

"Measurements of $\Delta m_{d,s}$ and $\Delta\Gamma_d$ at LHCb"

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on behalf of the LHCb collaboration

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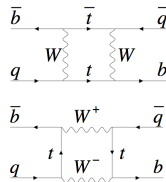
- Physics introduction on $B_{d/s}^0 - \bar{B}_{d/s}^0$ mixing: why measuring Δm_d , Δm_s and $\Delta\Gamma_d$
- How to measure $\Delta m_{d/s}$
 - LHCb most precise measurement of Δm_d
 - LHCb most precise measurement of Δm_s
- How to measure $\Delta\Gamma_d$
 - LHCb measurement of $\Delta\Gamma_d$ ($\Delta\Gamma_s$ covered by [G.Cowan's Talk](#))
- Implications of the measurements to the Standard Model and to possible New Physics scenarios
- Conclusions

$B_{d/s}^0 - \bar{B}_{d/s}^0$ oscillations: Physics motivations

In the Standard Model $B_{d/s}^0 - \bar{B}_{d/s}^0$ mix through the box diagrams

The two mass eigenstates B_H and B_L have:

- $\Delta m_q \propto m_W^2 m_{B_q} \hat{B}_{B_q} f_{B_q}^2 (V_{tq}^* V_{tb})^2 \quad q = d, s$
- $\Delta \Gamma_q \propto m_b^2 m_{B_q} \hat{B}_{B_q} f_{B_q}^2 ((V_{tq}^* V_{tb})^2 + V_{tq}^* V_{tb} V_{cq}^* V_{cb} \mathcal{O}(m_c^2/m_b^2) + (V_{cq}^* V_{cb})^2 \mathcal{O}(m_c^4/m_b^4))$

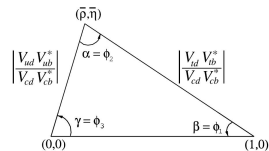


Current WA: [HFAG Summer 2016]

- $\Delta m_d = 0.5065 \pm 0.0016 \pm 0.0011 \text{ ps}^{-1}$
- $\Delta m_s = 17.757 \pm 0.020 \pm 0.007 \text{ ps}^{-1}$
- $\Delta \Gamma_d / \Gamma_d = (-0.2 \pm 1.0) \times 10^{-2}$

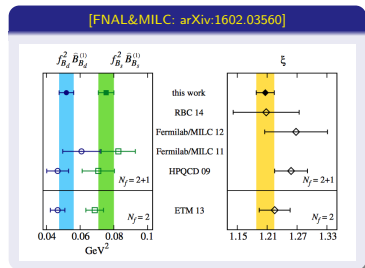
constrain the apex $(\bar{\rho}, \bar{\eta})$ of the CKM unitarity triangle

- $\hat{B}_{B_q} f_{B_q}^2$ uncertainties limit the precision of V_{CKM}



Some of the theoretical uncertainties cancel in the ratio:

- $\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s}}{m_{B_d}} \times \xi^2 \times \frac{|V_{ts}|^2}{|V_{td}|^2}$
- $\xi = 1.268 \pm 0.063$ Lattice QCD, PDG2016 \rightarrow [FNAL&MILC: arXiv:1205.7013]
- $= 1.206 \pm 0.019$ new calculation [FNAL&MILC: arXiv:1602.03560]



$B_{d/s}^0 - \bar{B}_{d/s}^0$ oscillations: measurement of $\Delta m_{d/s}$

Best precision is achieved by measuring the time-dependent mixing asymmetry in *flavour-specific* decays:

$$\blacksquare \mathcal{A}_{mix}^{th}(t) = \frac{\Gamma_{B_q^0 \rightarrow \bar{f}}(t) - \Gamma_{B_q^0 \rightarrow f}(t)}{\Gamma_{B_q^0 \rightarrow \bar{f}}(t) + \Gamma_{B_q^0 \rightarrow f}(t)} \sim \cos(\Delta m_q t) \implies \mathcal{A}_{mix}^{exp}(t) \propto (1 - 2\omega) e^{-(\Delta m_q \sigma_t)^2/2} \cos(\Delta m_q t)$$

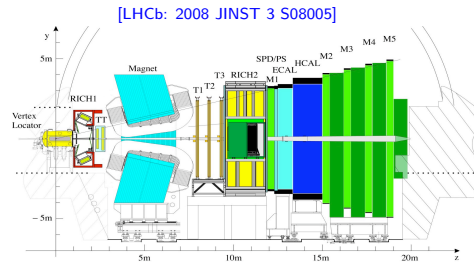
assuming no CPV in mixing and $\Delta\Gamma_q = 0$

The average statistical significance is:

$$\blacksquare S \sim \sqrt{N/2} f_{sig} \sqrt{\epsilon_{tag} (1 - 2\omega)^2} e^{-(\Delta m_q \sigma_t)^2/2}$$

Experimental key-factors fully addressed by LHCb:

- Signal yield and background suppression: $\sqrt{N/2} f_{sig}$
 - large σ_{bb}
 - $\mathcal{L}^{int} = 3 \text{ fb}^{-1}$ in Run1 (2 fb^{-1} in Run2, so far)
 - efficient trigger and reconstruction
 - tracking: impact parameter, momentum, mass resolutions
 - particle identification: $(\mu/\pi/K/p)$
- Flavour tagging: $\sqrt{\epsilon_{tag} (1 - 2\omega)^2} = 3 - 6\%$
 - Opposite-side (OS: $e, \mu, K, \text{Vertex}, \text{Charm}$)
 - Same-side (SS: π, p and K)
- Decay time resolution: $e^{-(\Delta m_q \sigma_t)^2/2}$
 - excellent vertexing $\sigma_t \sim 45 - 55 \text{ fs}$



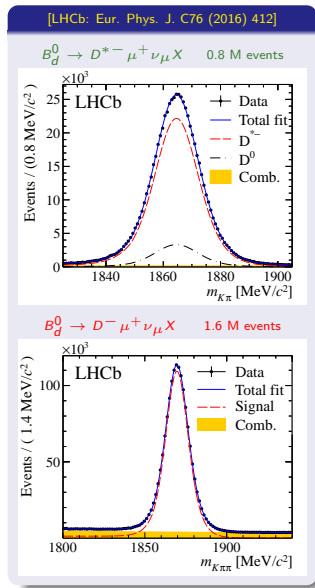
$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of Δm_d at LHCb

Δm_d was first measured at DESY by ARGUS [Phys.Lett. B192 (1987) 245-252] then at Cornell, LEP then at B-Factories.

Previous LHCb measurements used data samples of increasing size of different “flavour specific” hadronic and semileptonic B_d decays [LHCb: Phys. Lett. B709 (2012) 177, Phys. Lett. B719 (2013) 318, Eur. Phys. J. C73 (2013) 2655]

Latest LHCb measurement exploits the full Run1 data sample (3 fb^{-1})
→ most precise determination of Δm_d [LHCb: Eur. Phys. J. C76 (2016) 412]

- Uses semileptonic $B_d^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu X$ decays
 - large branching ratios ($\mathcal{B} \sim 2\text{--}5\%$)
- Event reconstruction & selection:
 - reconstruct $D^{*-} \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^-) \pi^-$ and $D^- \rightarrow K^+ \pi^- \pi^-$ decays
 - $D^{(*)-} \mu^+$ from a common vertex (displaced from PV)
 - missing neutrino: cannot apply mass or kinematic cuts to the B_d , only to D^0, D^{*-} or D^-
 - vetoes on mis-ID $J/\psi, \Lambda_c$
- Background:
 - Combinatorial
 - D^0 from B decays
 - $B^+ \rightarrow D^{(*)-} \mu^+ \pi^+ \nu_\mu$



$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of Δm_d at LHCb

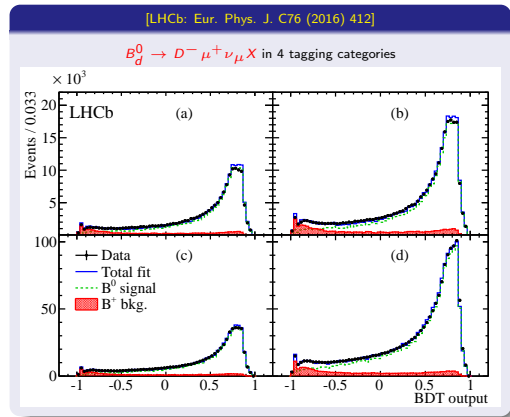
$B^+ \rightarrow D^{(*)-} \mu^+ \pi^+ \nu_\mu$ background:

- it is expected to be 10% and 13%, BUT its \mathcal{B} is known with a precision of 10% [PDG2016]
- its fraction is correlated with the fit value of Δm_d

→ need to suppress it to reduce the systematic uncertainty

MVA classifier was developed to discriminate such background from the signal:

- inputs:
 - geometrical and kinematical info on the B candidate ($D^{(*)-} \mu^+$)
 - isolation info on additional tracks reconstructed in a cone around the B candidate direction
- training:
 - on MC samples of signal $B^0 \rightarrow D^{*-} \mu^+ \nu_\mu$ and $B^+ \rightarrow D^{*-} \mu^+ \pi^+ \nu_\mu$
- output (BDT):
 - used both as selection cut (suppression of 70%) and to evaluate on data the remaining fraction (→3% and 6%)



$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of Δm_d at LHCb

Event reconstruction suffers from the missing neutrino:

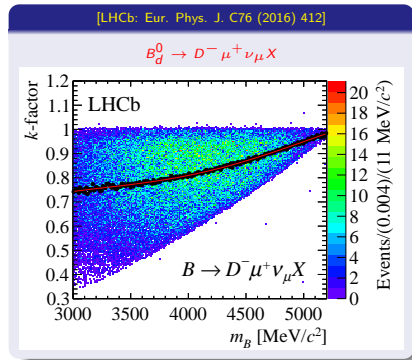
- B_d momenta & decay time are corrected by a k -factor determined on MC:

$$t = \frac{M_{B^0} \cdot L}{p_{D^{(*)}\mu} \cdot c / k(m_B)} \quad \text{with} \quad k(m_B) = \langle p_{D^{(*)}\mu} / p_{B^0}^{\text{true}} \rangle$$

→ limited time resolution

Flavour Tagging:

- determine q_{mix} from the tagging decision & the charge of the μ ($q_{\text{mix}} = \pm 1$)
- Split in four categories of increasing mistag ω to gain sensitivity
- Tagging power: $\epsilon \mathcal{D}^2 \sim 2.3\text{-}2.6\%$



$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of Δm_d at LHCb

Fit strategy:

- fit the m_{D^-}/m_{D^0} & $\delta m = m_{D^{*-}} - m_{D^0}$ distributions: disentangle **Signal** + B^+ (*sWeights*) from other backgrounds (combinatorial + D^0 from B)

- perform an *sFit* to the weighted distribution of the decay time:

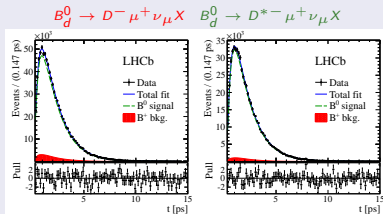
$$\mathcal{P}(t, q_{\text{mix}}) = (1 - f_{B^+})\mathcal{S}(t, q_{\text{mix}}) + f_{B^+}\mathcal{B}^+(t, q_{\text{mix}})$$

$$\mathcal{S}(t, q_{\text{mix}}) \propto a(t) \left[e^{-t/\tau} (1 + q_{\text{mix}}(1 - 2\omega) \cos(\Delta m_d t)) \otimes R(L) \otimes F(k) \right]$$

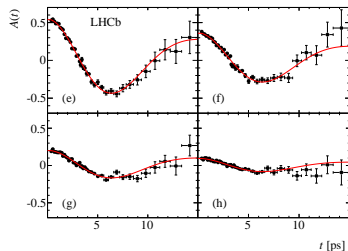
- time acceptance $a(t)$, f_{B^+} and ω extracted from fit to data
- convolution with resolution functions from MC $R(L), F(k)$

Assumptions: $\Delta\Gamma_d = 0$, $|q/p| = 1$

[LHCb: Eur. Phys. J. C76 (2016) 412]



$B_d^0 \rightarrow D^{*-} \mu^+ \nu_\mu X$ in 4 tagging categories



similar plots for $B_d^0 \rightarrow D^- \mu^+ \nu_\mu X$

$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of Δm_d at LHCb

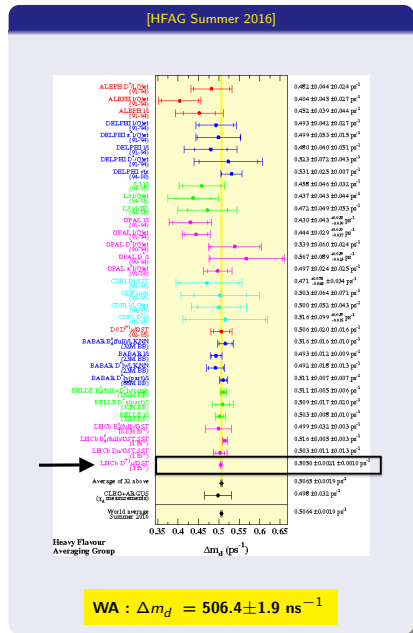
Results: [LHCb: Eur. Phys. J. C76 (2016) 412]

Mode	2011 sample Δm_d [ns ⁻¹]	2012 sample Δm_d [ns ⁻¹]	Total sample Δm_d [ns ⁻¹]
$B_d^0 \rightarrow D^- \mu^+ \nu_\mu X$	506.2 ± 5.1	505.2 ± 3.1	$505.5 \pm 2.7 \pm 1.1$
$B_d^0 \rightarrow D^{*-} \mu^+ \nu_\mu X$	497.5 ± 6.1	508.3 ± 4.0	$504.4 \pm 3.4 \pm 1.0$
combination			$505.0 \pm 2.1 \pm 1.0$

Systematic uncertainties:

Source of uncertainty	$D^- \mu^+ \nu_\mu$ [ns ⁻¹]		$D^{*-} \mu^+ \nu_\mu$ [ns ⁻¹]	
	Uncorrelated	Correlated	Uncorrelated	Correlated
B^+ background	0.4	0.1	0.4	-
Other backgrounds	-	0.5	-	-
k-factor distribution	0.4	0.5	0.3	0.6
Other fit-related	0.5	0.4	0.3	0.5
Total	0.8	0.8	0.6	0.8

Most precise measurement, dominates the average.



$B_s^0 - \bar{B}_s^0$ oscillations: Measurement of Δm_s at LHCb

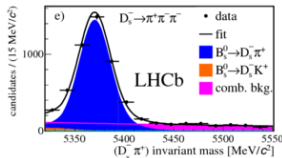
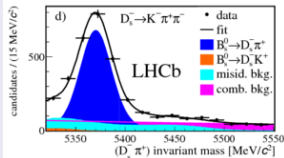
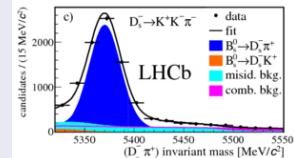
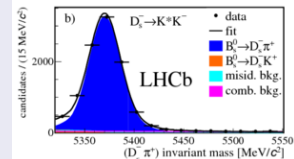
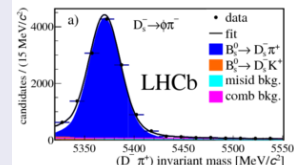
Δm_s was first measured by CDF in 2006: $\Delta m_s = 17.77 \pm 0.10 \pm 0.07 \text{ ps}^{-1}$ [CDF: Phys.Rev.Lett. 97 (2006) 242003]

Previous LHCb measurements used partial Run1 data samples of “flavour specific” $B_s^0 \rightarrow D_s^- (3)\pi^+$ decays [LHCb: Phys. Lett. B709 (2012) 177], and semileptonic B_s^0 decays [LHCb: Eur. Phys. J. C73 (2013) 2655]

The most precise LHCb measurement exploits 1 fb^{-1} of Run1 data sample [LHCb: New J. Phys. 15 (2013) 053021]

- Uses $B_s^0 \rightarrow D_s^- \pi^+$ decays ~ 34000 signal events
 - hadronic flavour specific decay with the largest \mathcal{B} ($\sim 0.3\%$)
- Event selection: reconstruct D_s^- in 5 fully reconstructed decay modes: $\phi\pi$, K^*K , $(KK\pi)_{\text{nonres}}$, $K\pi\pi$ and 3π
 - MVA selection for an optimal discrimination of signal from background

[LHCb: New J. Phys. 15 (2013) 053021]



$B_s^0 - \bar{B}_s^0$ oscillations: Measurement of Δm_s at LHCb

Fit strategy:

- perform a simultaneous fit of the 5 data samples of all contributions

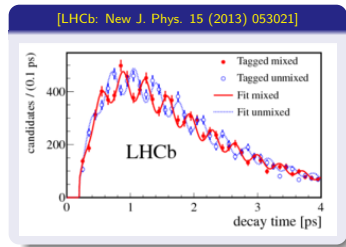
$$\mathcal{P}(m, t, \sigma_t, q, \eta) = \mathcal{P}_m(m) \mathcal{P}_{t,q}(t, q | \sigma_t, \eta) \mathcal{P}_{\sigma_t}(\sigma_t) \mathcal{P}_\eta(\eta)$$

$$\mathcal{P} = f_{\text{sig}} \mathcal{S} + \sum_i f_{\text{bkg}}^i \mathcal{B}_i$$

- $\mathcal{P}_m(m)$ mainly discriminate signal from background contributions
- $\mathcal{P}_{t,q}(t, q | \sigma_t, \eta)$:
 - Use per-event decay time resolution model $\langle \sigma_t \rangle \sim 44$ fs ($\mathcal{P}_{\sigma_t}(\sigma_t)$), calibrated on data using prompt D_s & π
 - Use per-event OS and SSK combined tagging decision and mistag: $\epsilon \mathcal{D}^2 = 3.5 \pm 0.5\%$ ($\mathcal{P}_\eta(\eta)$)

Result: $\Delta m_s = 17.768 \pm 0.023 \pm 0.006 \text{ ps}^{-1}$

Most precise measurement to date.



Systematic uncertainties

Source	Uncertainty [ps^{-1}]
z-scale	0.004
Momentum scale	0.004
Decay time bias	0.001
Total	0.006

More recently LHCb determined Δm_s also in the analysis of $B_s^0 \rightarrow J/\psi K^+ K^-$ for ϕ_s and $\Delta \Gamma_s$ measurements: $\Delta m_s = 17.711^{+0.055}_{-0.057} \pm 0.011 \text{ ps}^{-1}$ [LHCb: Phys. Rev. Lett. 114 (2015) 041801] (see also G.Cowan's Talk)

$B_q^0 - \bar{B}_q^0$ oscillations: Measurement of $\Delta\Gamma_q$

The decay rates of B_L and B_H to a given final state f can be different, therefore:

$$\Gamma(B_q^0(t) \rightarrow f) \propto e^{-\Gamma_q t} \left[\cosh(\Delta\Gamma_q t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma_q t/2) + A_{CP}^{dir,f} \cos(\Delta m_q t) + A_{CP}^{mix} \sin(\Delta m_q t) \right]$$
$$\Gamma(\bar{B}_q^0(t) \rightarrow f) \propto e^{-\Gamma_q t} \left[\cosh(\Delta\Gamma_q t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma_q t/2) - A_{CP}^{dir,f} \cos(\Delta m_q t) - A_{CP}^{mix} \sin(\Delta m_q t) \right]$$

assuming $|q/p| = 1$

The untagged rate: $\Gamma(B_q^0(t) \rightarrow f) \propto e^{-\Gamma_q t} [\cosh(\Delta\Gamma_q t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma_q t/2)]$

assuming production asymmetry $A_P = 0$

The effective lifetime $\tau_{B_q^0 \rightarrow f}^{\text{eff}}$ depends on $y_q = 2\Delta\Gamma_q \cdot \Gamma_q$:

$$\tau_{B_q^0 \rightarrow f}^{\text{eff}} = \frac{1}{\Gamma_q} \frac{1}{1 - y_q^2} \left[\frac{1 + 2A_{\Delta\Gamma}^f y_q + y_q^2}{1 + A_{\Delta\Gamma}^f y_q} \right]$$

$\Delta\Gamma_q$ can be measured by comparing $\tau_{B_q^0 \rightarrow f}^{\text{eff}}$ in different decay channels (different $A_{\Delta\Gamma}^f$)

For example: [T.Gershon, J. Phys. G 38:015007, 2011]

- $A_{\Delta\Gamma}^f = 0$ for *flavour specific* decays
- $A_{\Delta\Gamma}^f = \cos 2\beta$ for $B_d \rightarrow J/\psi K_S^0$

$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of $\Delta\Gamma_d$ at LHCb

Strategy: measure effective lifetime $\tau_{B_d^0}^{\text{eff}}$ using

- $B_d^0 \rightarrow J/\psi K^{*0}$ (flavour specific)
- $B_d^0 \rightarrow J/\psi K_s^0$ (CP eigenstate)

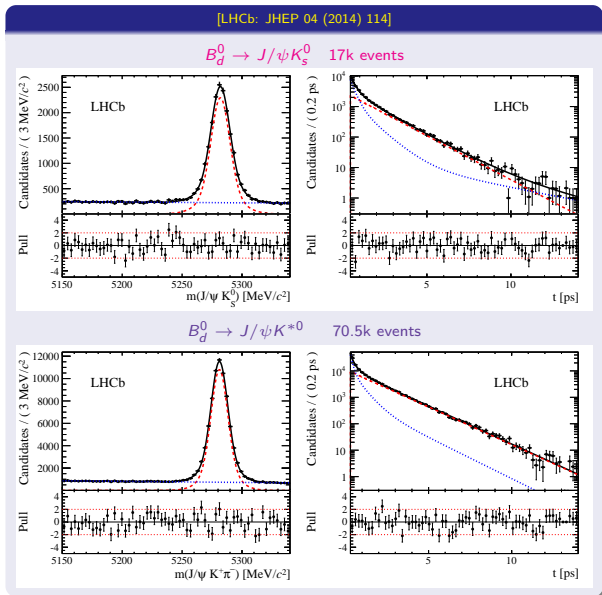
Selection:

- Run1 data sample (1 fb⁻¹)
- minimize any decay time biasing selection cuts

Fit strategy:

- fit the distributions of **time** and invariant **mass**:

$$\mathcal{P}(m, t) = f_{\text{sig}} \mathcal{S}(m, t) + \sum_i f_{\text{bkg}}^i \mathcal{B}_i(m, t)$$
- time resolution $\sigma_t \sim 45, 65$ fs



$B_d^0 - \bar{B}_d^0$ oscillations: Measurement of $\Delta\Gamma_d$ at LHCb

Effective lifetime results:

$$\tau_{B_d^0 \rightarrow J/\psi K^{*0}}^{\text{eff}} = 1.524 \pm 0.006 \pm 0.004 \text{ ps}$$

$$\tau_{B_d^0 \rightarrow J/\psi K_S^0}^{\text{eff}} = 1.499 \pm 0.013 \pm 0.005 \text{ ps}$$

[LHCb: JHEP 04 (2014) 114]

$$\tau_{B_q^0 \rightarrow f}^{\text{eff}} = \frac{1}{\Gamma_q} \frac{1}{1 - y_q^2} \left[\frac{1 + 2A_{\Delta\Gamma}^f y_q + y_q^2}{1 + A_{\Delta\Gamma}^f y_q} \right]$$

- $A_{\Delta\Gamma}^f = 0$ for *flavour specific* decays
- $A_{\Delta\Gamma}^f = \cos 2\beta$ for $B_d \rightarrow J/\psi K_S^0$

we measure:

$$\Gamma_d = 0.656 \pm 0.003 \pm 0.002 \text{ ps}^{-1}$$

$$\Delta\Gamma_d = -0.029 \pm 0.016 \pm 0.007 \text{ ps}^{-1}$$

Systematic uncertainties	$\tau_{B_d^0 \rightarrow J/\psi K^{*0}}^{\text{eff}}$ [fs]	$\tau_{B_d^0 \rightarrow J/\psi K_S^0}^{\text{eff}}$ [fs]	$\Delta\Gamma_d/\Gamma_d$ $\times 10^{-3}$
VELO reconstruction	2.3	0.9	4.1
Simulation sample size	2.3	2.9	6.3
Mass-time correlation	1.8	2.1	4.7
Trigger and selection eff.	1.2	2.0	4.0
Background modelling	0.2	2.2	3.8
Mass modelling	0.2	0.4	0.8
Peaking background	–	0.3	0.5
Effective lifetime bias	–	–	–
B_d production asym.	–	1.1	1.9
LHCb length scale	0.3	0.3	–
Total	3.9	4.9	10.7

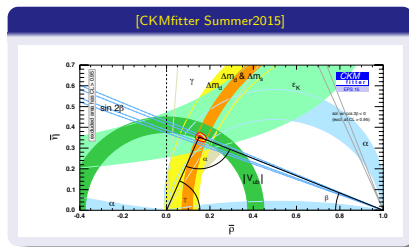
$$\Delta\Gamma_d/\Gamma_d = (-4.4 \pm 2.5 \pm 1.1) \times 10^{-2}$$

From the measurements to the SM-CKM picture

Measurement	Value	reference
Δm_d [ps^{-1}]	$0.5050 \pm 0.0021 \pm 0.0010$	[LHCb: Eur. Phys. J. C76 (2016) 412]
	0.5064 ± 0.0019	[HFAG Summer 2016]
Δm_s [ps^{-1}]	$17.768 \pm 0.023 \pm 0.000$	[LHCb: New J. Phys. 15 (2013) 053021]
	17.757 ± 0.021	[HFAG Summer 2016]
$\Delta\Gamma_d/\Gamma_d$	$(-4.4 \pm 2.5 \pm 1.1) \times 10^{-2}$	[LHCb: JHEP 04 (2014) 114]
	$(-0.1 \pm 1.1 \pm 0.9) \times 10^{-2}$	[ATLAS: JHEP06 (2016) 081]
	$(-0.2 \pm 1.0) \times 10^{-2}$	[HFAG Summer 2016]

Within SM, such measurements constrain

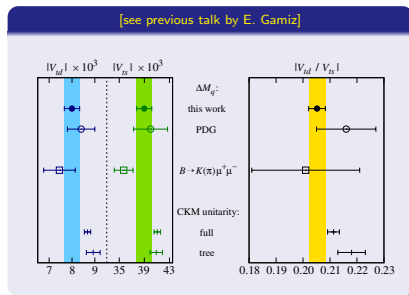
$$\frac{|V_{ts}|^2}{|V_{td}|^2} = 0.2159 \pm 0.0004(\text{exp}) \pm 0.0107(\text{lattice}) \quad [\text{PDG2016}]$$



With the latest, improved LatticeQCD calculations

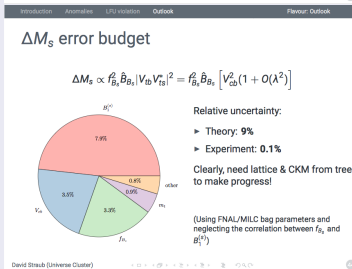
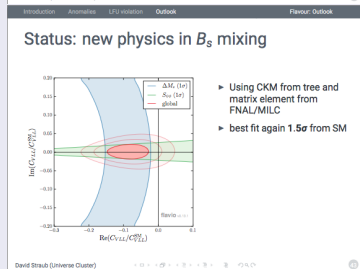
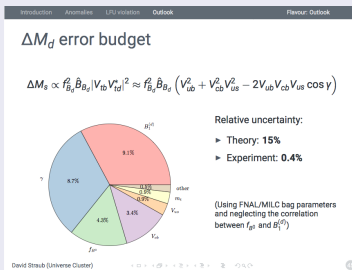
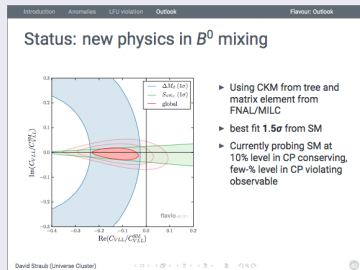
$$\frac{|V_{ts}|^2}{|V_{td}|^2} = 0.2052 \pm 0.0032 \quad [\text{FNAL\&MILC: arXiv:1602.03560}]$$

a tension ($\mathcal{O}(2\sigma)$) arises when comparing $|V_{ts}|$, $|V_{td}|$ results from mixing measurement with results from tree-processes



From the measurements to possible hints of NP ?

[D. Straub, Talk @ LHCb Implication Workshop 2016]

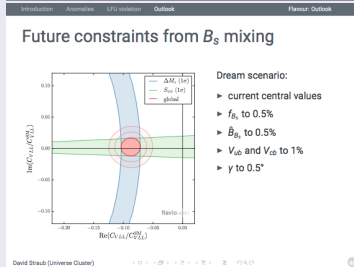
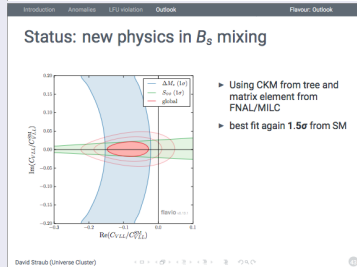
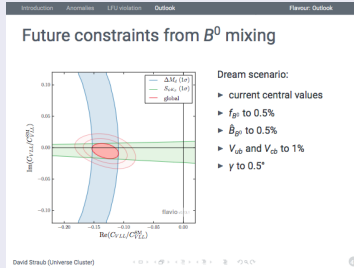
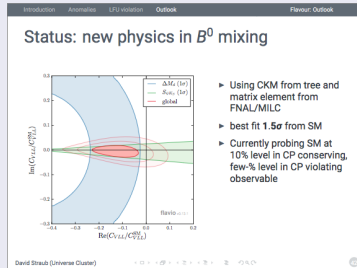


plots can be reproduced from this [link](#) to the open source code flavio

Current measurements are compatible with SM in 1.5σ

From the measurements to possible hints of NP ?

[D. Straub, Talk @ LHCb Implication Workshop 2016]



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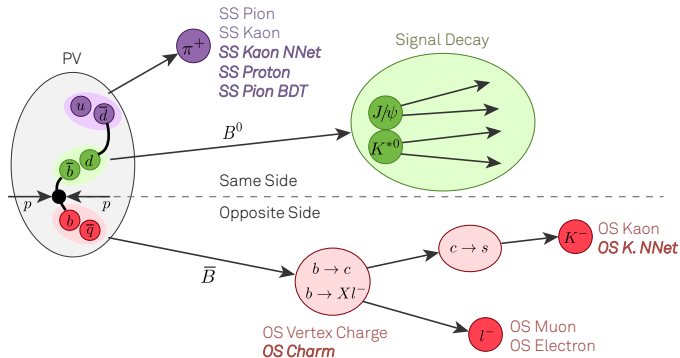
Future improvements can reveal NP

- LHCb measurements of Δm_d and Δm_s have reached a precision of ‰, and dominate the current World Averages.
- Together with the measurement of $\Delta\Gamma_d$ and $\Delta\Gamma_s$, they provide useful constraints to the CKM parameters $|V_{ts}|$ and $|V_{td}|$ and important tests of the SM.
- The precision of $|V_{ts}|$ and $|V_{td}|$ is currently limited by theoretical uncertainties.
- Latest Lattice QCD calculations allowed a factor ~ 3 of improvement in $|V_{ts}|^2/|V_{td}|^2$ with respect to previous calculations that renewed the interest on $B_q^0 - \bar{B}_q^0$ mixing parameters.

Looking forward for further improvements on theoretical computations and on experimental measurements (for prospects at LHCb see [talk by V. Chobanova](#))

BACKUP

Flavour Tagging: identifying the initial B flavour



OS tagging: exploits the properties of the decays of the b -hadron **opposite** to the signal B [LHCb: Eur. Phys. J. C72 (2012) 2022]

- μ, e ($b \rightarrow c l^- \bar{\nu}_l$), K ($b \rightarrow c \rightarrow s$), Q_{vtx} (inclusive secondary vertex reconstruction)

SS tagging: exploits the hadronization process of the **signal** B , or in the decays of excited states B^{**}

- $SS\pi, SS\rho$ [LHCb: LHCb-PAPER-2016-039, arXiv:1610.06019] (tag the B_d) (see also M. Calvi's Talk),
- SSK [LHCb: JINST 11 (2016) P05010] (tag the B_s)

tagging power: $\varepsilon(1 - 2\omega)^2 \sim 3 - 6\%$ depending on the B decay channel