

# Experimental overview on $D_{(s)}^+$ purely leptonic decays

**Hailong Ma (IHEP,CAS)**

9<sup>th</sup> International Workshop on the CKM Unitarity Triangle,  
Nov. 28-Dec. 2, 2016, TIFR, Mumbai, India

# Contents

## ■ Introduction

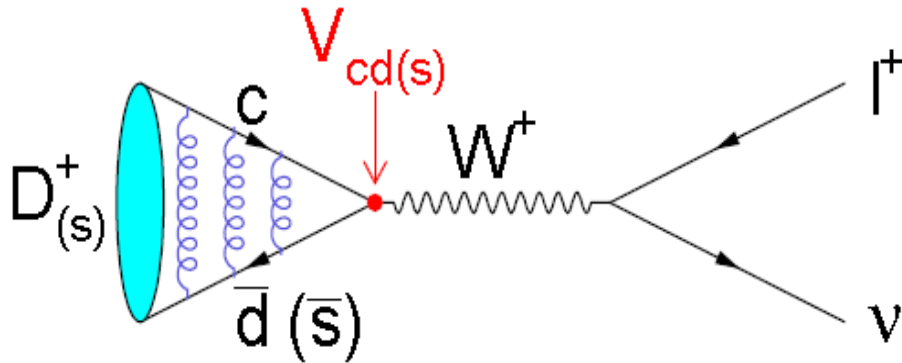
## ■ $D_{(s)}^+ \rightarrow l^+ \nu$

➤ Overview in the past 30 years

➤ Measurement or prospect at BESIII

## ■ Summary

# Introduction



**Leptonic D decays are ideal window to probe for weak and strong effects**

**In the SM:**

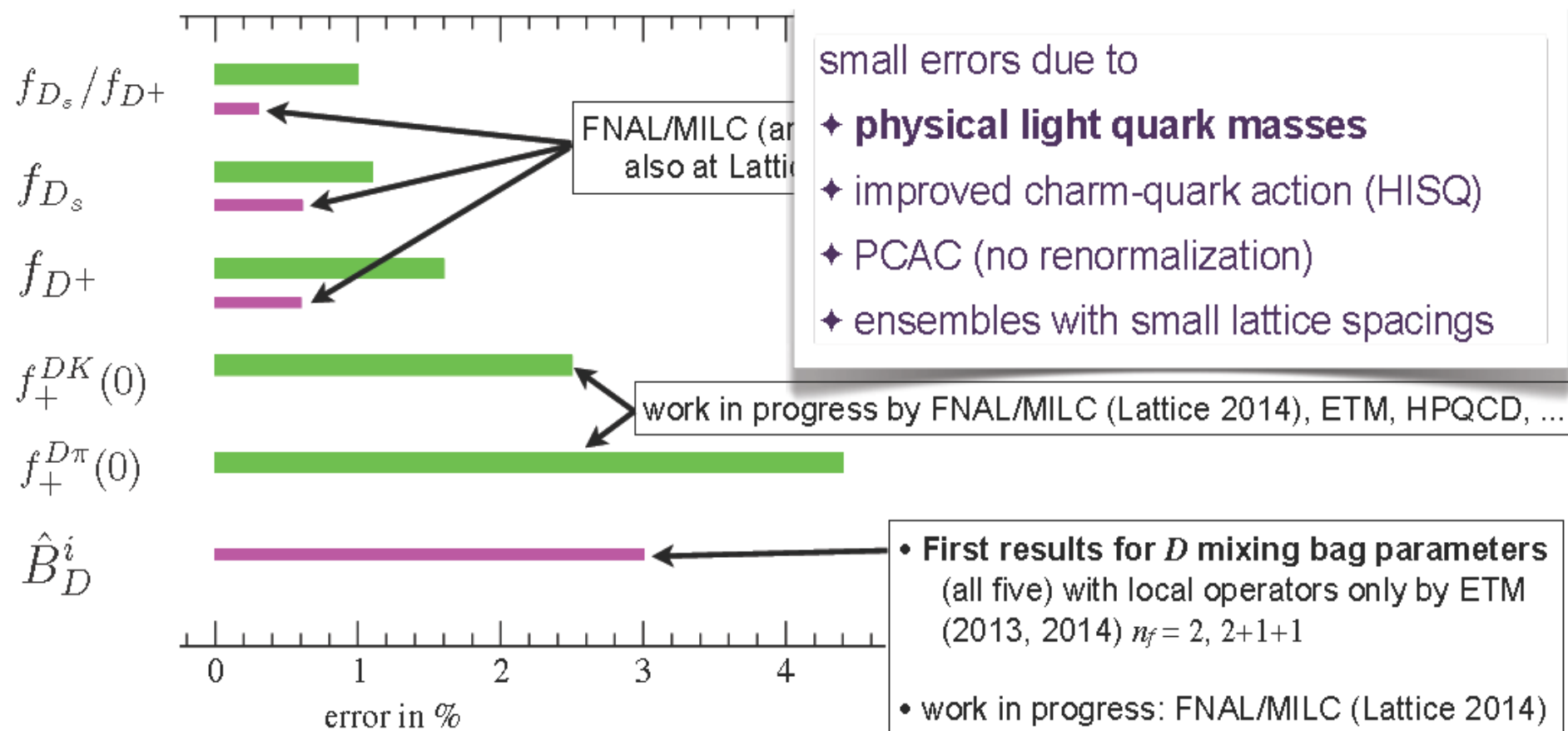
$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

- **Precision measurements of decay constants  $f_{D^+}$ ,  $f_{D_s}$  of D mesons can calibrate LQCD calculations at higher accuracy.** Once they pass experimental tests, the precise LQCD calculations on  $f_D/f_B$ ,  $f_{D_s}/f_{B_s}$  will be helpful for measurements in B decays
- **Recent LQCD calculations on  $f_{D_{(s)}^+}$  [0.5(0.5)%] provide good chance to precisely measure the CKM matrix element  $|V_{cs(d)}|$ , which are important for the unitarity test of the CKM matrix**

# Progress in LQCD Calculation

Taking from Aida X. El-Khadra's talk at Beauty2014

errors (in %) comparison: **FLAG-2 averages** vs. **new results**

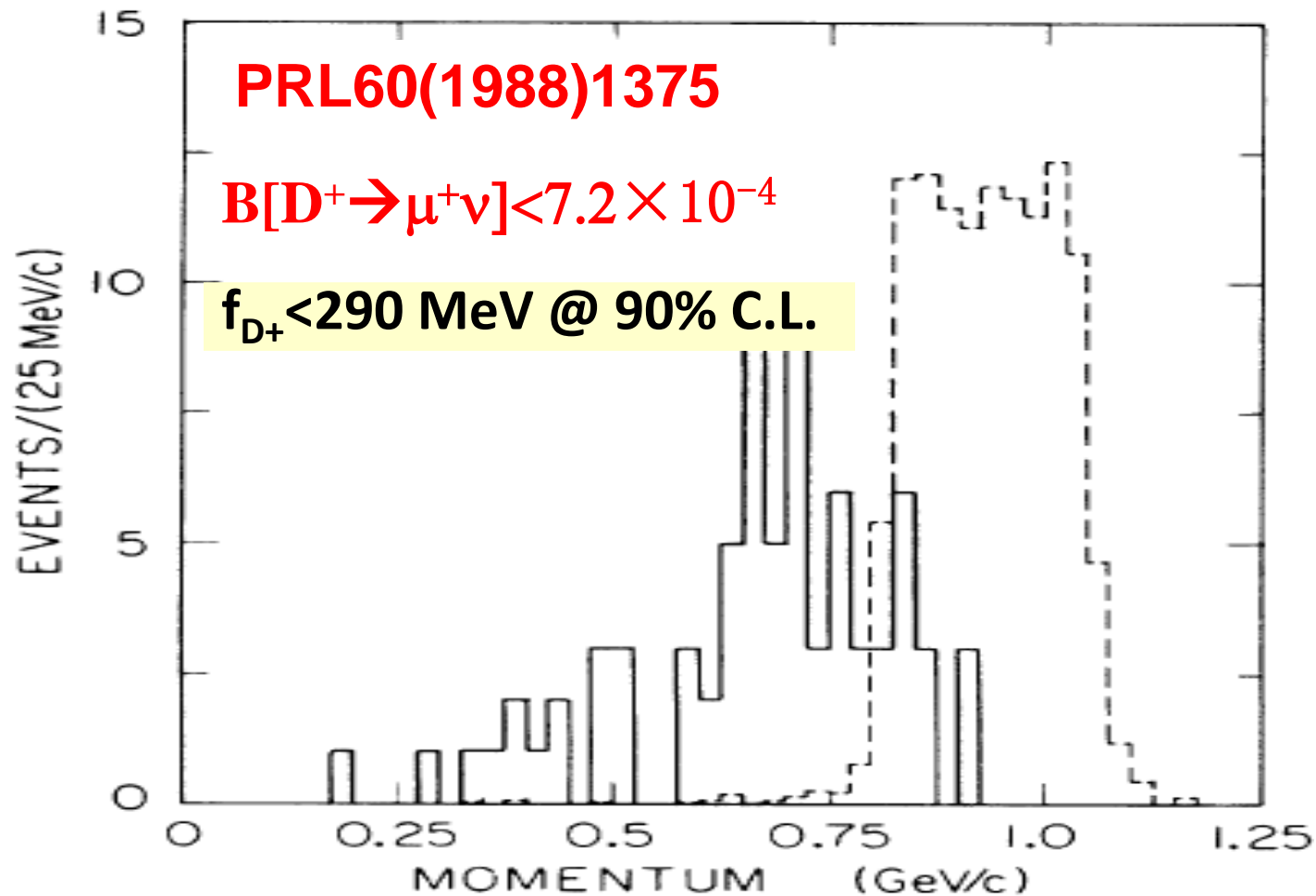


review by C. Bouchard @ Lattice 2014

# Experimental review of $D^+ \rightarrow l^+ \nu$

# No $D^+ \rightarrow \mu^+ \nu$ signal found at Mark-III

9.6 pb<sup>-1</sup> at  $\psi(3770)$



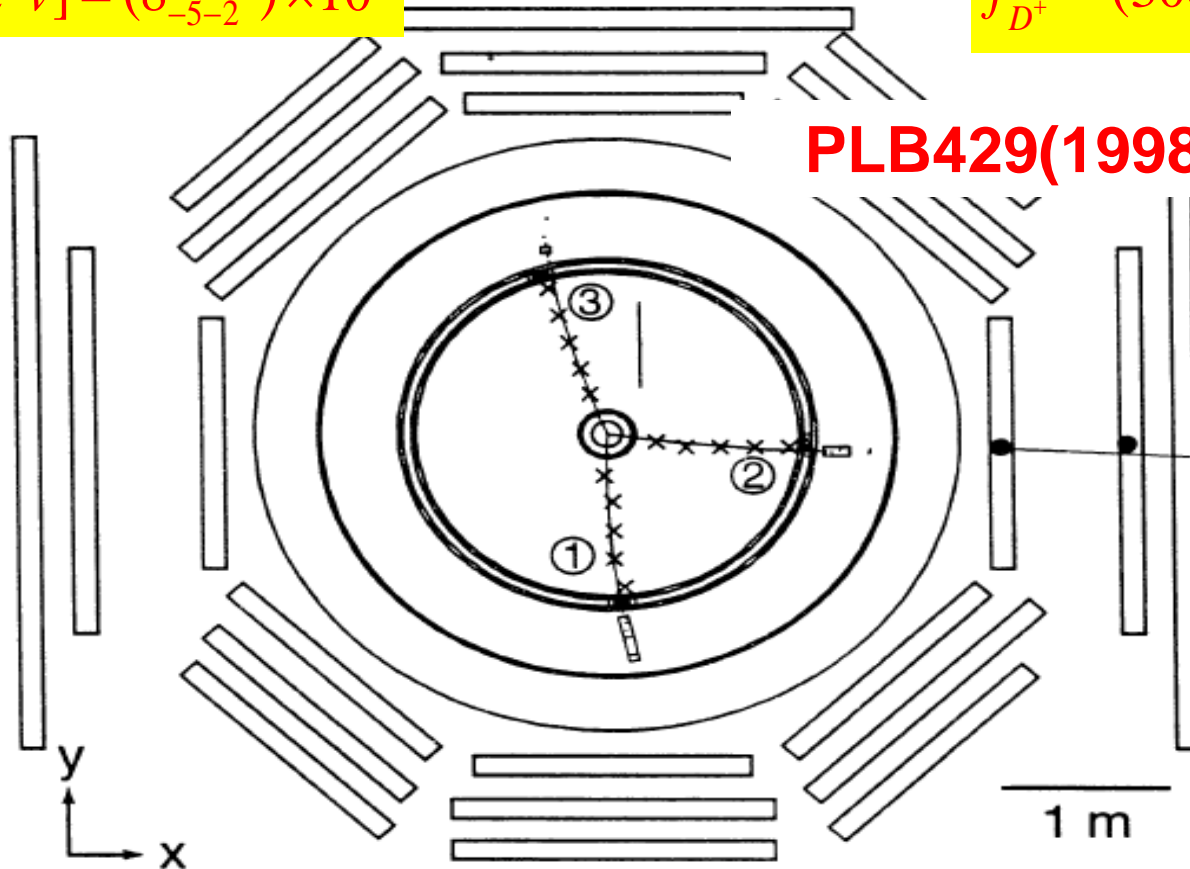
# 1 $D^+ \rightarrow \mu^+ \nu$ signal found at BES-I

22.3 pb<sup>-1</sup> at 4.03 GeV

$$B[D^+ \rightarrow \mu^+ \nu] = (8_{-5-2}^{+16+5}) \times 10^{-4}$$

$$f_{D^+} = (300_{-150-40}^{+180+80}) \text{ MeV}$$

PLB429(1998)188

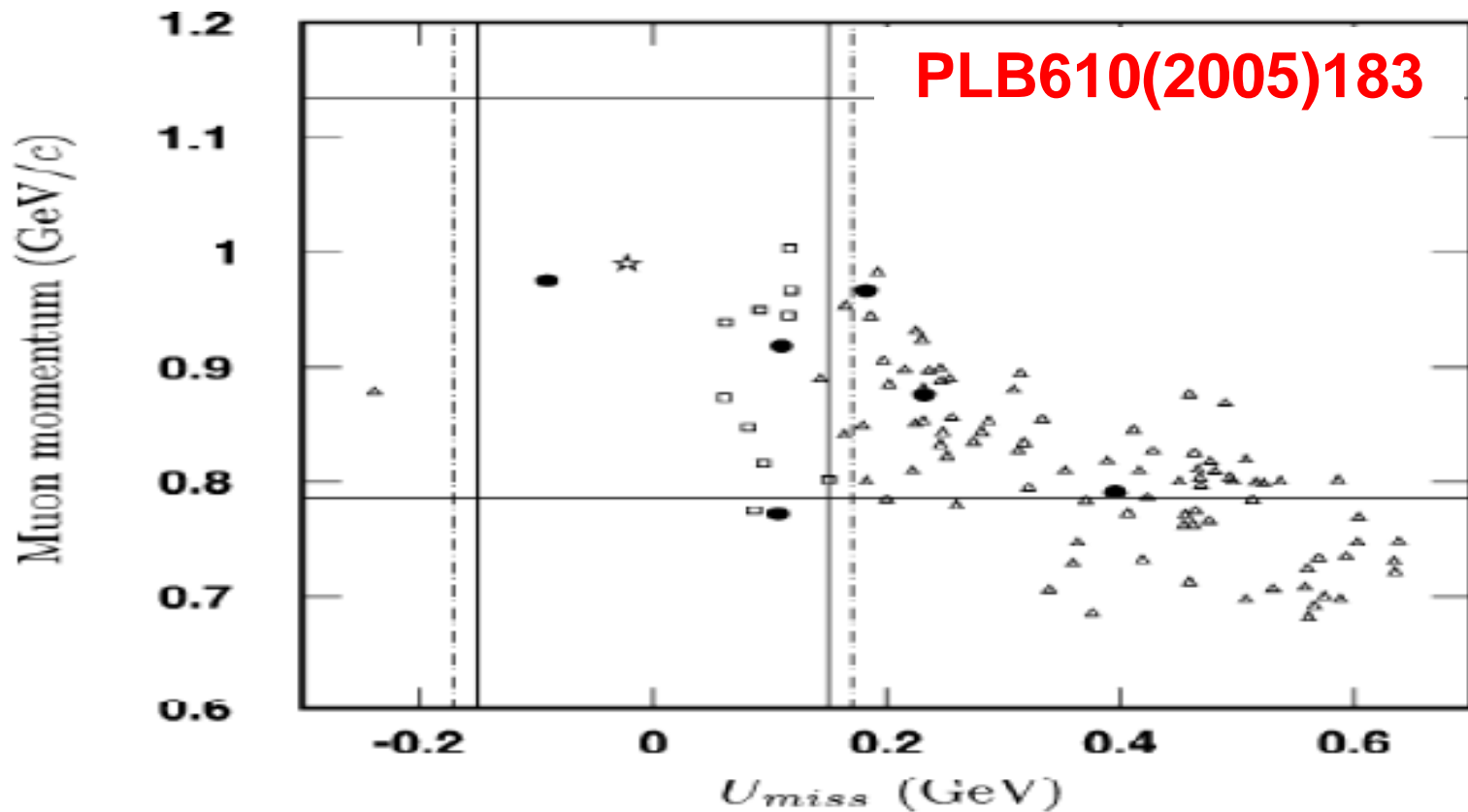


# 2.7 $D^+ \rightarrow \mu^+ \nu$ signals found at BES-II

33  $\text{pb}^{-1}$  around  $\psi(3770)$

$$B[D^+ \rightarrow \mu^+ \nu] = (12.2_{-5.3}^{+11.1} \pm 1.0) \times 10^{-4}$$

$$f_{D^+} = (371_{-119}^{+129} \pm 25) \text{ MeV}$$



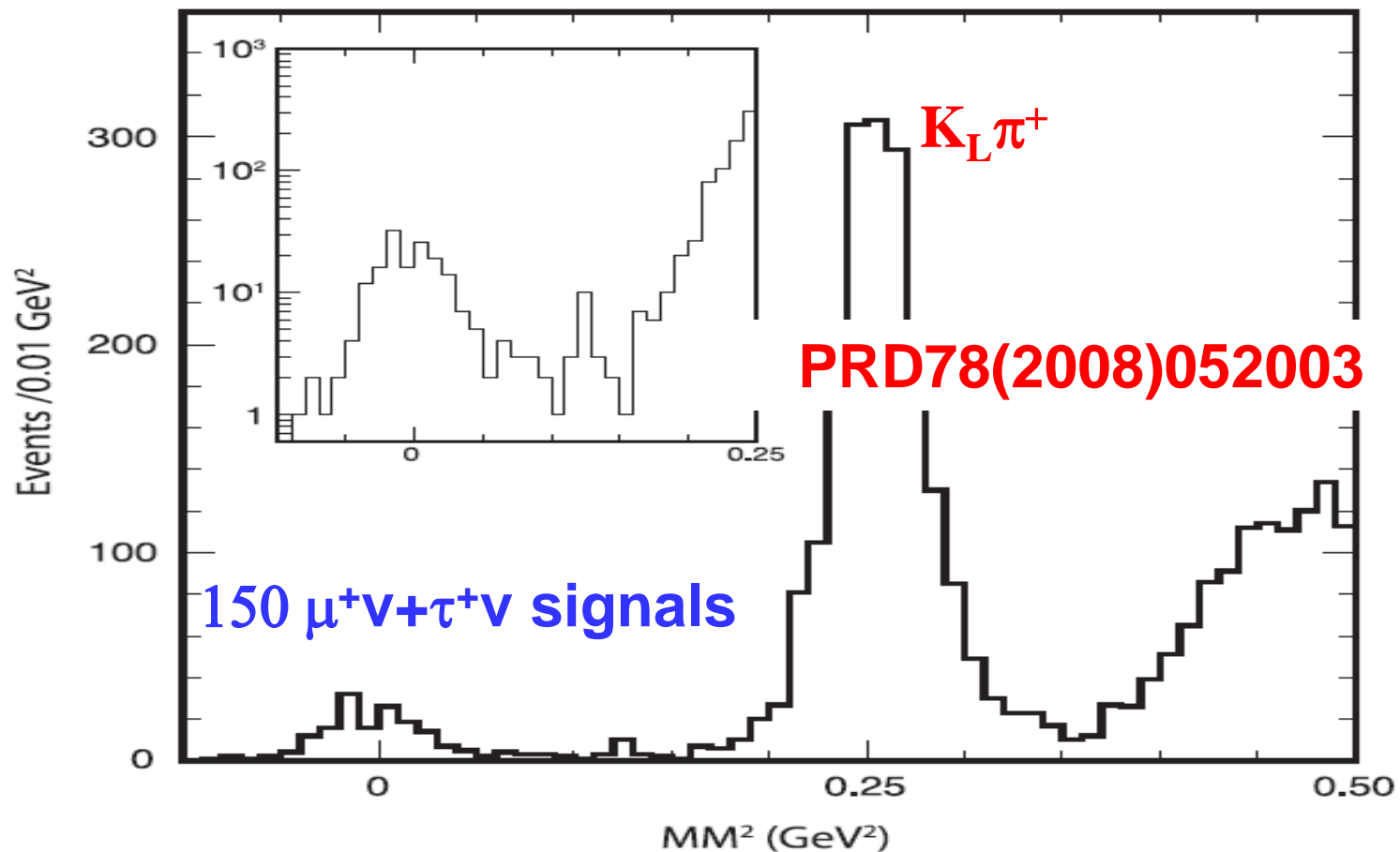


# Measurements at CLEO-c

818 pb<sup>-1</sup> around  $\psi(3770)$  (2004–2008)

$$B[D^+ \rightarrow \mu^+ \nu] = (3.82 \pm 0.32 \pm 0.09) \times 10^{-4}$$

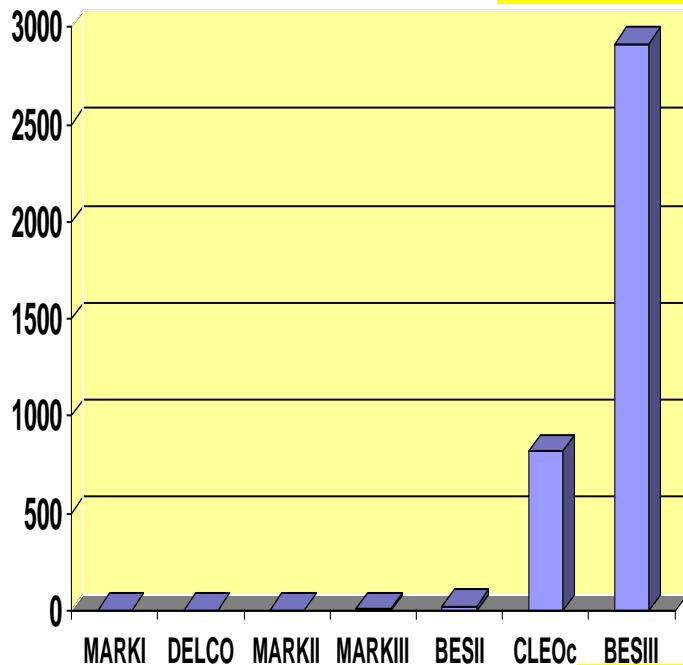
$$f_{D^+} = 205.8 \pm 7.5 \pm 2.5 \text{ MeV}$$



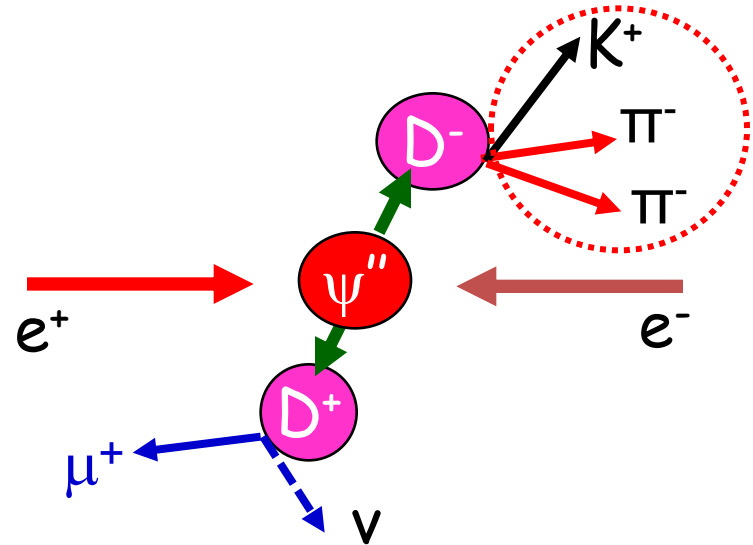
# D<sup>+</sup> sample at BESIII

2.93 fb<sup>-1</sup> data were taken at  $\psi(3770)$

2010.1-2011.5



3.6×CLEOc

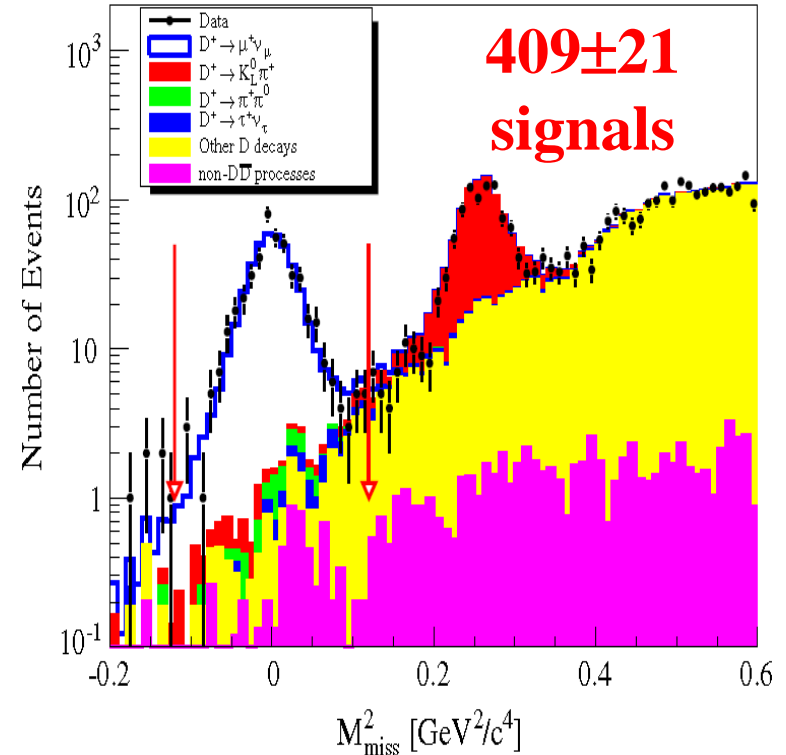
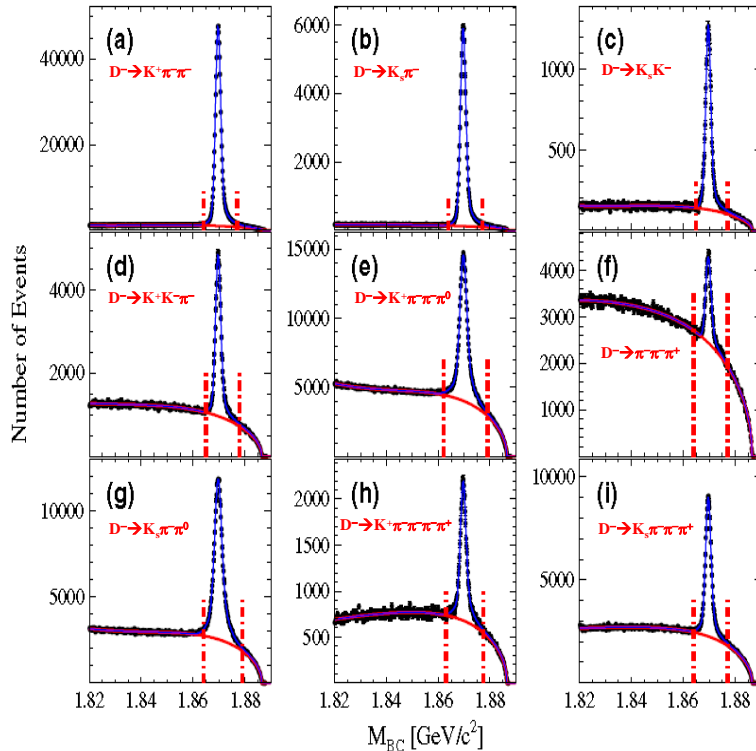


At the recoil side of singly tagged D<sup>-</sup> mesons, Leptonic decays can be studied

# Improved $B[D^+ \rightarrow \mu^+ \nu]$ , $f_{D^+}$ and $|V_{cd}|$ at BESIII

$\psi(3770) \rightarrow D^+ D^-$

PRD89(2014)051104R



$$N_{D_{\text{tag}}} = (170.31 \pm 0.34) \times 10^4$$

$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

Input  $\tau_{D^+}$ ,  $m_{D^+}$ ,  $m_{\mu^+}$  on PDG  
and  $|V_{cd}|$  of CKM-Fitter

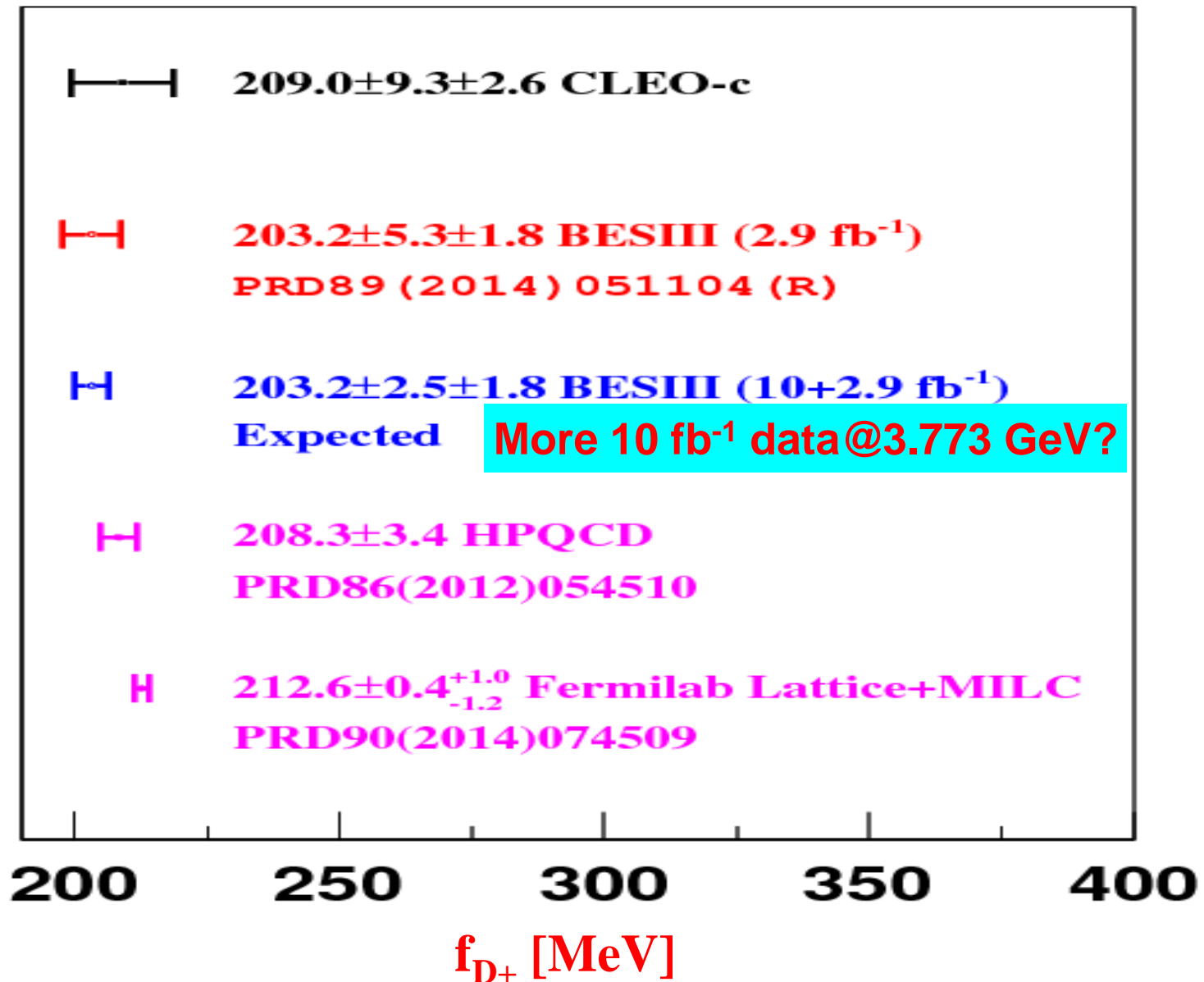
BES III

Input  $\tau_{D^+}$ ,  $m_{D^+}$ ,  $m_{\mu^+}$  on PDG and  
LQCD calculated  $f_{D^+} = 207 \pm 4$   
MeV [PRL100(2008)062002]

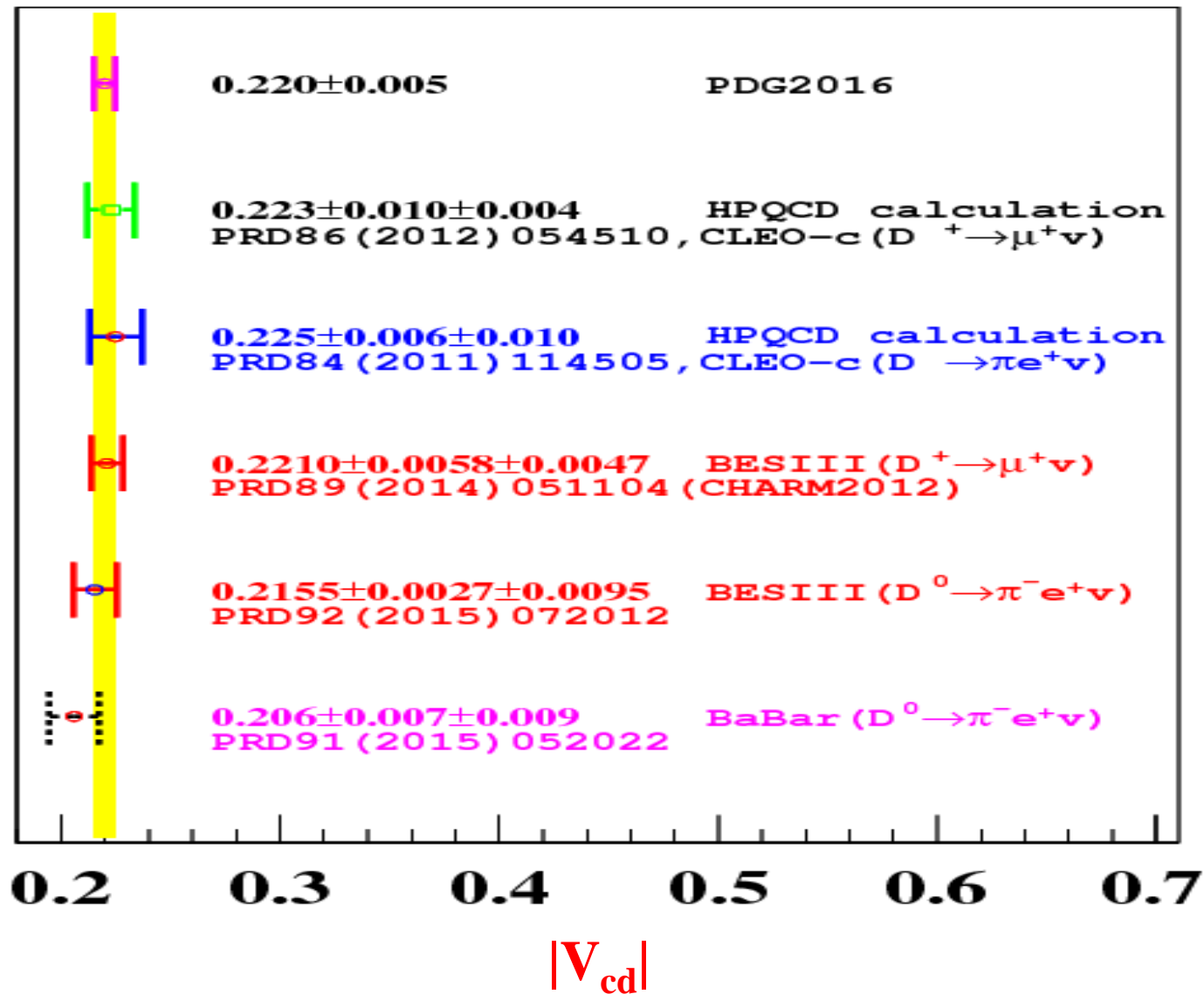
$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

# Comparison of $f_{D^+}$



# Comparison of $|V_{cd}|$



# Search for $D^+ \rightarrow \tau^+ \nu$ at BESIII

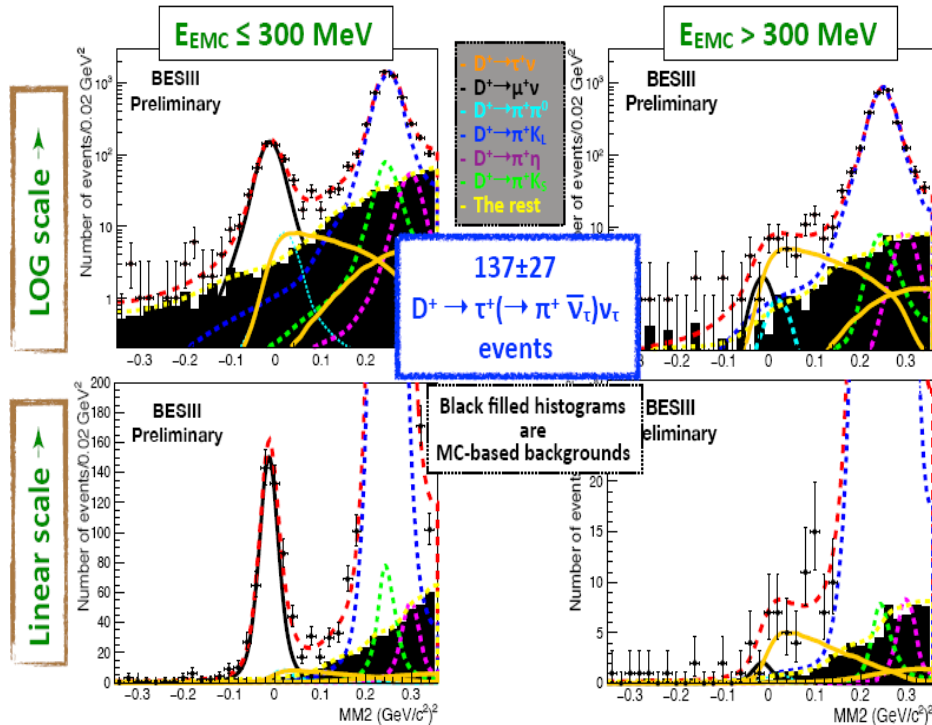
$$R \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D^+}^2}\right)^2}$$

- With the known masses,  $R = 2.67 \pm 0.01$  (very small uncertainty!).
  - Based on the previously measured  $\text{BF}(D^+ \rightarrow \mu^+ \nu_\mu) = (3.74 \pm 0.17) \times 10^{-4}$ , expect  $\text{BF}(D^+ \rightarrow \tau^+ \nu_\tau) = (9.99 \pm 0.45) \times 10^{-4}$ .  
CLEO was very close ( $< 1.2 \times 10^{-3}$  @ 90% C.L.) w/  $0.818 \text{ fb}^{-1}$  data.
  - Requirements are very similar to PRD 89, 051104 (R) (2014).  
Notable differences are listed below.
  - Tag side:
    - ▶ 6 tag modes:  $D^+ \rightarrow K \pi^+ \pi^-, K \pi^+ \pi^+ \pi^0, K_S \pi^+, K_S \pi^+ \pi^0, K_S \pi^+ \pi^+ \pi^-, K K^+ \pi^+$ ,  
where  $K_S \rightarrow \pi^+ \pi^-$  and  $\pi^0 \rightarrow \gamma \gamma$ .
  - Signal side:
    - ▶ No PID on the signal charged track.
    - ▶ The missing momentum (representing the neutrino(s) for a signal event) not in beam direction.
    - ▶ The most energetic neutral EMC shower (i.e., not matched to the charged track) not aligned with the missing momentum.
- ==> With the all requirements, signal efficiency  $\sim 72\%$ .  
The last two requirements suppress backgrounds from  $D^+ \rightarrow K_L \pi^+$  and  $D^+ \rightarrow \pi^0 \pi^+$  in the signal region of MM2.

# Search for $D^+ \rightarrow \tau^+ \nu$ at BESIII

11

## Fitting to DATA

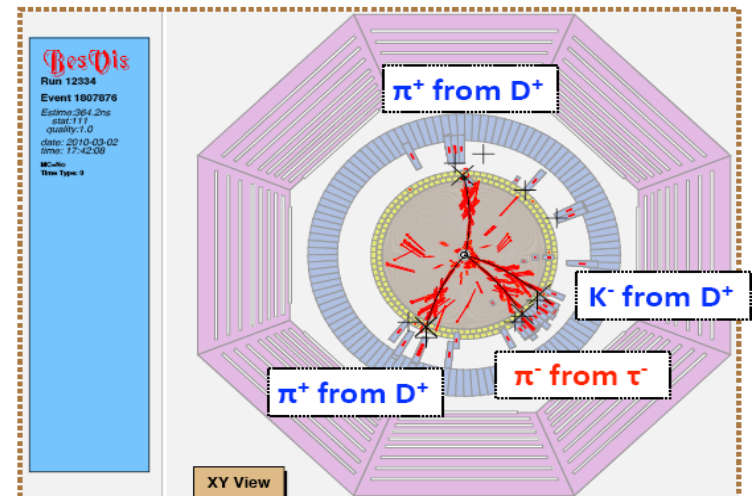


## Preliminary Result

- $137 \pm 27 D^+ \rightarrow \tau^+(\rightarrow \pi^+ \bar{\nu}_\tau) \nu_\tau$  events.
- $> 4\sigma$  statistical significance. **First evidence!**
- $BF(D^+ \rightarrow \tau^+ \nu_\tau) = [1.20 \pm 0.24(\text{stat.})] \times 10^{-3}$ .
- $R = 3.21 \pm 0.64$  consistent with the SM prediction,  $R = 2.66 \pm 0.01$ , within  $\sim 0.9\sigma$ .

## (un-binned maximum likelihood fit)

- Fix the  $D^+ \rightarrow \mu^+ \nu$  component based on the world average. Float it in our systematic check.
- Float  $D^+ \rightarrow \tau^+(\rightarrow \text{generic decays}) \nu_\tau$  component. (our signal efficiency is still for  $D^+ \rightarrow \tau^+(\rightarrow \pi^+ \bar{\nu}_\tau) \nu_\tau$  events)
- Peaking backgrounds:
  - $D^+ \rightarrow K_L \pi^+$  : Large: Float its normalization.
  - $D^+ \rightarrow K_S \pi^+$  : Small: Fix its size based on the PDG.
  - $D^+ \rightarrow \pi^0 \pi^+$  : Small: Fix its size based on the PDG.
  - $D^+ \rightarrow \eta \pi^+$  : Small: Fix its size based on the PDG.
- The rest of the background (relatively smooth): Fix its shape based on MC (in the nominal fit only) and float its normalization.
- All shapes are MC-based (KeysPDF), convoluted with a common single Gaussian (the mean and the width of this Gaussian are floated).



# Experimental studies of $D_s^+ \rightarrow l^+ \nu$

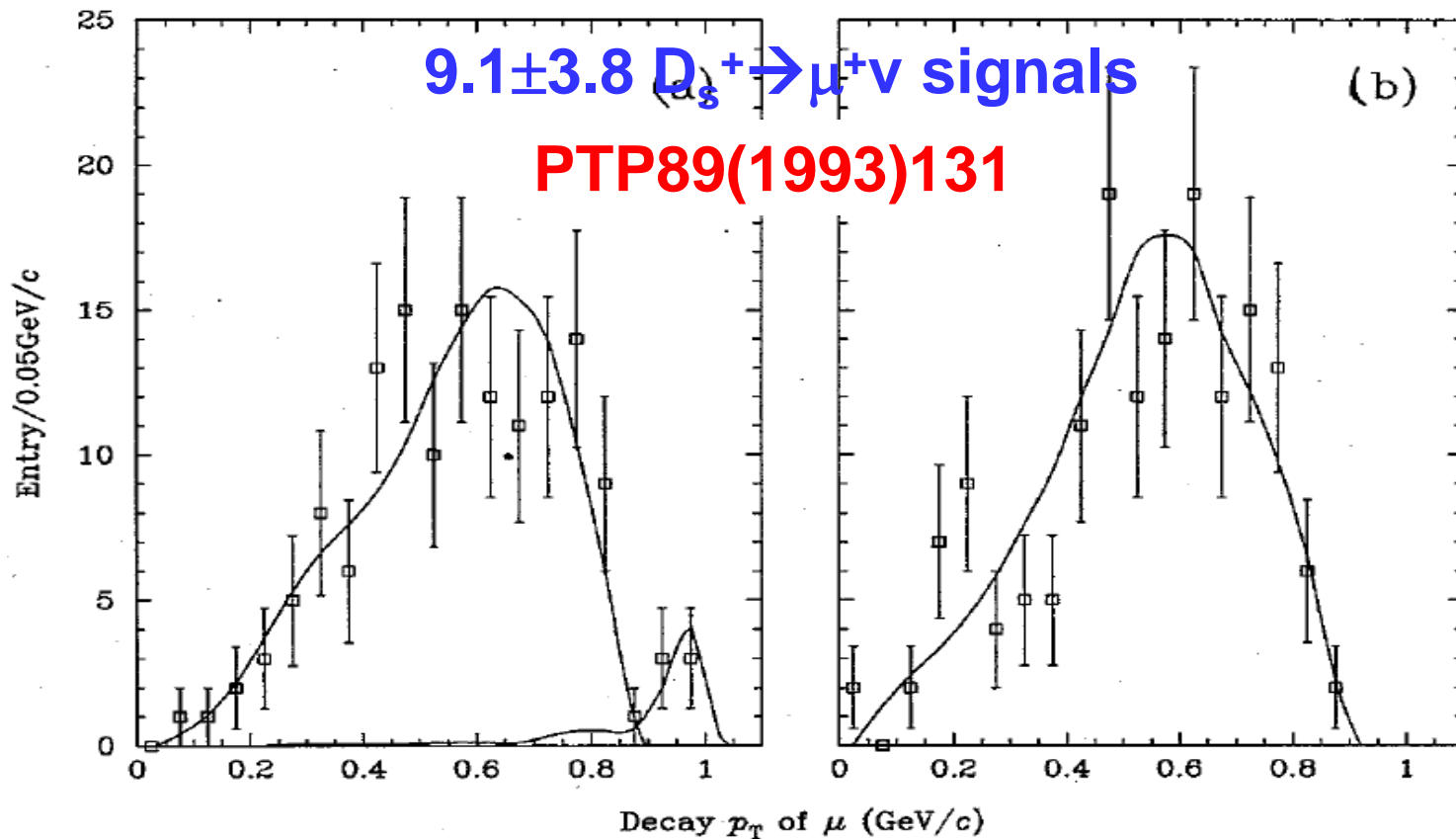


# Measurement at WA75

Fixed target experiment

$$B[D_s^+ \rightarrow \mu^+ \nu] = (4.0_{-1.4-0.6}^{+1.8+0.8} \pm 1.7) \times 10^{-3}$$

$$f_{D_{s^+}} = 232 \pm 45 \pm 20 \pm 48 \text{ MeV}$$

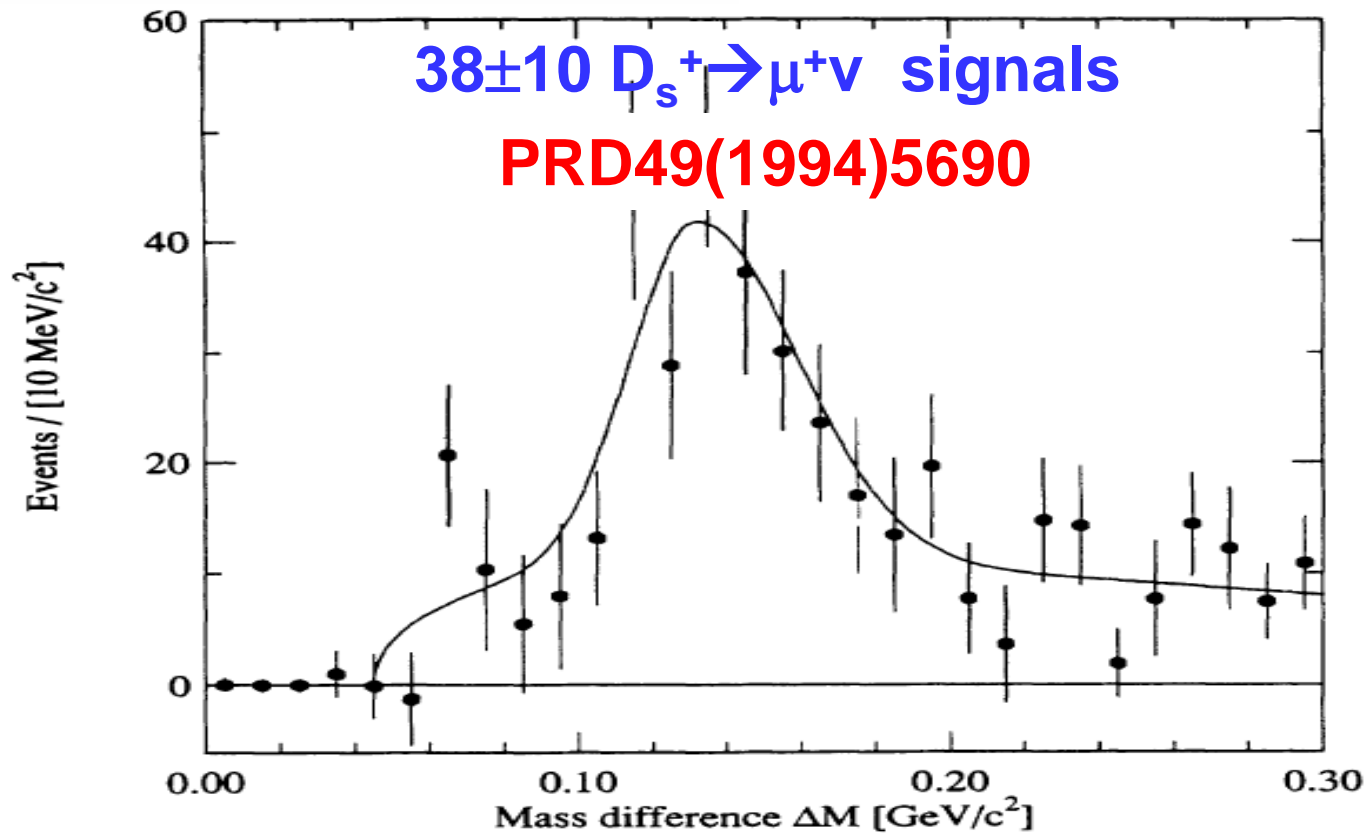


# Measurement at CLEOII

2.13 fb<sup>-1</sup> at 10.6 GeV

$$\frac{\Gamma(D_s^+ \rightarrow \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)} = 0.245 \pm 0.052 \pm 0.074$$

$$f_{D_{s^+}} = 344 \pm 37 \pm 52 \pm 42 \text{ MeV}$$

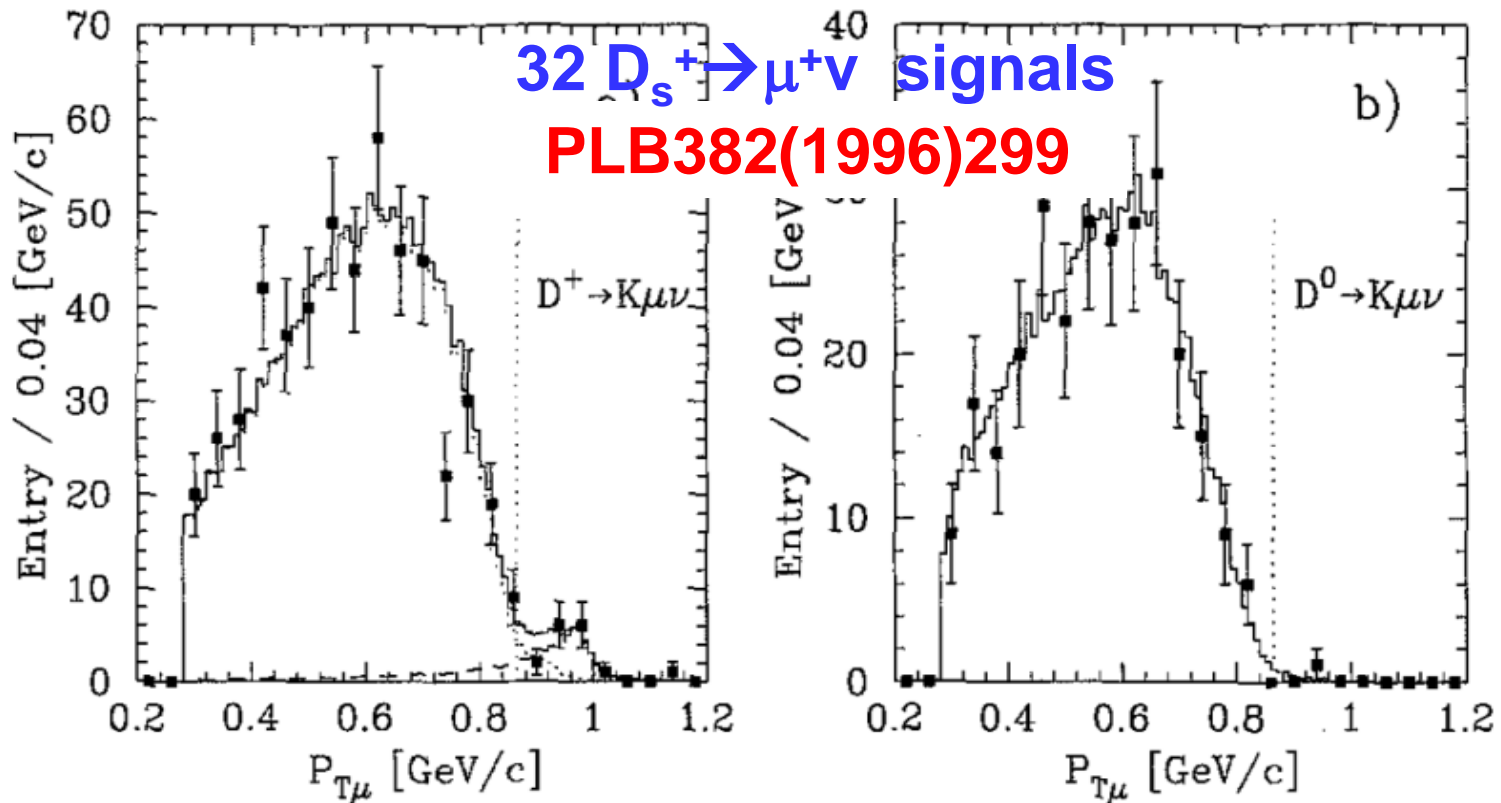


# Measurement at E653

Fermilab fixed target experiment

$$B[D_s^+ \rightarrow \mu^+ \nu] = (3.0 \pm 1.2 \pm 0.6 \pm 0.5) \times 10^{-3}$$

$$f_{D_{s^+}} = 194 \pm 35 \pm 20 \pm 14 \text{ MeV}$$

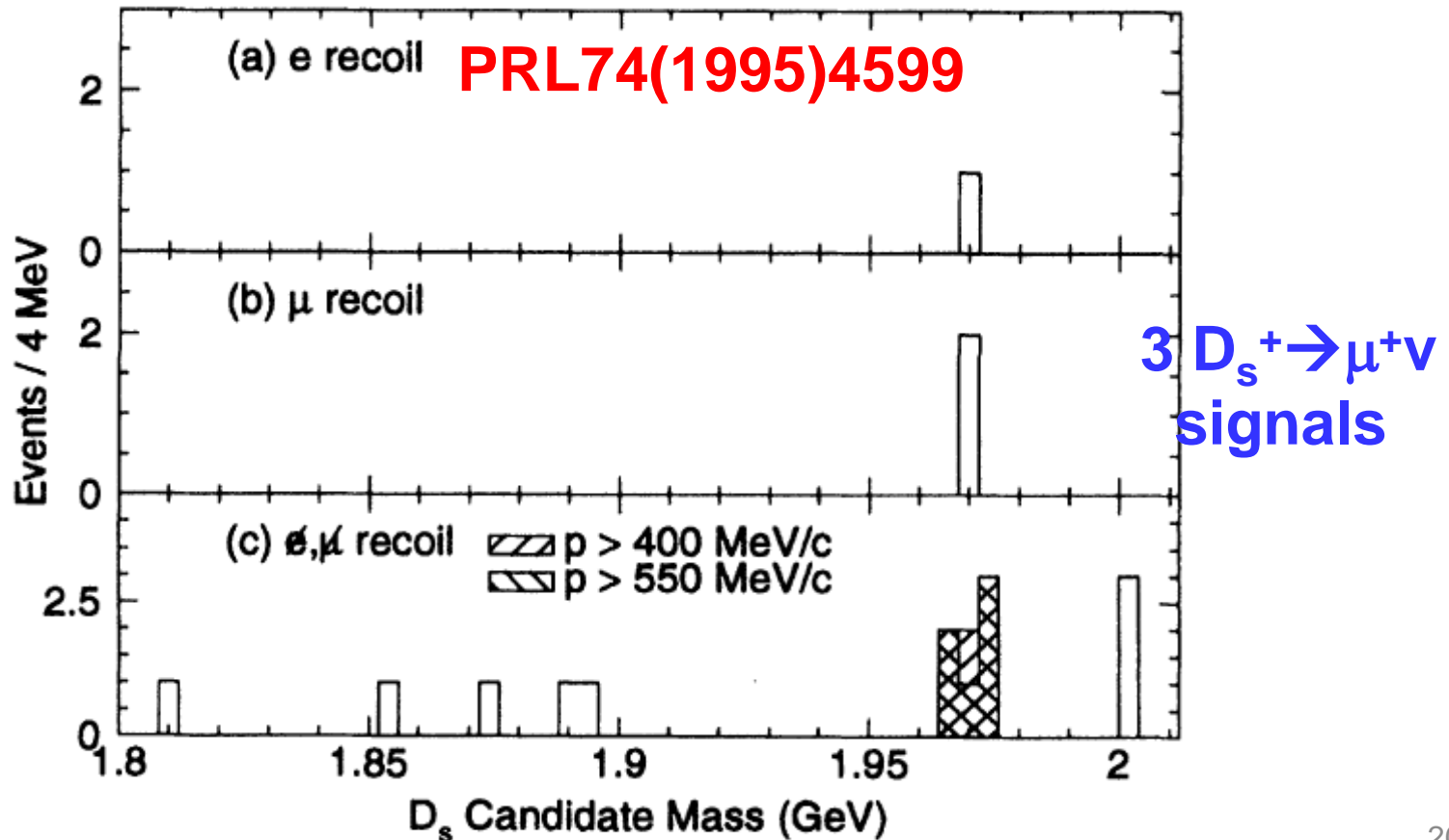


# First absolute measurement from BES-I

22.3 pb<sup>-1</sup> at 4.03 GeV

$$B[D_s^+ \rightarrow \mu^+ \nu] = (1.5_{-0.6-0.2}^{+1.3+0.3}) \%$$

$$f_{D_s^+} = (430_{-130-40}^{+150+40}) \text{ MeV}$$

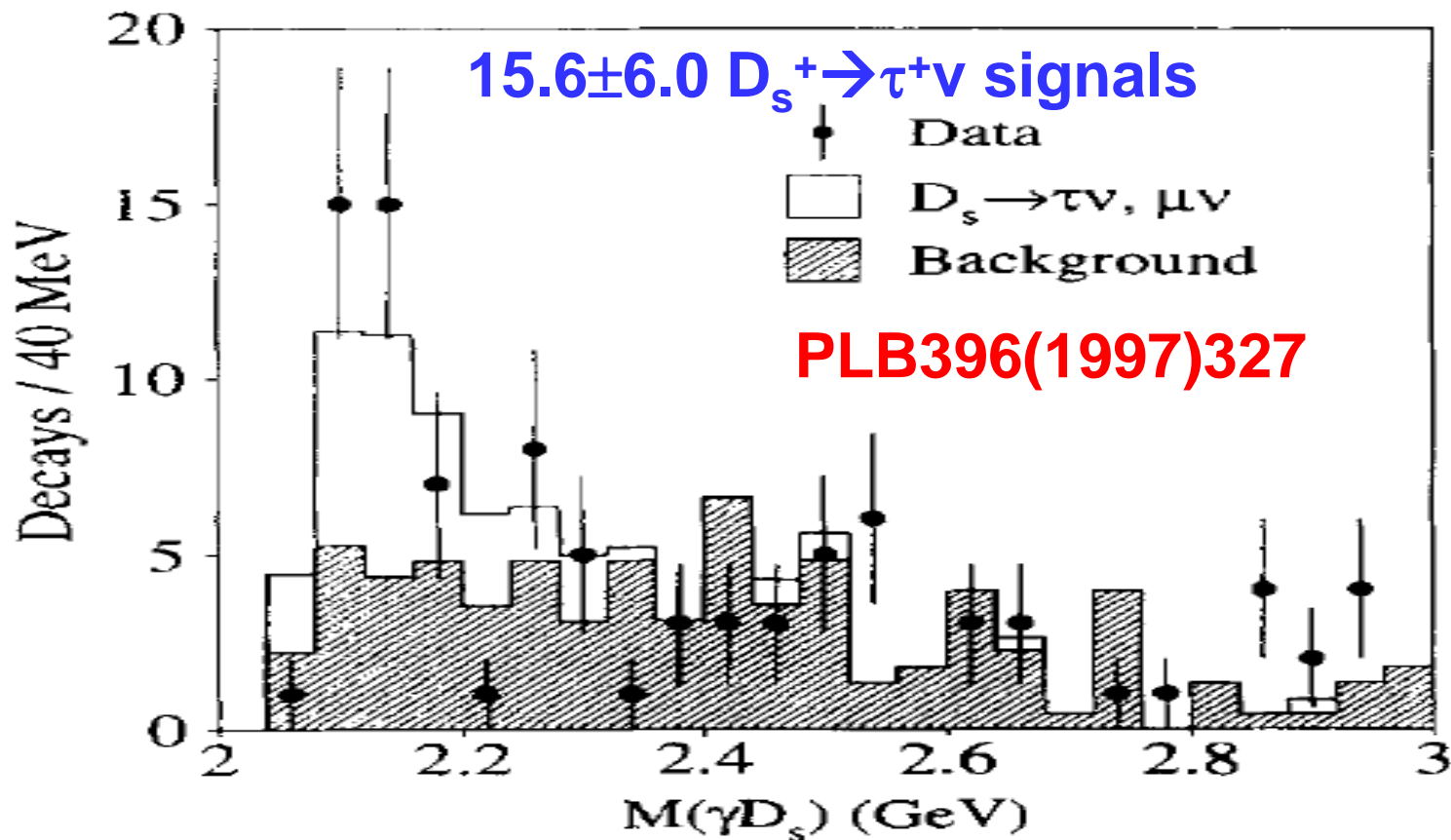


# Measurement at L3

$Z \rightarrow q\bar{q}$ ,  $49.6 \text{ pb}^{-1}$  at 91.2 GeV

$$B[D_s^+ \rightarrow \tau^+ \nu] = (7.4 \pm 2.8 \pm 1.6 \pm 1.8)\%$$

$$f_{D_s^+} = 309 \pm 58 \pm 33 \pm 38 \text{ MeV}$$

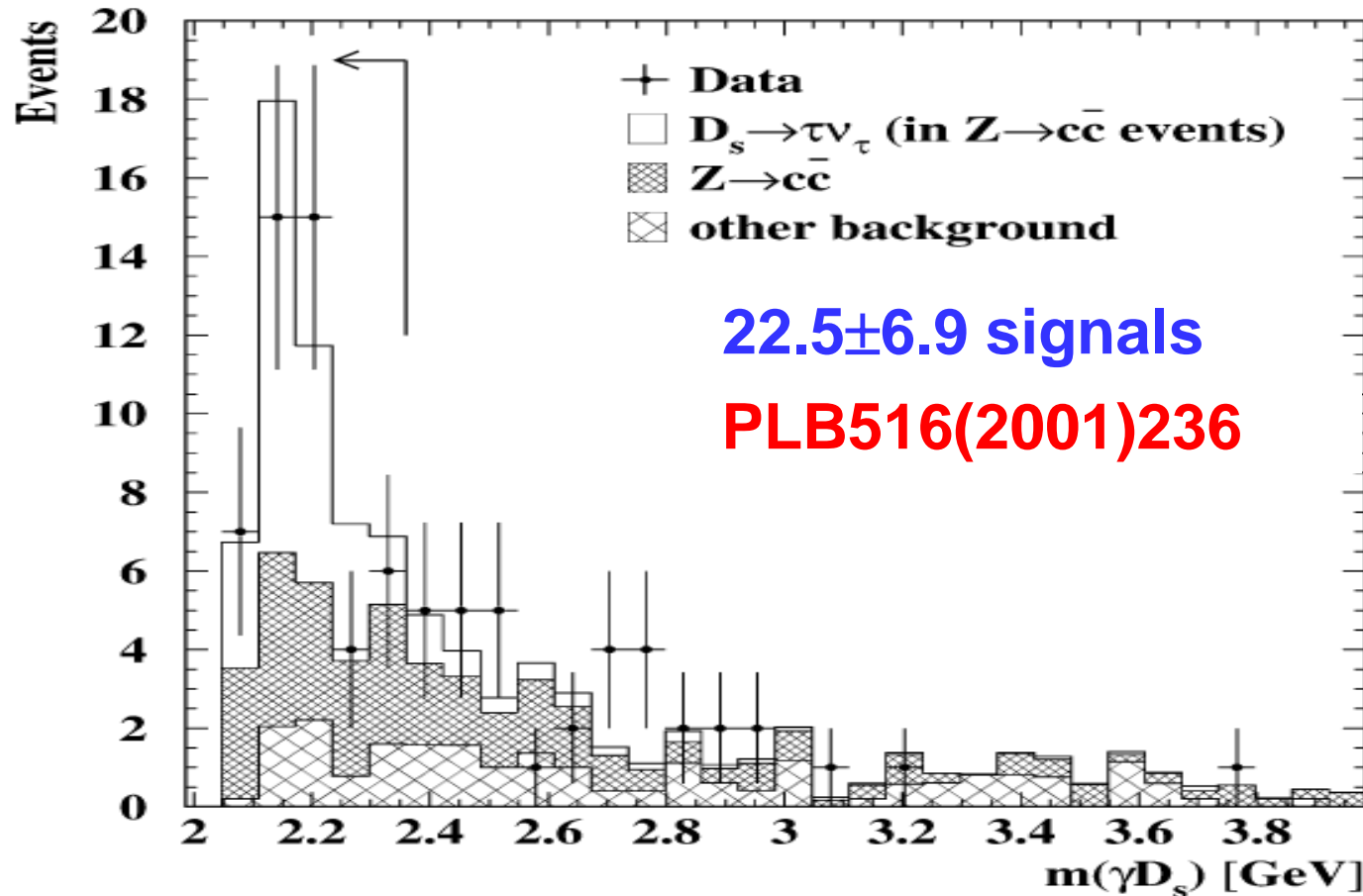


# Measurement at OPAL

$3.9 \times 10^6 Z \rightarrow q\bar{q}$

$B[D_s^+ \rightarrow \tau^+ \nu] = (7.1 \pm 2.1 \pm 2.0)\%$

$f_{D_s^+} = 286 \pm 44 \pm 41 \text{ MeV}$



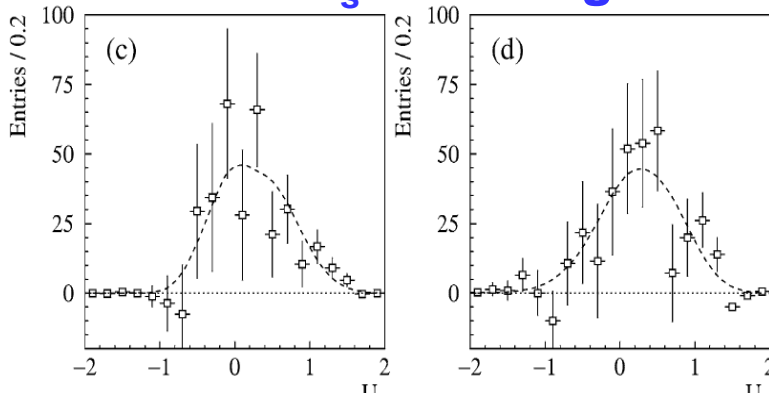
# Measurement at ALPHA

$3.96 \times 10^6$  Z hadronic decays

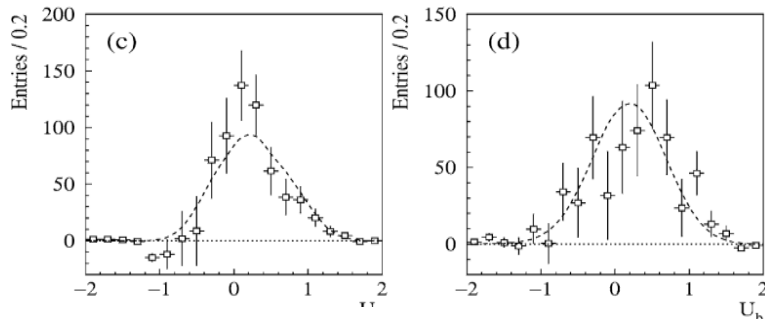
$$f_{D_{s^+}} = 285 \pm 19 \pm 40 \text{ MeV}$$

$$B[D_{s^+} \rightarrow \mu^+ \nu] = (0.47 \pm 0.25) \times 10^{-3}$$
$$B[D_{s^+} \rightarrow \tau^+ \nu] = (5.79 \pm 0.77 \pm 1.84)\%$$

$306 \pm 62$   $D_{s^+} \rightarrow \tau^+ \nu$  signals

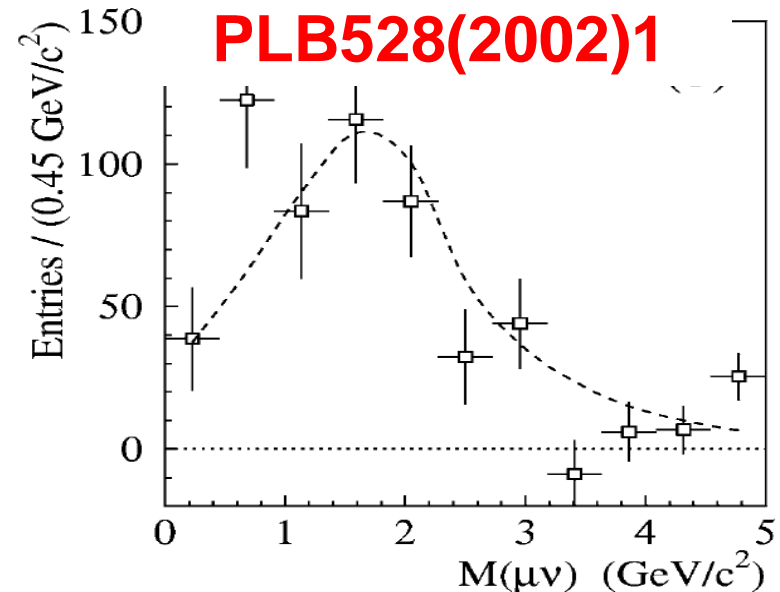


Electron channel



Muon channel

$575 \pm 84$   $D_{s^+} \rightarrow \mu^+ \nu$  signals



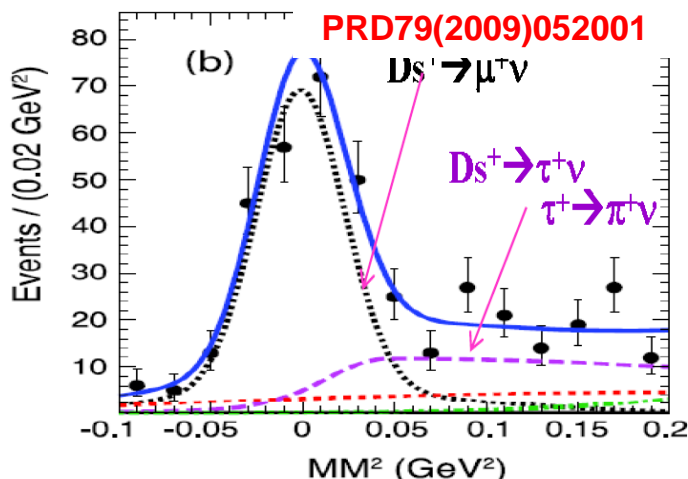
# Absolute measurements at CLEO-c

$D_s^{*+}D_s^-$ , 600 pb<sup>-1</sup> @ 4.17 GeV

Absolute measurement gives significantly improved statistical and systematic errors [697 signal]

235±14  $D_s^+ \rightarrow \mu^+ \nu + \tau^+ \nu$  signals

126±16  $D_s^+ \rightarrow \tau^+ \nu$  signals

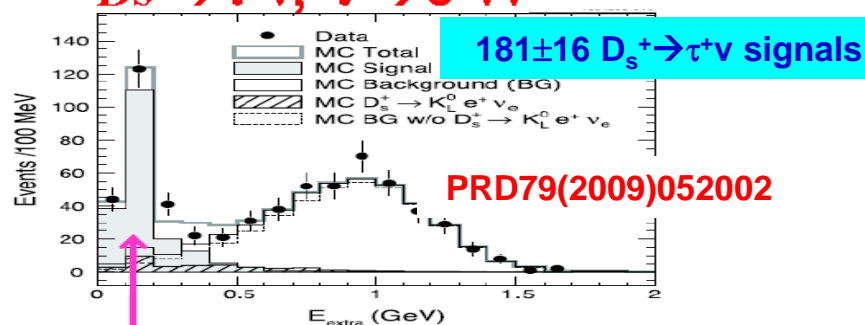


$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.65 \pm 0.45 \pm 0.17) \times 10^{-3}$$

$$B[D_s^+ \rightarrow \tau^+ \nu] = (6.42 \pm 0.81 \pm 0.18)\%$$

$$f_{D_{s^+}} = 263.3 \pm 8.2 \pm 1.9 \text{ MeV}$$

$D_s^+ \rightarrow \tau^+ \nu$ ,  $\tau^+ \rightarrow e^+ \nu \nu$

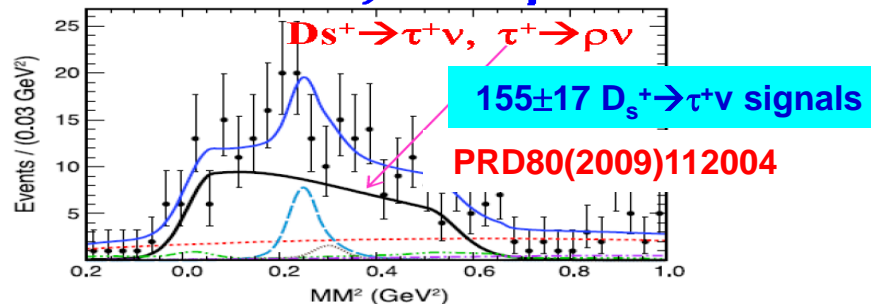


Signal for  $D_s^+ \rightarrow \tau^+ \nu$

$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.30 \pm 0.47 \pm 0.21)\%$$

$$f_{D_{s^+}} = 252.2 \pm 11.1 \pm 5.2 \text{ MeV}$$

$D_s^+ \rightarrow \tau^+ \nu$ ,  $\tau^+ \rightarrow \rho \nu$



$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.52 \pm 0.57 \pm 0.22)\%$$

$$f_{D_{s^+}} = 257.8 \pm 13.3 \pm 5.2 \text{ MeV}$$



# Absolute measurements at BaBar

523 fb<sup>-1</sup> @ 10.58 GeV

Better statistical [1023] but  
larger systematics

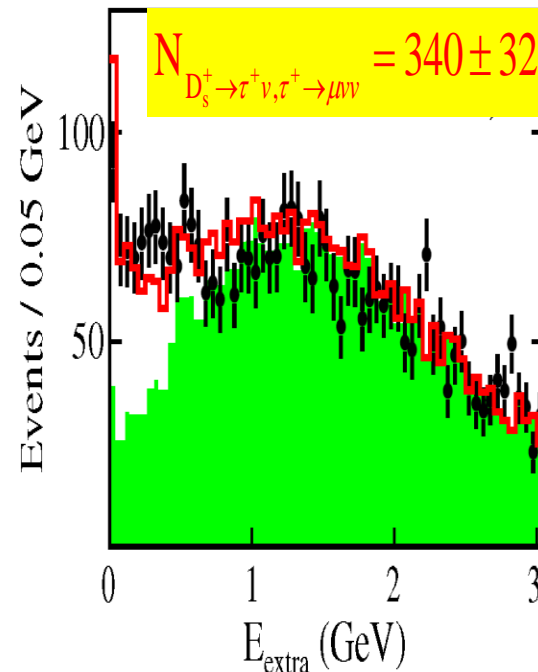
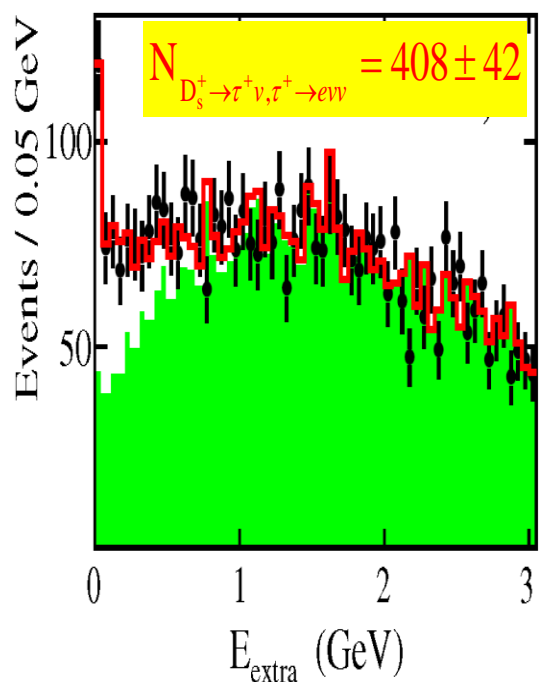
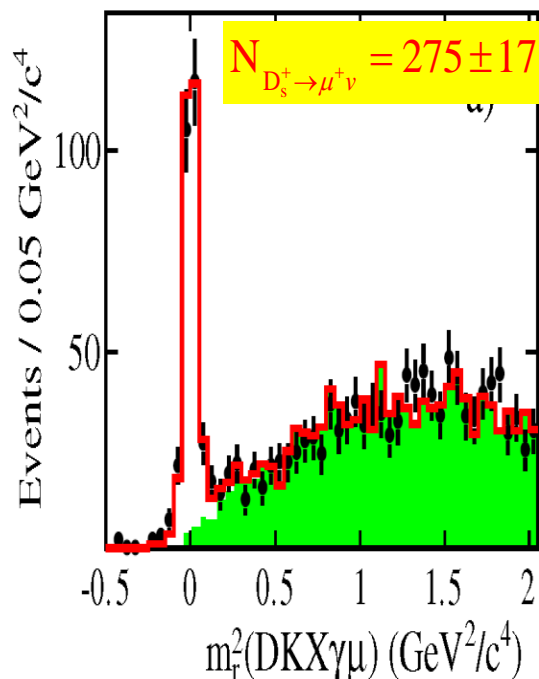
$$e^+e^- \rightarrow c\bar{c} \rightarrow D_{\text{tag}}K_{\text{frag}}X_{\text{frag}}D_s^{*-}$$

$$B[D_s^+ \rightarrow \mu^+\nu] = (6.02 \pm 0.38 \pm 0.34) \times 10^{-3}$$

$$B[D_s^+ \rightarrow \tau^+\nu] = (5.00 \pm 0.35 \pm 0.49)\%$$

PRD82(2010)091103

$$f_{D_{s^+}} = 258.6 \pm 6.4 \pm 7.5 \text{ MeV}$$



# Absolute measurements at Belle

913 fb<sup>-1</sup> @ 10.58 GeV

Better statistical [2698] but larger systematics

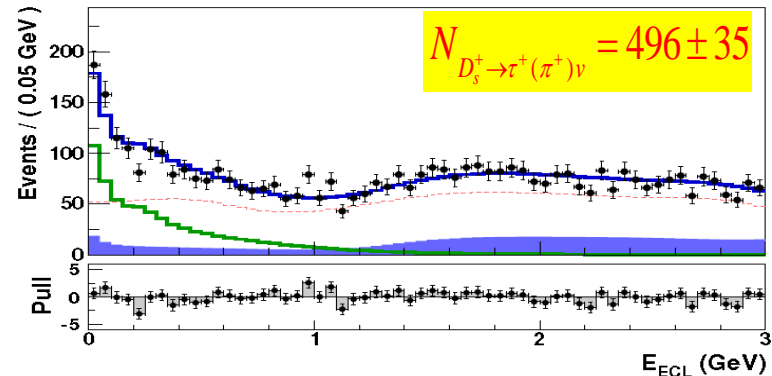
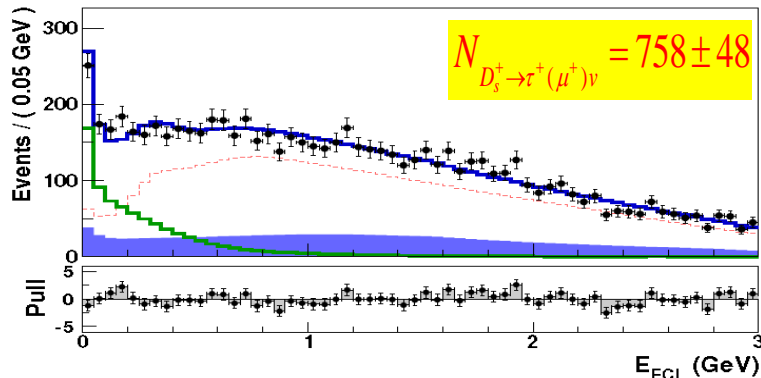
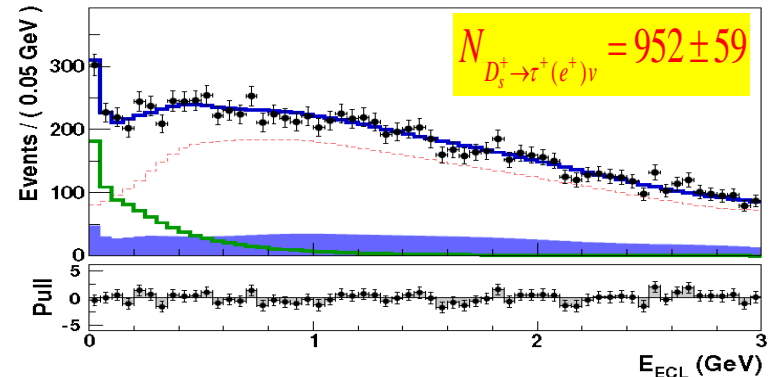
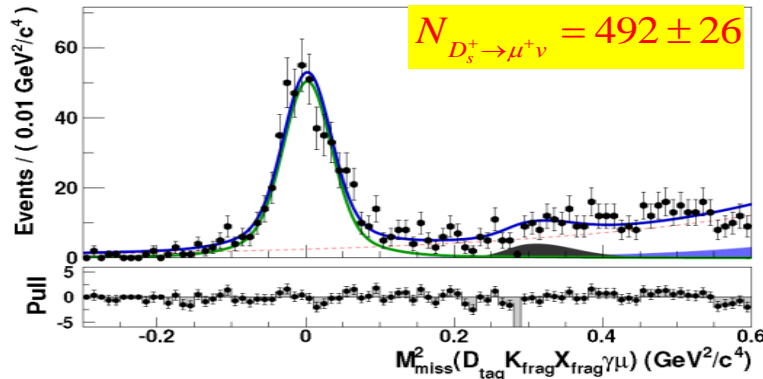
$$e^+e^- \rightarrow c\bar{c} \rightarrow D_{\text{tag}}K_{\text{frag}}X_{\text{frag}}D_s^{*-}$$

JHEP1309(2013)129

$$B[D_s^+ \rightarrow \mu^+ \nu] = (5.31 \pm 0.28 \pm 0.20) \times 10^{-3}$$

$$B[D_s^+ \rightarrow \tau^+ \nu] = (5.70 \pm 0.21 \pm 0.31)\%$$

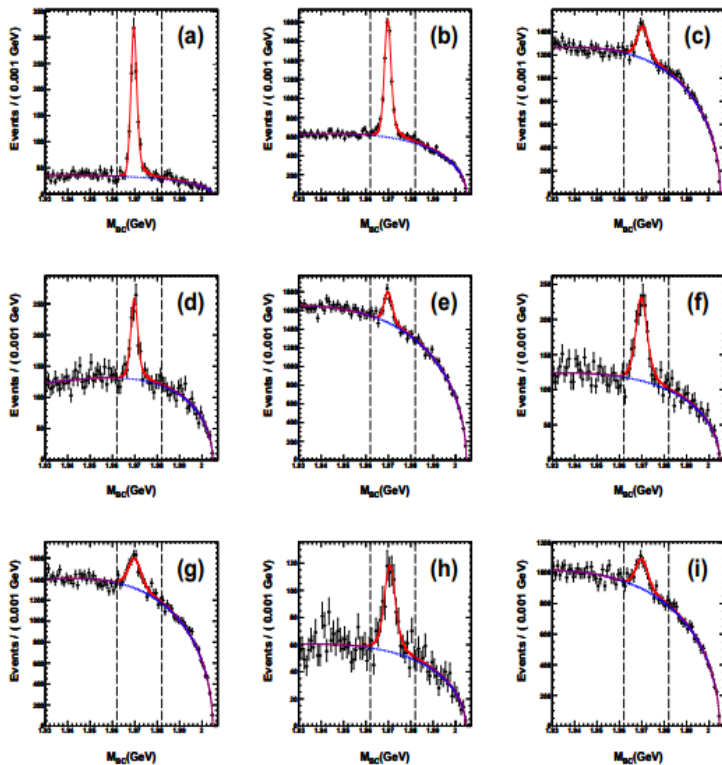
$$f_{D_{S^+}} = 255.5 \pm 4.2 \pm 5.1 \text{ MeV}$$



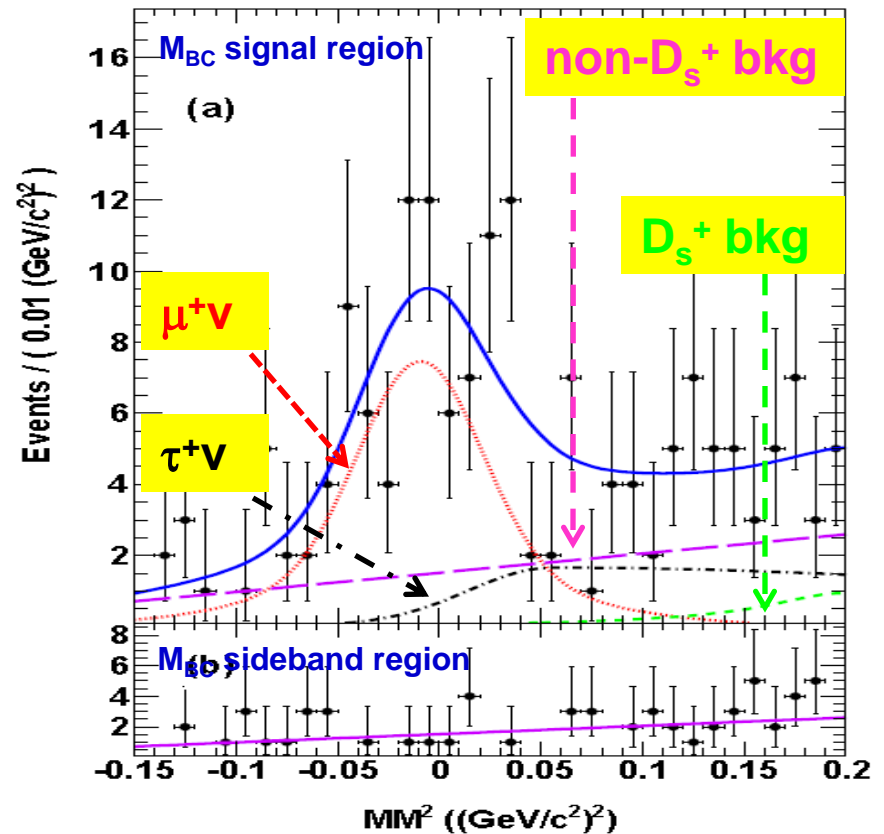
# Absolute measurements @ 4.009 at BESIII

482 pb<sup>-1</sup> @ 4.009 GeV

PRD94(2016)072004



$$N_{D_s^{\text{tag}}} = 15127 \pm 312$$

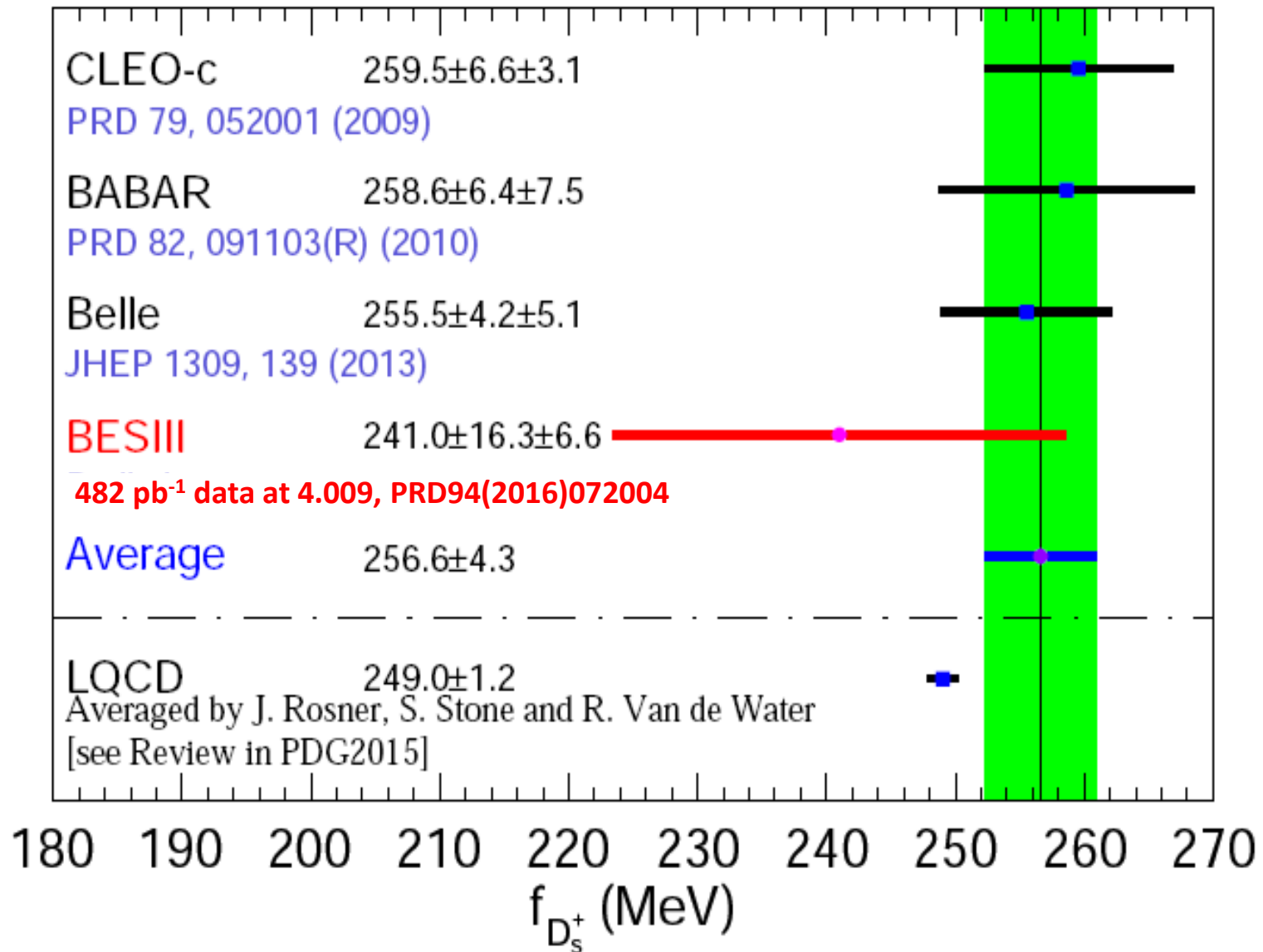


$$B[D_s^+ \rightarrow \mu^+ \nu] = (0.495 \pm 0.067 \pm 0.026)\%$$

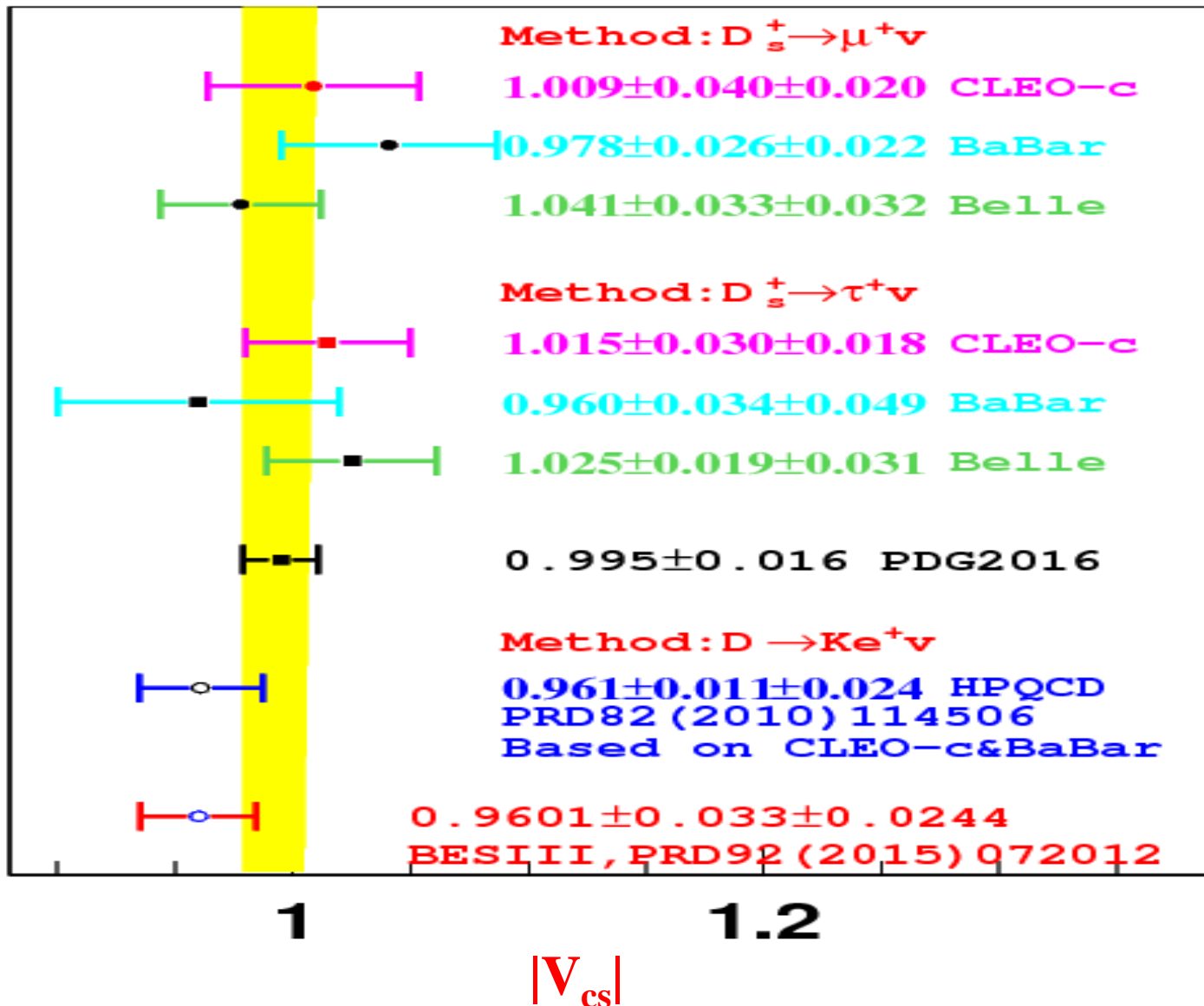
$$B[D_s^+ \rightarrow \tau^+ \nu] = (4.83 \pm 0.65 \pm 0.26)\%$$

$$f_{D_{s^+}} = (241.0 \pm 16.3 \pm 6.6) \text{ MeV}$$

# Comparison of $f_{D_s^+}$



# Comparison of $|V_{cs}|$



# Comparisons of Existing $f_{D^+}$ , $f_{D_{s^+}}$ and $f_{D^+}:f_{D_{s^+}}$

	Experiments	Femilab Lattice+MILC (2014)		HPQCD (2012)	
	Averaged	Expected	$\Delta$	Expected	$\Delta$
$f_{D^+}(\text{MeV})$	$203.9 \pm 4.7$	$212.6 \pm 0.4^{+1.0}_{-1.2}$	$1.8\sigma$	$208.3 \pm 3.4$	$0.8\sigma$
$f_{D_{s^+}}(\text{MeV})$	$256.9 \pm 4.4$	$249.0 \pm 0.3^{+1.1}_{-1.5}$	$1.7\sigma$	$246.0 \pm 3.6$	$1.4\sigma$
$f_{D^+}:f_{D_{s^+}}$	$1.260 \pm 0.036$	$1.1712 \pm 0.0010^{+0.0029}_{-0.0032}$	$2.5\sigma$	$1.187 \pm 0.013$	$1.9\sigma$

- Precisions of the LQCD calculations of  $f_{D^+}$ ,  $f_{D_{s^+}}$ ,  $f_{D^+}:f_{D_{s^+}}$  are 0.5%, 0.5% and 0.3%
- The experimentally measured and the theoretical expected  $f_{D^+}$ ,  $f_{D_{s^+}}$ ,  $f_{D^+}:f_{D_{s^+}}$  differ by  $\sim 2\sigma$
- Further improved measurement with larger data sample is necessary!

# Prospect on $D_s^+ \rightarrow l^+ \nu$ at BESIII

**$\sim 3 \text{ fb}^{-1}$  data @ 4.18 GeV is in hand**

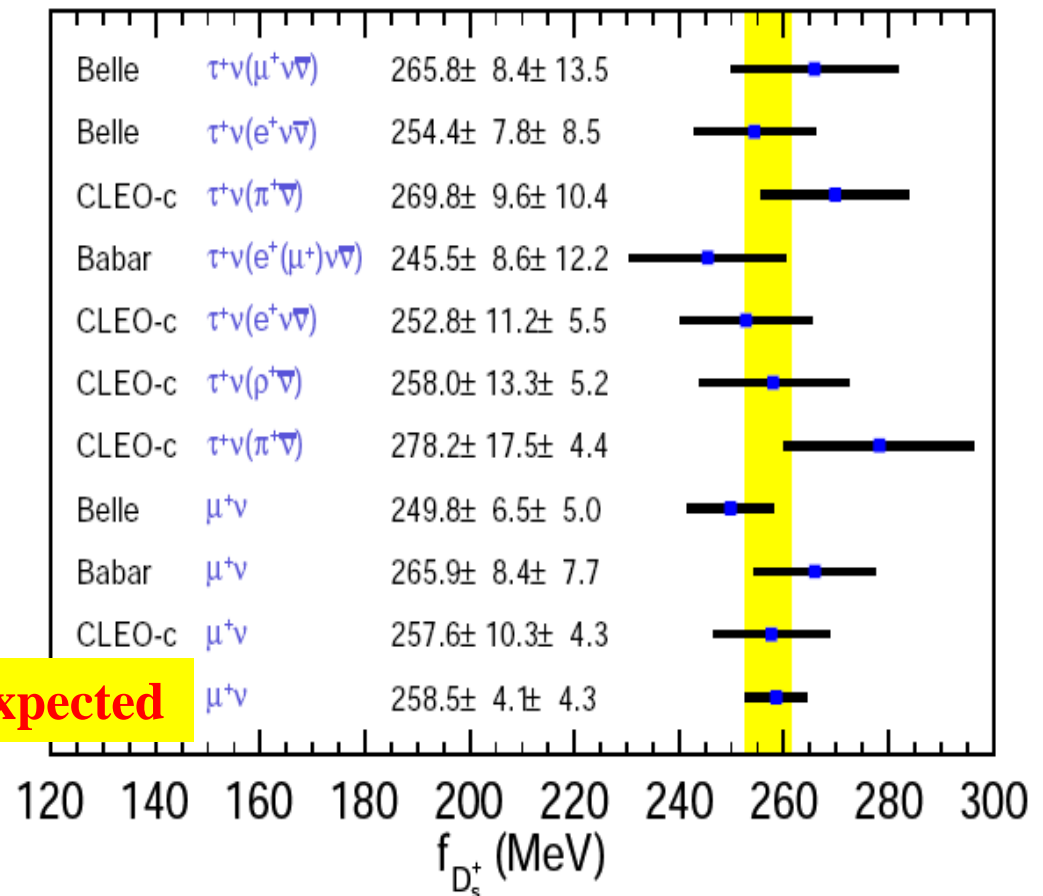
**$\mu$  counter of BESIII may help to suppress background in  $D_s^+ \rightarrow \mu^+ \nu$**

**Statistics roughly estimated with CLEO-c results**

**If systematic is the same as CLEO-c measurement**

**$D_s^+ \rightarrow \tau^+ \nu$  should further improve measurements**

Ds decay constant



# Summary

- In recent 10 years, significantly improved measurements of  $f_{D(s)^+}$  and  $|V_{cs(d)}|$  using  $D(s)^+$  leptonic decays have been obtained. These are key for LQCD calibration and CKM UT.
- BESIII measure  $f_{D^+}$  and  $|V_{cd}|$  using  $D^+ \rightarrow \mu^+ \nu$  with  $3 \text{ fb}^{-1}$  data at  $\psi(3770)$ . More data, more chance.
- BESIII preliminary result shows evidence for  $D^+ \rightarrow \tau^+ \nu$
- BESIII report  $f_{D_s^+}$  with  $482 \text{ pb}^{-1}$  data at  $4.009 \text{ GeV}$ . Improved measurement of  $f_{D_s^+}$  and  $|V_{cs}|$  by  $D_s^+ \rightarrow l^+ \nu$  with  $3 \text{ fb}^{-1}$  data at  $4.18 \text{ GeV}$  is expected in the near future



**Thank you!**