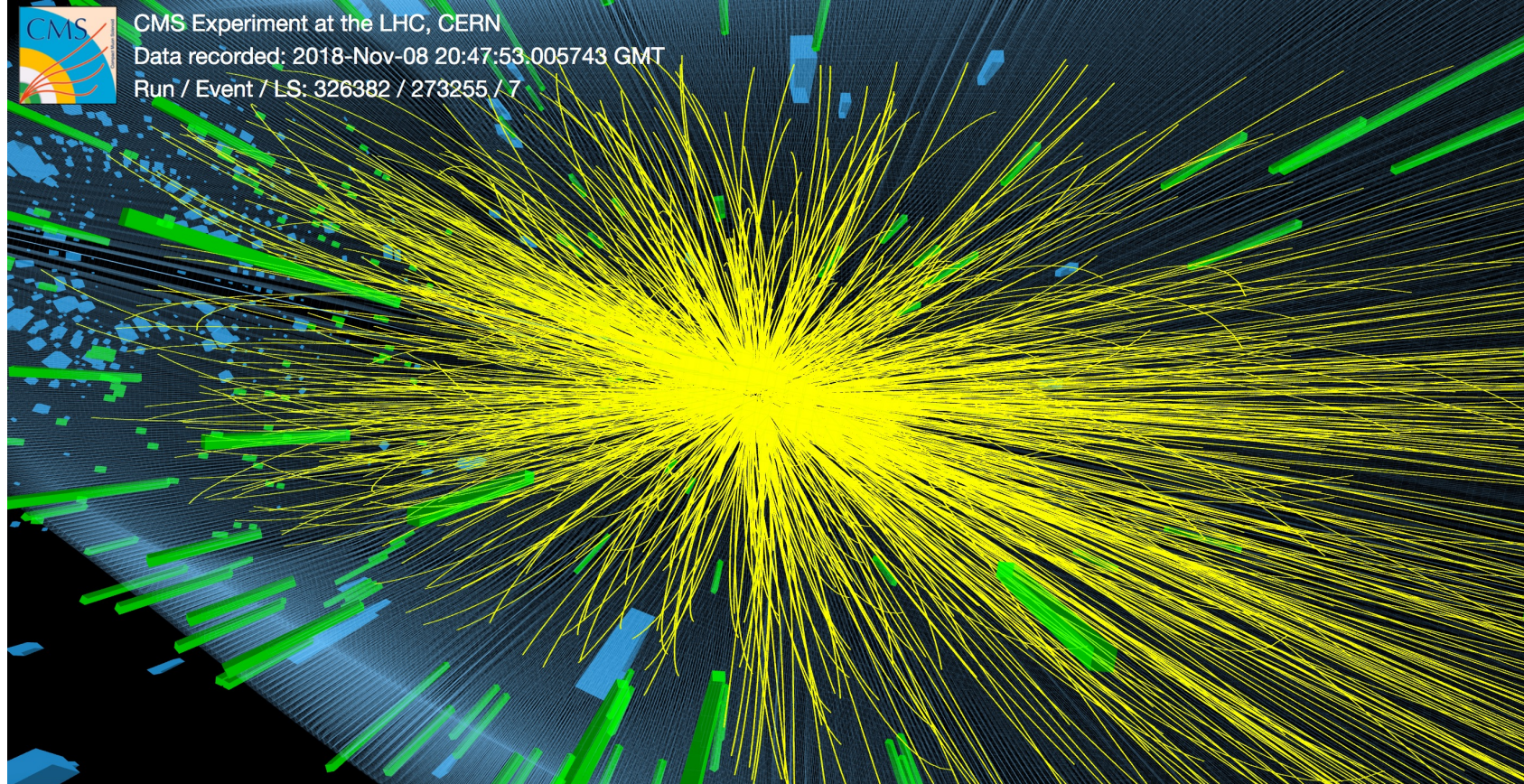




CMS Experiment at the LHC, CERN  
Data recorded: 2018-Nov-08 20:47:53.005743 GMT  
Run / Event / LS: 326382 / 273255 / 7



# FLOW, NONFLOW, AND FLOW FLUCTUATIONS AT CMS

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**ENERGY**

Office of  
Science



**VANDERBILT  
UNIVERSITY**



# Outline

- Flow, nonflow, and flow fluctuations
- Flow study before CMS
- CMS flow measurements in PbPb collisions
- Flow in small collision systems
- Recent development
- Summary

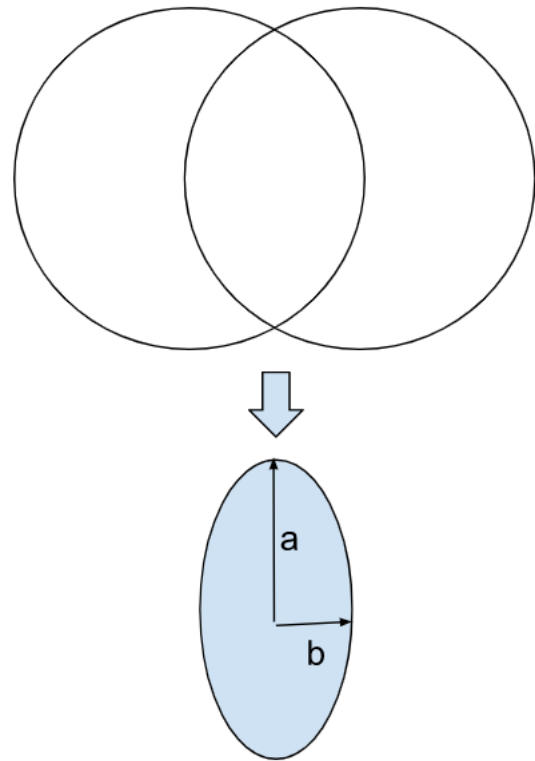


# Flow, nonflow, and flow fluctuations



# Flow in heavy ion collisions

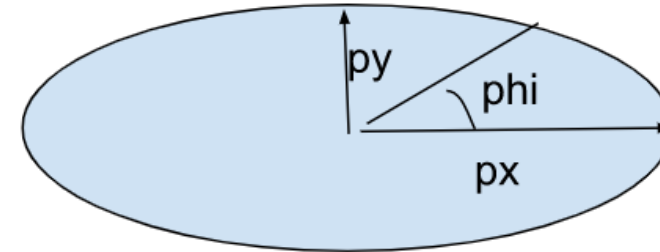
## Initial state anisotropy



Reaction plane:  
Plane formed by  
beam axis and  
impact parameter  
vector

$$e = \frac{a^2 - b^2}{a^2 + b^2}$$

## Final state anisotropy

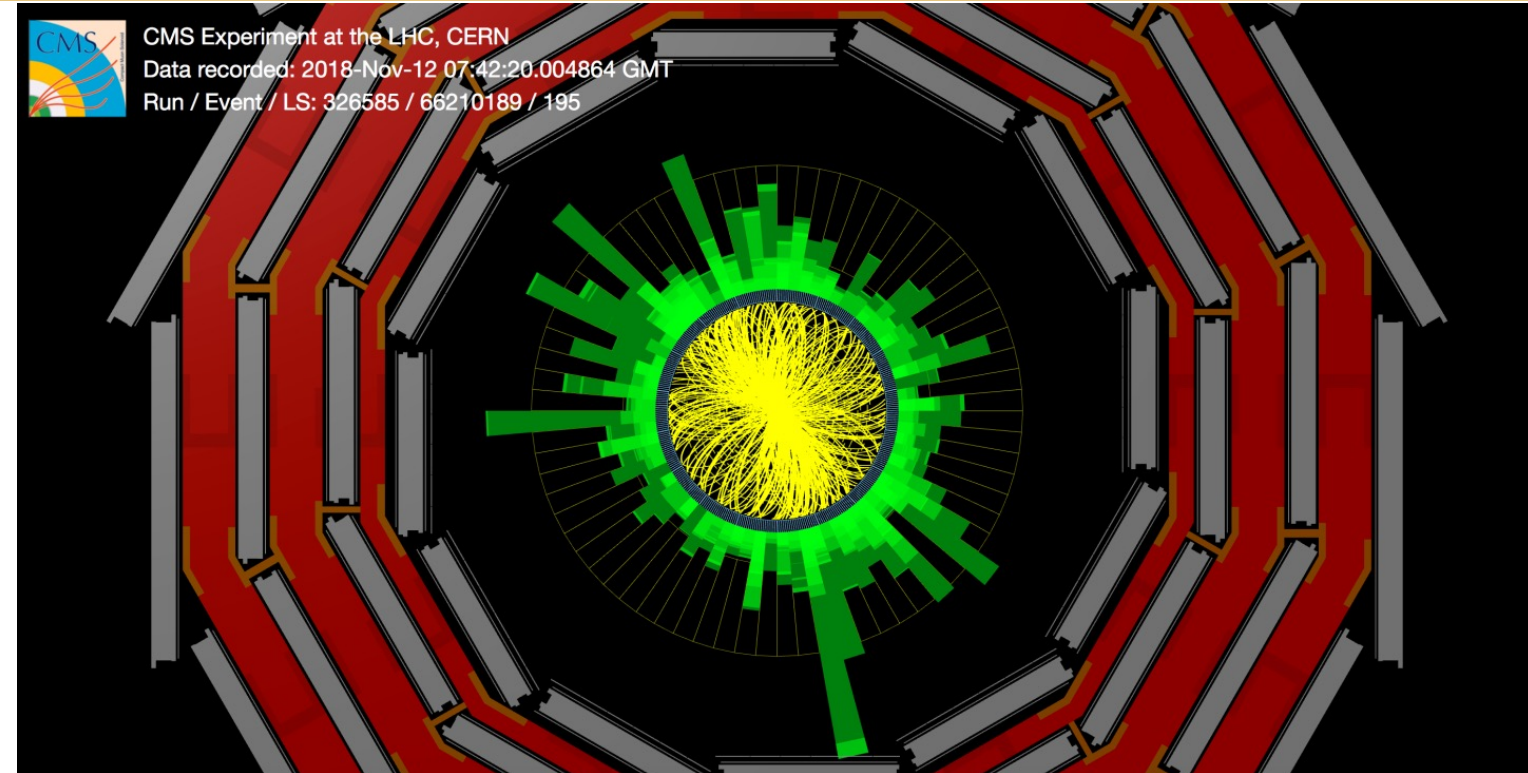
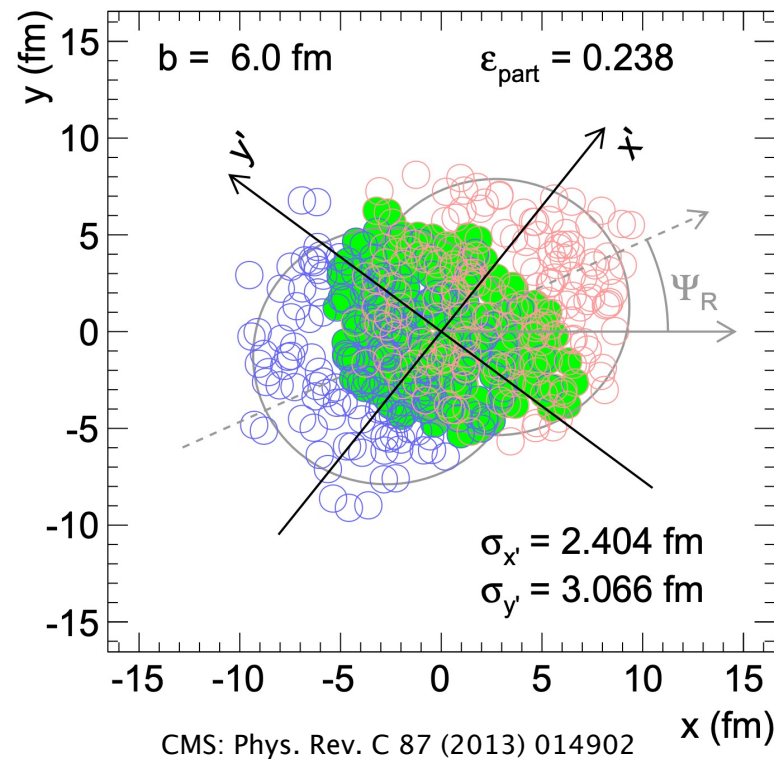


Event plane  
angle = 0 in this  
case

$$\begin{aligned} v_2 &= \frac{(p_x)^2 - (p_y)^2}{(p_x)^2 + (p_y)^2} \\ &= \frac{(p_T)^2 (\cos^2(\phi) - \sin^2(\phi))}{(p_T)^2} \\ &= \cos^2(\phi) - \sin^2(\phi) \\ &= \cos(2\phi) \end{aligned}$$

- Initial state anisotropy ( $\epsilon_2$ ) + hydrodynamics  $\rightarrow$  final state  $v_2$
  - Initial state anisotropy ( $\epsilon_2$ ) + random streaming of particles (No QGP)  $\rightarrow$  **NO** final state  $v_2$
  - **No** initial state anisotropy ( $\epsilon_2 \sim 0$ ) + hydrodynamics  $\rightarrow$  **No** final state  $v_2$  or small  $v_2$  from fluctuations
- $v_2$  is sensitive to QGP production

# Flow in heavy ion collisions



- One PbPb collision -> hundreds of nucleon-nucleon (NN) collisions
- Particles produced in preferred angles from hundreds of NN collisions at the same time -> collective FLOW of the created medium: Quark-Gluon Plasma
  - Initial state geometry, fluctuations
  - Medium properties, parton-medium interactions

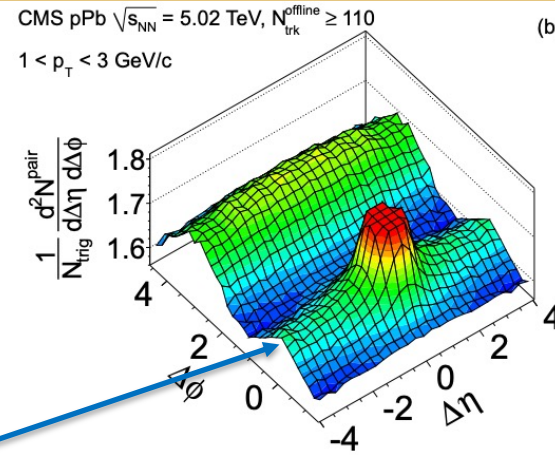
$$dN/d\phi \propto 1 + \sum_n 2v_n \cos(n(\phi - \Psi_n))$$

Elliptic flow:  $v_2$

Triangular flow:  $v_3$

# Nonflow and flow

- Nonflow
  - Jets
  - BEC
  - Momentum Conservation
  - ...



- Ridge: Near-side long range correlations

**$v_n$**   
Azimuthal anisotropy

$$dN/d\phi \propto 1 + \sum_n 2v_n \cos(n(\phi - \Psi_n))$$

- CGC
- Color Reconnection and Rope Hadronization

- Initial geometry + Hydrodynamics
- Transport models

Ridge and  $v_n$  but **not related to FLOW** or QGP

**FLOW** and QGP

$v_n$  analysis method with nonflow removal:

- Two particle correlation method with  $v_n\{EP\}$ ,  $v_n\{SP\}$ ,  $v_n^{sub}\{2, |\Delta\eta| > 2\}$ , ...



$v_n$  fluctuations

- Multiparticle correlations with  $v_n\{4, 6, 8, 10, \dots, LYZ\}$  (Better removing nonflow)

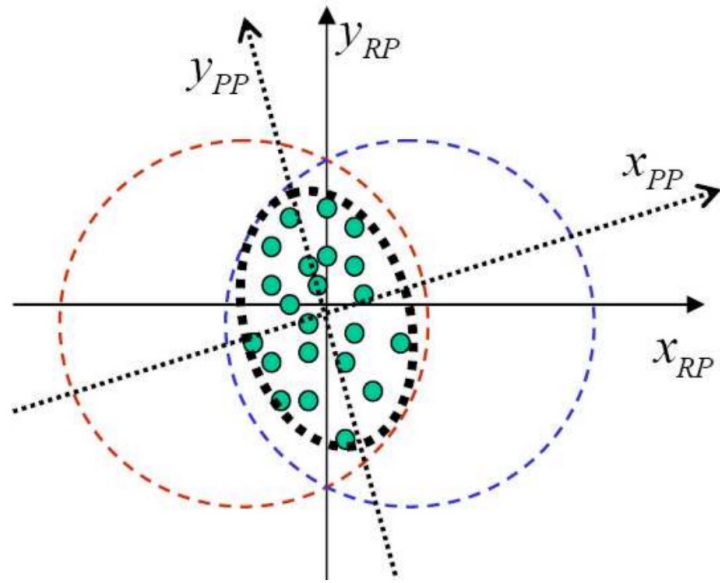
- Path length dependence
  - Jet energy loss
  - Quarkonium suppression

$v_n$  is **not hydrodynamic FLOW** but probes QGP

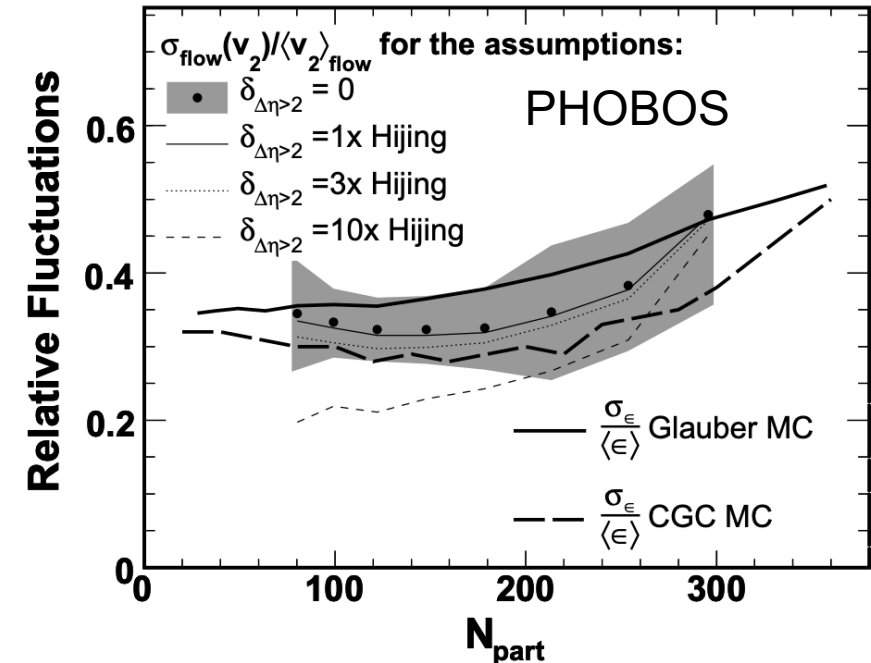
Not nonflow, also not flow



# Flow fluctuations

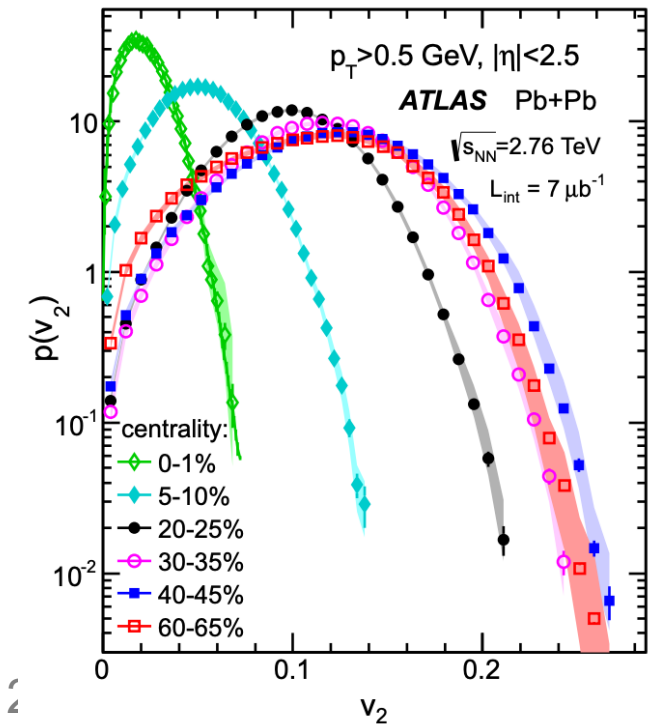
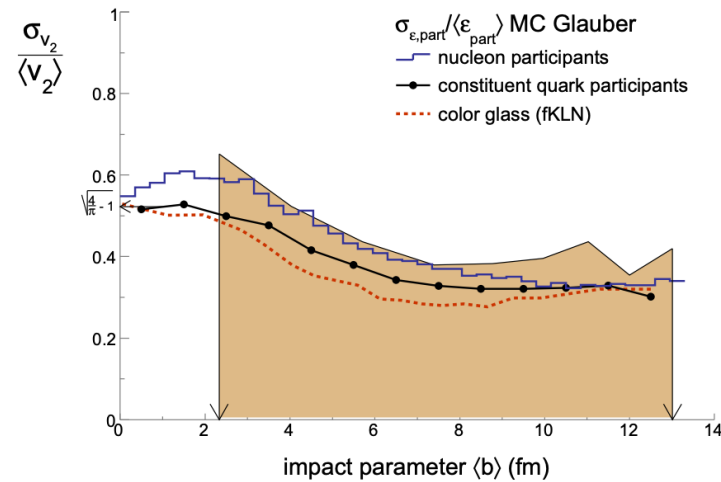
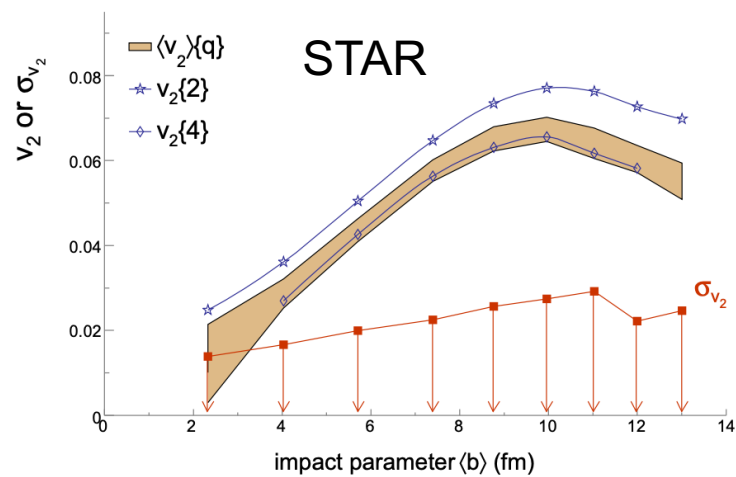


- **RP: the reaction plane**
  - Defined by the impact parameter
  - Initial geometry:  $\epsilon_{std}$
- **PP: the participant plane**
  - Defined by the major axis of the created system
  - Initial geometry:  $\epsilon_{part}$



S. A. Voloshin, A. M. Poskanzer, A. Tang and G. Wang, PLB, 659 (2008), 537-541

The fluctuation in initial eccentricity of the participant zone -> flow fluctuations  
 Note: flow fluctuations can be due to different reasons

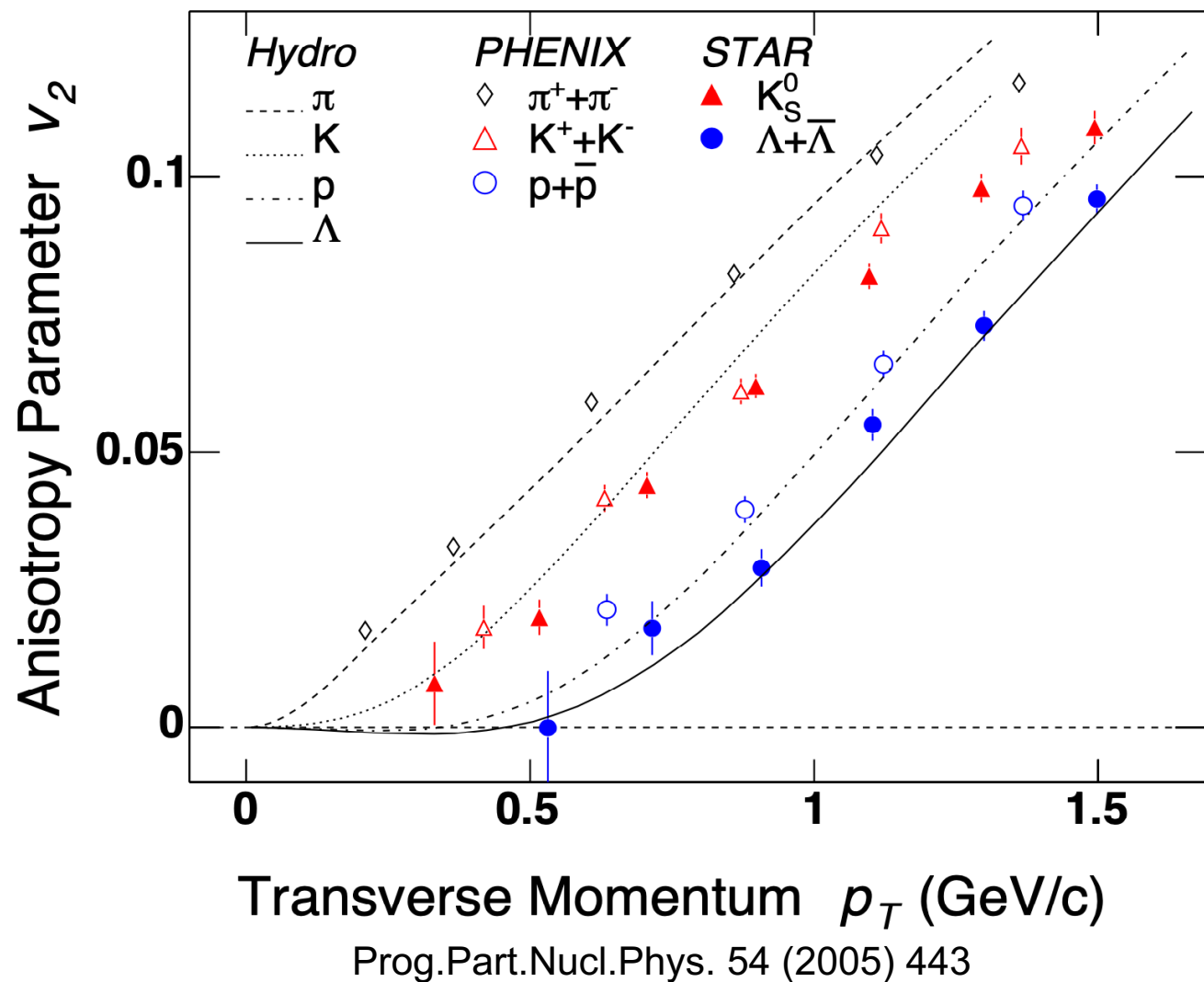


# Flow study before CMS

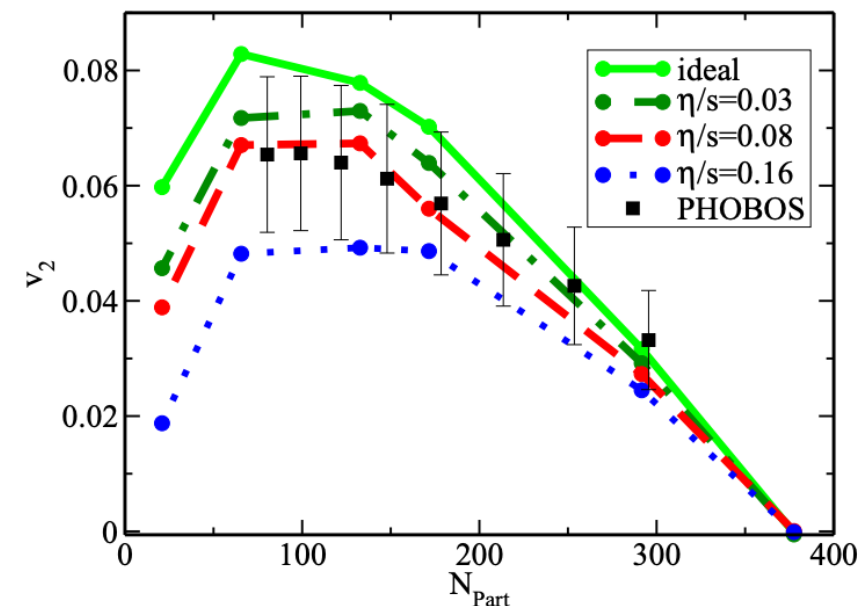




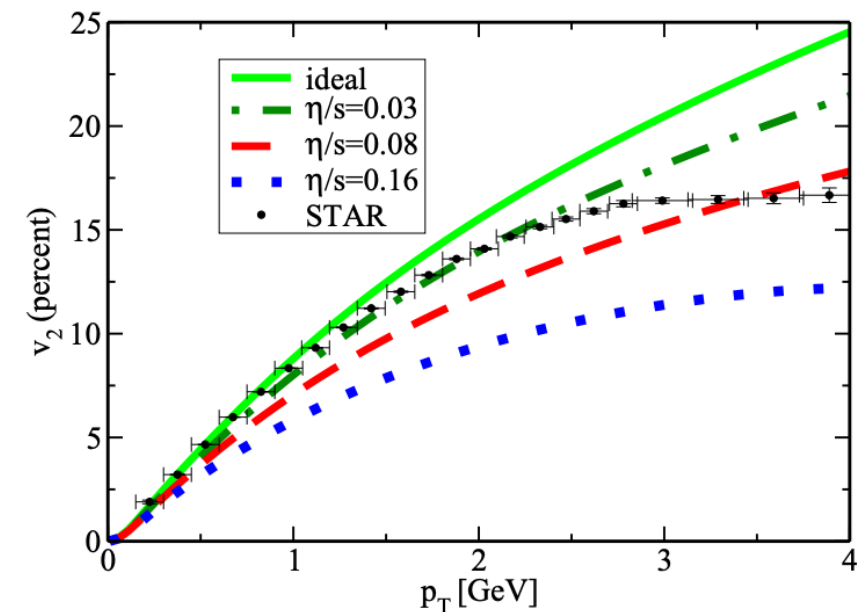
# $v_2$ and properties of QGP



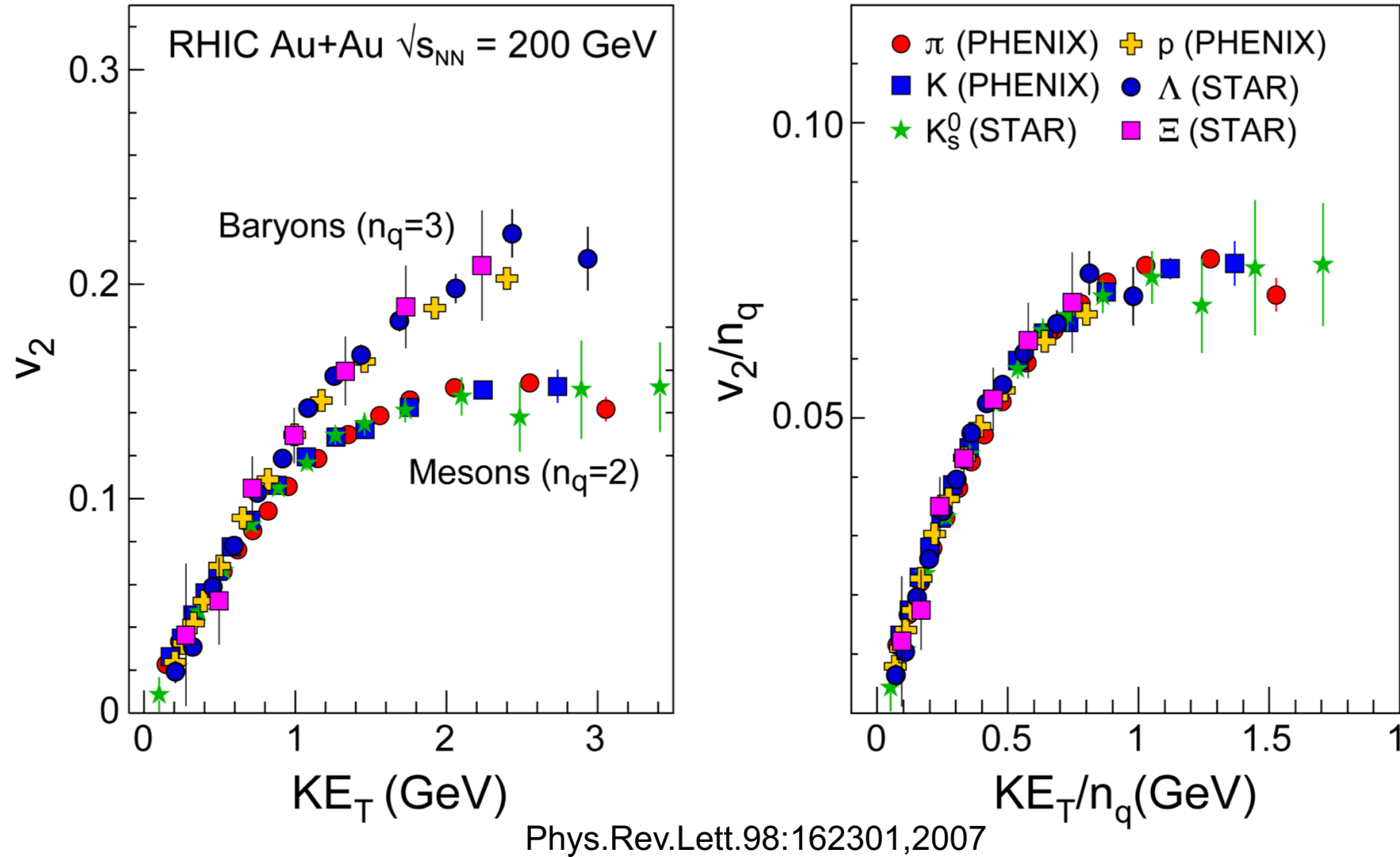
Measurements of  $v_2$  provide constraints for the properties of QGP



Phys.Rev.Lett.99:172301,2007



# NCQ scaling



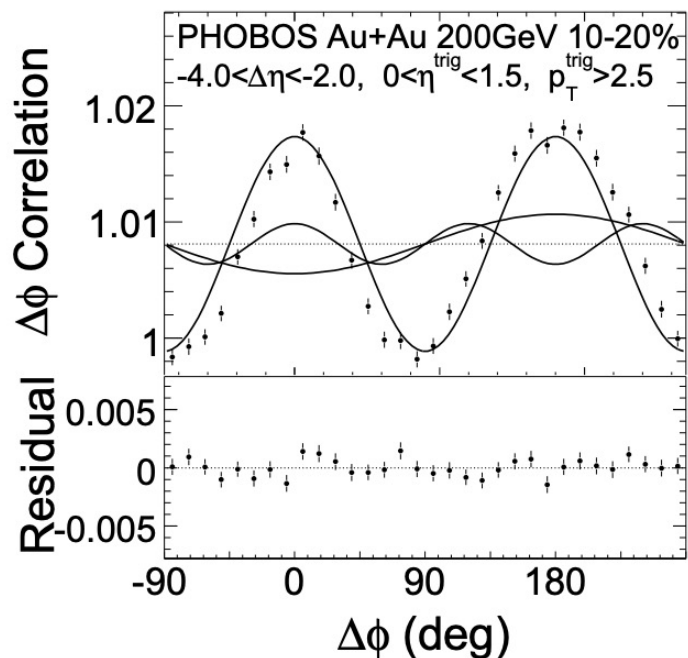
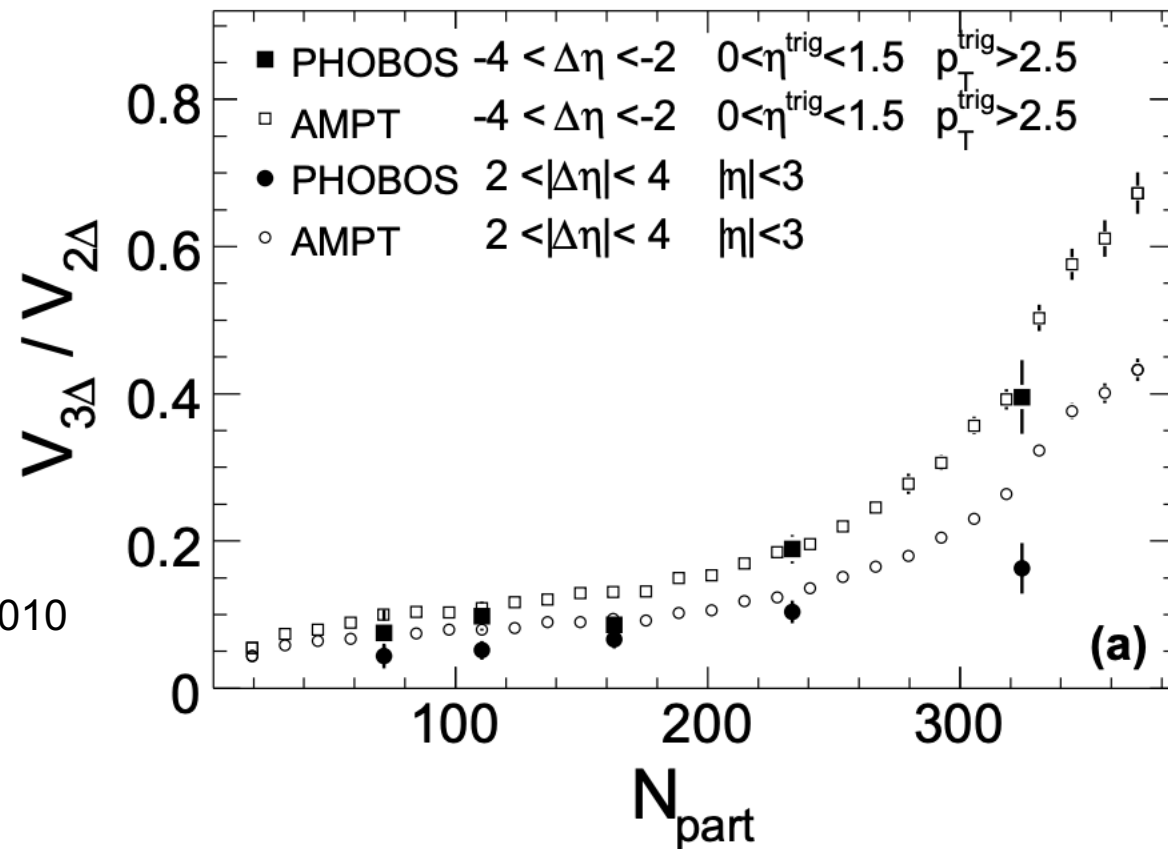
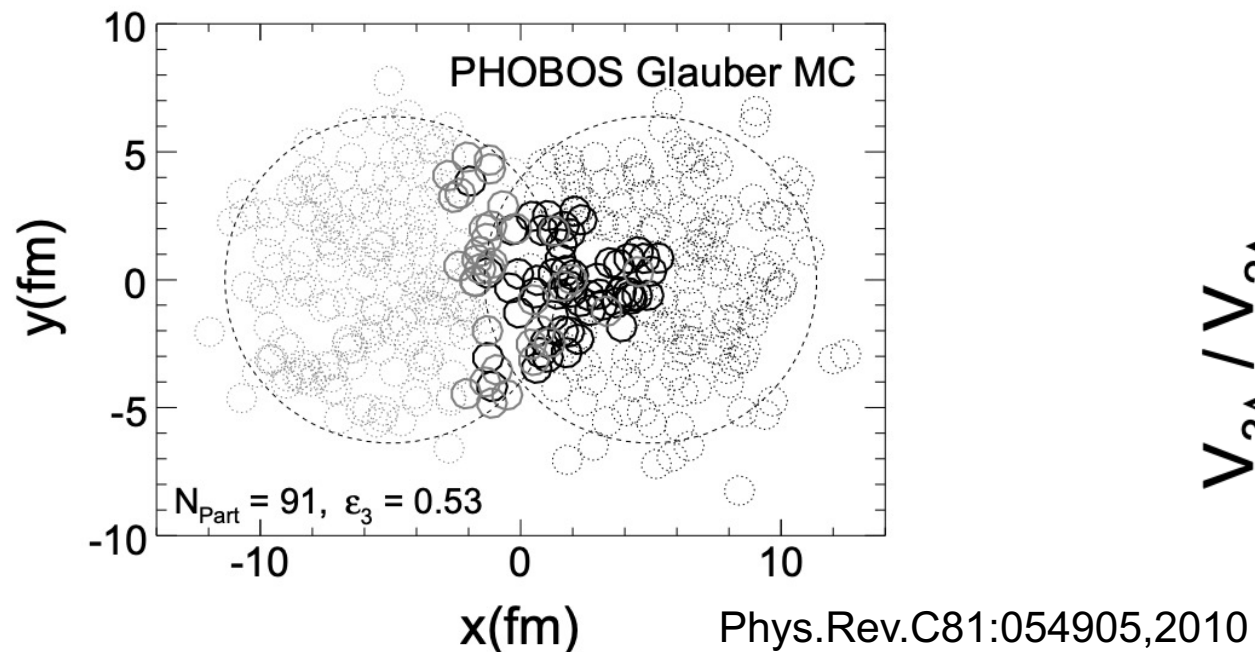
Transverse kinetic energy  $KE_T$ :

$$\sqrt{p_T^2 + m^2} - m$$

- The flowing could be at the partonic level
- More evidence of QGP



# Higher order harmonics



$$\frac{dN^{\text{pairs}}}{d\Delta\phi} = \frac{N^{\text{pairs}}}{2\pi} \left( 1 + \sum_n 2V_{n\Delta} \cos(n\Delta\phi) \right)$$

- Higher harmonics due to fluctuations at the initial state

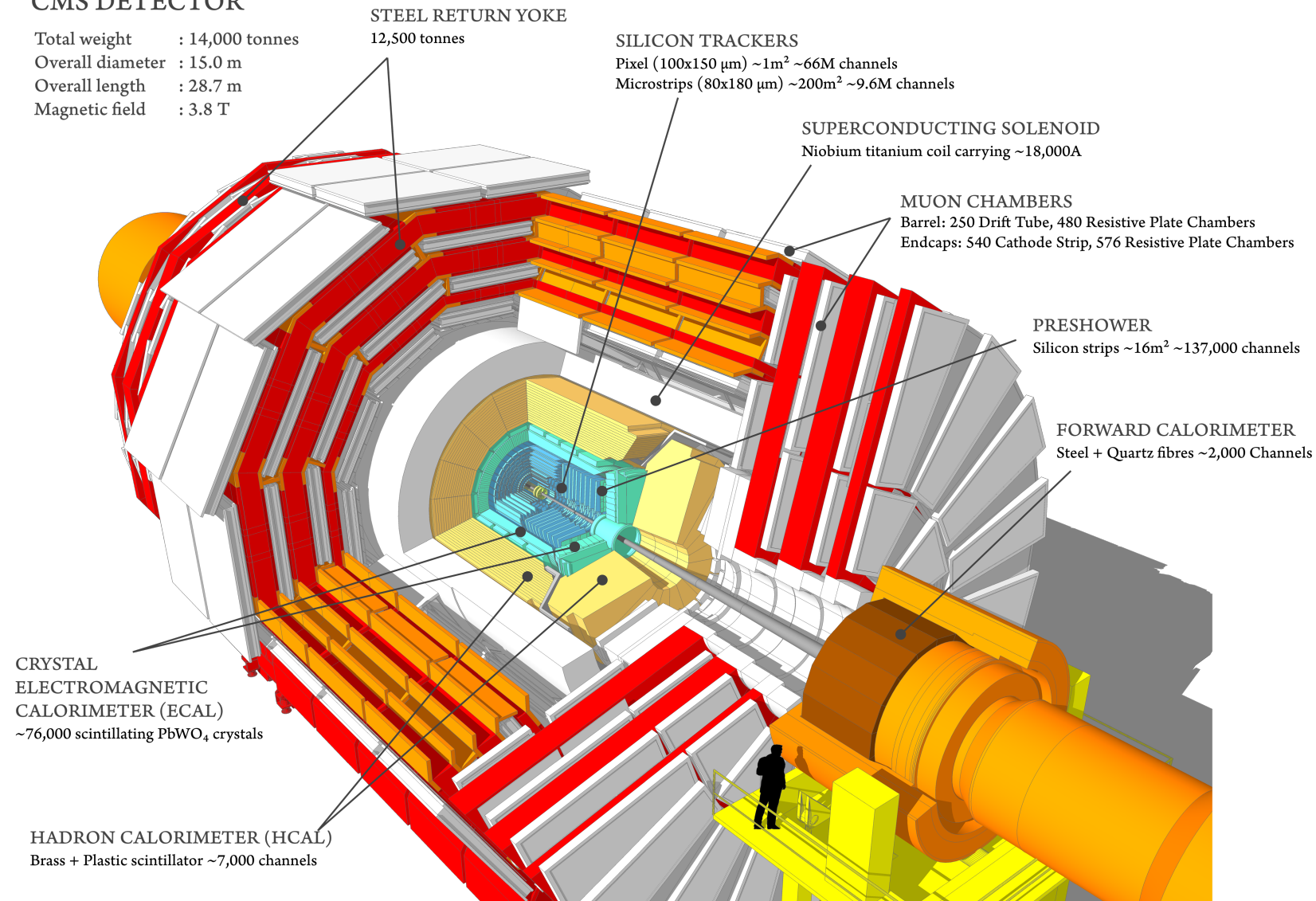
# CMS flow measurements in PbPb collisions



# CMS detectors

## CMS DETECTOR

Total weight : 14,000 tonnes  
Overall diameter : 15.0 m  
Overall length : 28.7 m  
Magnetic field : 3.8 T



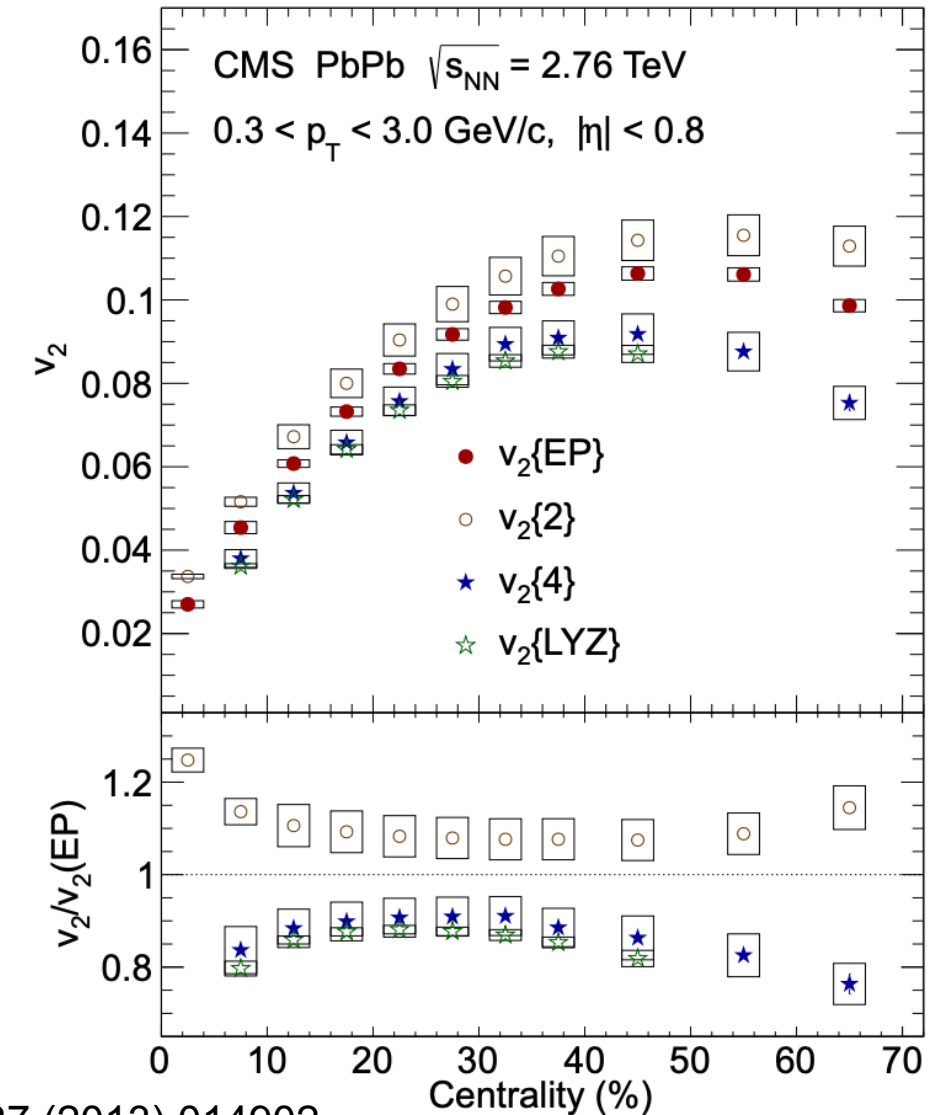
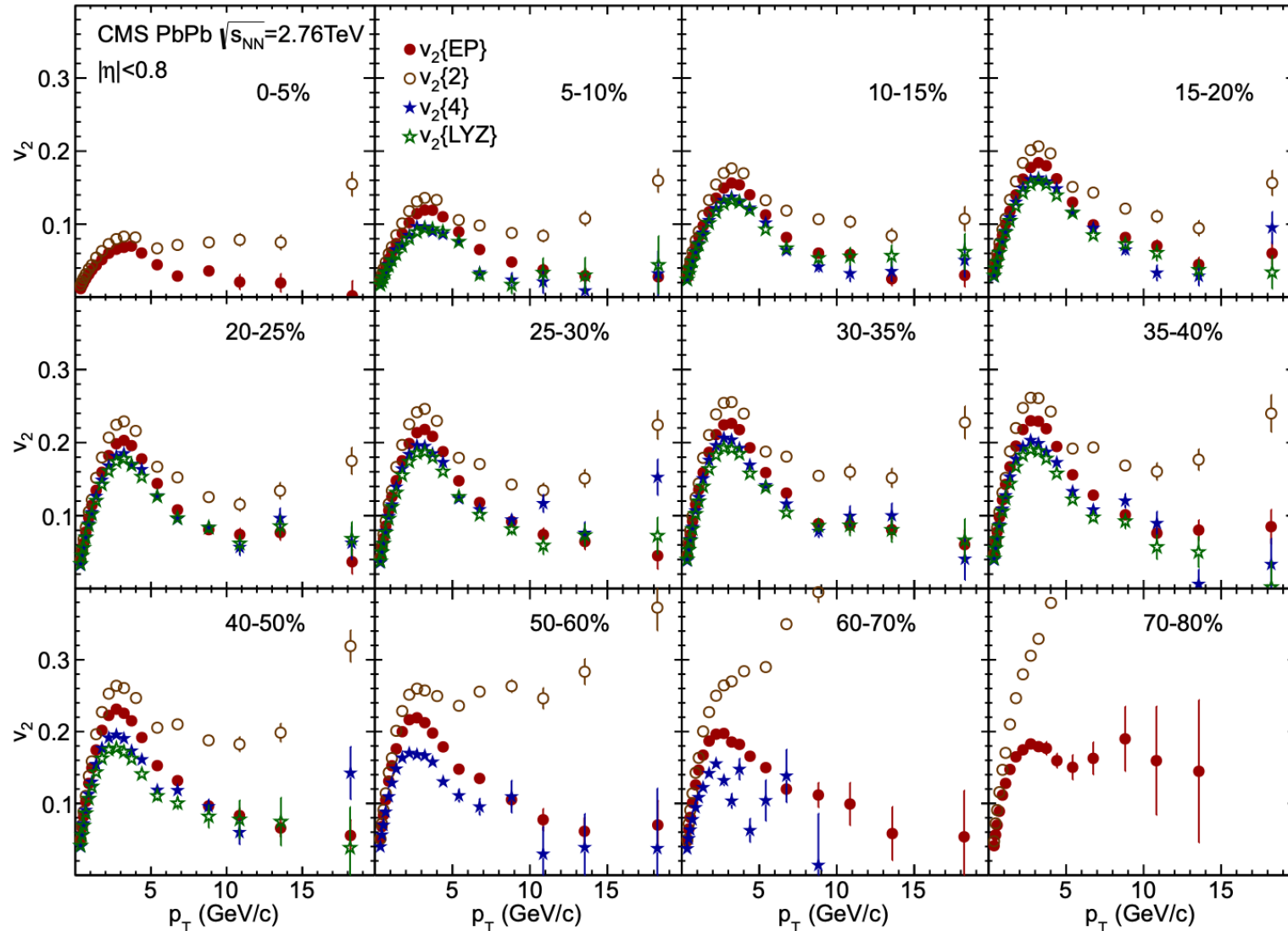
- Tracker with  $|\eta| < 2.4$
- Hadronic Forward (HF) calorimeter with  $2.9 < |\eta| < 5.2$

# A typical analysis in CMS

- A very long process with different layers of reviews
  - Proposal an analysis
  - Multiple reports and review in the analysis (Flow/Corr for example) group -> Green light for pre-approval
  - Pre-approval talk and homework
  - Review by analysis review committee, lots of meetings/reports -> Green light for approval
  - Approval talk and homework
  - Collaboration wide review and comments
  - Final reading
  - Submit to a journal
- Could take 6 months – several years to submit



# $v_2$ at LHC energy – first CMS analysis

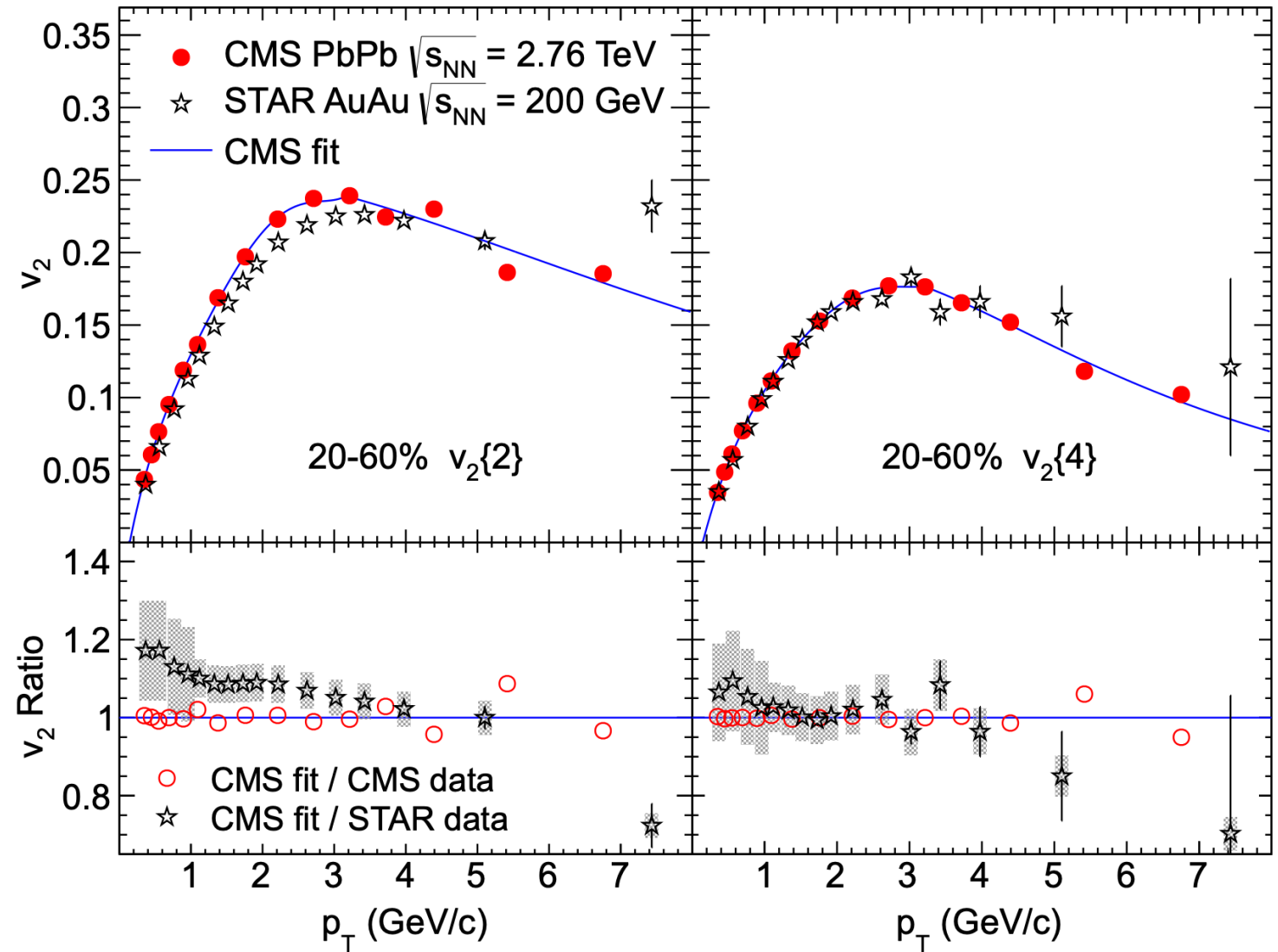
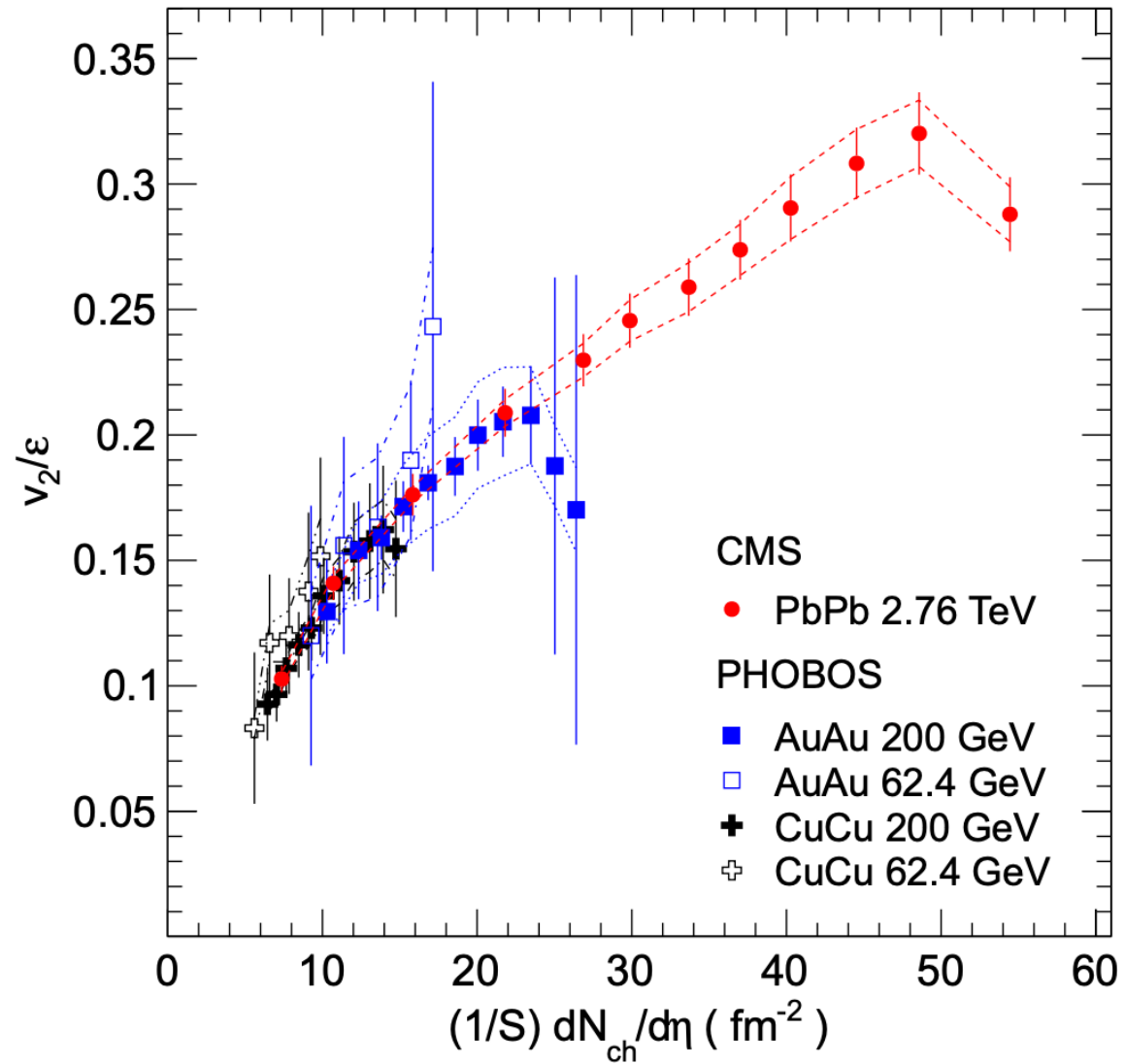


Phys. Rev. C 87 (2013) 014902

- Strong  $v_2$  signals at LHC energy with different analysis methods



# $v_2$ at LHC energy – first CMS analysis



Phys. Rev. C 87 (2013) 014902

- The  $v_2$  values are larger (<20%) at LHC energy compared to RHIC





# Example of systematic studies

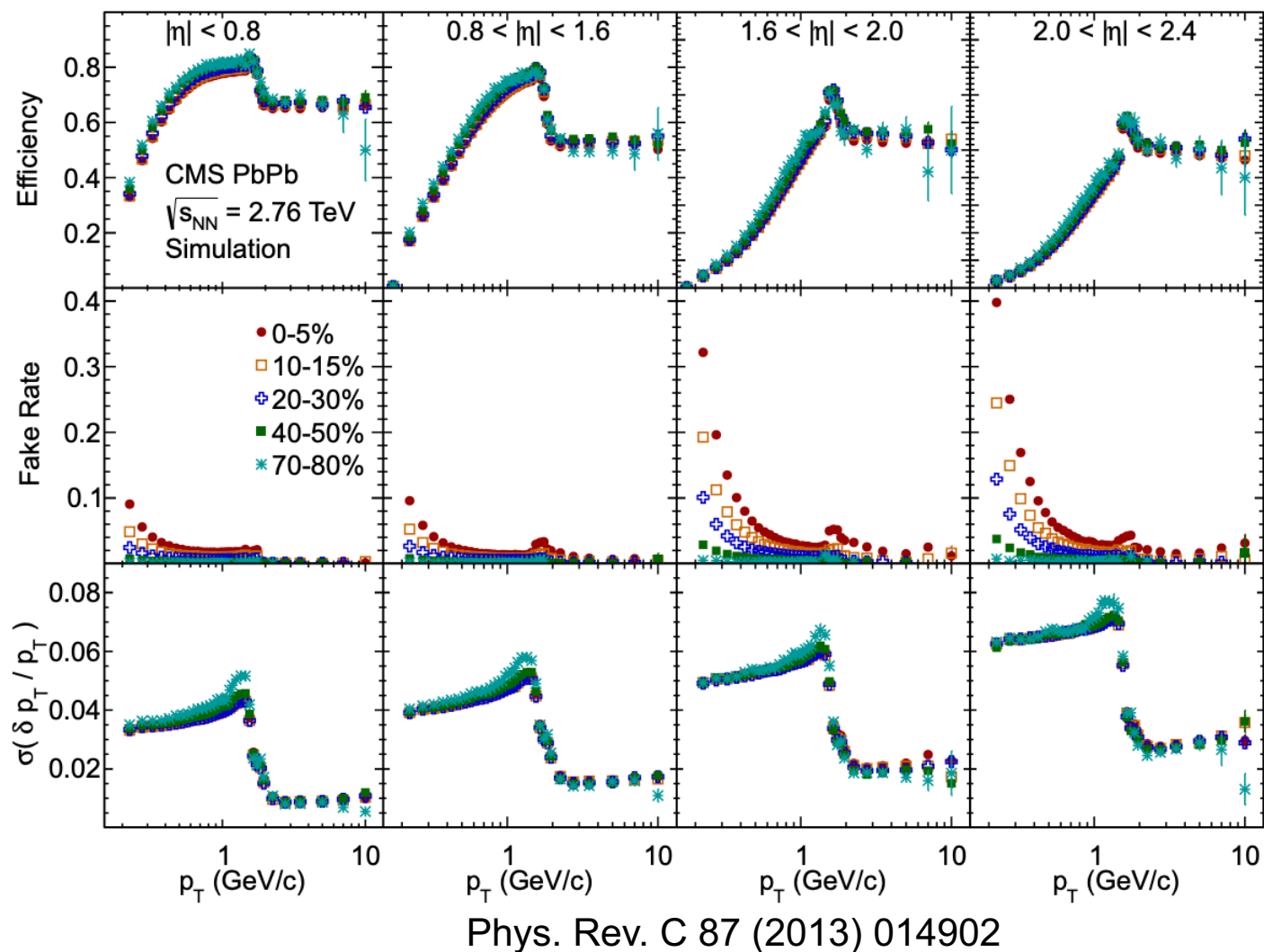


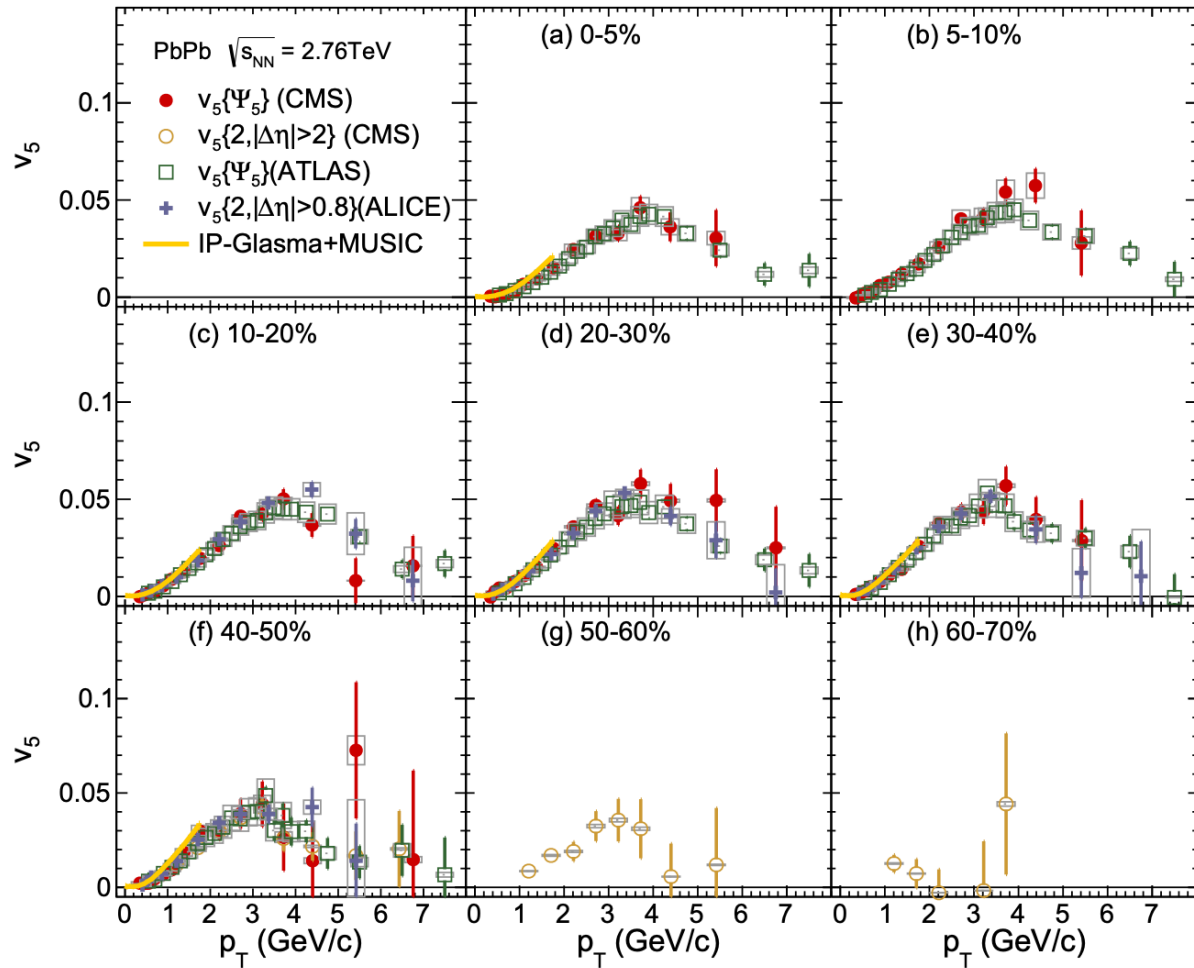
Table 2: Systematic uncertainties in the measurement of  $v_2(p_T)$  for  $|\eta| < 0.8$  with the event-plane method for different  $p_T$  and centrality ranges.

Source	$p_T$ (GeV/c)	Centrality		
		0 – 10%	10 – 70%	70 – 80%
Part. composition	All	0.5%	0.5%	0.5%
Cent. determination	All	1.0%	1.0%	1.0%
Corrections	< 0.3	4.0%	2.0%	3.0%
	0.3 – 0.5	2.0%	< 1.0%	2.0%
	0.5 – 22.0	< 1.0%	< 1.0%	2.0%
Total	< 0.3	4.2%	2.3%	3.2%
	0.3 – 0.5	2.3%	1.5%	2.3%
	0.5 – 22.0	1.5%	1.5%	2.3%

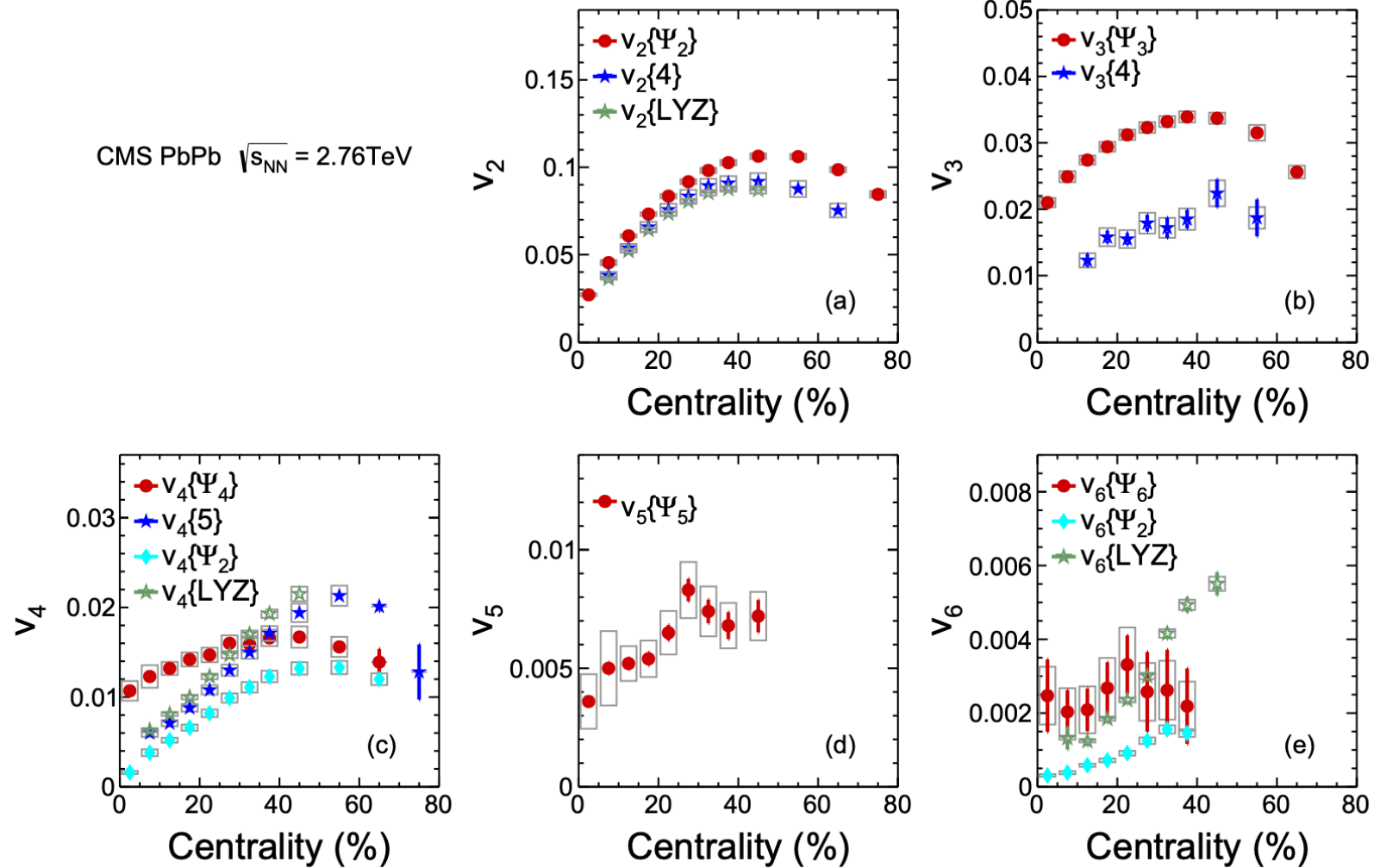
- Other possible sources of systematics:
  - Event selections
  - Trigger efficiency
  - Pileup
  - Track selections
  - ...

- Detailed cross check of analysis methods/systematic studies are carefully reviewed

# Higher order harmonics

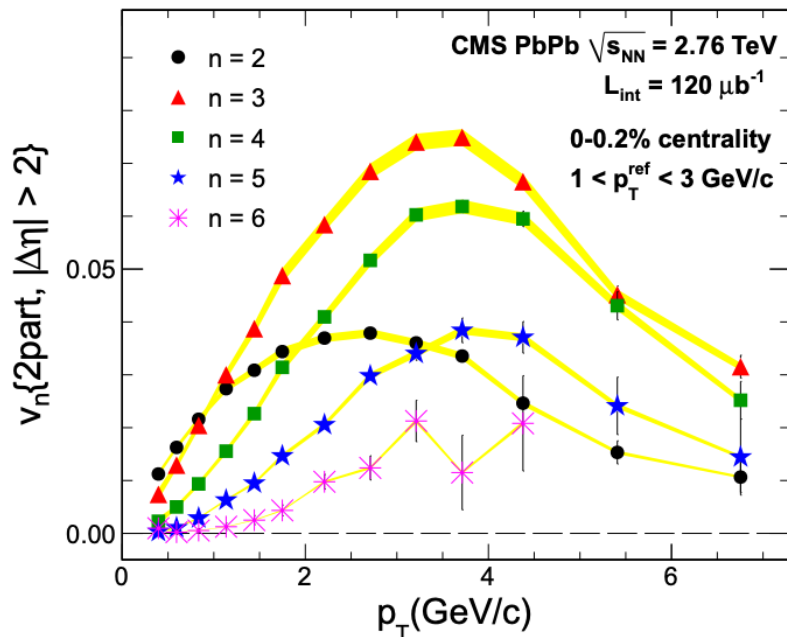
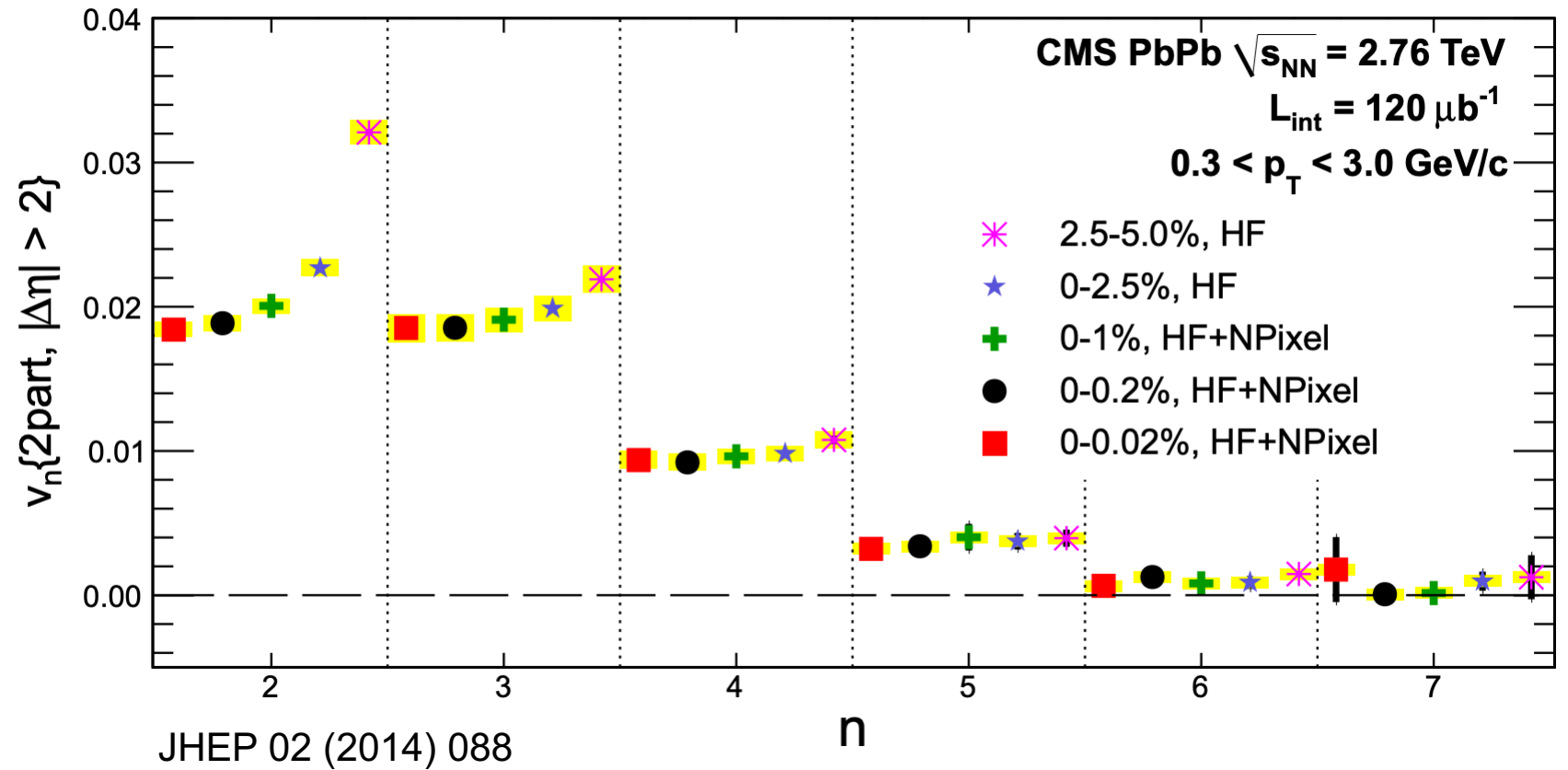
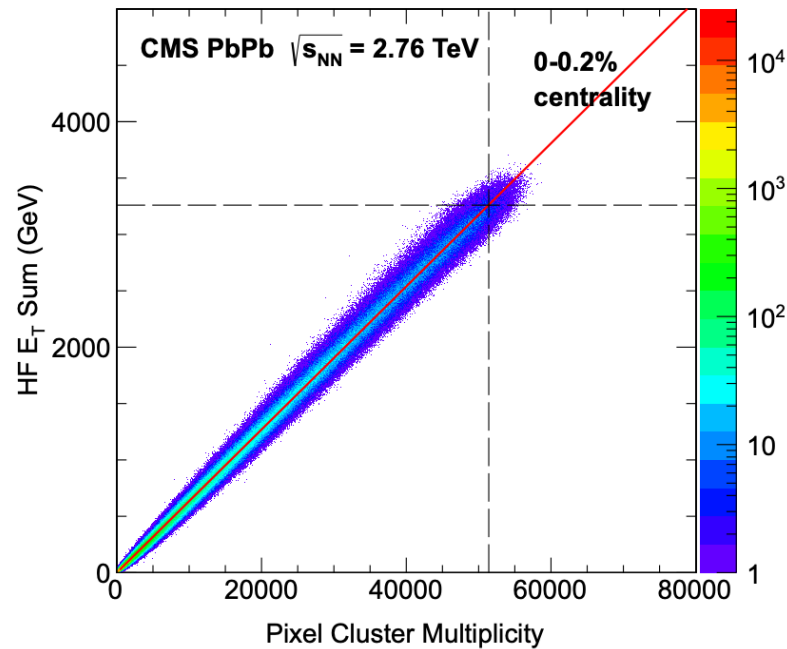


Phys. Rev. C 89 (2014) 044906



- Higher order harmonics with fluctuation driven confirmed

# Ultra-central collisions



- $v_3$  larger than  $v_2$  for  $p_T$  larger than 1 GeV in UCC
- $p_T$  integrated  $v_3$  larger than (or close to)  $v_2$  for most central

# Flow decorrelations

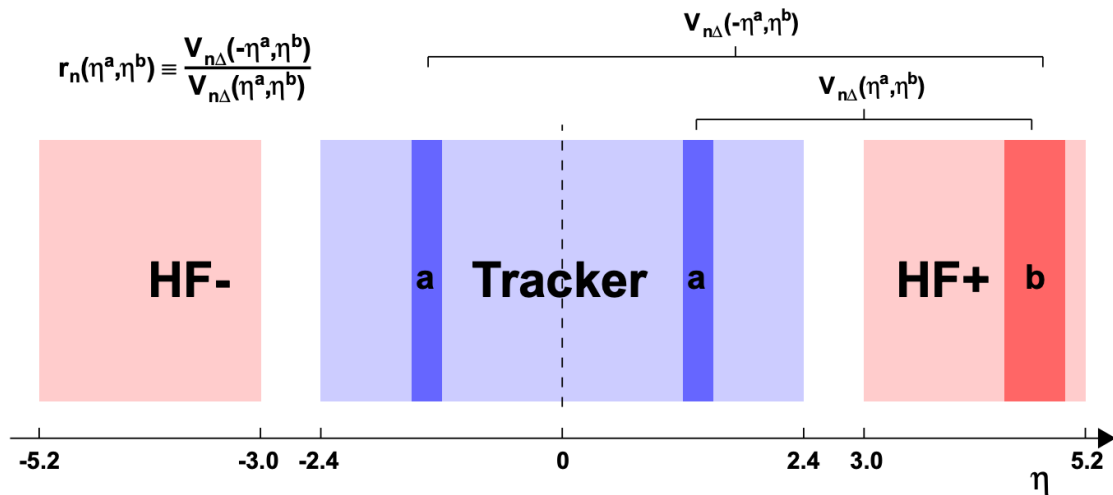
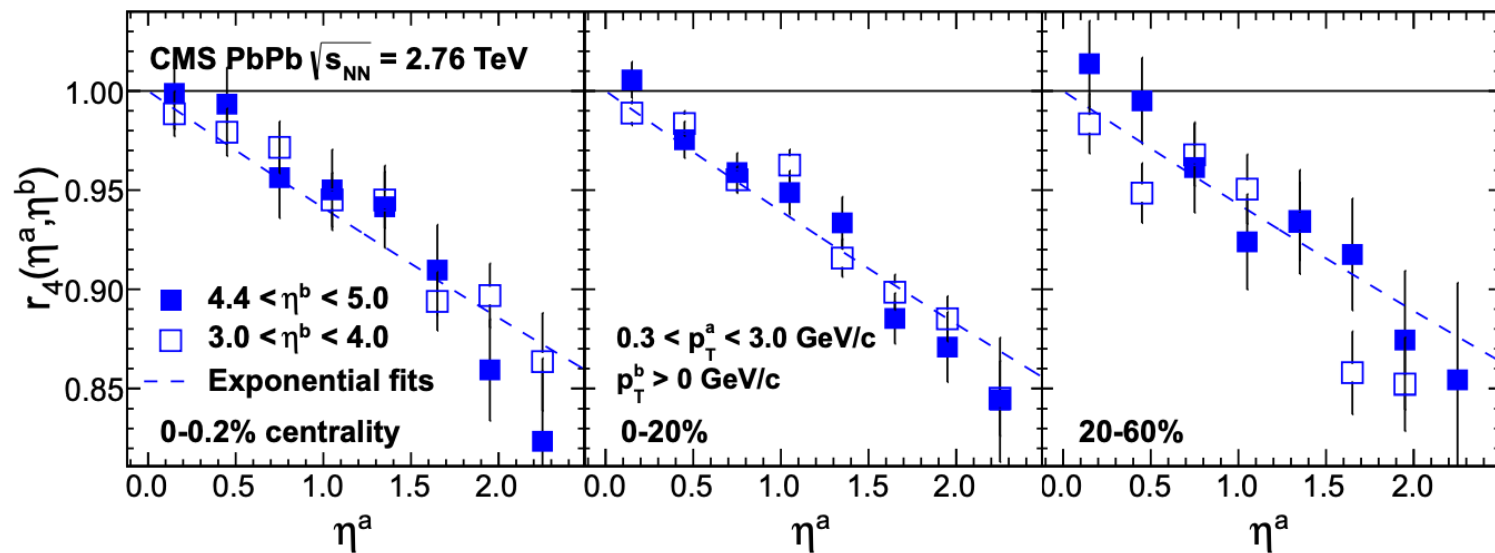
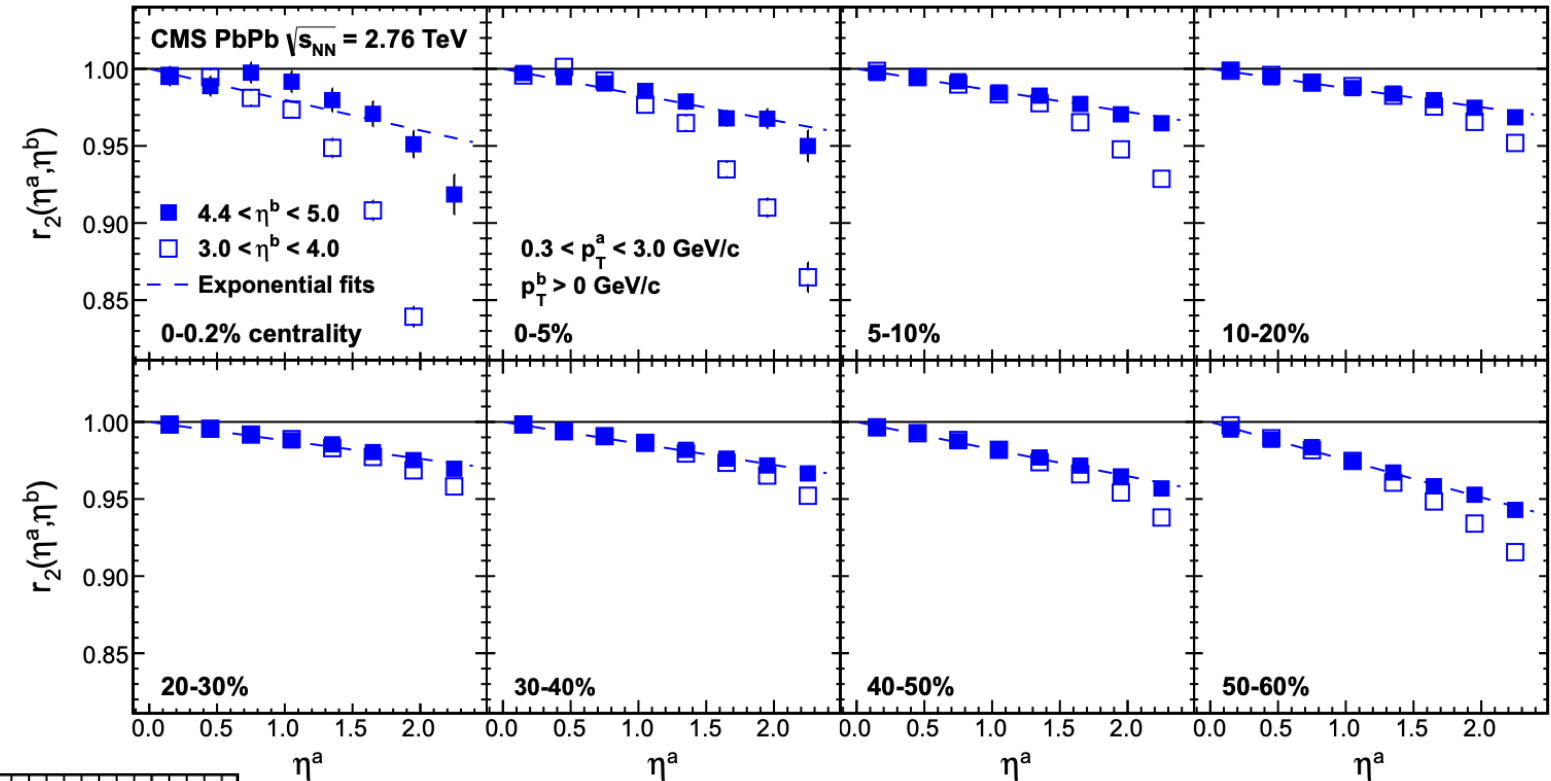


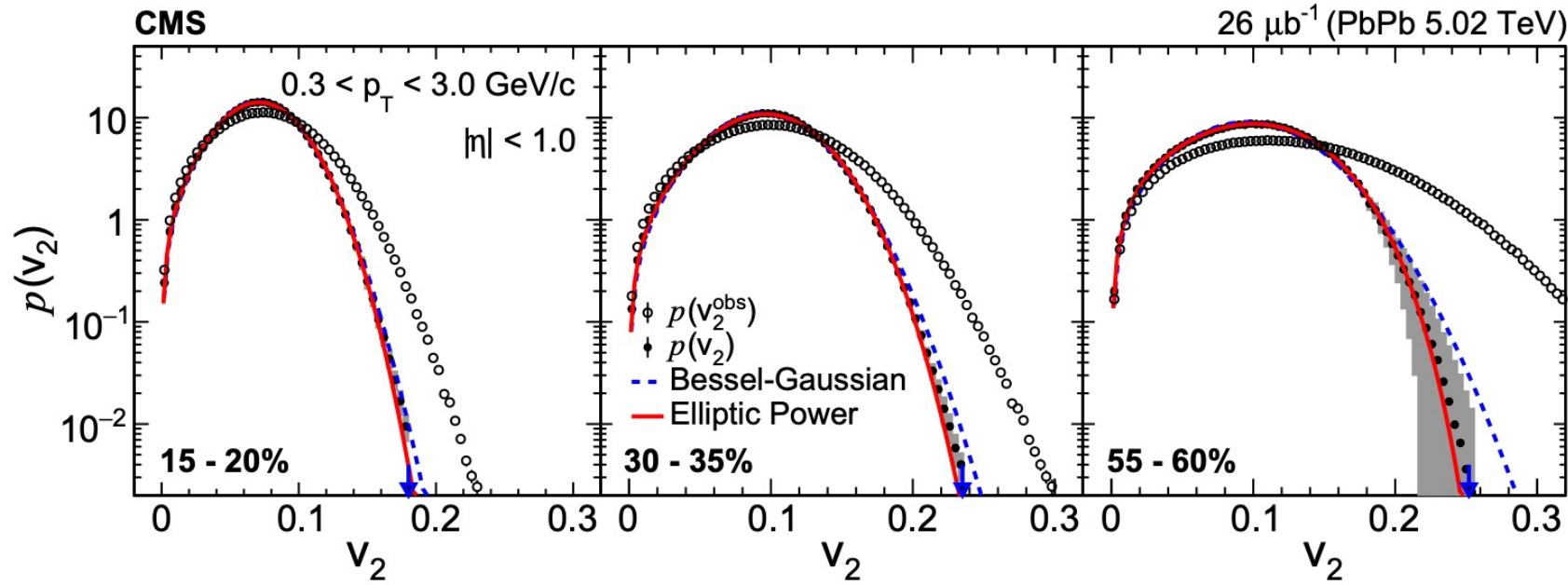
Figure 8: (Color online) A schematic illustrating the acceptance coverage of the CMS tracker and HF calorimeters, and the procedure for deriving the  $\eta$ -dependent factorization ratio,  $r_n(\eta^a, \eta^b)$ .



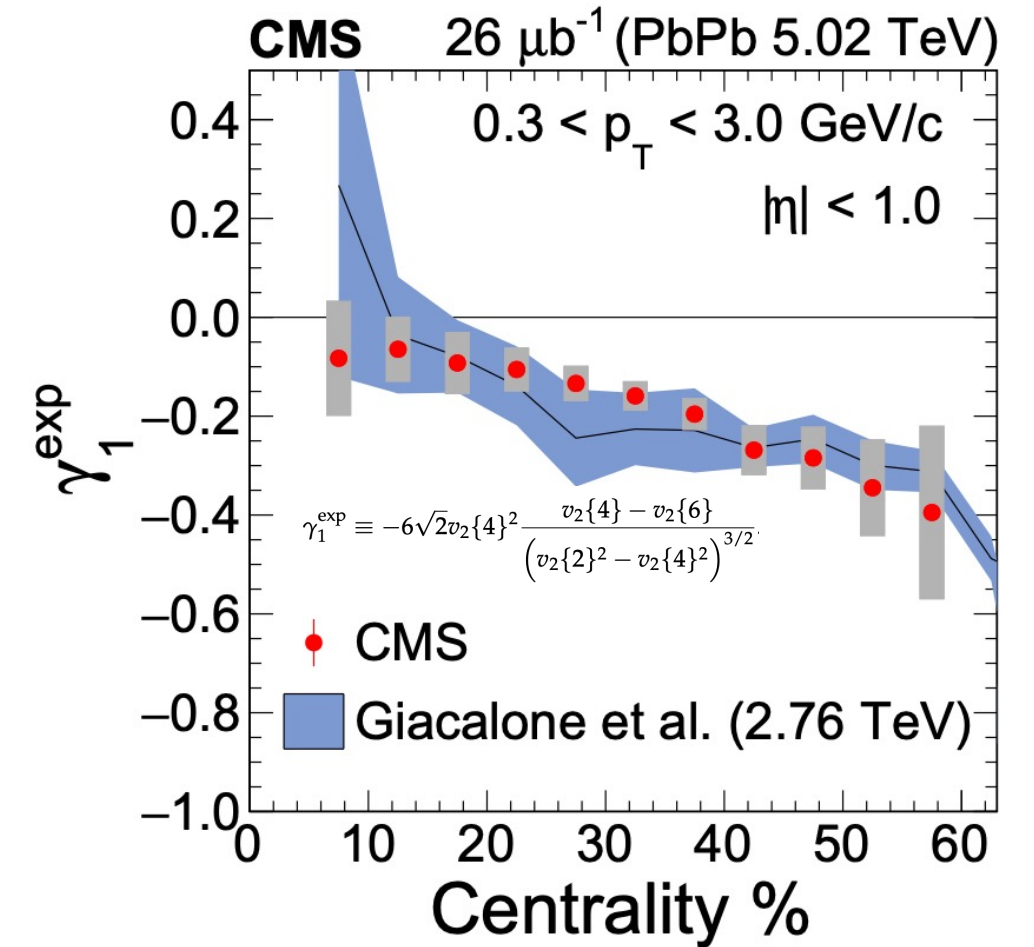
- Factorization break down
- Clear evidence of  $\eta$  dependence event plane fluctuations



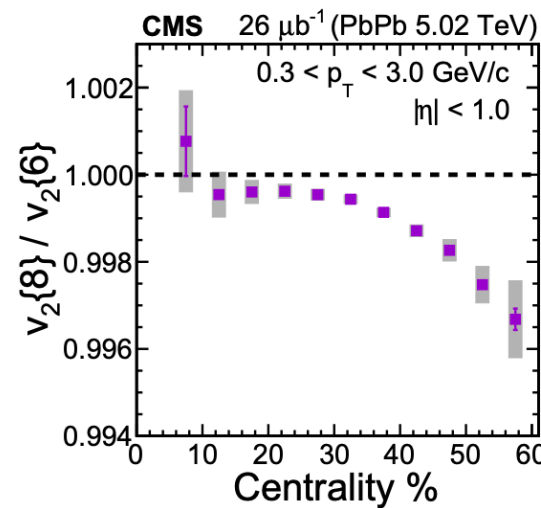
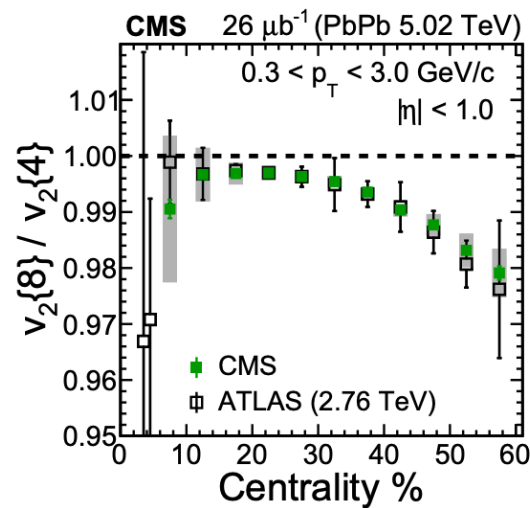
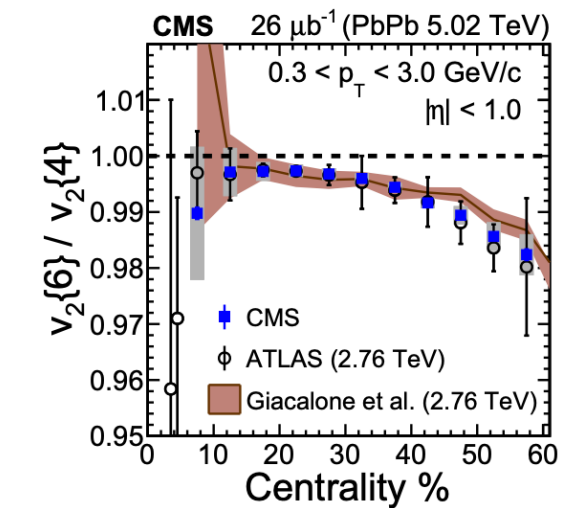
# Flow fluctuations



Phys. Lett. B 789 (2019) 643



- Event-by-event flow fluctuations with unfolding method
- Evidence of non-Gaussian fluctuations

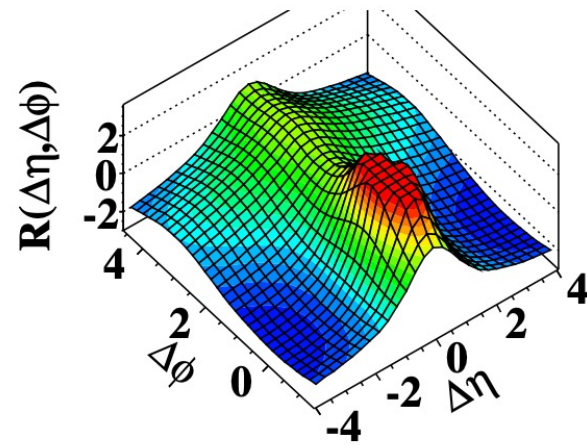


# Flow in small collisions systems

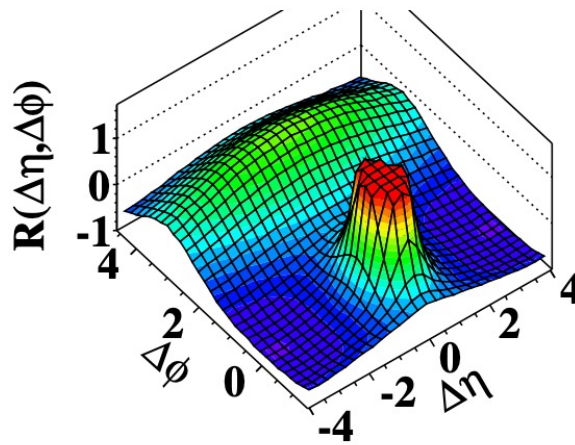


# Ridge in proton-proton collisions

(a) CMS MinBias,  $p_T > 0.1 \text{ GeV}/c$

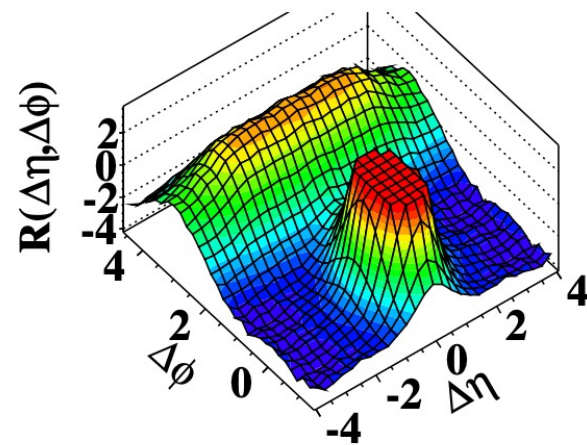


(b) CMS MinBias,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$

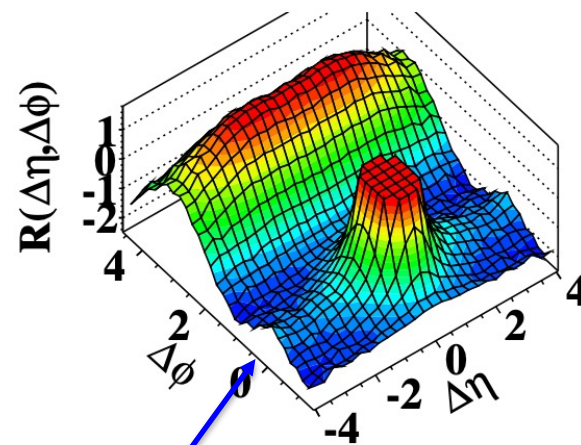


JHEP 1009:091,2010

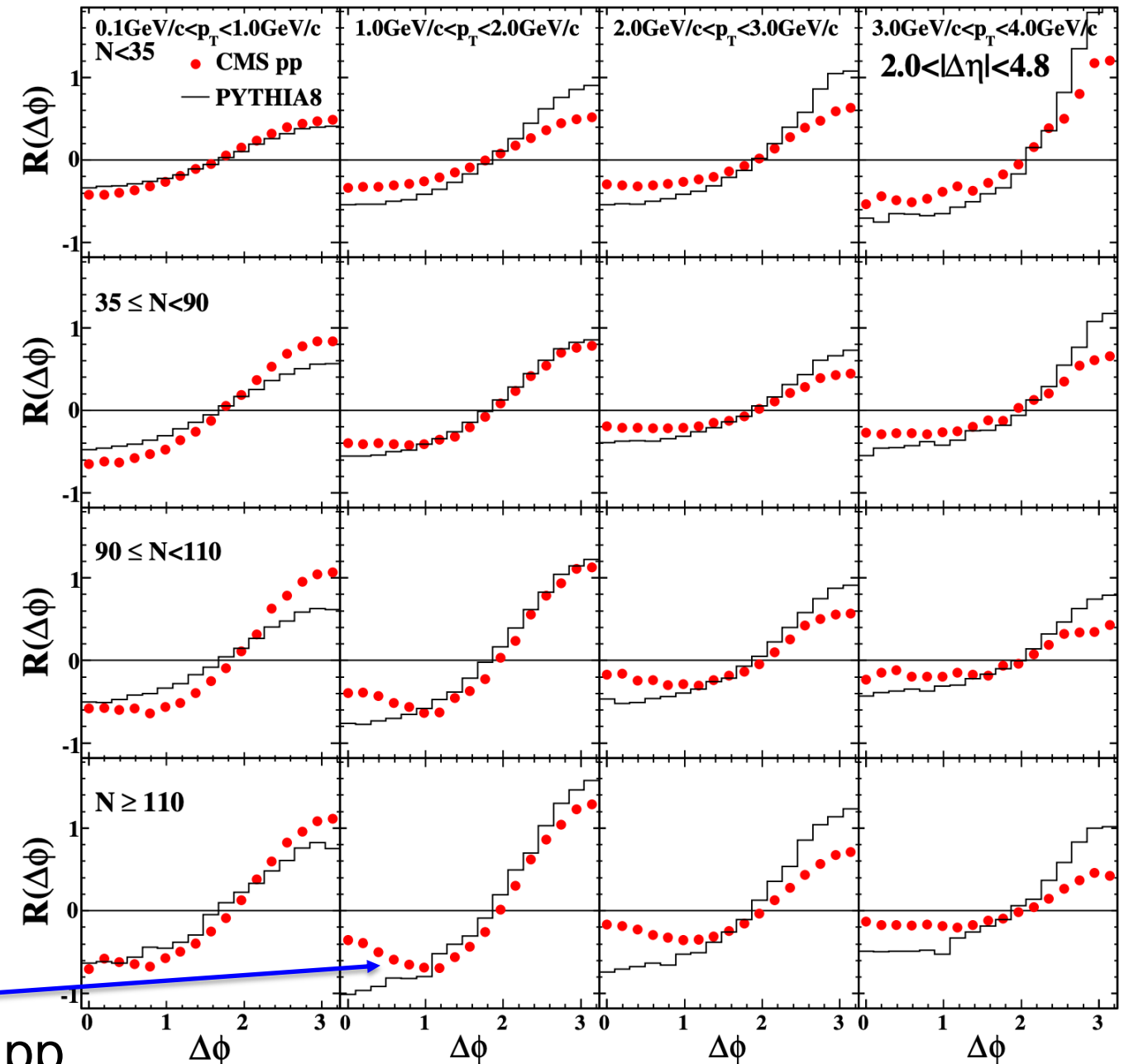
(c) CMS  $N \geq 110$ ,  $p_T > 0.1 \text{ GeV}/c$



(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$

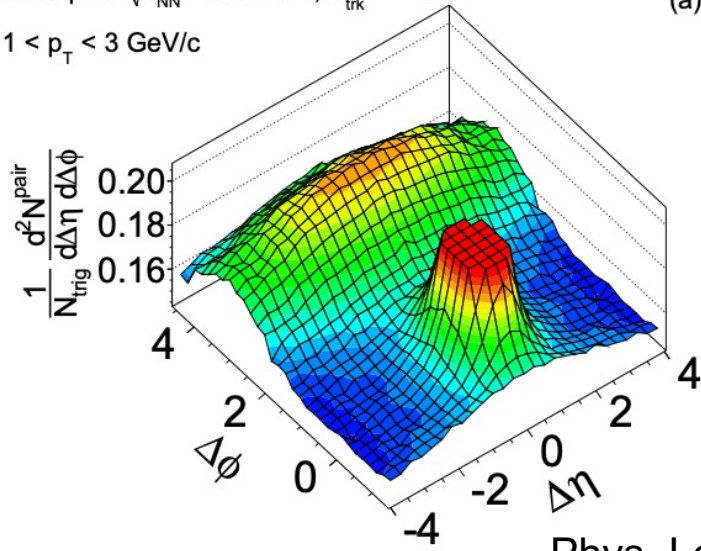


- Clear evidence of ridge in high multiplicity pp

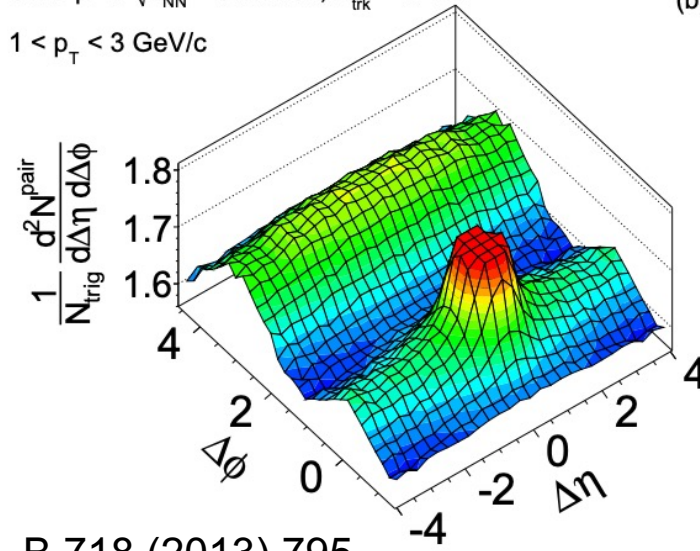


# Ridge in pPb collisions

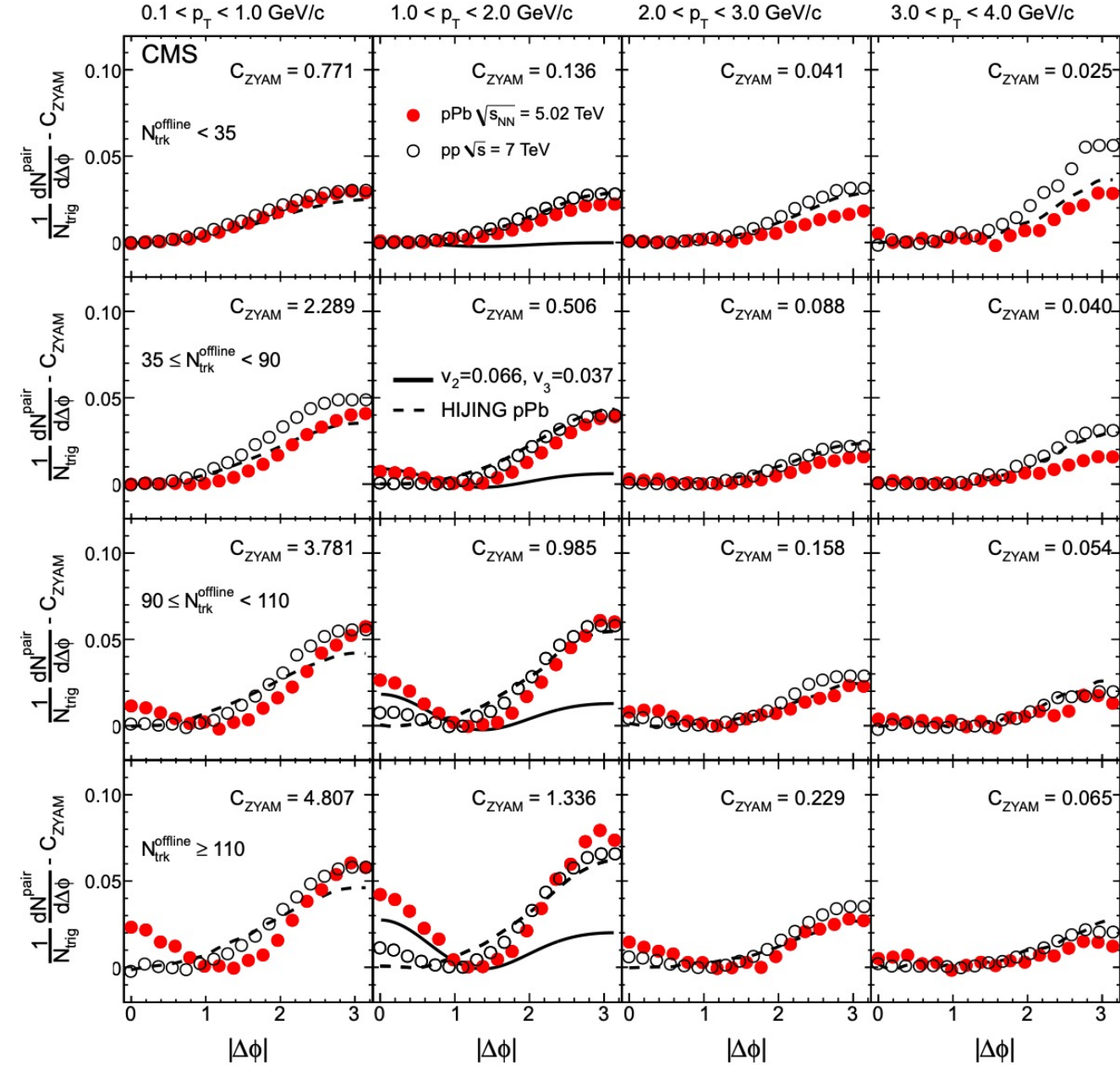
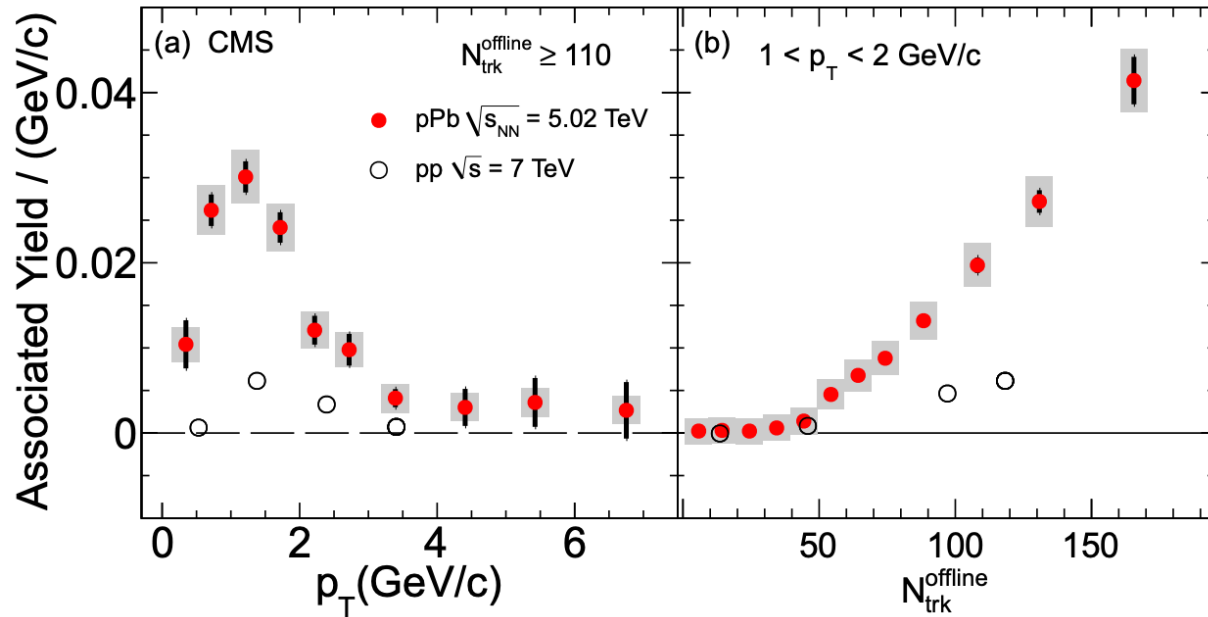
CMS pPb  $\sqrt{s_{NN}} = 5.02$  TeV,  $N_{trk}^{offline} < 35$   
 $1 < p_T < 3$  GeV/c



(a) CMS pPb  $\sqrt{s_{NN}} = 5.02$  TeV,  $N_{trk}^{offline} \geq 110$   
 $1 < p_T < 3$  GeV/c



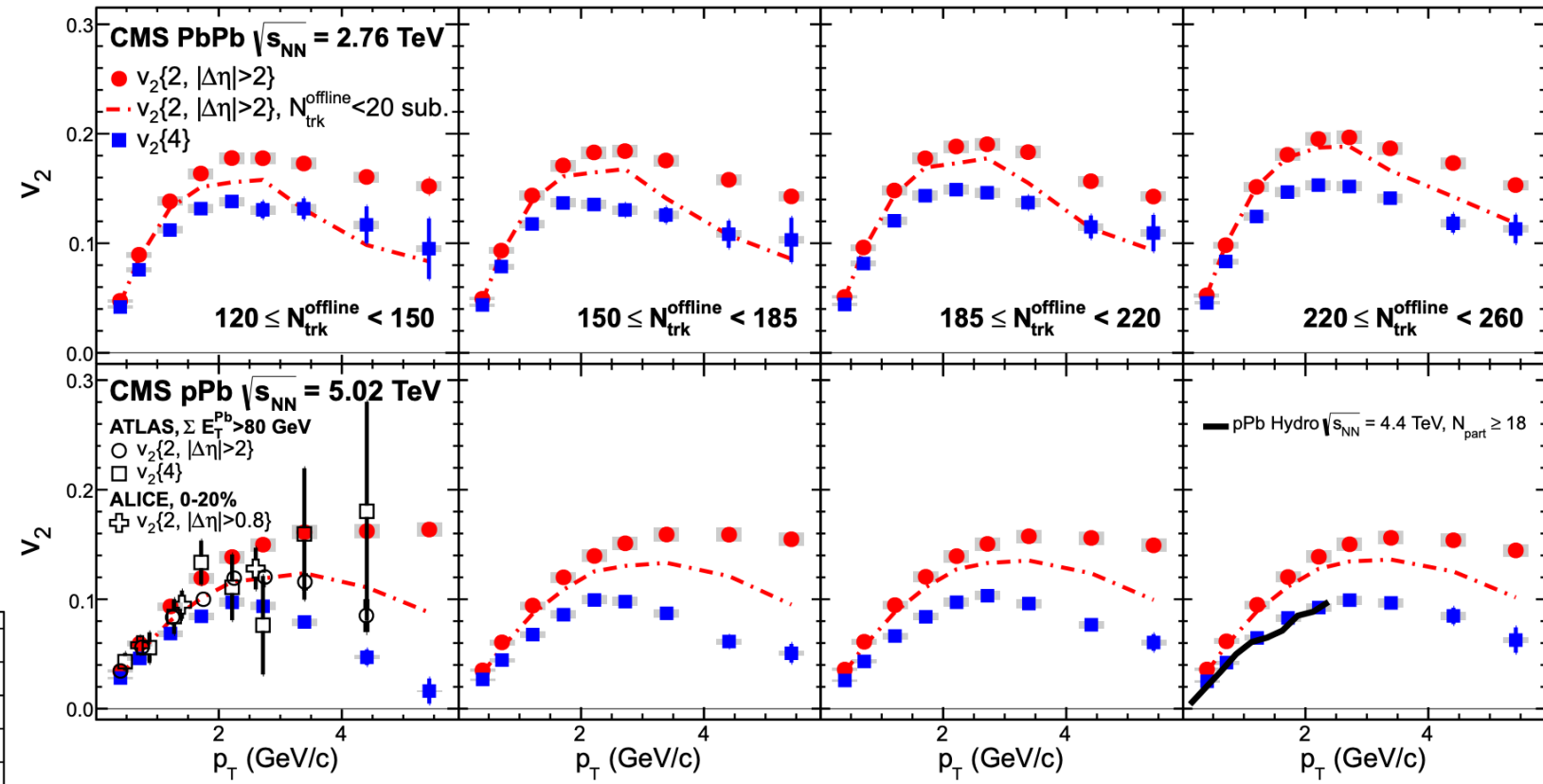
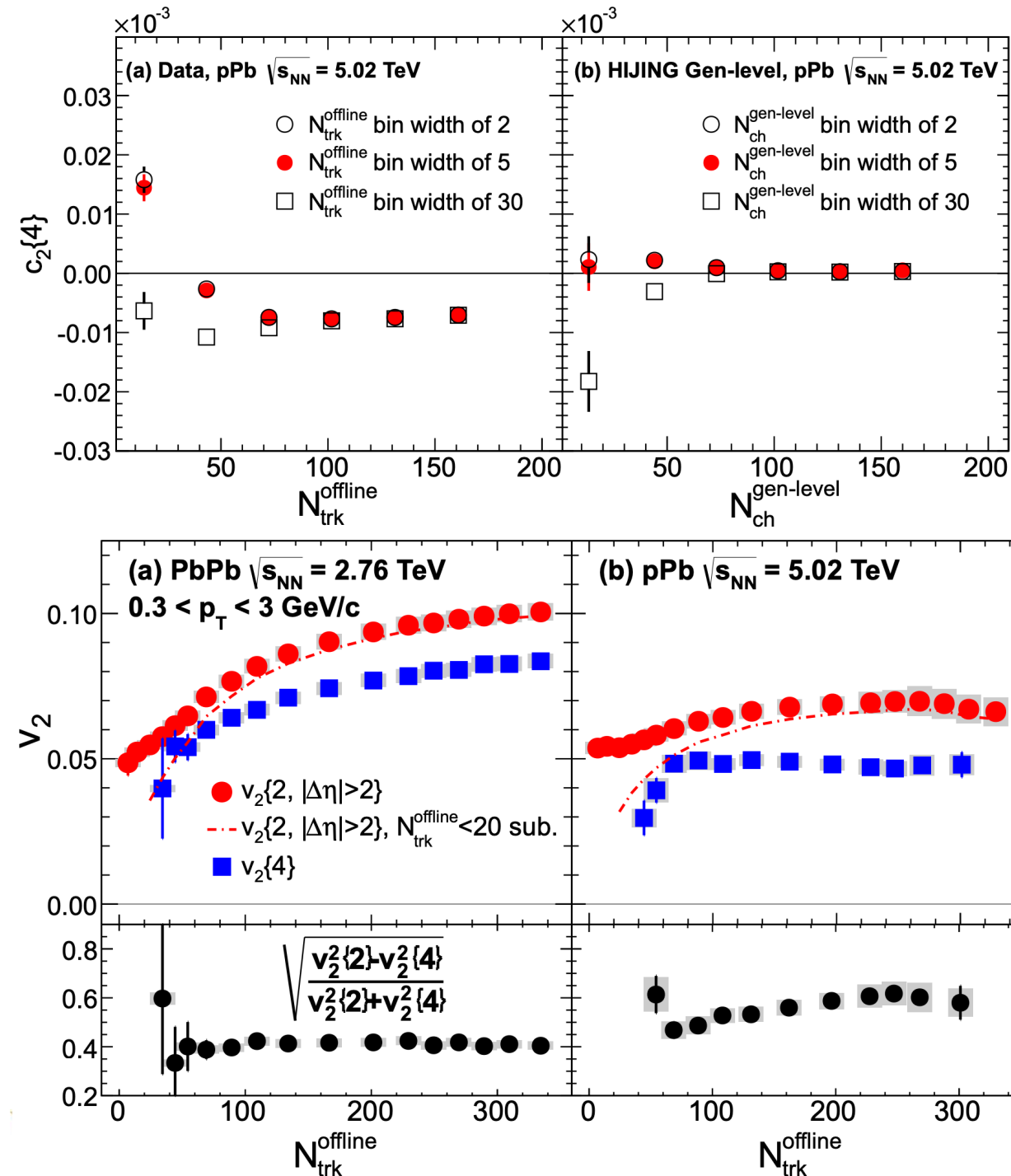
Phys. Lett. B 718 (2013) 795



- Clear evidence of ridge also in pPb collisions



# Multiparticle correlations in pPb collisions



- Need to carefully consider the multiplicity fluctuation effect for multiparticle correlations
- Fluctuations larger in pPb compared to PbPb
- Hydrodynamic predictions agree with data

# More details of two particle correlations at CMS

Reconstructed tracks with  $|\eta| < 2.4$

Signal pair distribution:

Background pair distribution:

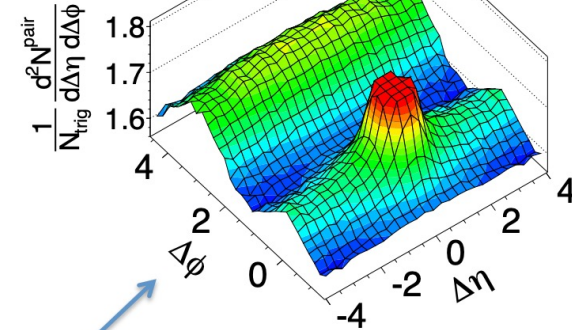
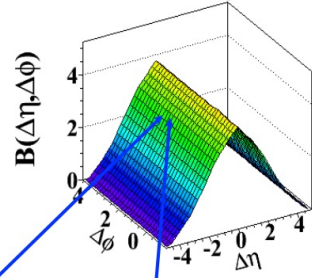
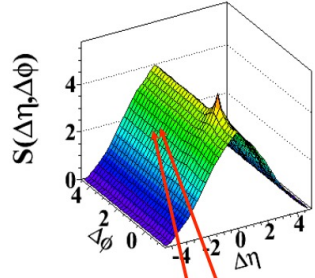
$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{same}}}{d\Delta\eta d\Delta\phi}$$

$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{mix}}}{d\Delta\eta d\Delta\phi}$$

CMS pPb  $\sqrt{s_{\text{NN}}} = 5.02$  TeV,  $N_{\text{trk}}^{\text{offline}} \geq 110$   
 $1 < p_{\text{T}} < 3$  GeV/c

same event pairs

mixed event pairs



Physics Letters B  
718 (2013) 795–814

Associated hadron yield per trigger:

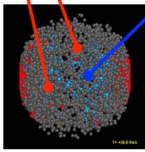
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} = B(0,0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

Long-range:  $|\Delta\eta| > 2$   
 Short-range:  $|\Delta\eta| < 1$   
 Near-side:  $\Delta\phi \sim 0$   
 Away-side:  $\Delta\phi \sim \pi$

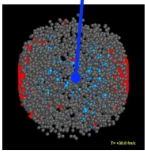
$$\Delta\eta = \eta^{\text{assoc}} - \eta^{\text{trig}}$$

$$\Delta\phi = \phi^{\text{assoc}} - \phi^{\text{trig}}$$

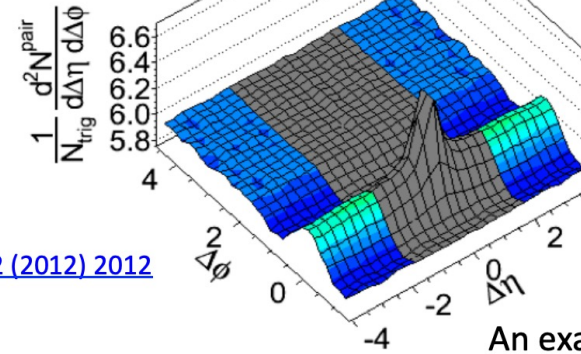
Event 1:



Event 2:

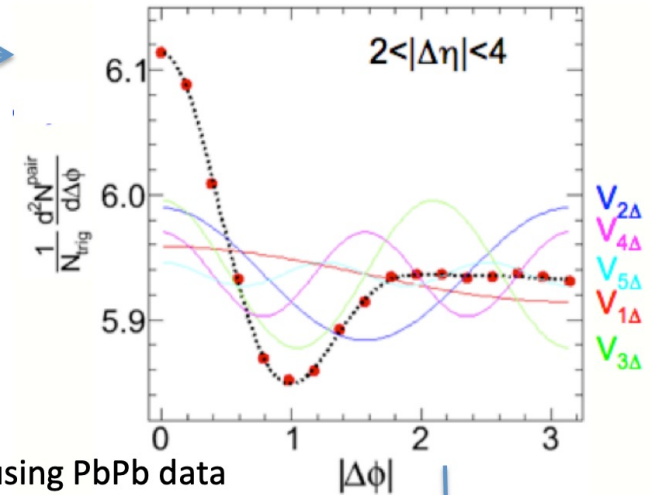


(a) CMS  $\int L dt = 3.1 \mu\text{b}^{-1}$   
 PbPb  $\sqrt{s_{\text{NN}}} = 2.76$  TeV, 0-5% centrality



EPJ C 72 (2012) 2012

An example using PbPb data



Assuming factorization:

$$V_{n\Delta} = v_n(p_{\text{T}}^{\text{trig}}) \times v_n(p_{\text{T}}^{\text{assoc}})$$

$$v_n\{2, |\Delta\eta| > 2\}(p_{\text{T}}) = \frac{V_{n\Delta}(p_{\text{T}}, p_{\text{T}}^{\text{ref}})}{\sqrt{V_{n\Delta}(p_{\text{T}}^{\text{ref}}, p_{\text{T}}^{\text{ref}})}}$$

Take low reference  $p_{\text{T}}$  bin (0.3-3 GeV/c)

Fourier decomposition:

$$\frac{dN^{\text{pair}}}{d\Delta\phi} \sim 1 + 2 \sum_{n=1} V_{n\Delta} \cos(n\Delta\phi)$$

# Reducing nonflow with peripheral subtraction

- Away-side correlations contain non-flow effects
- Subtract the data for high multiplicity by low multiplicity to correct for this

Fourier decomposition:

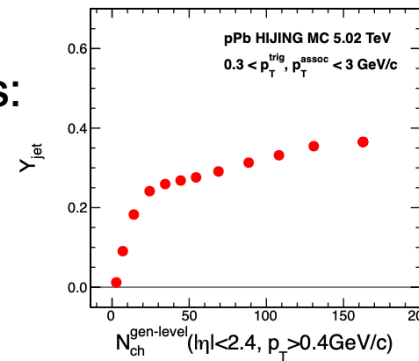
$$\frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} = \frac{N_{\text{assoc}}}{2\pi} \left\{ 1 + \sum_n 2V_{n\Delta} \cos(n\Delta\phi) \right\}$$

Subtracting peripheral correlations in  $v_2, v_3$  calculations:

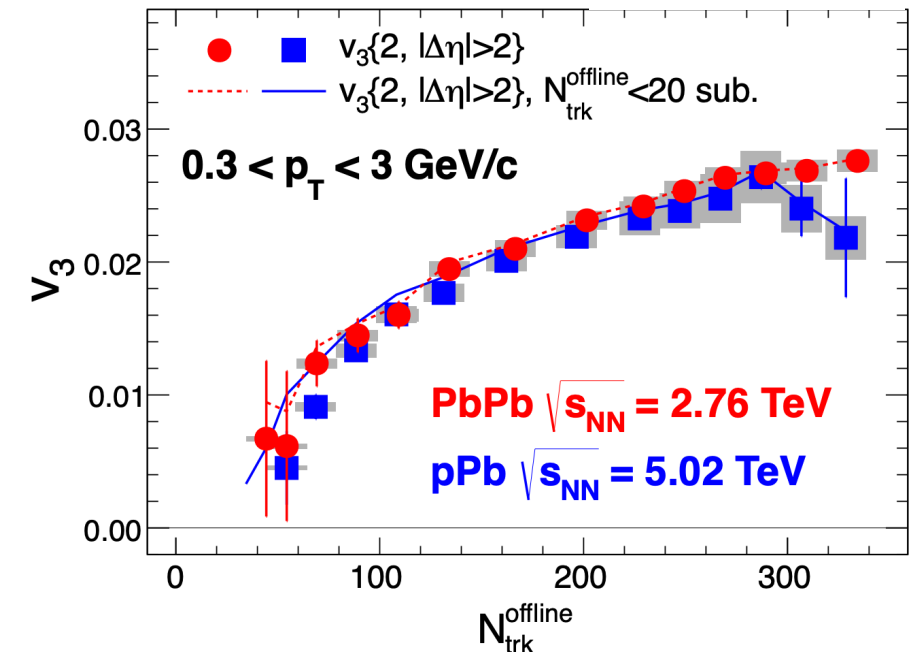
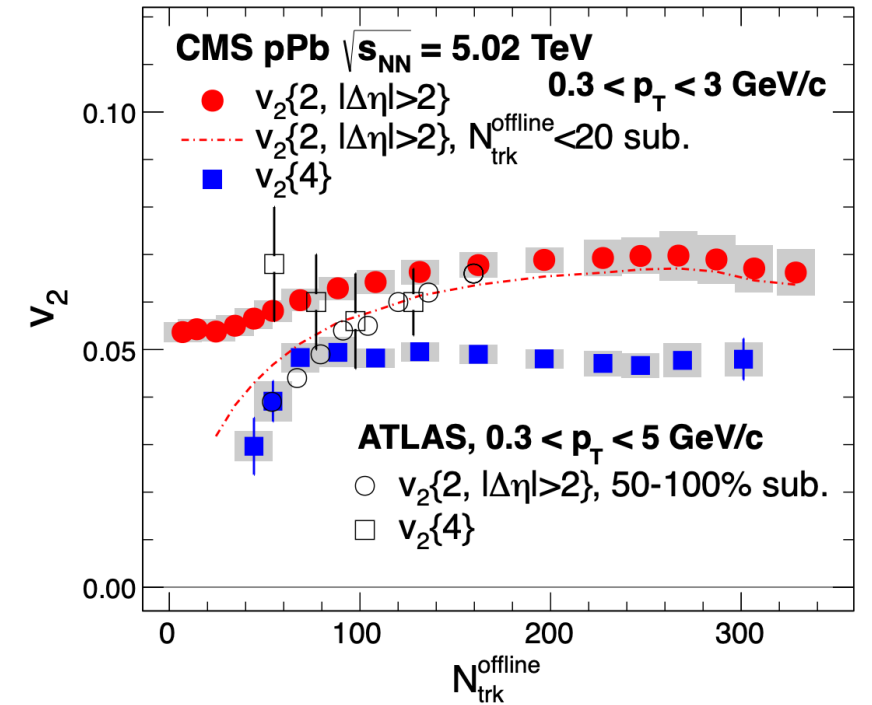
$$V_{n\Delta}(\text{cent}) - V_{n\Delta}(\text{peri}) \times \frac{N_{\text{assoc}}(\text{peri})}{N_{\text{assoc}}(\text{cent})} \times \frac{Y^{\text{jet}}(\text{cent})}{Y^{\text{jet}}(\text{peri})}$$

Subtract  $N_{\text{trk}}^{\text{offline}} < 20$  (70-100%) to avoid removing signal ( $N_{\text{trk}}^{\text{offline}} \sim 40$ )

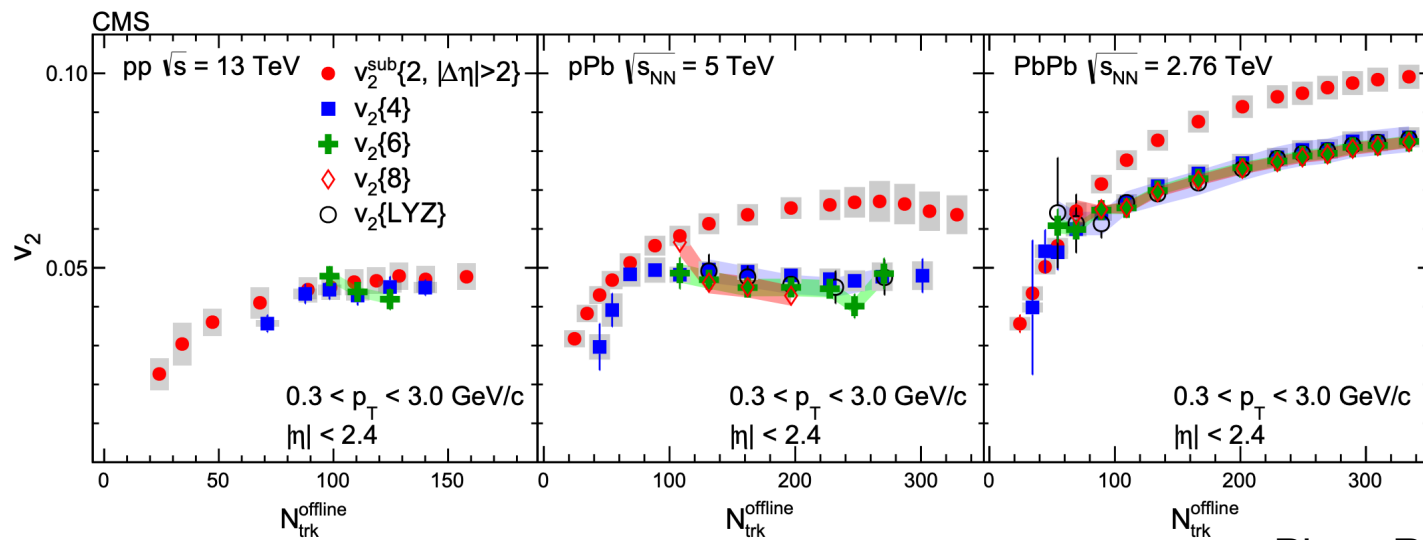
Account for the fact that jet correlation increases with multiplicity



- The method reduce nonflow at low multiplicities

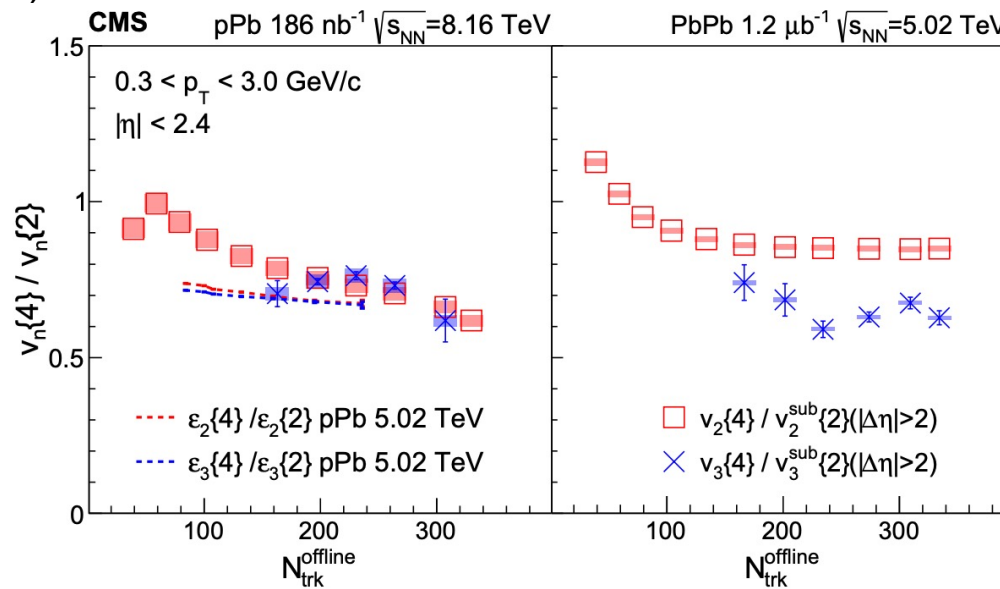
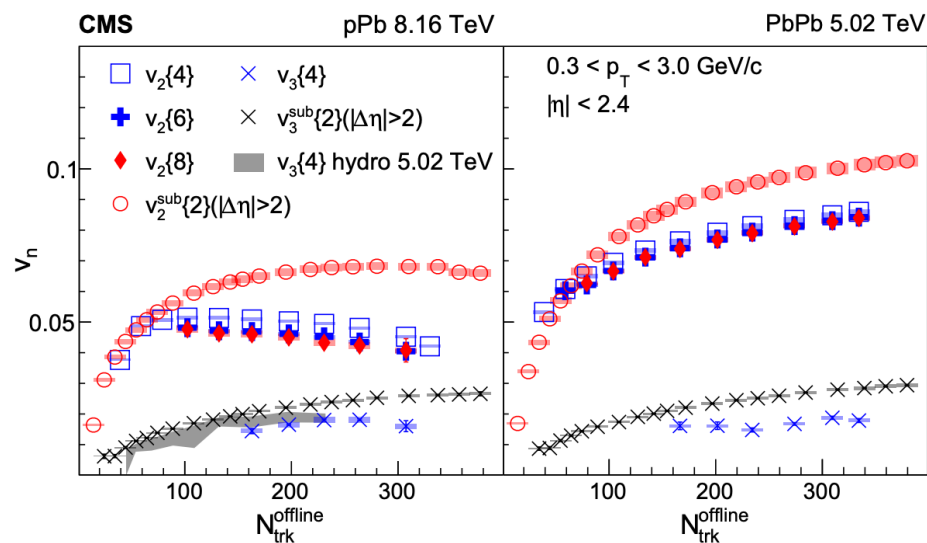
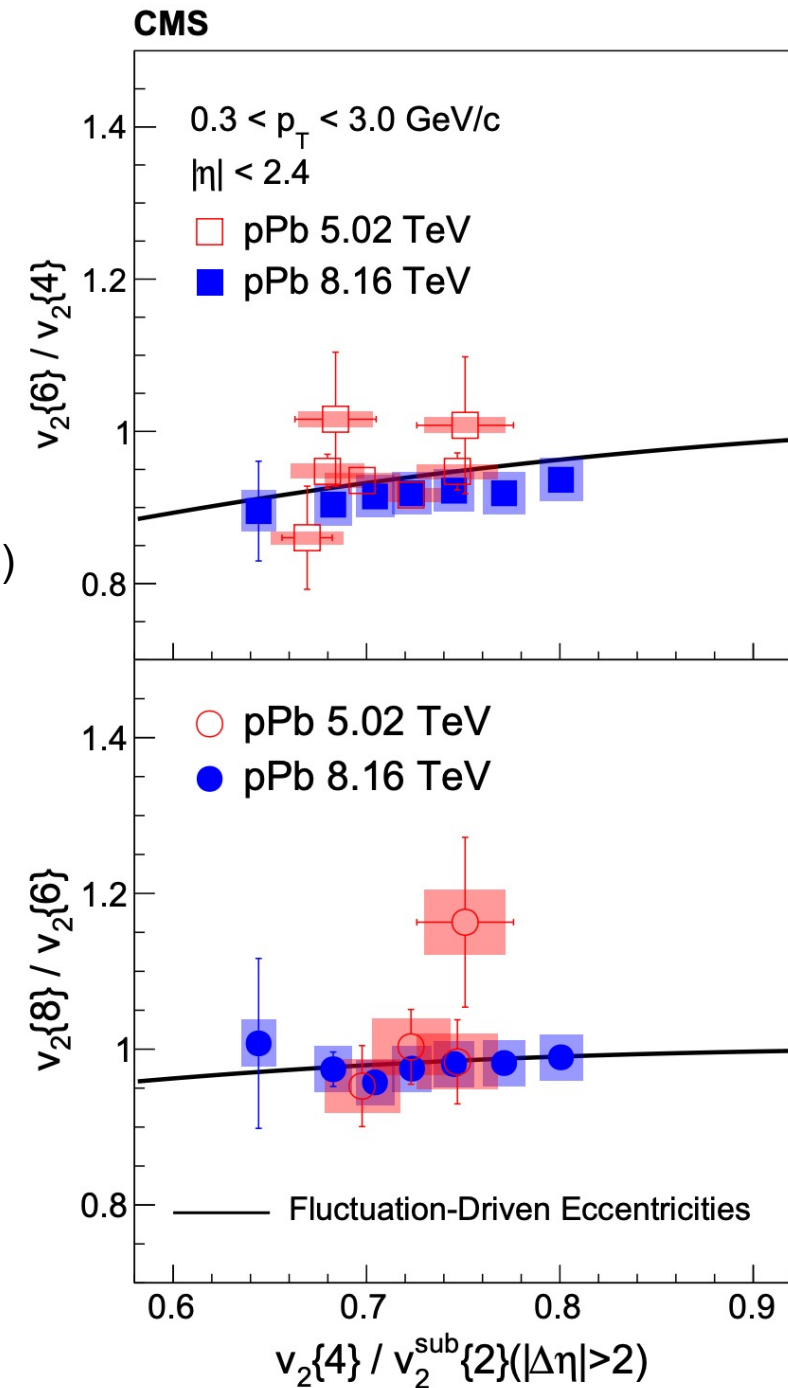


# More evidence of small system flow



Phys. Lett. B 765 (2017) 193

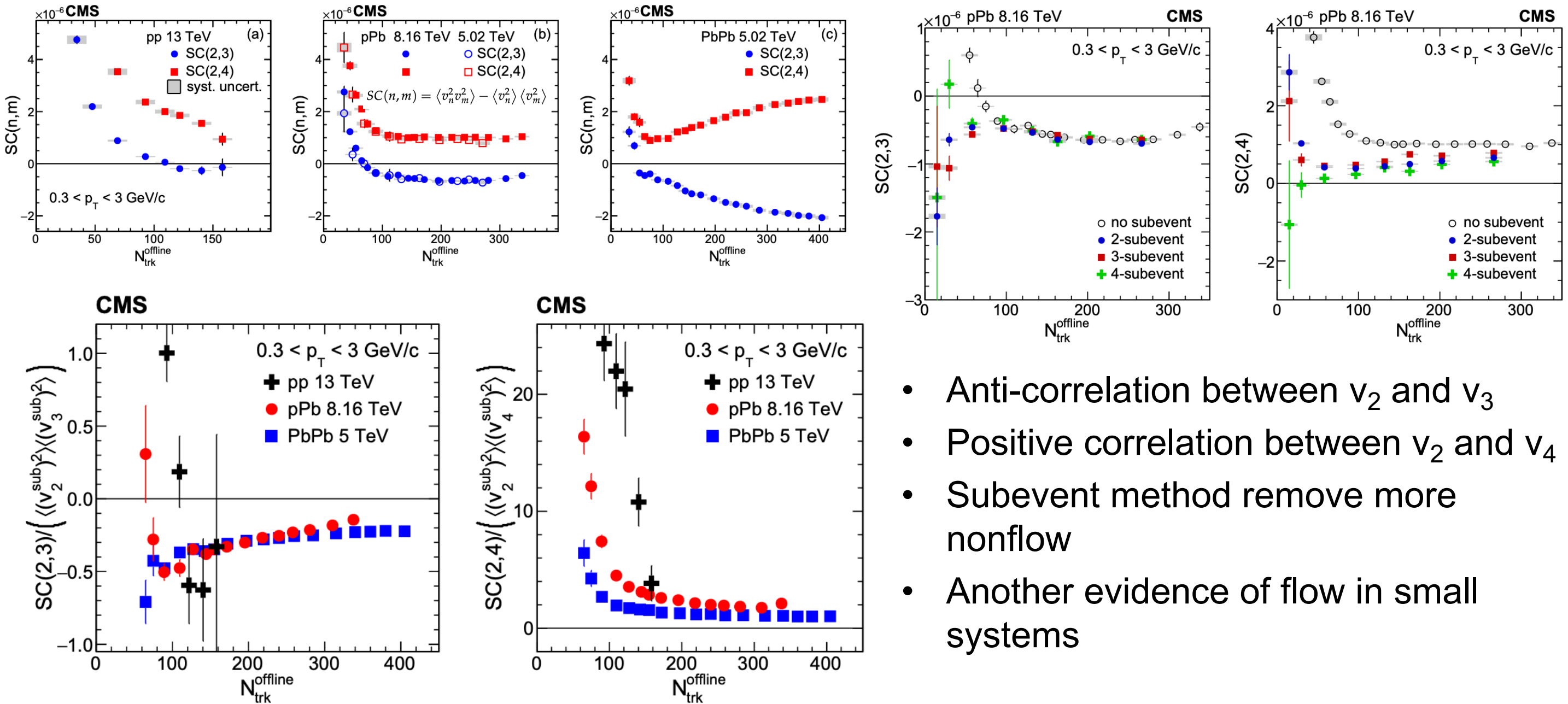
Phys. Rev. C 101, 014912 (2020)



- The evidence of small system flow is more clear



# Symmetric cumulant



- Anti-correlation between  $v_2$  and  $v_3$
- Positive correlation between  $v_2$  and  $v_4$
- Subevent method remove more nonflow
- Another evidence of flow in small systems

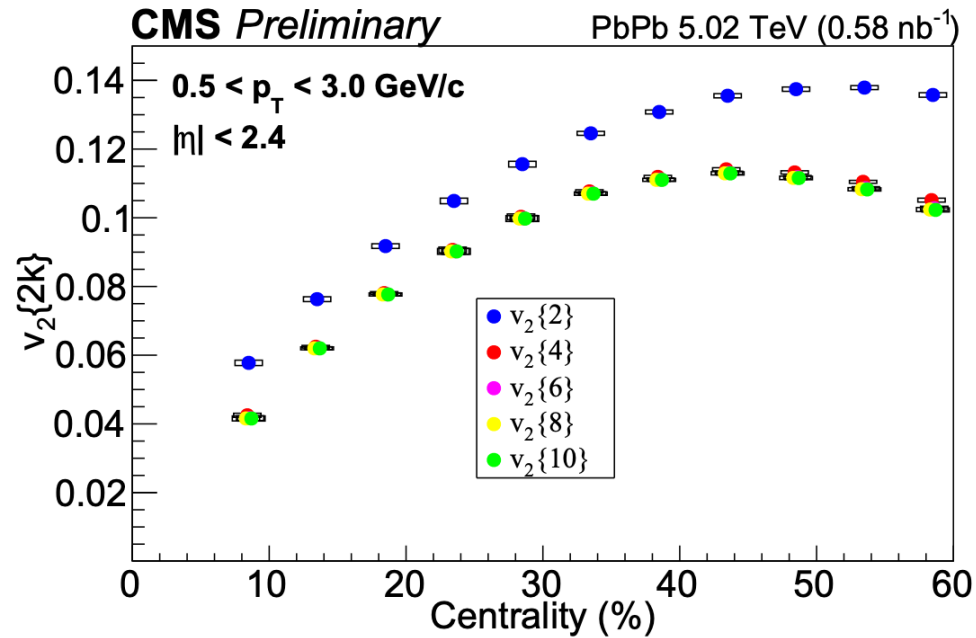


# Recent development

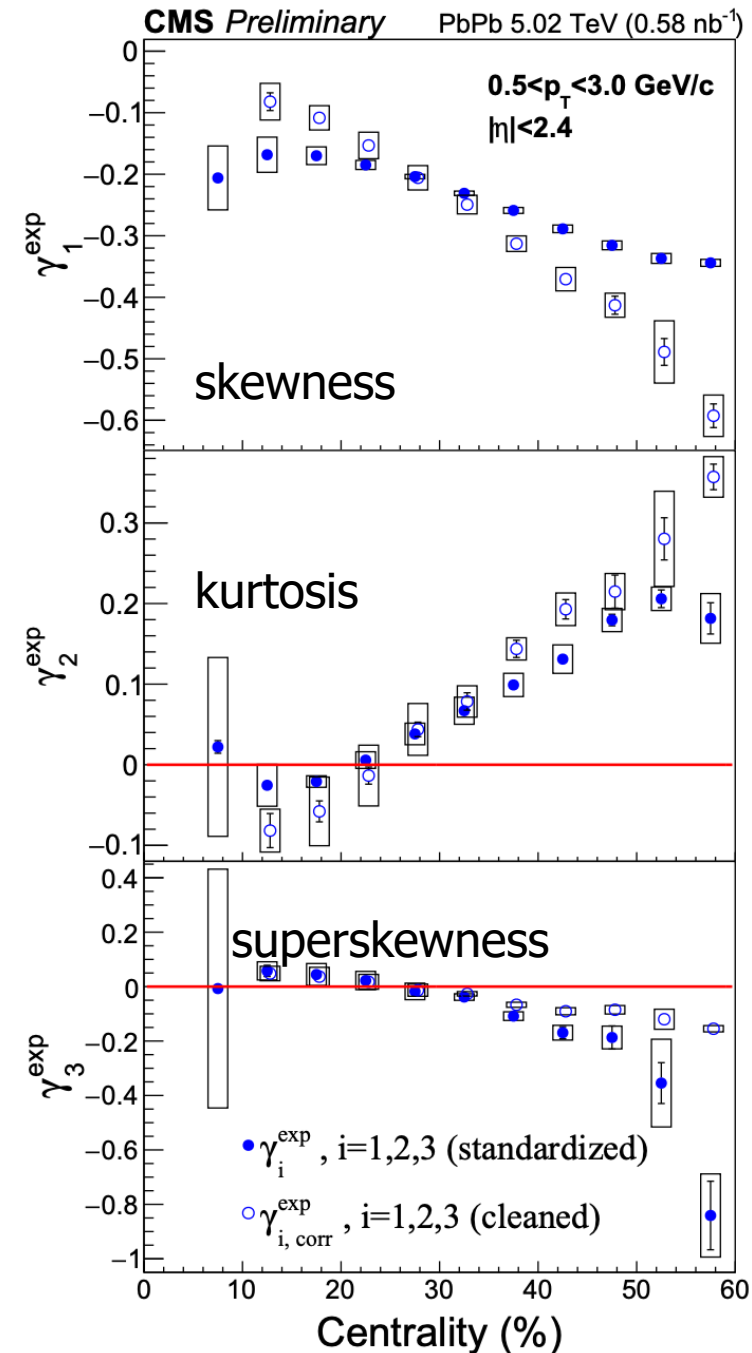


# CHARGED HADRONS – CUMULANTS IN PBPB

CMS-PAS-HIN-21-010



- Measurements of  $v_2$  with up to 10 particle correlations from the cumulant method
- Splittings between cumulant of different orders are sensitive to non-Gaussian fluctuations of  $v_2$
- Hydrodynamics and initial state models can be tested with the moments: skewness, kurtosis, and superskewness



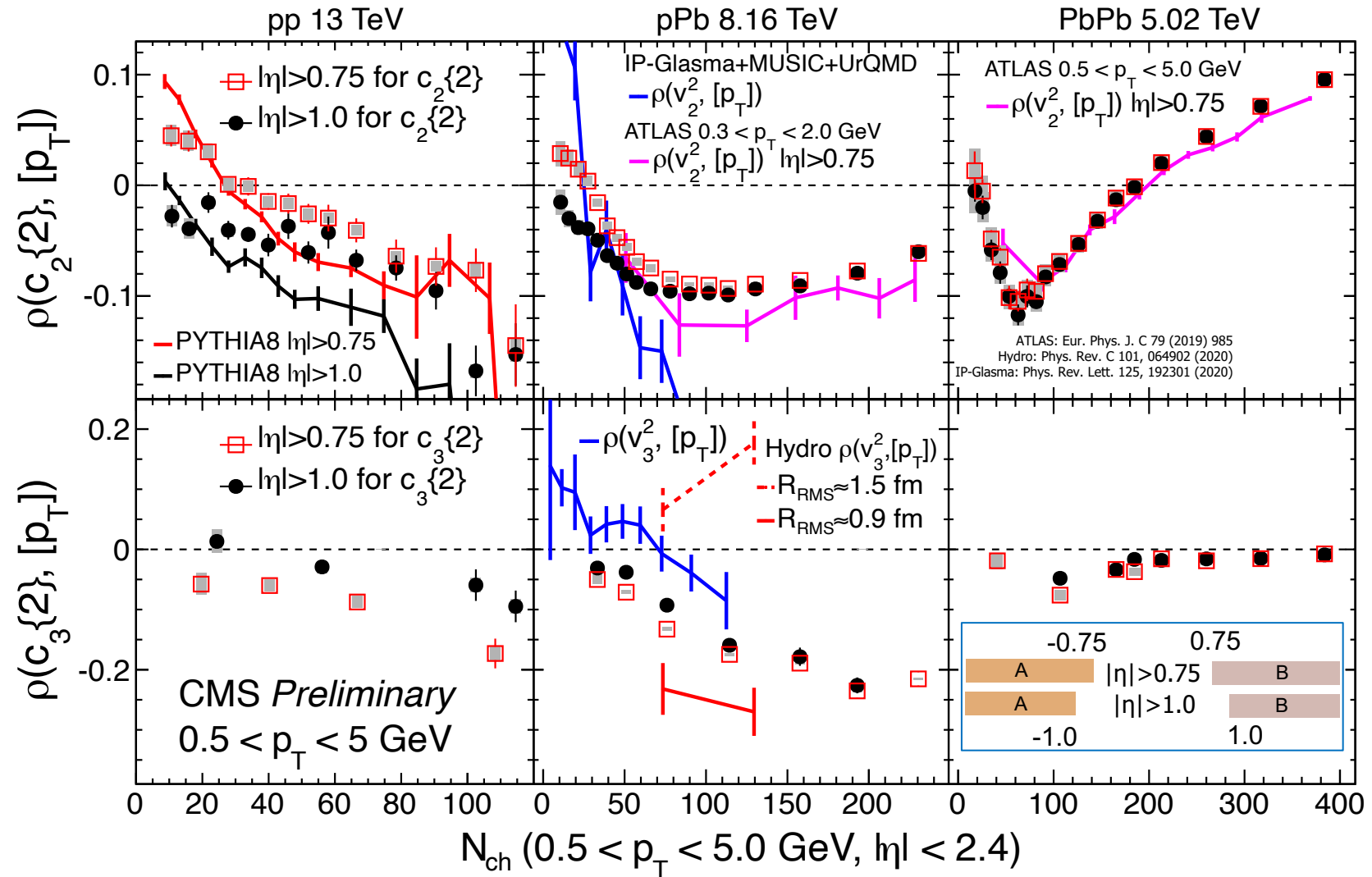
# FLOW-MEAN PT CORRELATIONS

CMS-PAS-HIN-21-012

$$\rho(v_2^2, [p_T]) = \frac{\text{cov}(v_2^2, [p_T])}{\sqrt{\text{Var}(v_2^2)_{dyn}} \sqrt{\text{Var}([p_T])_{dyn}}}$$

n=2

n=3



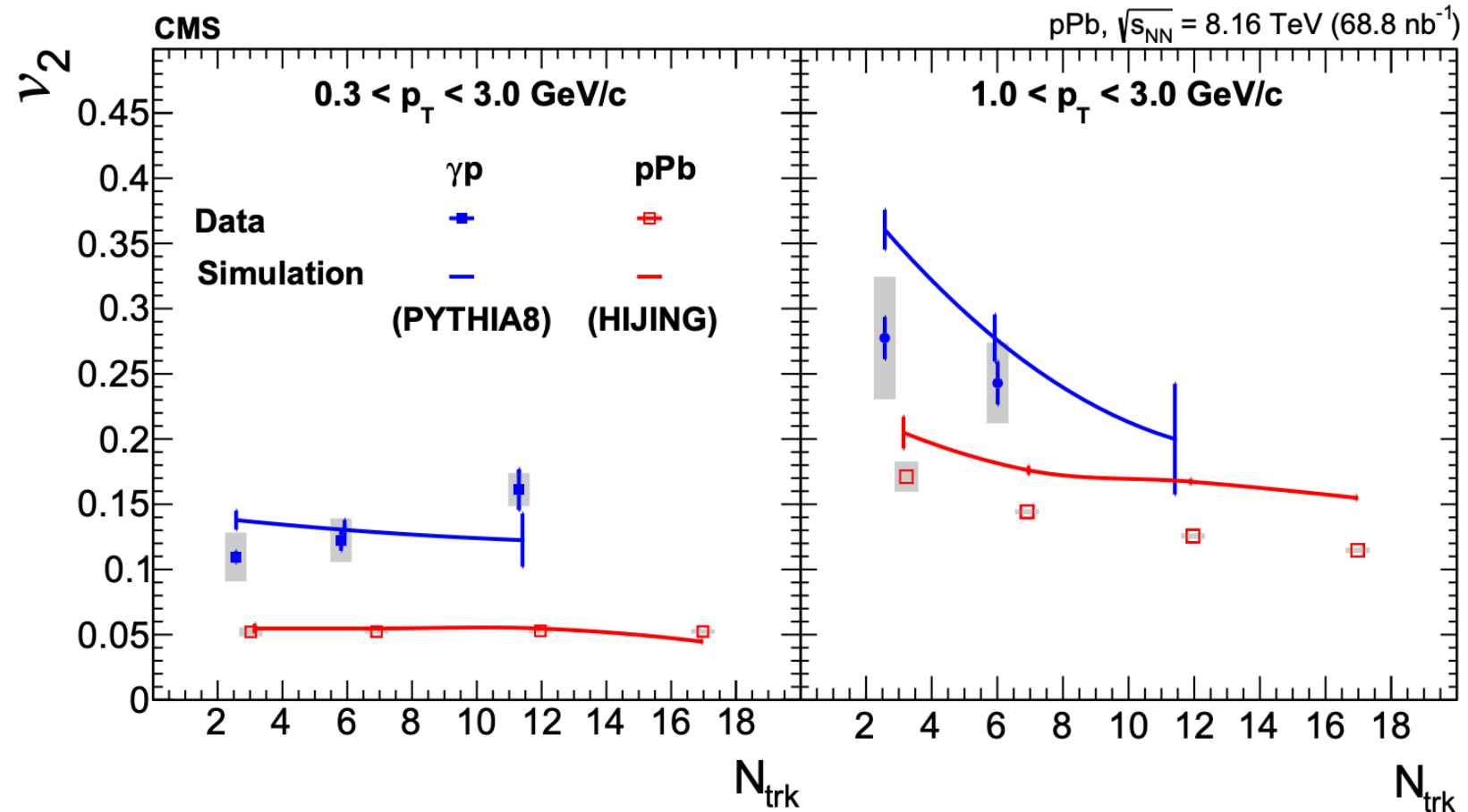
- Apparent sign change for  $\rho(c_2\{2\}, [p_T])$  in pPb -> agree with IP-Glasma+hydrodynamics
- However, no sign change is observed when using  $|\eta| > 1.0$  for  $c_2\{2\}$
- After removing nonflow with larger  $\eta$  gap, no evidence of CGC in data
- Data better described by the smaller initial fireball  $R_{RMS} = 0.9$  fm in hydrodynamics





# FLOW IN PHOTON-P COLLISIONS

[arXiv:2204.13486](https://arxiv.org/abs/2204.13486)



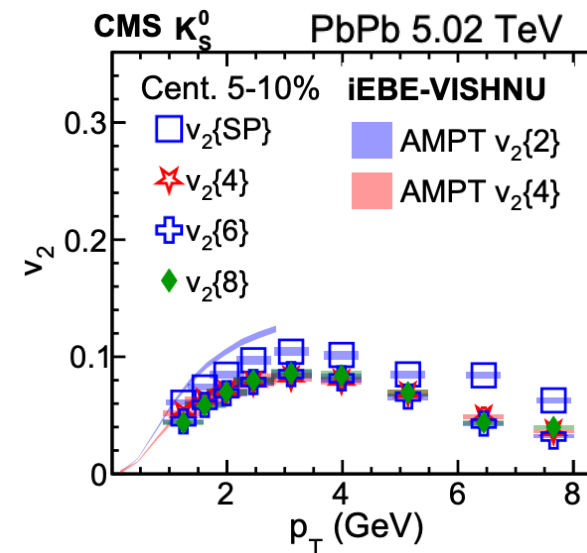
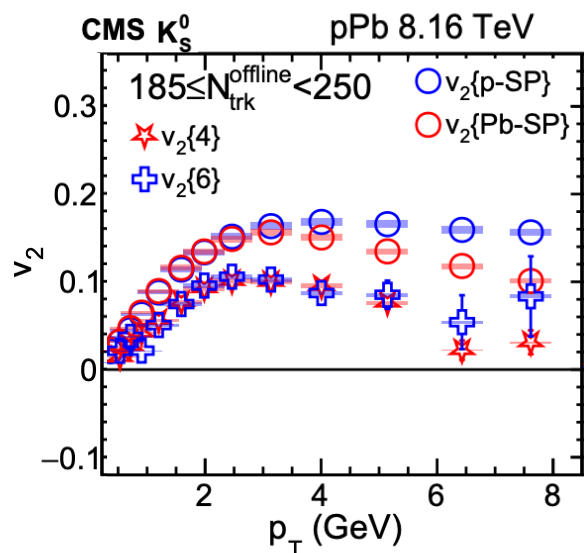
- Search for azimuthal anisotropy in  $\gamma p$  interactions with pPb UPC
- Nonflow peripheral subtraction not applied
- Consistent with simulations without collective effects for both  $\gamma p$  and pPb in the  $N_{\text{trk}}$  range



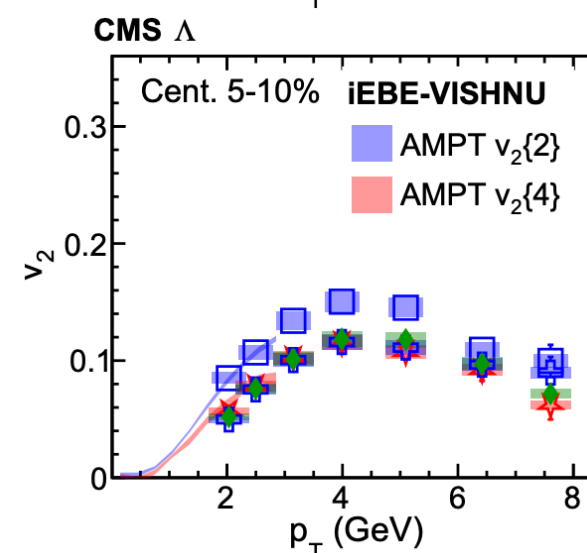
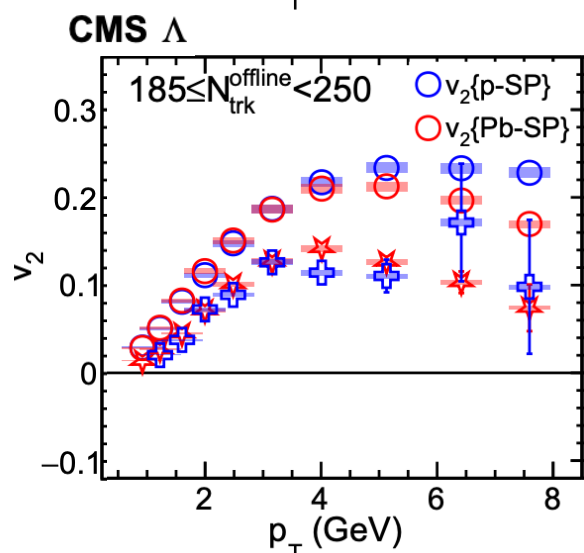
# STRANGE PARTICLE FLOW

arXiv:2205.00080

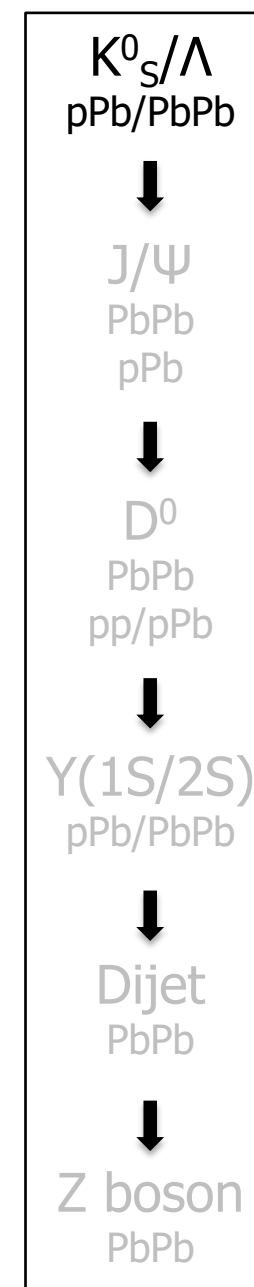
$K_S^0$



$\Lambda$



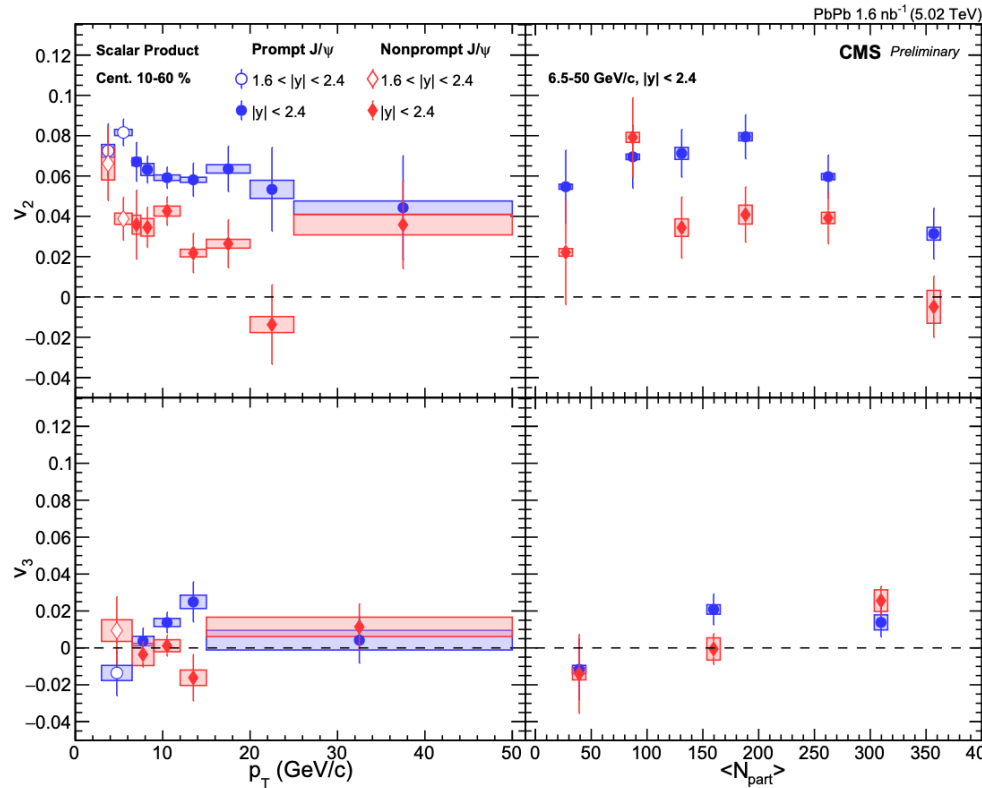
- $K_S^0$  and  $\Lambda$  flow studied with multiparticle correlations
- Four and six particle correlations are nearly identical
- Compared with PbPb to illustrate the system size dependence of event-by-event fluctuations



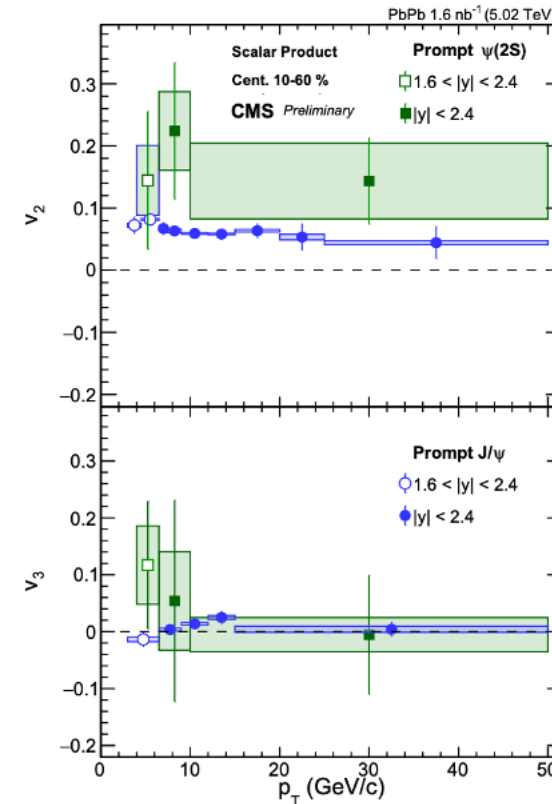
# J/ψ AND Ψ(2S) FLOW IN PBPB

CMS-PAS-HIN-21-008

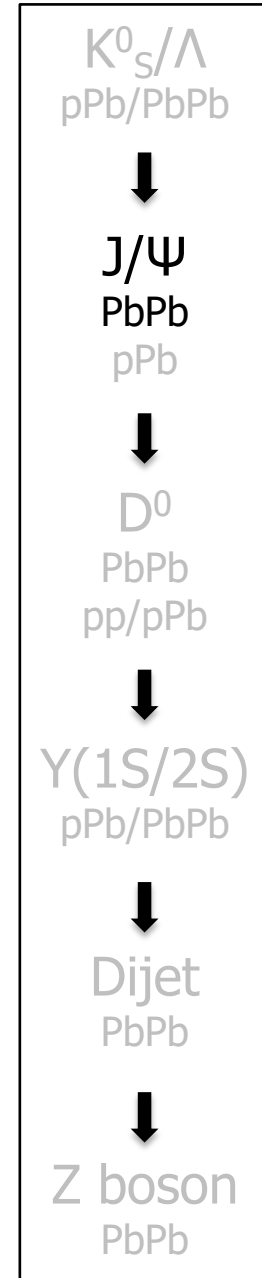
Prompt J/ψ and b→J/ψ



Prompt Ψ(2S)

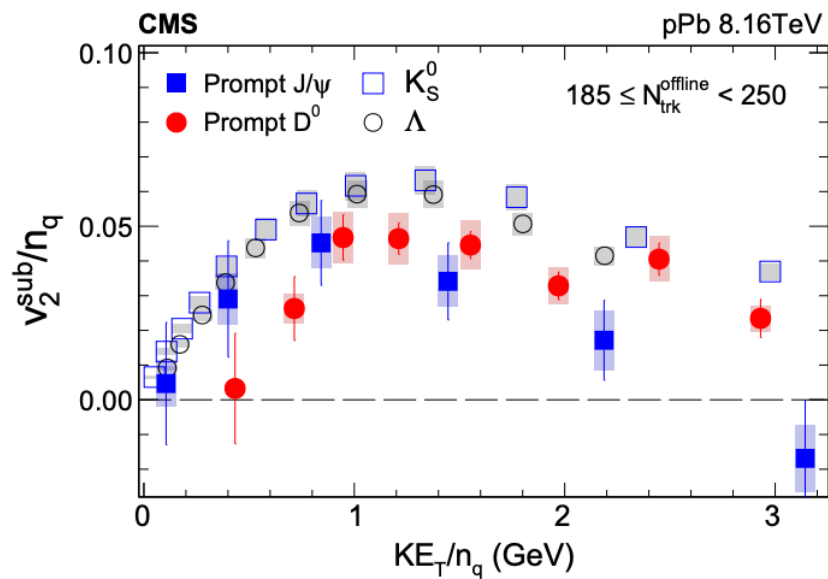
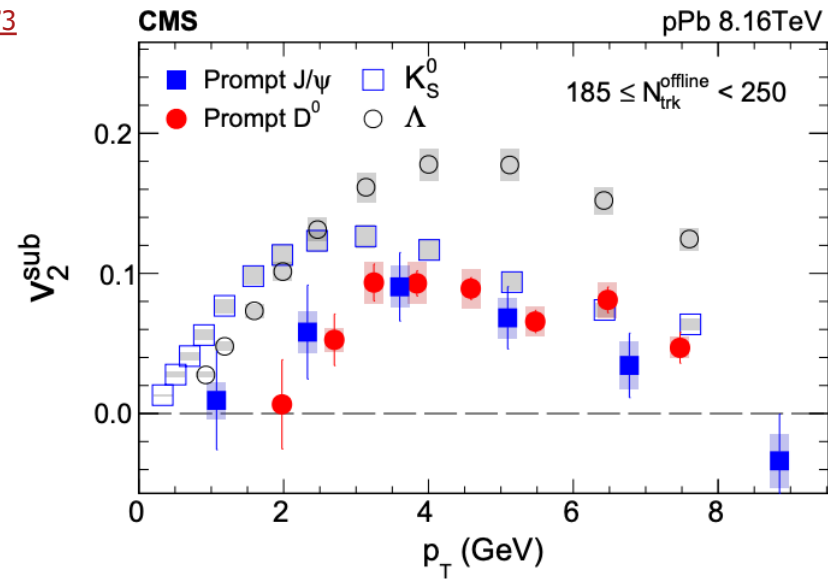


- Significant  $v_2$  for Prompt J/ψ and b→J/ψ
  - Different dynamics for c and b quark
- First separation of  $v_3$  for prompt and b→J/ψ
- First Ψ(2S) with  $v_2 > 0$ ; consistent with 0 for  $v_3$

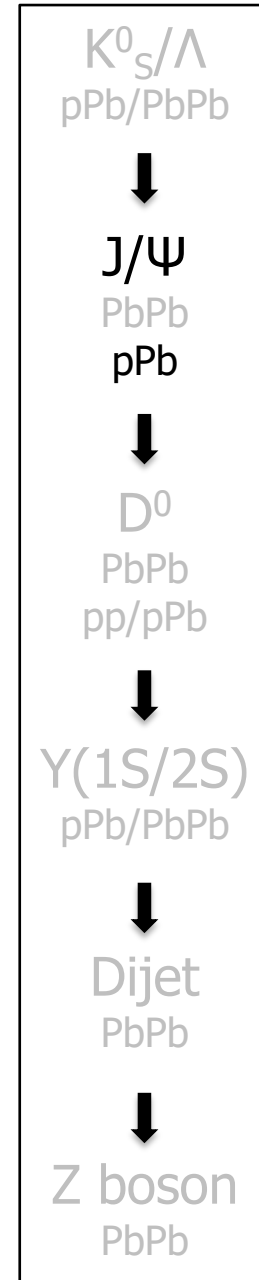


# J/PSI AND D<sup>0</sup> IN PPB

[arXiv:1810.01473](https://arxiv.org/abs/1810.01473)

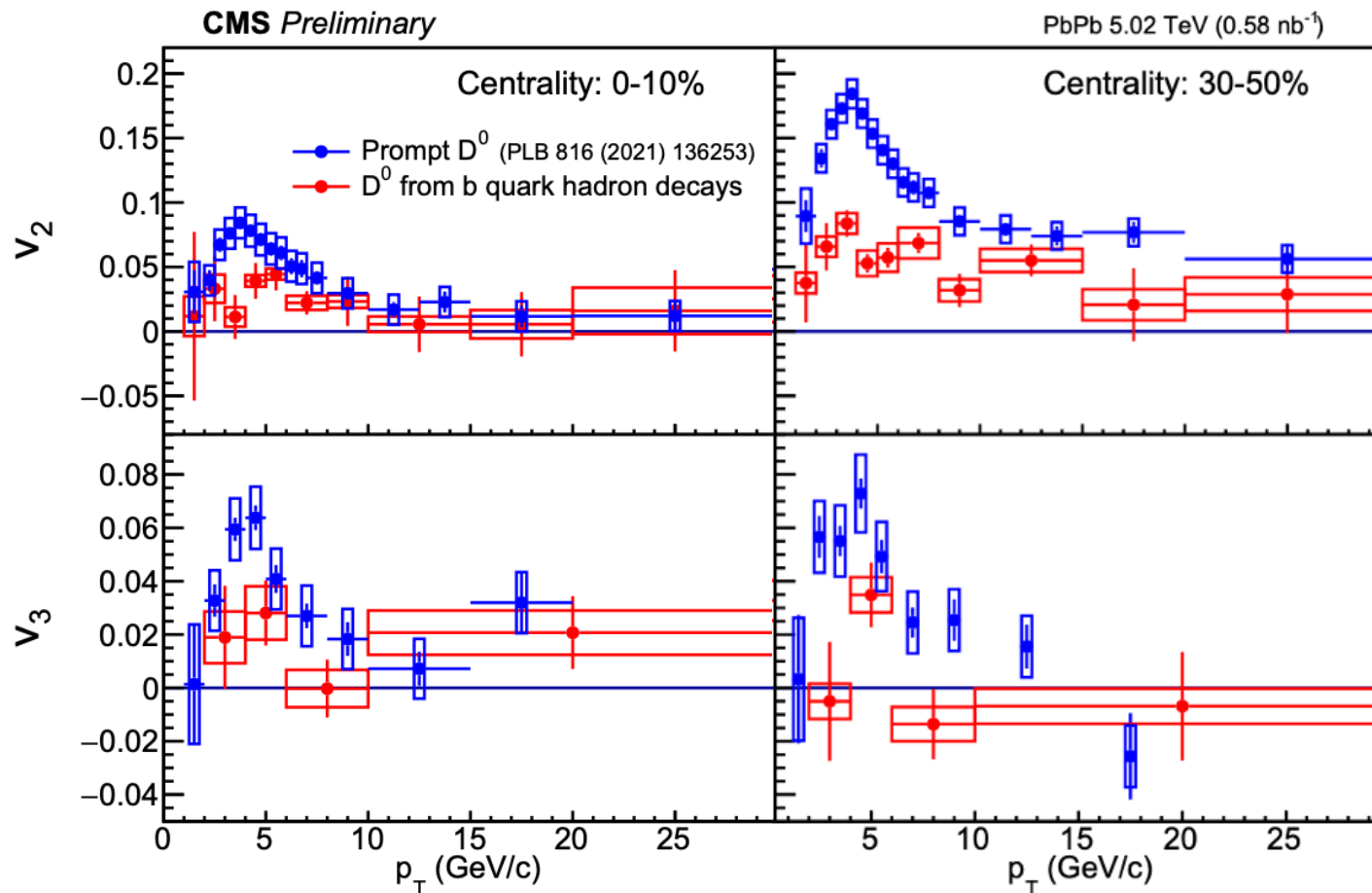


- Evidence of charm quark collectivity in high multiplicity pPb
- Heavy quarks exhibit weaker collective behavior

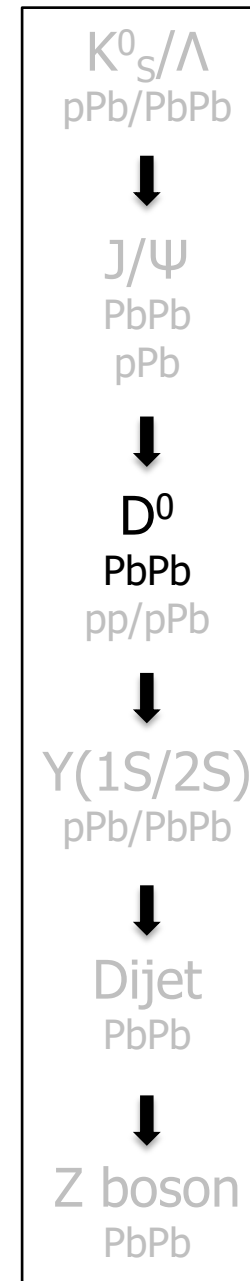


# PROMPT $D^0$ AND $B \rightarrow D^0$ FLOW IN PBPB

CMS-PAS-HIN-21-003

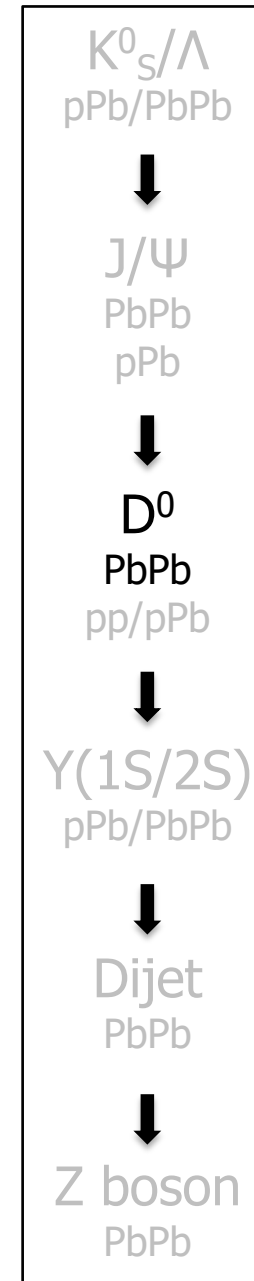
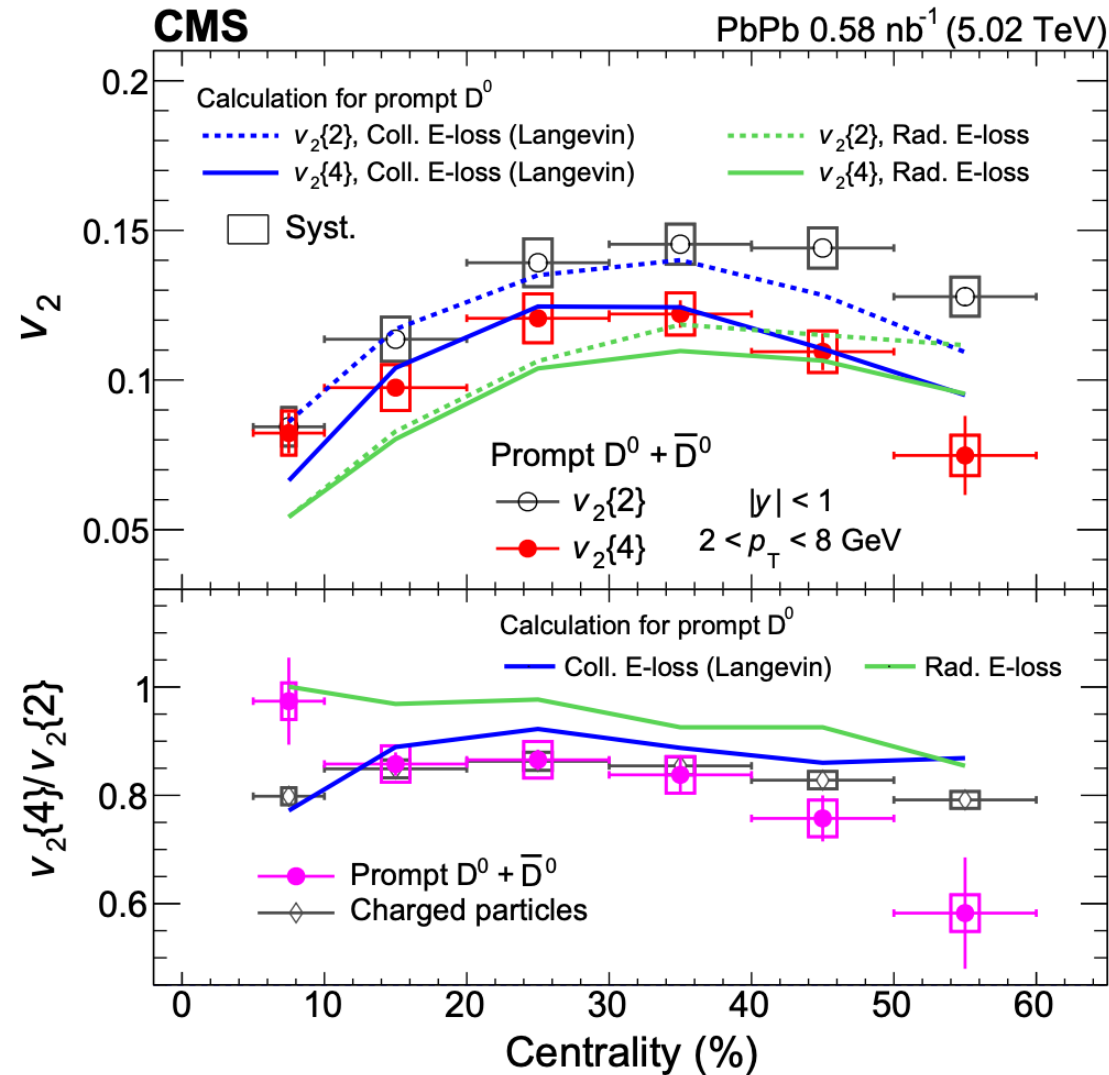


- $(b \rightarrow D^0) v_n$  significantly lower than prompt  $D^0 v_n$
- $(b \rightarrow D^0) v_2$ , less centrality dependence compared to prompt  $D^0 v_2$ 
  - b quark collectivity affected by fluctuations



# D<sup>0</sup> WITH MULTIPARTICLE CORRELATIONS

arXiv:2112.12236



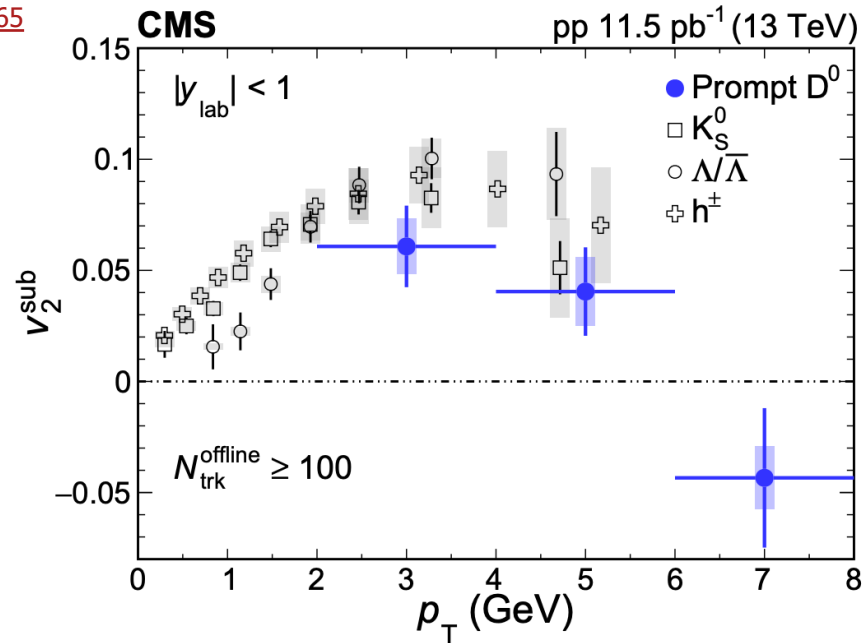
- Probe event-by-event fluctuations
- $v_2\{4\} < v_2\{2\}$  for D<sup>0</sup>
- Indications of possible differences in energy loss fluctuations between D<sup>0</sup> and charged hadrons



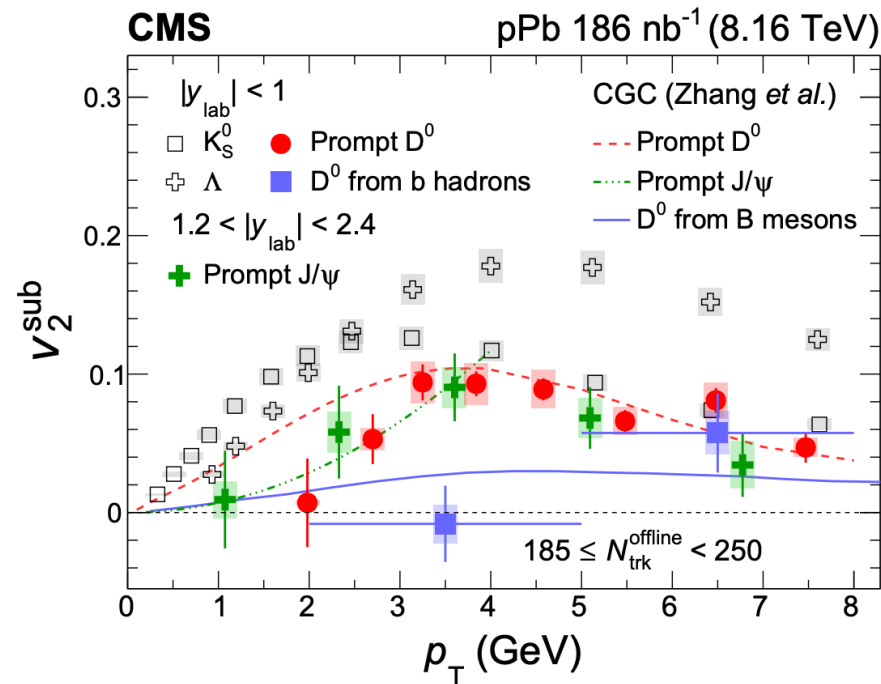
# D<sup>0</sup> FLOW IN PP AND PPb

[arXiv:2009.07065](https://arxiv.org/abs/2009.07065)

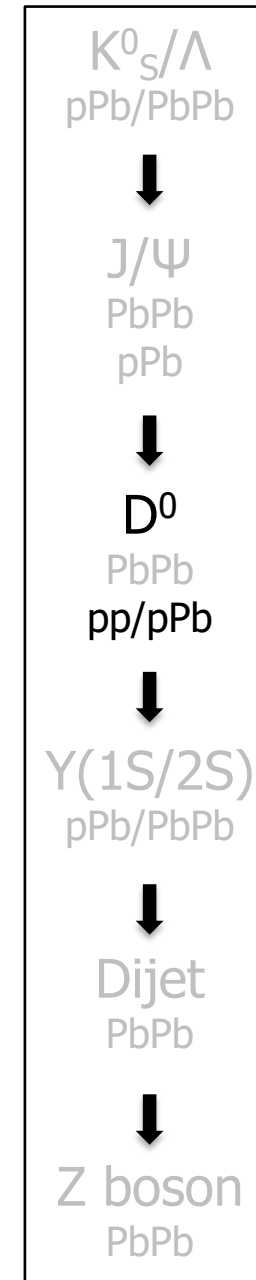
pp



pPb

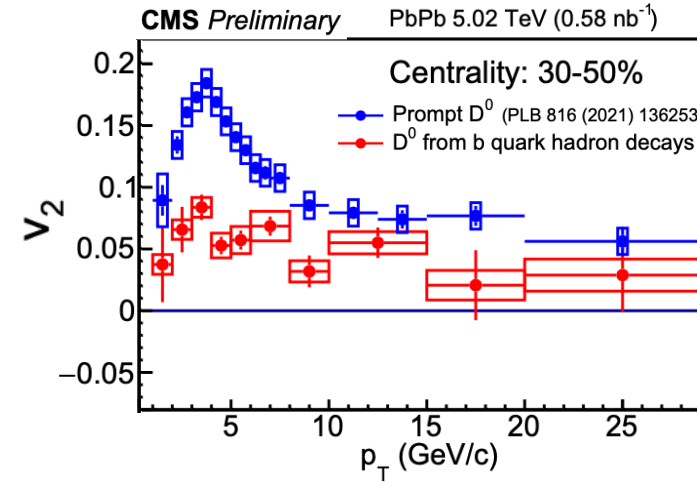
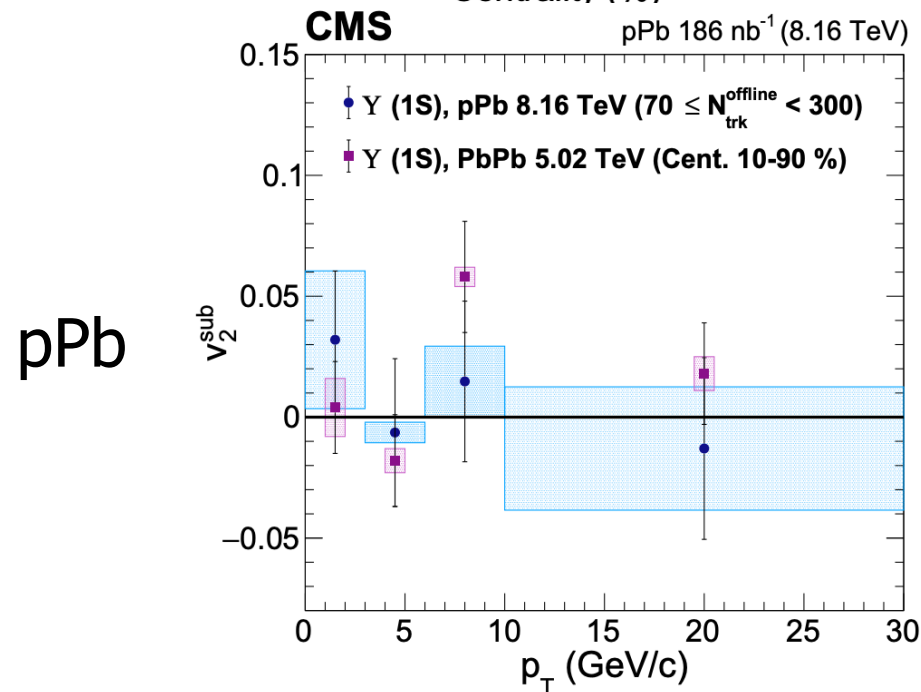
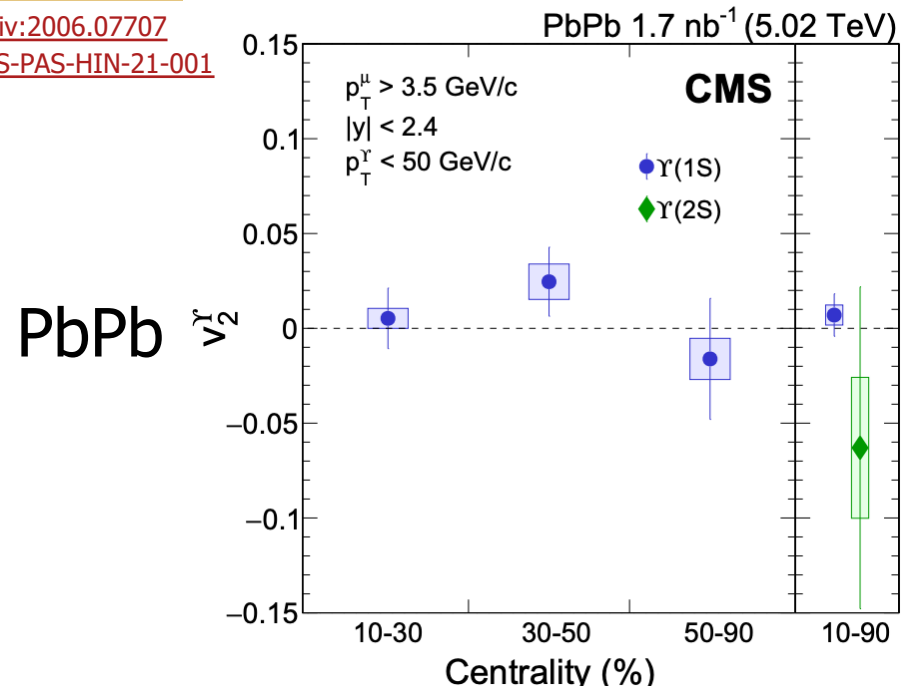


- Indications of positive D<sup>0</sup> v<sub>2</sub> in pp
- (b→D<sup>0</sup>) has much smaller v<sub>2</sub> compared to prompt D<sup>0</sup> in pPb
- mass dependent v<sub>2</sub>

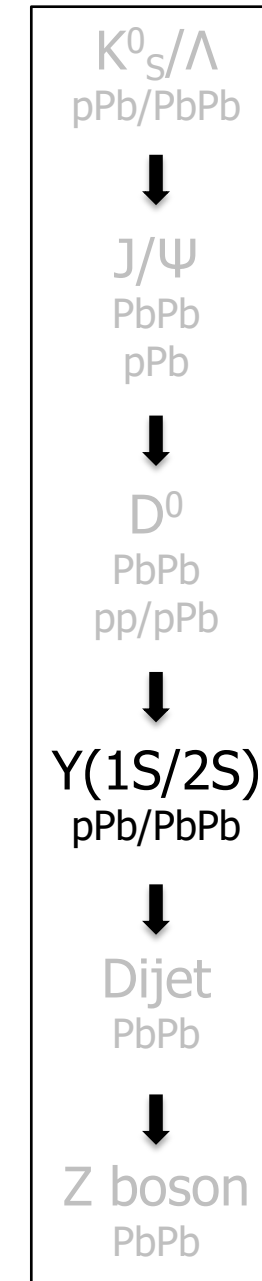


# Y(1S) AND Y(2S) FLOW

[arXiv:2006.07707](https://arxiv.org/abs/2006.07707)  
[CMS-PAS-HIN-21-001](#)



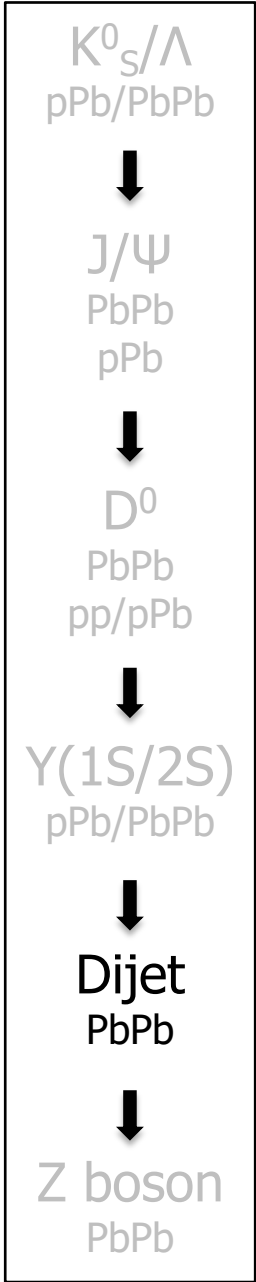
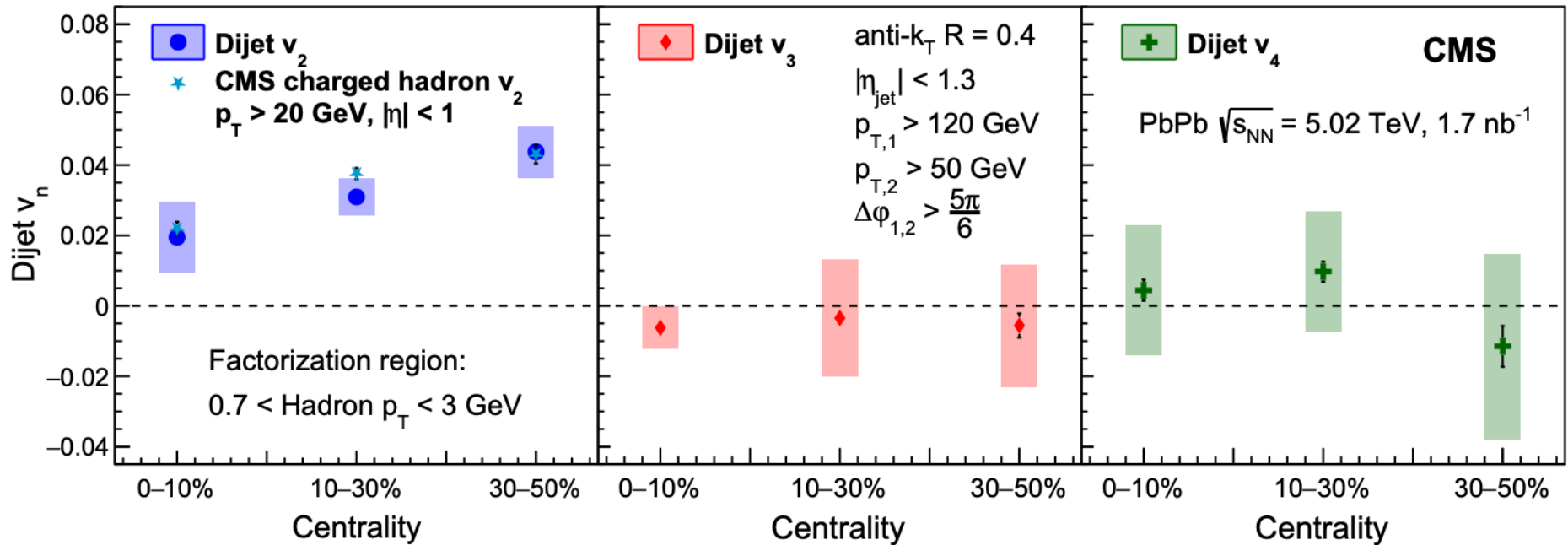
- $v_2$  of Y(1S) and Y(2S) are both consistent with 0 in PbPb
- But non-zero ( $b \rightarrow D^0$ )  $v_2$  in PbPb
- Y(1S)  $v_2$  consistent with 0 in pPb





# DIJET FLOW IN PBPB

CMS-PAS-HIN-21-002

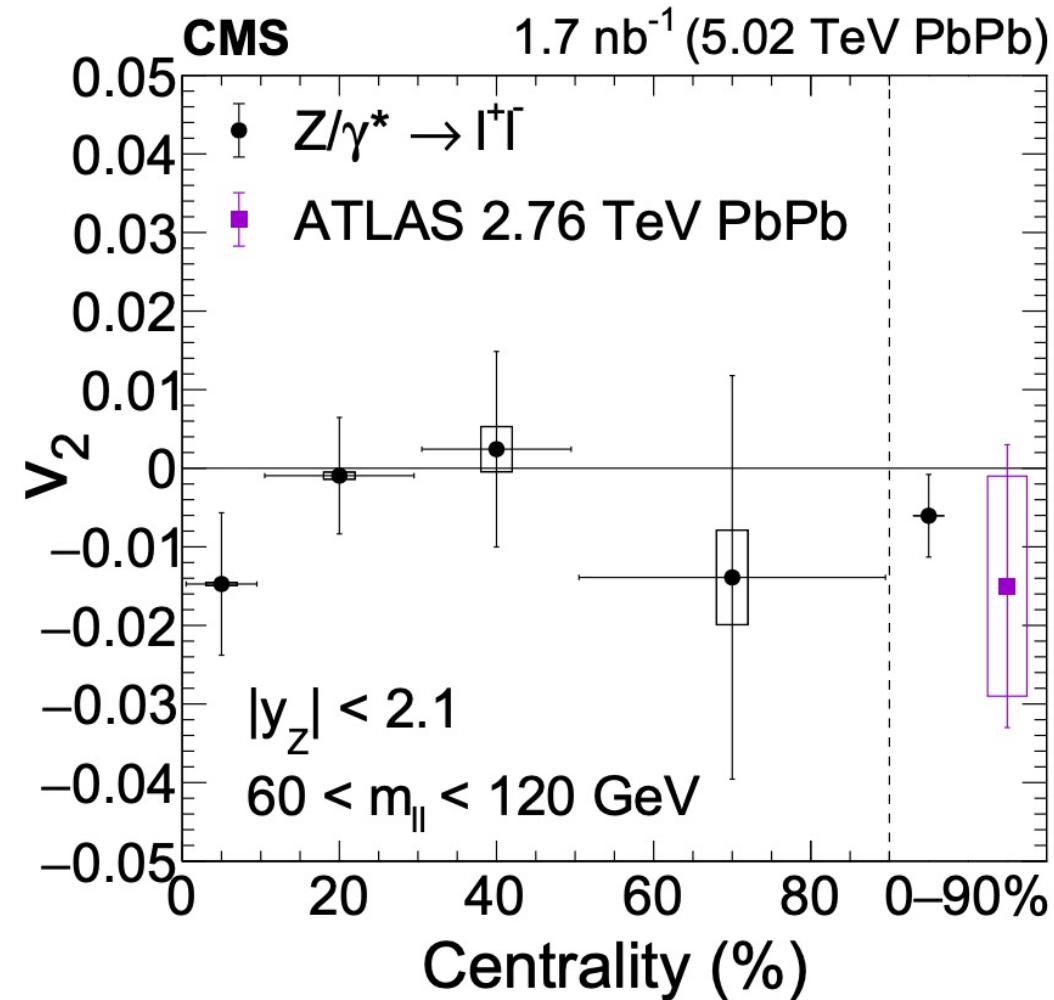


- Significant  $v_2$  for dijet  $\rightarrow$  path length dependence of energy loss
- Dijet  $v_3$  and  $v_4$  are consistent with 0  $\rightarrow$  need better precision to constraint initial state effect

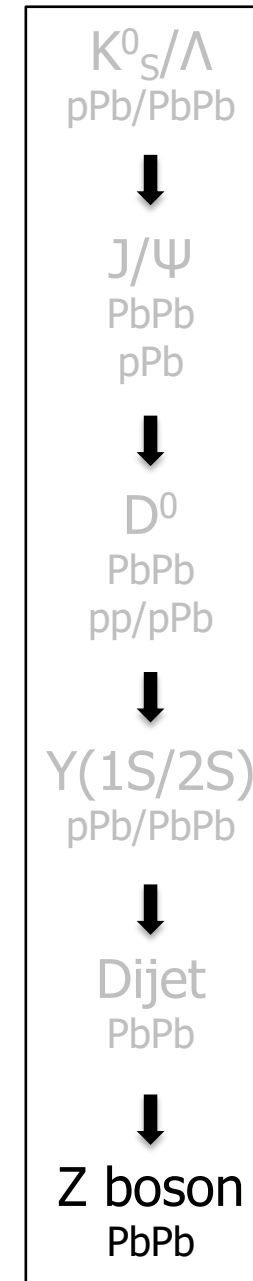


# Z BOSON FLOW IN PBPB

[arXiv:2103.14089](https://arxiv.org/abs/2103.14089)



- $v_2$  is consistent with 0 for Z bosons in PbPb
- Z bosons do not experience significant final-state interactions in the medium



# Summary

Flow measurements in CMS with

- Collision system size scan: PbPb, pPb, pp,  $\gamma$ p collisions
- Particle species scan: Charged hadrons, strange/charm/bottom hadrons, Jets, Z boson

## Do we see flow signals?

	Charged hadron	Strange	Prompt $J/\psi$	$b \rightarrow J/\psi$	Prompt $D^0$	$b \rightarrow D^0$	$Y(1S/2S)$	Dijet	Z boson
PbPb	Yes	Yes	Yes	Yes	Yes	Yes	No	Yes	No
pPb	Yes	Yes	Yes		Yes	No	No		
pp	Yes	Yes			Yes				

- We provided a large amount of data with various methods for different particles

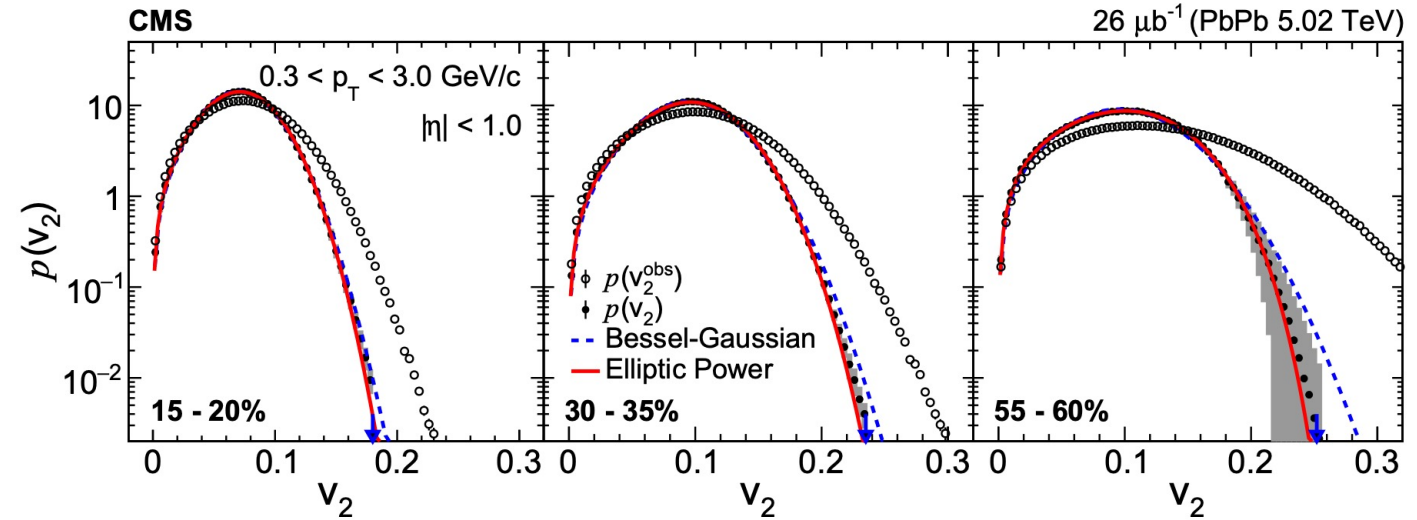
# Challenges and future measurements at CMS

## Two particle correlations

- Peripheral subtraction needed, assumption of no  $v_2$  signal at some low  $N_{ch}$

## Multiparticle particle correlations

- Still affected by **nonflow**, need subevent event method
- 2-sub, 3-sub, 4-sub, ...



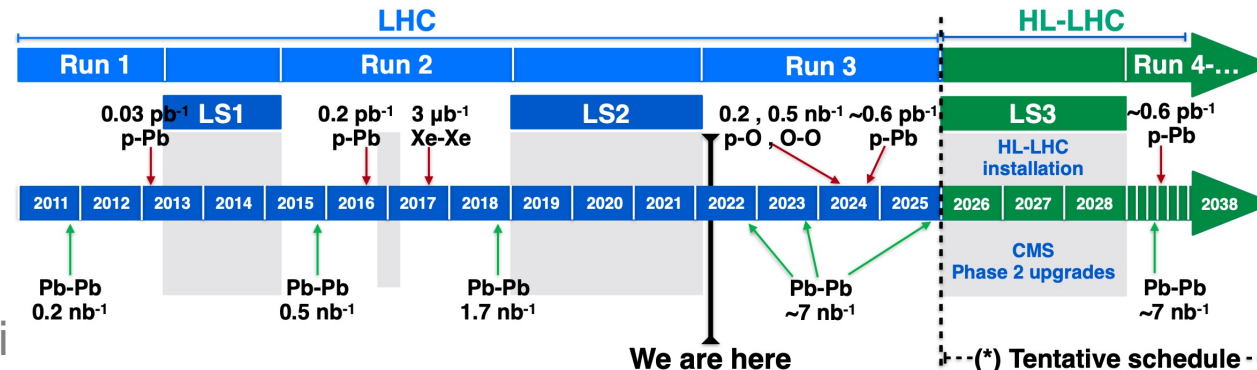
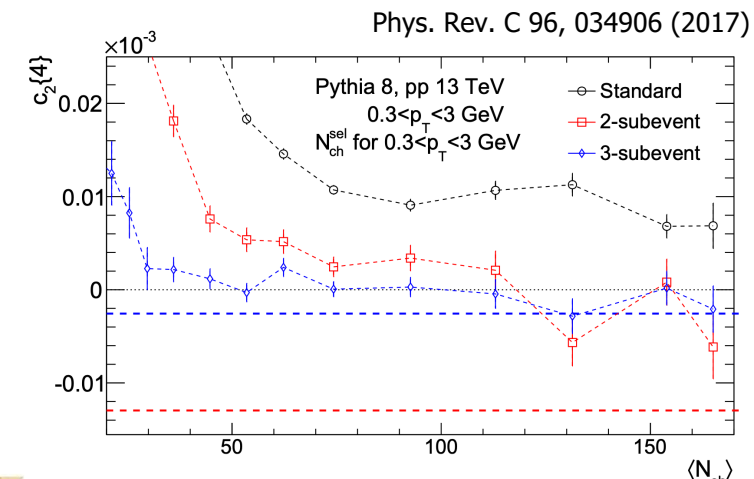
- True  $v_n$  distribution without statistical **fluctuations** not measured yet at small systems
- Challenging for unfolding to work

(a) Three subevents  $\langle\langle 4 \rangle\rangle_{a,a|b,c} \equiv \langle\langle e^{in(\phi_1^a + \phi_2^a - \phi_3^b - \phi_4^c)} \rangle\rangle$

(b) Two subevents  $\langle\langle 4 \rangle\rangle_{a,a|b,b} \equiv \langle\langle e^{in(\phi_1^a + \phi_2^a - \phi_3^b - \phi_4^b)} \rangle\rangle$

## Questions:

- What are properties of QGP?
- What is the smallest possible QGP droplet?
- What are the origin of flow in small systems



## CMS future upgrade

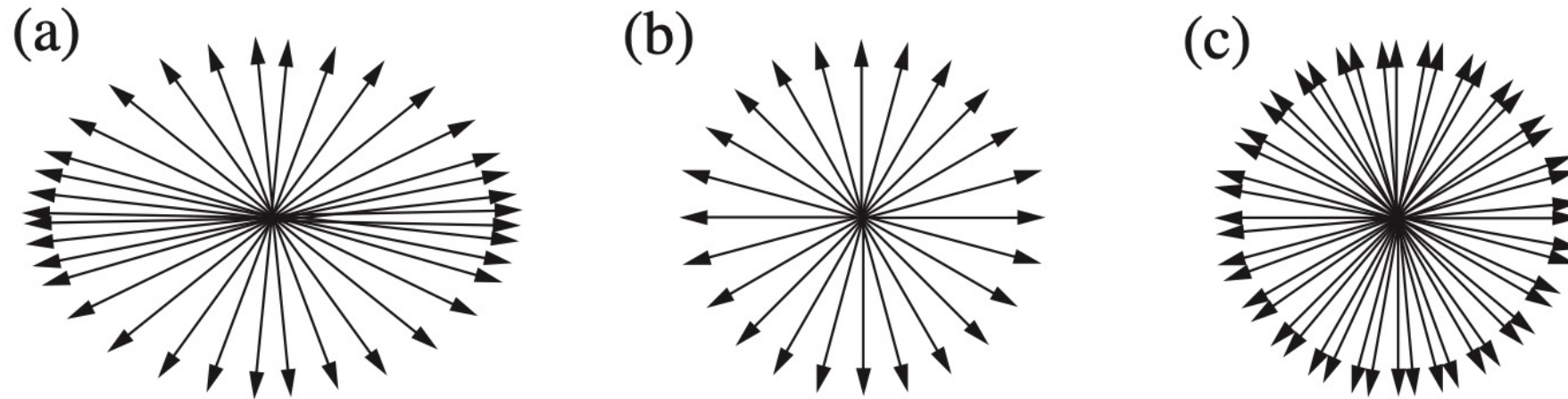
- Particle identification
- Larger  $\eta$  coverage



# Backup



# Nonflow example



The particle distributions in the transverse plane, where for a)  $v_2 > 0, v_2\{2\} > 0$ , b)  $v_2 = 0, v_2\{2\} = 0$ , c)  $v_2 = 0, v_2\{2\} > 0$ .

# Flow fluctuations

$$v\{2\}^2 = \langle v^2 \rangle = \langle v \rangle^2 + \sigma_v^2$$

Neglecting nonflow

$$v\{4\}^2 = \left( 2\langle v^2 \rangle^2 - \langle v^4 \rangle \right)^{1/2}$$

$$\approx \langle v \rangle^2 - \sigma_v^2.$$

Phys.Rev.C80:014904,2009

$$v_2\{4\}^2 \approx \langle v_2 \rangle^2 - \sigma_{v_2}^2$$

When  $\sigma_{v_2}/\langle v_2 \rangle \ll 1$

$$v_2\{2\}^2 - v_2\{4\}^2 \approx \delta_2 + 2\sigma_{v_2}^2$$

Nonflow      Flow fluctuations

$$R_{v(2-4)} = \sqrt{\frac{v_2\{2\}^2 - v_2\{4\}^2}{v_2\{2\}^2 + v_2\{4\}^2}}$$

by setting  $\delta_2 = 0$ .      An upper limit to

$$\sigma_{v_2}/\langle v_2 \rangle$$

$$R_{\varepsilon(2-4)} = \sqrt{\frac{\varepsilon\{2\}^2 - \varepsilon\{4\}^2}{\varepsilon\{2\}^2 + \varepsilon\{4\}^2}}$$

$\sigma_\varepsilon \ll \varepsilon$

$$\sigma_\varepsilon/\langle \varepsilon \rangle$$