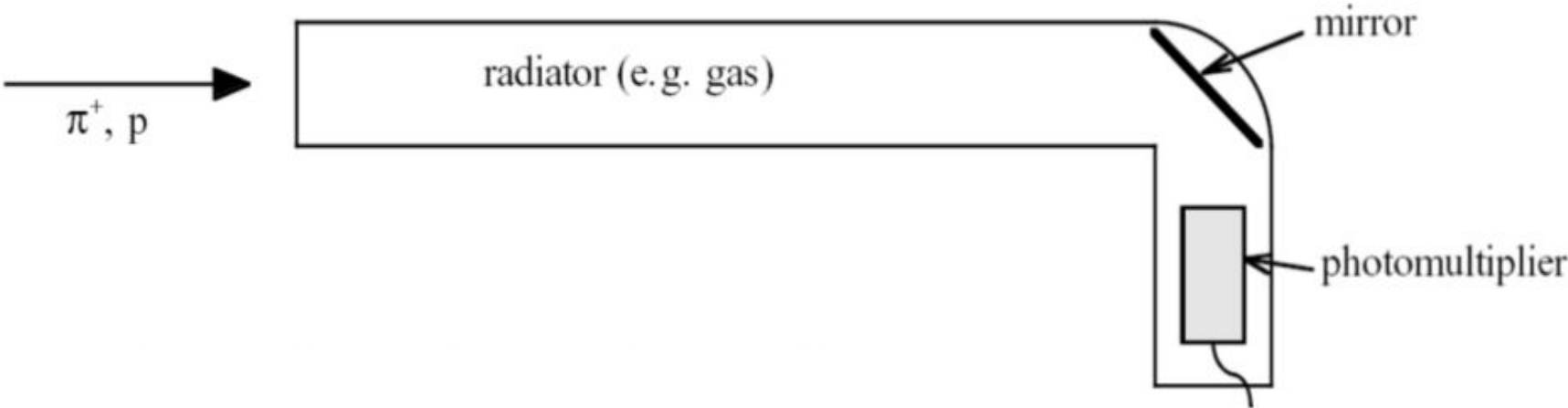
The total amount of energy radiated per unit length is:

$$\frac{dE}{dx} = \frac{q^2}{4\pi} \int_{v > \frac{c}{n(\omega)}} \mu(\omega) \omega \left(1 - \frac{c^2}{v^2 n^2(\omega)} \right) d\omega$$

This integral is done over the frequencies ω for which the particle's speed v is greater than speed of light of the media $\frac{c}{n(\omega)}$. The integral is non-divergent because at high frequencies the refractive index becomes less than unity.

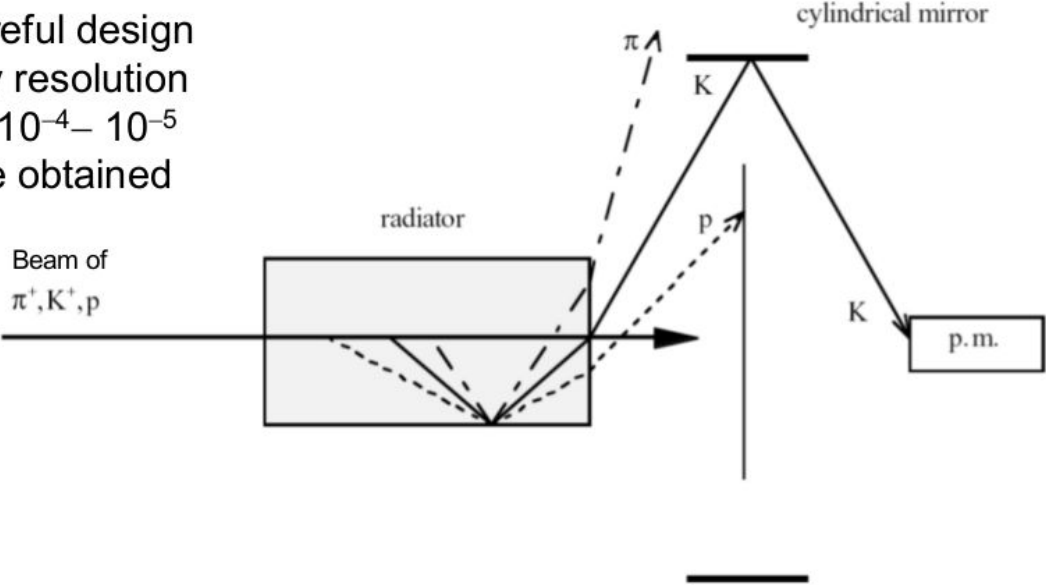
$$\frac{dE}{dx} = \frac{q^2}{4\pi} \int_{v > \frac{c}{n(\omega)}} \mu(\omega) \omega \left(1 - \frac{1}{\beta^2 n^2(\omega)} \right) d\omega$$

A basic Cherenkov detector

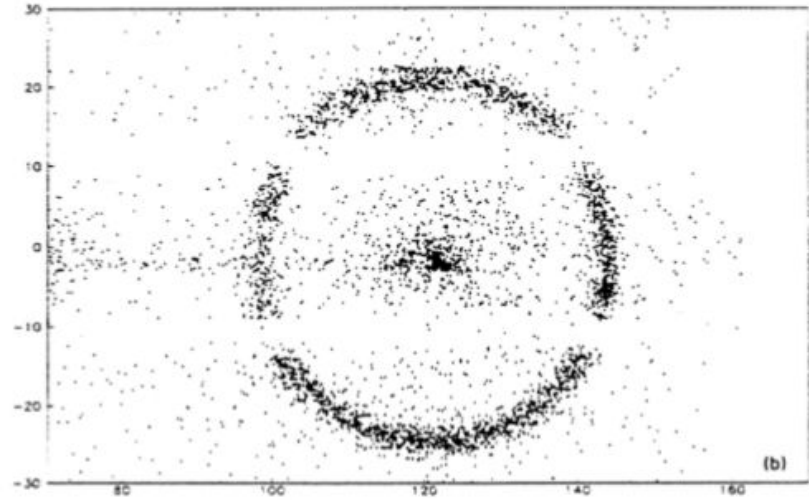
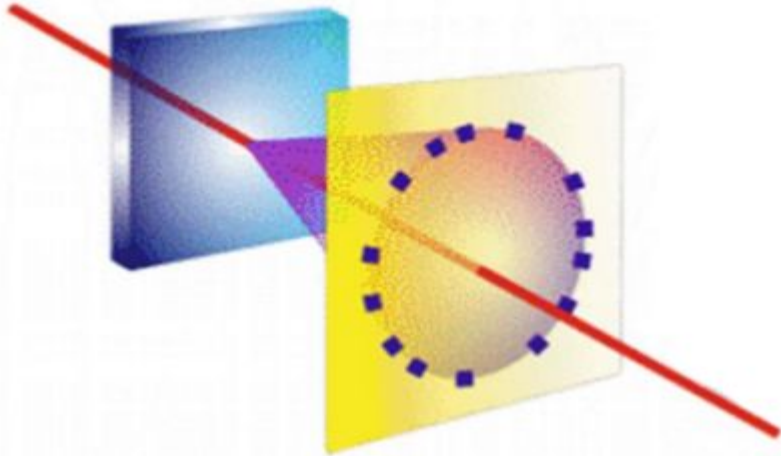


Distinguishing Particles using a Cherenkov detectors

With careful design
velocity resolution
 $\sigma_{\beta}/\beta \approx 10^{-4} - 10^{-5}$
can be obtained



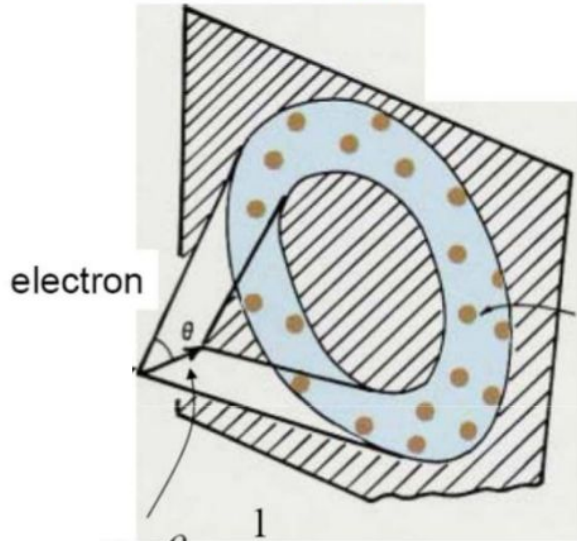
Detection Basics



Cherenkov radiator options

Material	$n-1$	β_c	θ_c	photons/cm
solid natrium	3.22	0.24	76.3	462
Lead sulfite	2.91	0.26	75.2	457
Diamond	1.42	0.41	65.6	406
Zinc sulfite	1.37	0.42	65	402
silver chloride	1.07	0.48	61.1	376
Flint glass	0.92	0.52	58.6	357
Lead crystal	0.67	0.6	53.2	314
Plexiglass	0.48	0.66	47.5	261
Water	0.33	0.75	41.2	213
Aerogel	0.075	0.93	21.5	66
Pentan	1.70E-03	0.9983	6.7	7
Air	2.90E-03	0.9997	1.38	0.3
He	3.30E-05	0.999971	0.46	0.03

Cherenkov in water



$$\cos \theta = \frac{1}{n\beta}$$

$n=1.34$ in water

→ $\theta = 42\text{deg.}$ for $\beta = 1$

- No. of Cherenkov photons with wavelength 300-600 nm, emitted by a relativistic particle per cm is about 340

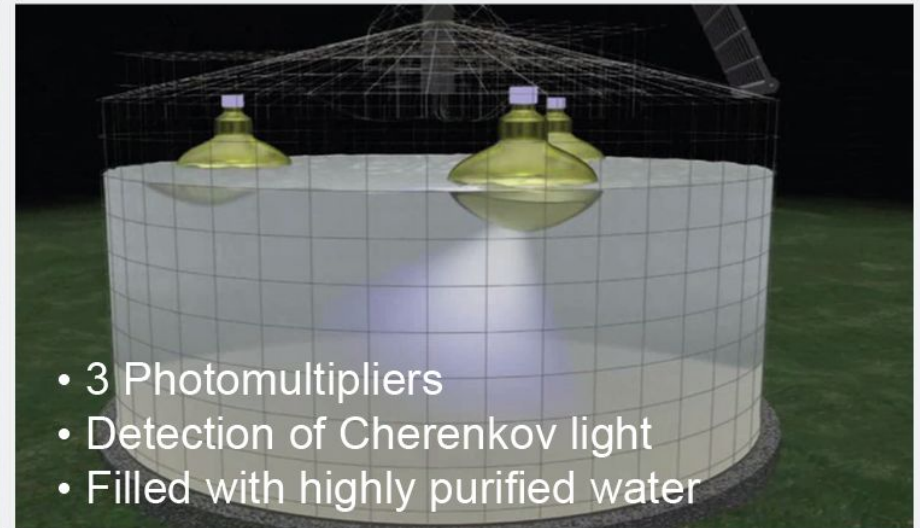
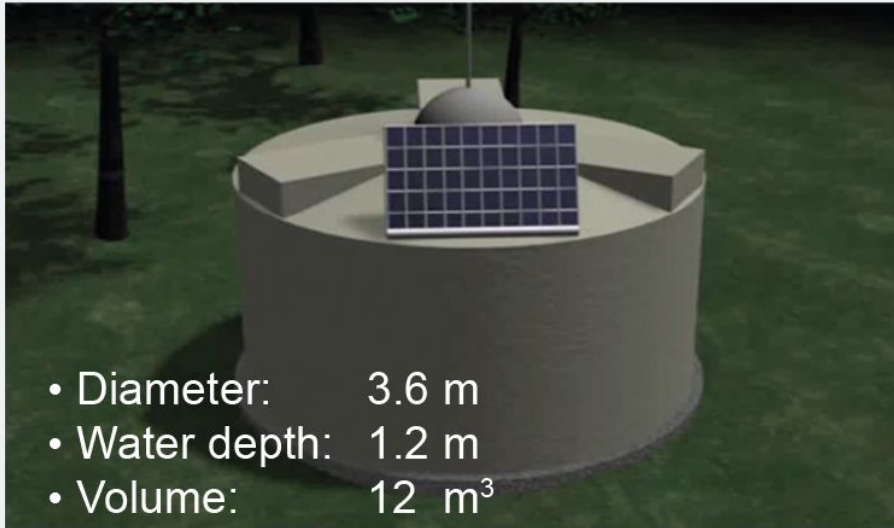
We require,

- Efficient detection of the photons
- Large Photodetectors

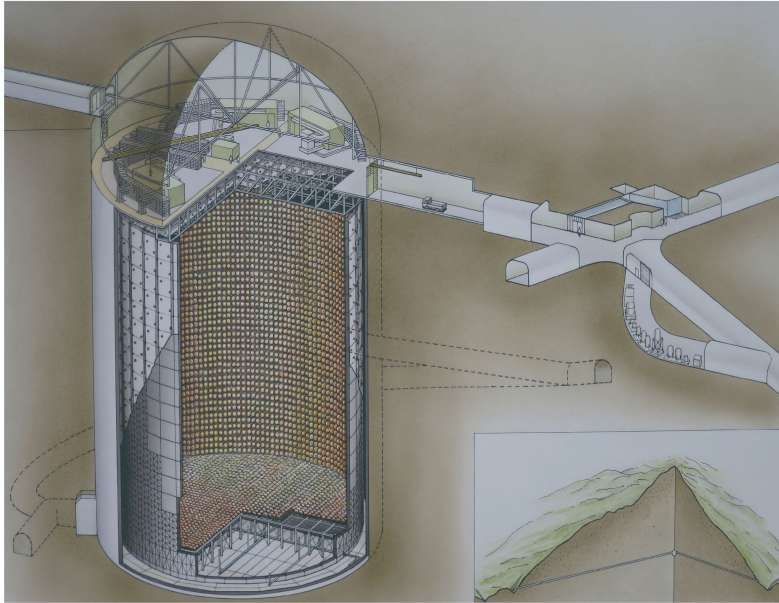
Water Cherenkov Detector in Auger Experiment

Surface Detector

1,660 surface detector stations
(1,500 m apart from each other)



Super-Kamiokande Neutrino Experiment



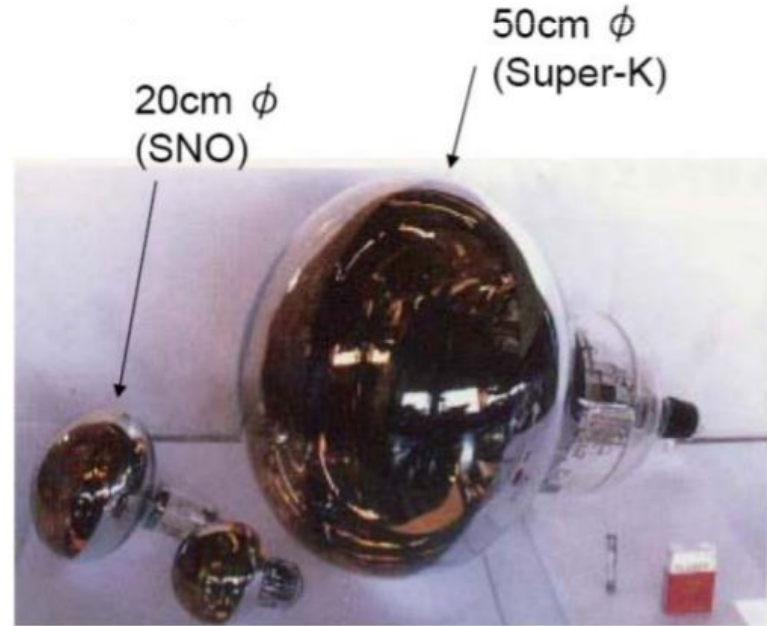
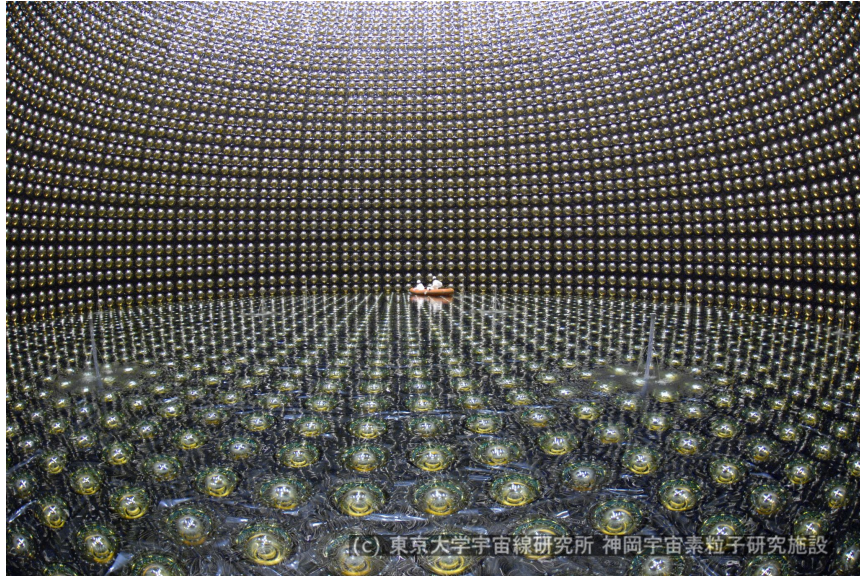
SUPERKAMIOKANDE INSTITUTE FOR COSMIC RAY RESEARCH UNIVERSITY OF TOKYO

(C) 東京大学宇宙線研究所 神岡宇宙素粒子研究施設

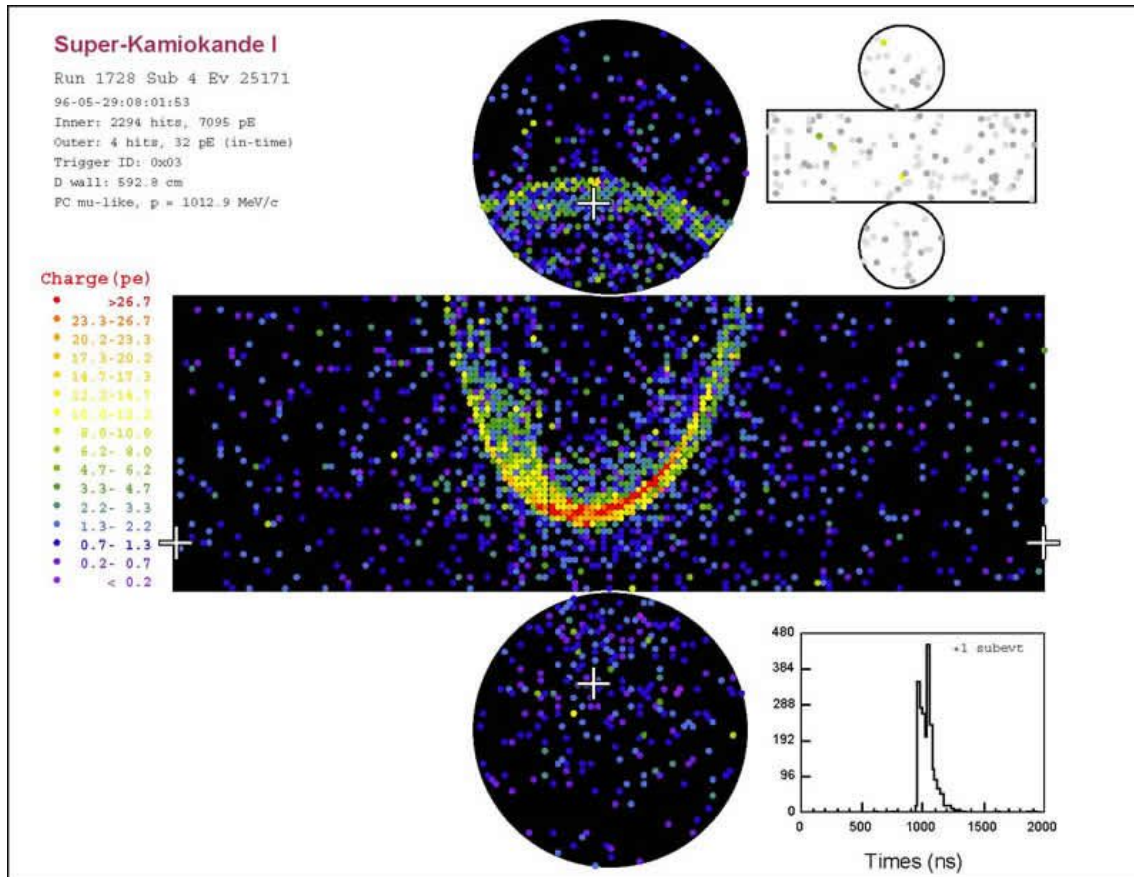
1982/1/30

- A cylindrical (39.3 m dia & 41.4 m) high stainless steel tank, PMTs installed to the detector wall.
- 50 kt water.
- The PMT support structure divides the tank into two distinct, optically isolated volumes:
 - inner detector (ID)
 - outer detector (OD)
- The inwarded PMTs are installed to the ID wall and the outwarded PMTs to the OD wall.

Super-Kamiokande Neutrino Experiment: Detectors



Cherenkov at SK

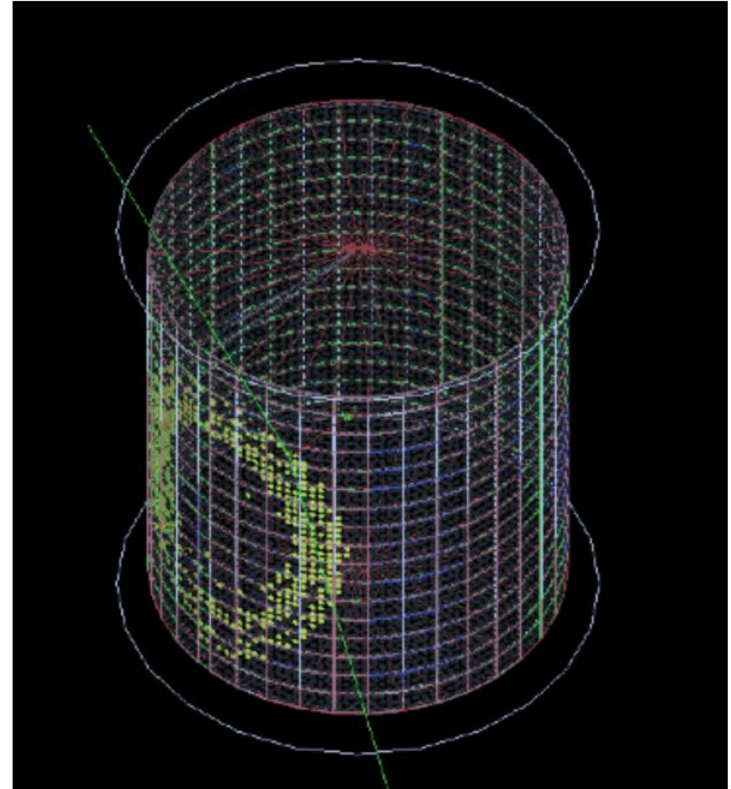


A Water Cherenkov Simulator Framework

WCSim

- Open-source
- GEANT4-based code for water cherenkov detectors.

<https://github.com/Wcsim/WCSim>



What can we do?

Construct the Detector

Particle Interactions

Detector Outputs

Trigger

Digitization of the Output

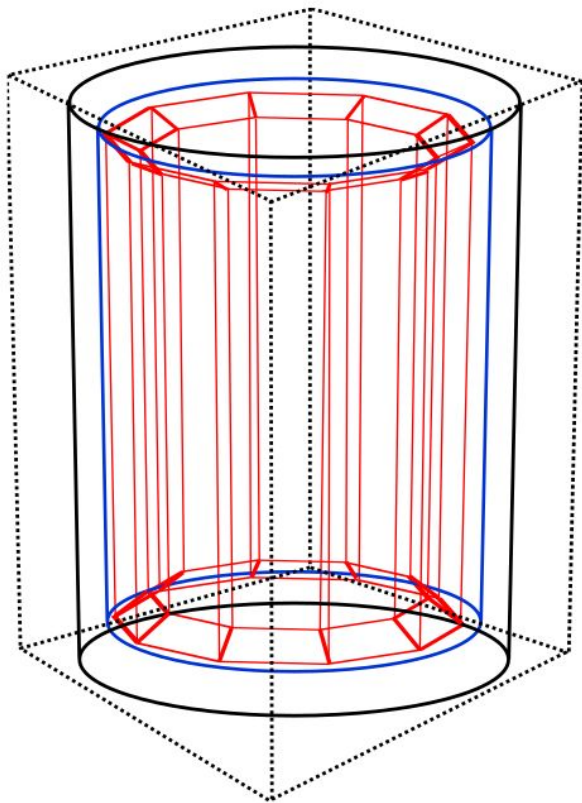
Output Storage &
Further Analysis

```
WCSimConstructCylinder.cc  
WCSimConstructEggShapedHyperK.cc  
WCSimConstructGeometryTables.cc  
WCSimConstructMaterials.cc  
WCSimConstructPMT.cc  
WCSimDarkRateMessenger.cc  
WCSimDetectorConfigs.cc  
WCSimDetectorConstruction.cc  
WCSimDetectorMessenger.cc  
WCSimEnumerations.cc  
WCSimEventAction.cc  
WCSimLC.cc  
WCSimPhysicsListFactory.cc  
WCSimPhysicsListFactoryMessenger.cc  
WCSimPmtInfo.cc  
WCSimPMTObject.cc  
WCSimPMTQE.cc  
WCSimPrimaryGeneratorAction.cc  
WCSimPrimaryGeneratorMessenger.cc  
WCSimRandomMessenger.cc  
WCSimRootDict.cc  
WCSimRootDict.h  
WCSimRootDict_rdict.pcm  
WCSimRootEvent.cc  
WCSimRootGeom.cc  
WCSimRootOptions.cc  
WCSimRootTools.cc  
WCSimRunAction.cc  
WCSimRunActionMessenger.cc  
WCSimStackingAction.cc  
WCSimSteppingAction.cc  
WCSimTrackInformation.cc  
WCSimTrackingAction.cc  
WCSimTrajectory.cc  
WCSimTuningMessenger.cc  
WCSimTuningParameters.cc  
WCSimVisManager.cc  
WCSimWCAddDarkNoise.cc  
WCSimWCDAQMessenger.cc  
WCSimWCDigi.cc  
WCSimWCDigitizer.cc  
WCSimWCHit.cc  
WCSimWCPMT.cc  
WCSimWCSD.cc  
WCSimWCTrigger.cc
```

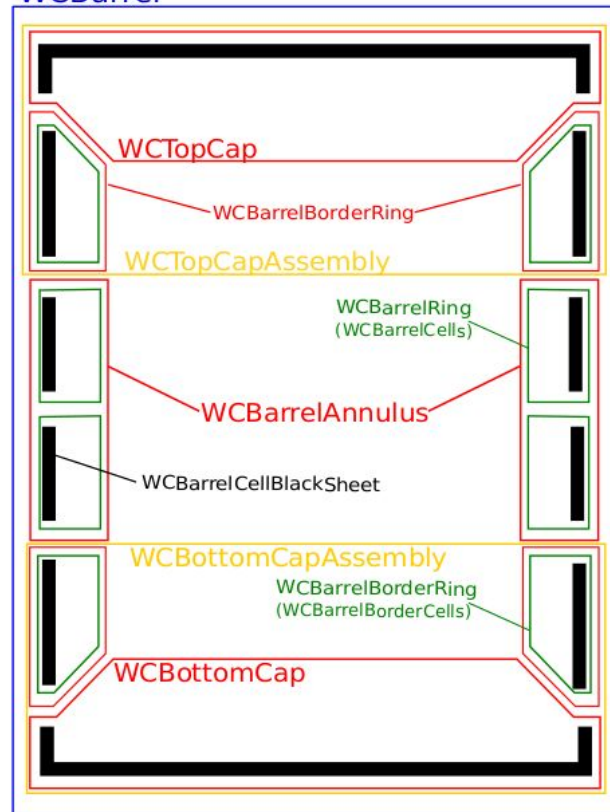
WCSim Geometry

- Consists of a cylindrical detector
- `src/WCSimConstructCylinder.cc`
- `WCSimDetectorConstruction::ConstructCylinder()`
- The inner detector : blacksheet and PMTs
- Active element: PMTs
- Blacksheet: goes around the back of the PMTs, reduces reflections and optically separates the inner and outer detector

Detector construction



WCBarrel

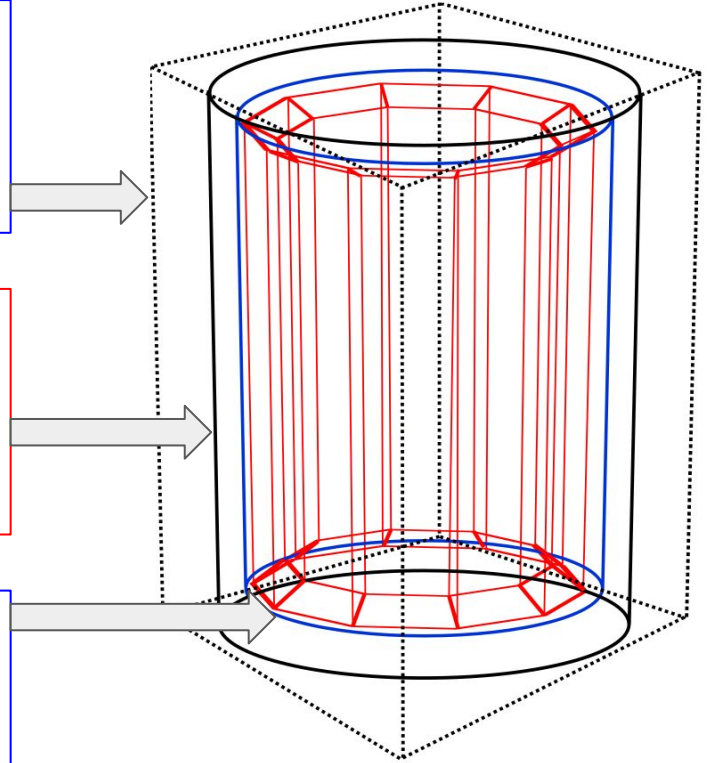


Hierarchy of Volumes

World Volume = ExpHall
File = src/WCSimDetectorConstruction.cc
Shape = Rectangular Box
Material = Air

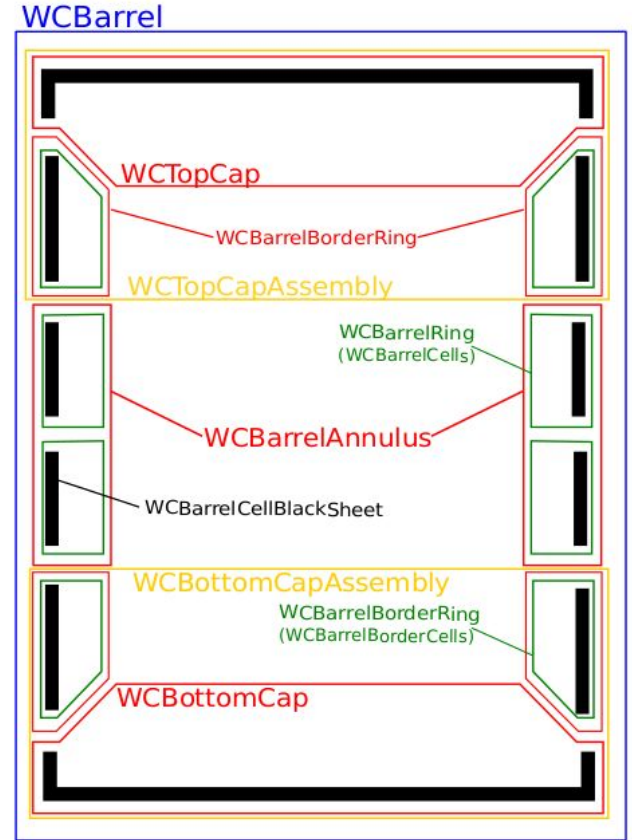
Daughter Volume = WC
File = src/WCSimConstructCylinder.cc
Shape = Tubs
Material = Air

Daughter Volume = WCBarrel
File = src/WCSimConstructCylinder.cc
Shape = Tubs
Material = Water



Hierarchy of Volumes

- WCBarel consists of: PMTs and blacksheets
- It is divided into two parts :
the annulus (WCBarelAnnulus) &
the caps (WCTopCapAssembly
and WCBottomCapAssembly)



Hierarchy of Volumes

WBarrelAnnulus



WBarrelRing



WBarrelCell

[Contains one or more PMTs WCPMT) and the blacksheet (WBarrelCellBlackSheet).

Each cell is flat, represents one modular detector section.]

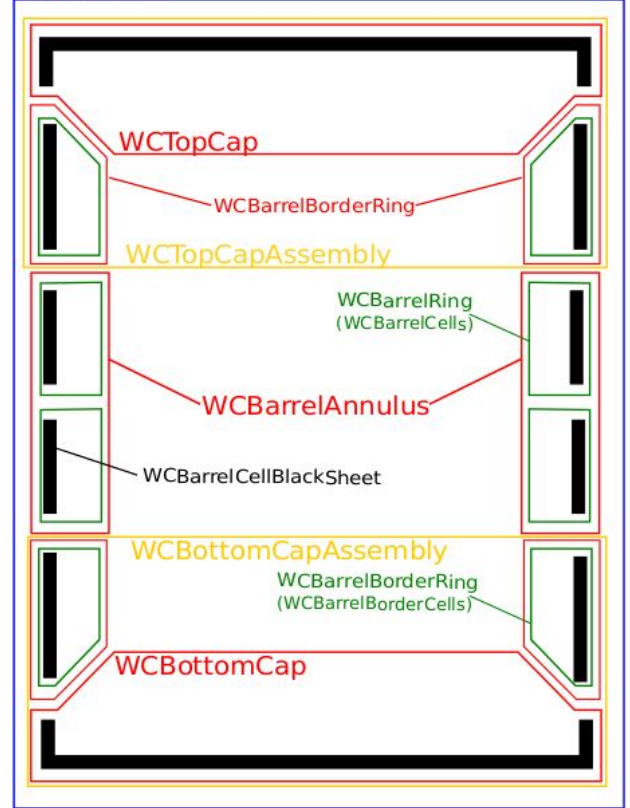
WTopCapAssembly/
WBottomCapAssembly
(Two mirrored volumes that close the ends of the barrel)



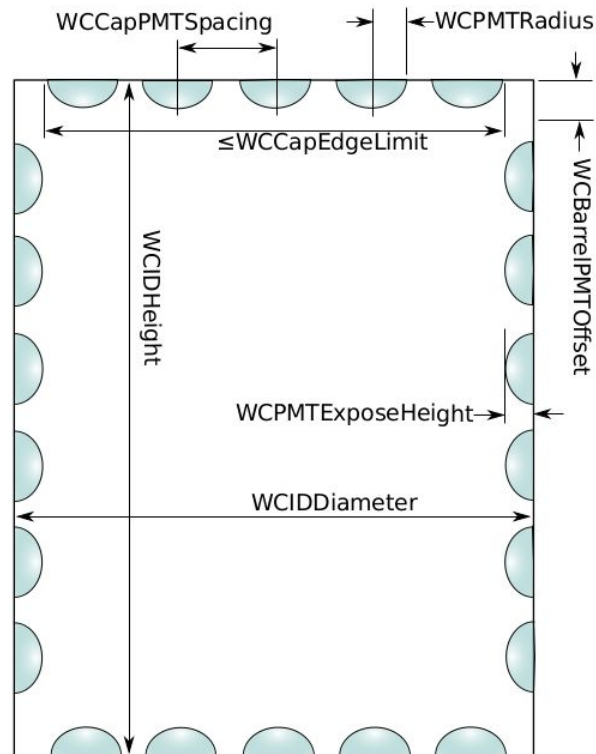
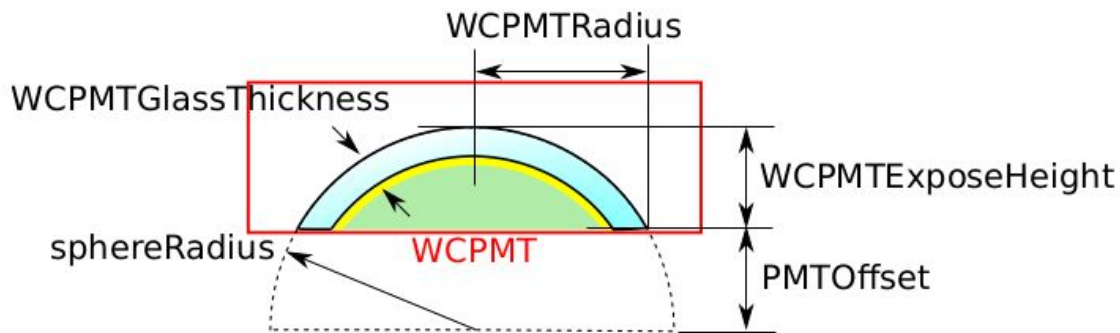
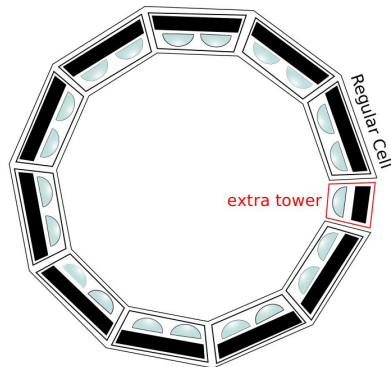
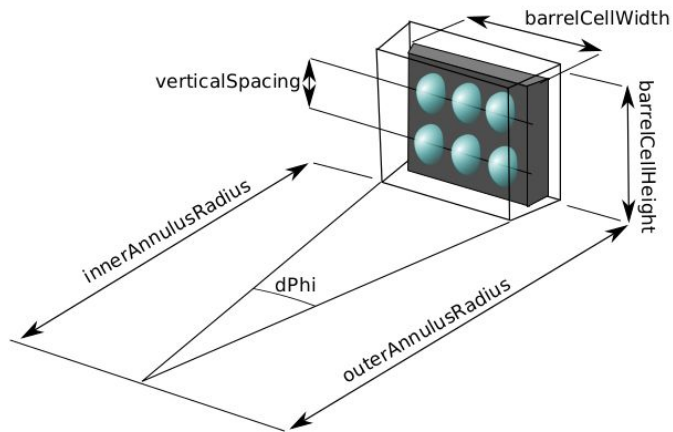
WBarrelBorderRing

[This volume connects the annulus to the cap. It is essentially the uppermost (or lowermost) ring of PMTs]

WBarrel



Detector construction



Super-K geometry

```
void WCSimDetectorConstruction :: SetSuperKGeometry ()
{
WCSimPMTObject * PMT = CreatePMTObject ( " PMT20inch " );
WCPMTName = PMT - > GetPMTName ();
WCPMTExposeHeight = PMT - > GetExposeHeight ();
WCPMTRadius = PMT - > GetRadius ();
WCPMTGlassThickness = PMT - > GetPMTGlassThickness ();
WCIDDiameter = 33.6815* m ;
WCIDHeight= 36.200* m ;
WCBarrelPMTOffset = 0.0715* m ; // offset from vertical
WCBarrelNumPMTHorizontal = 150;
WCBarrelNRings = 17.;
WCPMTperCellHorizontal = 4;
WCPMTperCellVertical = 3;
WCCapPMTSpacing = 0.707* m ;
WCCapEdgeLimit = 16.9* m ;
WCBlackSheetThickness = 2.0* cm ;
WCAddGd = false ;
}
```

***Thank you for the
kind attention!***