

# Measurements of CKM angles at Belle

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On behalf of the Belle Collaboration

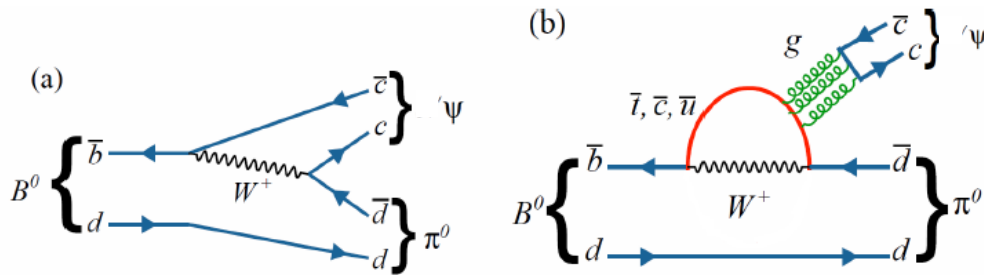


## Outline

- $B^0 \rightarrow \psi(2S)\pi^0$
  - $B^0 \rightarrow \underline{D}_{CP} h^0$
  - $B^0 \rightarrow \overline{D}^{(*)0} h^0$
  - $B^0 \rightarrow \rho^+ \rho^-$  - Related to  $\phi_2$  or  $\alpha$  measurement
- Related to  $\phi_1$  or  $\beta$  measurement



# $B^0 \rightarrow \psi(2S)\pi^0$



➤ At quark level the decay is proceed via  $b \rightarrow c\bar{c}d$  transitions, similar to  $B^0 \rightarrow J/\psi\pi^0$  decays.

- These decays are sensitive to the CP violating angle  $\phi_1 = \arg(-V_{cd}V_{cb}^*/V_{td}V_{tb}^*)$  of the unitarity triangle.
- In the absence of penguin contribution, the direct CP asymmetry  $A=0$  and the mixing-induced CP asymmetry  $S = -\sin(2\phi_1)$ . The non vanishing  $A$  and the deviation of  $S$  from  $-\sin(2\phi_1)$  arise from the penguin contributions, hence these quantities are useful to probe the Physics beyond the SM.
- These decays are also useful to constrain the penguin pollution in  $b \rightarrow c\bar{c}s$  transitions.

[M. Ciuchini et. al., PRL 95, 221804(2005); S. Faller et.al., PRD 79, 014030(2009); P. Fringe et. al., PRL 115, 061802(2015)]

V. Chobanova et al.,  
PRD (R) 93, 031101 (2016)



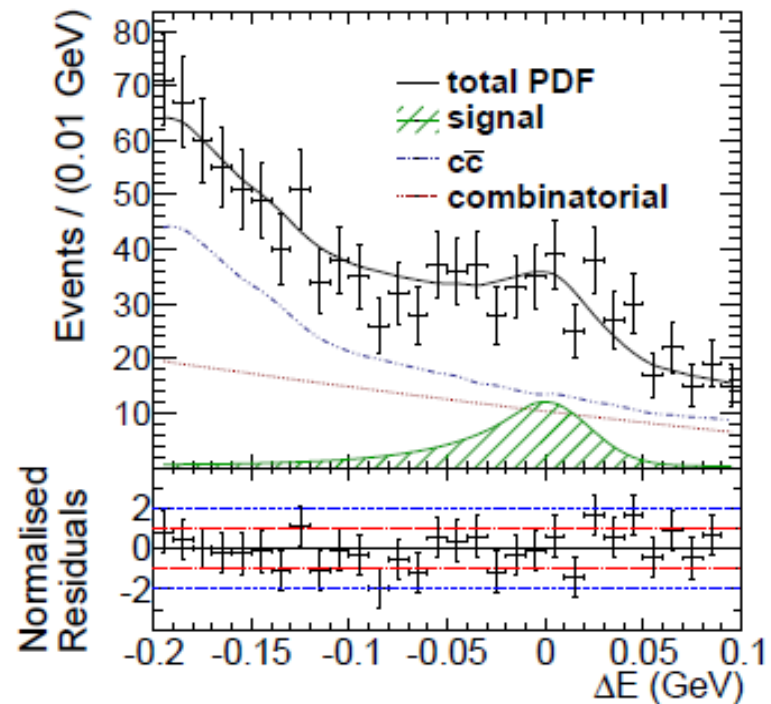
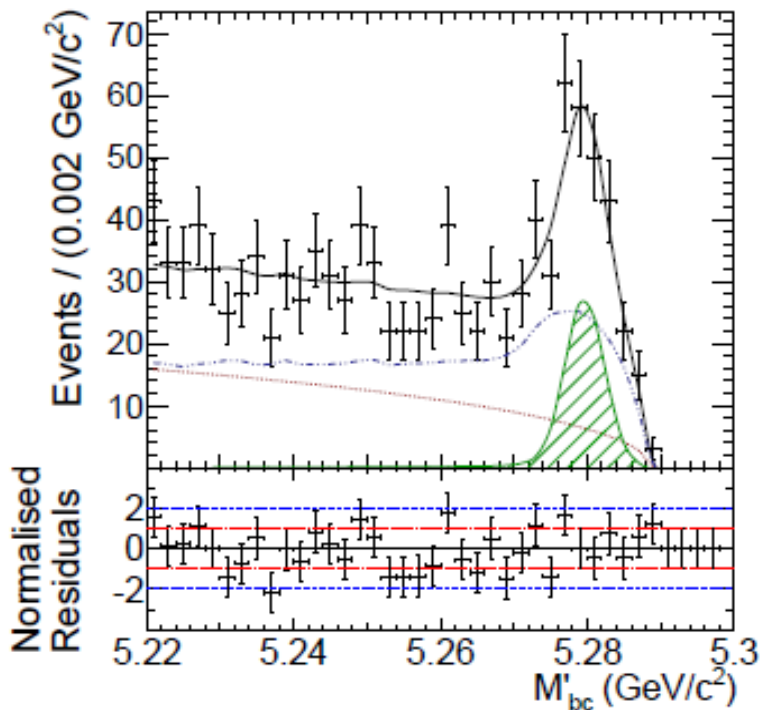
# $B^0 \rightarrow \Psi(2S)\pi^0$

- This Analysis uses full Belle data set of  $772 \times 10^6$  BB
- $\Psi(2S)$  is reconstructed from four sub-decays:
  - $l^+l^-$  ( $l=e,\mu$ )
  - $J/\Psi\pi^+\pi^-$  ( $J/\Psi \rightarrow l^+l^-$ )
- We include the bremsstrahlung photons that are within 50 mrad of each of electron and positron tracks in  $e^+e^-$  modes [both in  $\Psi(2S)$  &  $J/\Psi$ ]
- Vertex- and mass-constraint fits are performed both in  $\Psi(2S)$  &  $J/\Psi$  and mass-constraint fit is performed in  $\pi^0$  reconstructions to improve the momentum resolution.
- Continuum background is suppressed by requiring the ratio of second- to zeroth-order Fox-Wolfram moments  $R_2 < 0.5$ .
- Modified beam-energy-constrained mass and energy difference are used in 2D fit procedure.

$$\Delta E = E_B - E_{\text{beam}}, \quad M'_{bc} \equiv \sqrt{(E_{\text{beam}})^2 - \left| \vec{p}_{\Psi(2S)} + \sqrt{(E_{\text{beam}} - E_{\Psi(2S)})^2 - m_{\pi^0}^2} \frac{\vec{p}_{\pi^0}}{|\vec{p}_{\pi^0}|} \right|^2},$$

- All four sub-decay modes for  $\Psi(2S)$  are combined for the branching fraction measurement.

# $B^0 \rightarrow \psi(2S)\pi^0$



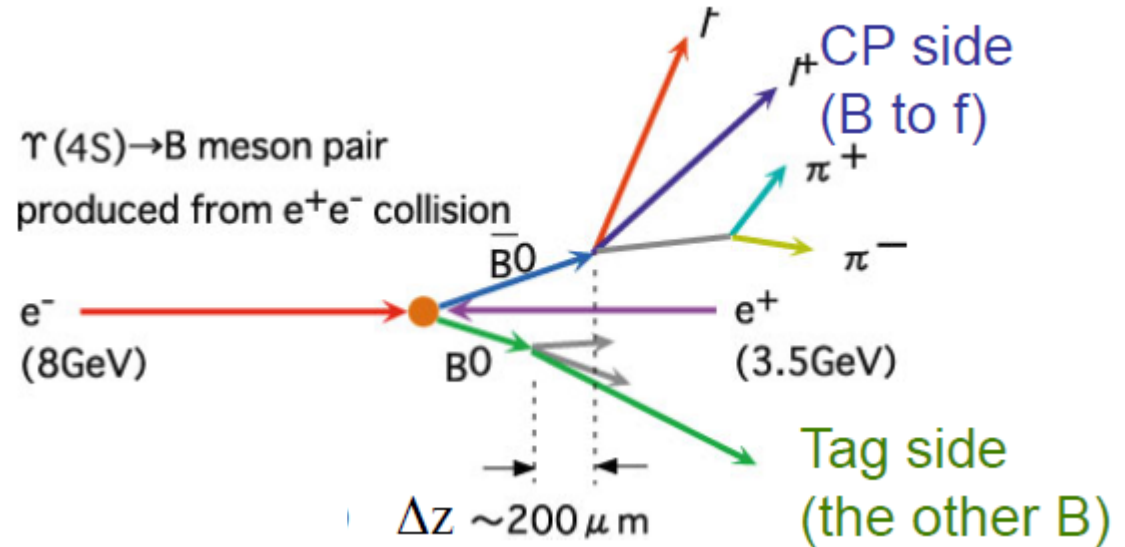
- Observed signal yield =  $85 \pm 12$  with a significance of  $7.2\sigma$  including the systematic uncertainty (First observation)
- $\mathcal{B}(B^0 \rightarrow \psi(2S)\pi^0) = [1.17 \pm 0.17(\text{stat}) \pm 0.08(\text{syst})] \times 10^{-5}$ .
- No CPV measurement yet for this mode.



# Time-dependent CPV

$$\Delta t = \frac{\Delta z}{\beta\gamma c}$$

$\beta\gamma = 0.425$

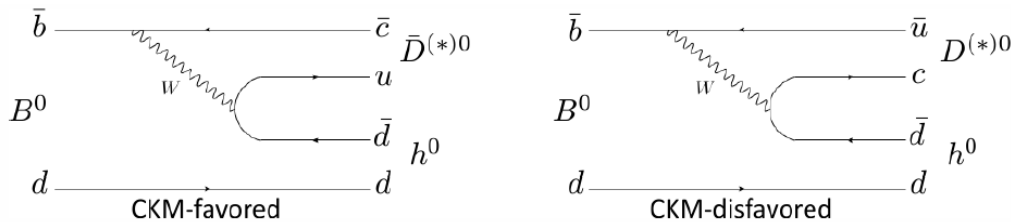


$$A_{CP}(\Delta t) = \frac{\Gamma(\bar{B}^0(\Delta t) \rightarrow f) - \Gamma(B^0(\Delta t) \rightarrow f)}{\Gamma(\bar{B}^0(\Delta t) \rightarrow f) + \Gamma(B^0(\Delta t) \rightarrow f)} = \mathcal{S}_f \sin(\Delta m_d \Delta t) + \mathcal{A}_f \cos(\Delta m_d \Delta t)$$



# $B^0 \rightarrow D_{CP} h^0$

- The decay is mediated via the tree-level diagram (penguin pollution free)

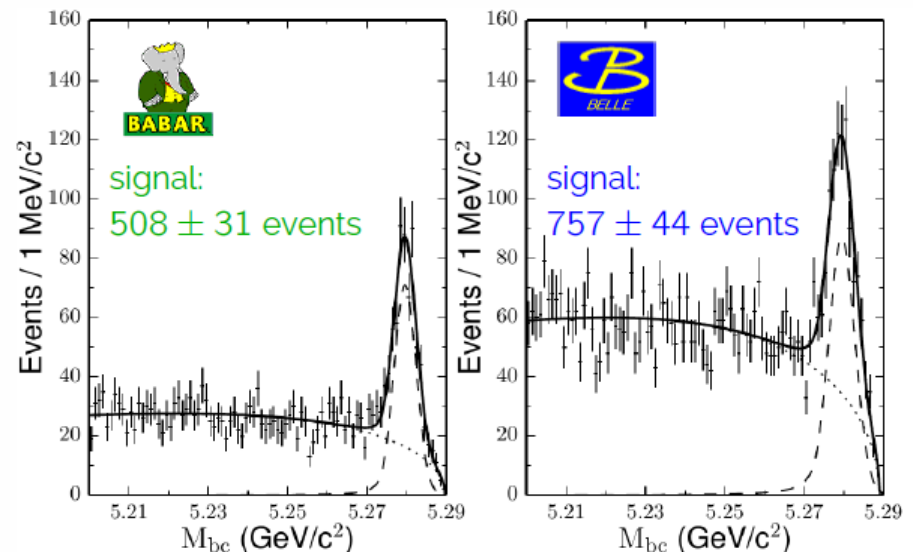


Belle + BaBar Joint Analysis

A. Abdesselam *et. al.*,  
PRL 115, 121604 (2015)

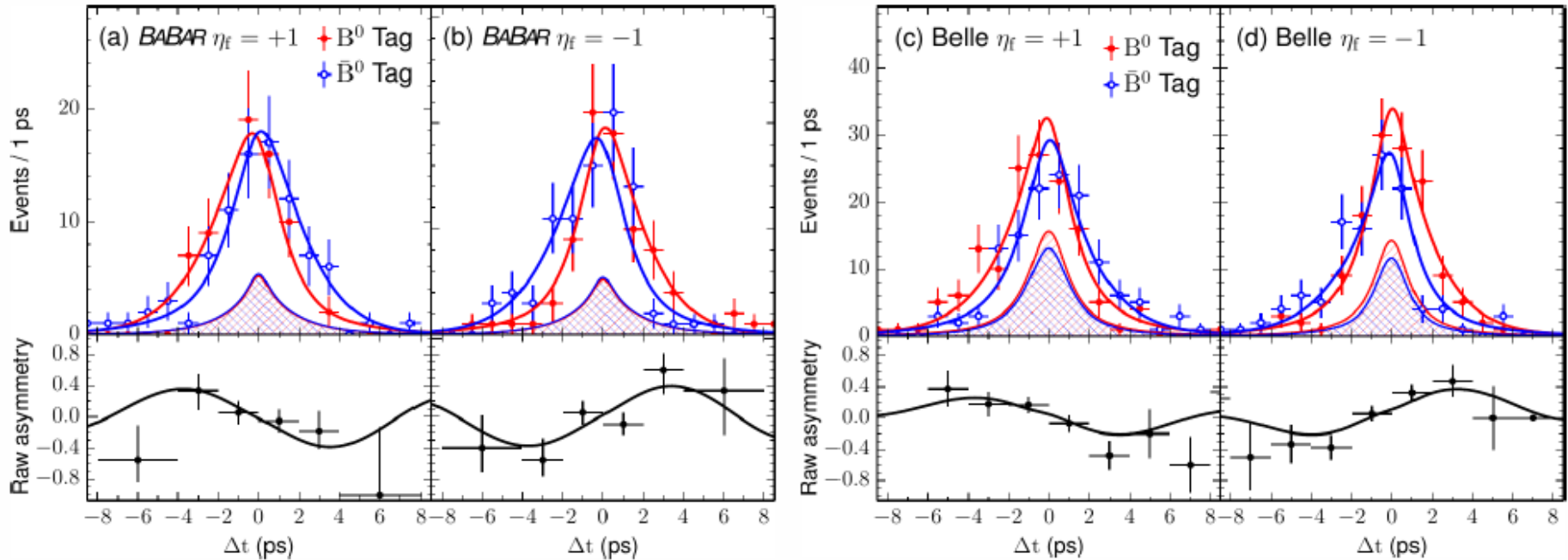
- CPV parameter  $\sin(2\phi_1)$  could be accessed, complementary to the measurement from  $b \rightarrow ccs$  transitions.
- Total 12 modes reconstructed with  $D^0 \rightarrow K^+K^-, K_S\pi^0, K_S\omega$ ;  $D^{*0} \rightarrow D^0\pi^0$  and  $h^0 = \eta, \omega, \pi^0$
- Neural Network is used to reduce the dominant continuum background
- 1D unbinned fit to the variable  $M_{bc}$  in order to extract the signal yield.

Decay mode	BABAR	Belle
$\bar{B}^0 \rightarrow D_{CP}\pi^0$	$241 \pm 22$	$345 \pm 25$
$\bar{B}^0 \rightarrow D_{CP}\eta$	$106 \pm 14$	$148 \pm 18$
$\bar{B}^0 \rightarrow D_{CP}\omega$	$66 \pm 10$	$151 \pm 17$
$\bar{B}^0 \rightarrow D_{CP}^*\pi^0$	$72 \pm 12$	$80 \pm 14$
$\bar{B}^0 \rightarrow D_{CP}^*\eta$	$39 \pm 8$	$39 \pm 10$
$\bar{B}^0 \rightarrow D_{CP}^{(*)}h^0$ total	$508 \pm 31$	$757 \pm 44$



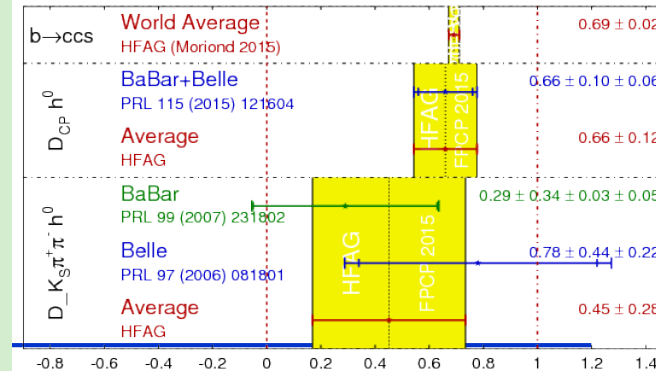


# B → D<sub>CP</sub> h<sup>0</sup>



- The time-dependent measurement is performed analyzing simultaneously the final data samples of Belle & BaBar experiments collected at Y(4S) resonance  $\sim 1.1$  /ab
- $-\eta_f S = 0.66 \pm 0.10 \pm 0.06$  ( $5.4 \sigma$  non-zero CP violation, in agreement with the CPV parameters in  $b \rightarrow ccs$ )  $\rightarrow$  first observation of CPV in this decay
- $C = -A = -0.02 \pm 0.07 \pm 0.03$  (no evidence for direct CPV)

$b \rightarrow cud \sin(2\beta) \equiv \sin(2\phi_1)$  **HFAG**  
FPCP 2015  
PRELIMINARY





# $B^0 \rightarrow \bar{D}^{(*)0} h^0$

- Similar to  $B \rightarrow D_{CP} h^0$ , but  $\bar{D}^0 \rightarrow K_S \pi^+ \pi^-$  is not a CP eigenstate, rather mixture of CP eigenstate  $K_S \rho^0$ , flavor specific  $K^{*+} \pi^-$  and  $K^{*-} \pi^+$ 
  - Standard time-dependent CP measurement does not work
    - Model independent measurement of  $\phi_1$  in  $b \rightarrow cud$  transitions using a binned Dalitz plot technique (first time for the  $\phi_1$  measurement)
    - Binned Dalitz distribution approach is originally proposed for  $\phi_3$  measurements by A. Giri *et. al.* [PRD 68, 054018 (2003)]

This approach is sensitive to  $\phi_1$  or both  $\sin 2\phi_1$  and  $\cos 2\phi_1$ .

V. Vorobyev et al.,  
PRD 94, 052004 (2016)

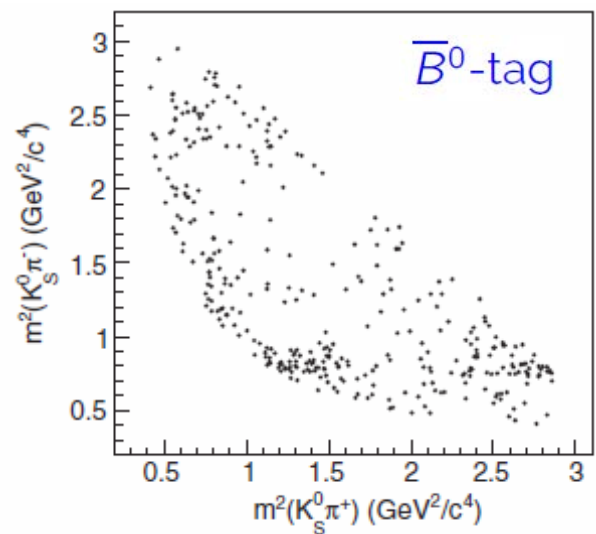
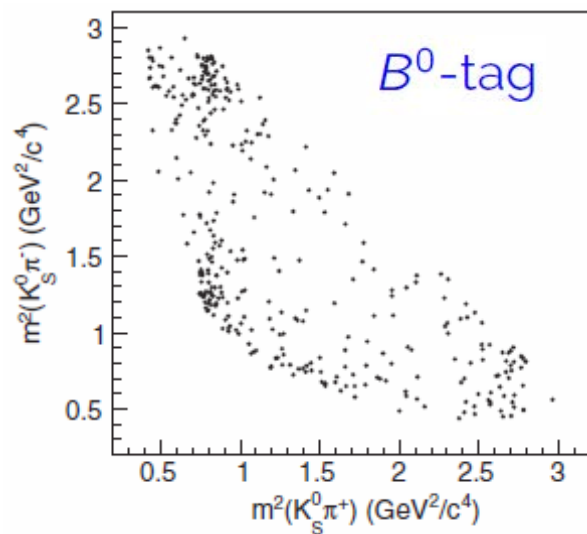
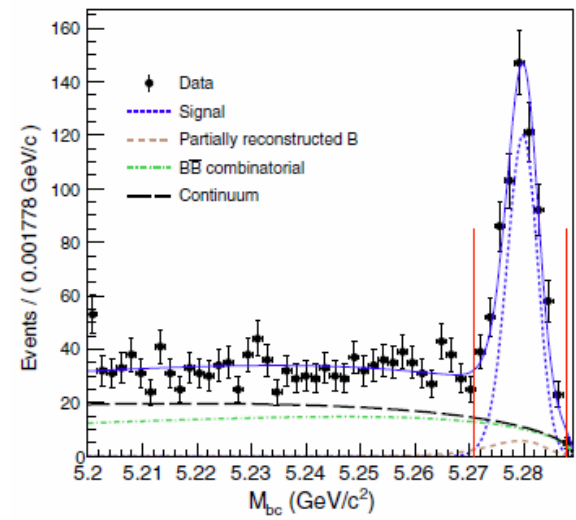
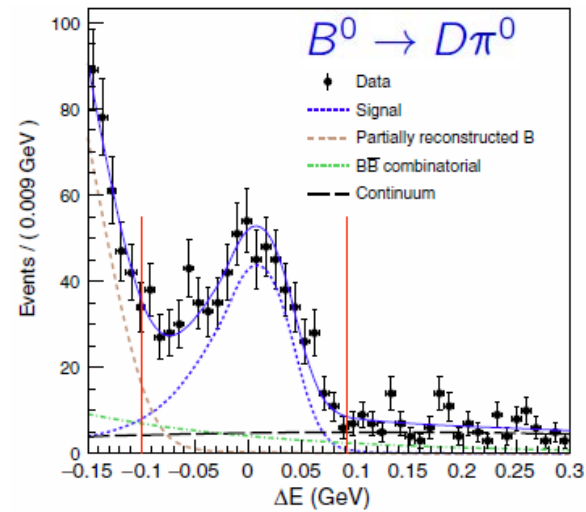




# $B^0 \rightarrow D^{(*)0} h^0$

- Standard 2D fit to  $M_{bc}$  &  $\Delta E$
- $f_{sig}$  used in the fit of the CPV parameter.

Mode	$N_{sig}$	$f_{sig}$ (%)
$B^0 \rightarrow \bar{D}^0 \pi^0$	$464 \pm 26$	$72.1 \pm 4.1$
$B^0 \rightarrow \bar{D}^0 \eta \gamma \gamma$	$99 \pm 14$	$50.5 \pm 7.0$
$B^0 \rightarrow \bar{D}^0 \eta \pi^+ \pi^- \pi^0$	$51.3 \pm 8.8$	$66 \pm 11$
$B^0 \rightarrow \bar{D}^0 \omega$	$182 \pm 18$	$58.4 \pm 5.7$
$B^0 \rightarrow \bar{D}^0 \eta'$	$28.2 \pm 6.4$	$70 \pm 16$
$B^0 \rightarrow \bar{D}^{*0} \pi^0$	$103 \pm 17$	$44.1 \pm 7.4$
$B^0 \rightarrow \bar{D}^{*0} \eta$	$36.1 \pm 7.6$	$64 \pm 13$
Total	$962 \pm 41$	$61 \pm 2.6$





# $B^0 \rightarrow D^{(*)0} h^0$

Complicated Signal PDF (TD binned analysis):

$$\mathcal{P}_i(\Delta t, \varphi_1) = h_2 e^{-\frac{|\Delta t|}{\tau_B}} \left[ 1 + q_B \frac{K_i - K_{-i}}{K_i + K_{-i}} \cos(\Delta m_B \Delta t) + 2q_B \xi_{h^0} (-1)^L \frac{\sqrt{K_i K_{-i}}}{K_i + K_{-i}} \sin(\Delta m_B \Delta t) \times (S_i \cos 2\varphi_1 + C_i \sin 2\varphi_1) \right],$$

Where

- The Dalitz probability  $K_i$  is obtained from the control sample  $B^+ \rightarrow \bar{D}^0 \pi^+$
- The strong phase parameters  $S_i$  and  $C_i$  are from coherent decay of  $D^0 \bar{D}^0$  pairs by CLEO [PRD 82, 112006(2006)]

mode	$\sin 2\phi_1$	$\cos 2\phi_1$
$B^0 \rightarrow D\pi^0$	$0.61 \pm 0.37$	$0.88^{+0.46}_{-0.52}$
$B^0 \rightarrow D\omega$	$-0.12 \pm 0.58$	$1.28^{+0.62}_{-0.69}$
others	$0.44 \pm 0.51$	$0.89^{+0.49}_{-0.55}$
<b>combined</b>	$0.43 \pm 0.27 \pm 0.08$	$1.06 \pm 0.33^{+0.21}_{-0.15}$

↓

$$\phi_1 = 11.7^\circ \pm 7.8^\circ \pm 2.1^\circ$$

The value  $\sin 2\phi_1 = 0.691 \pm 0.017$  in  $b \rightarrow ccs$  golden mode gives two solutions

- $\phi_1 = 21.9^\circ$  (1.3 standard deviations away)
- $\phi_1 = 68.1^\circ$  (5.1 standard deviations away)

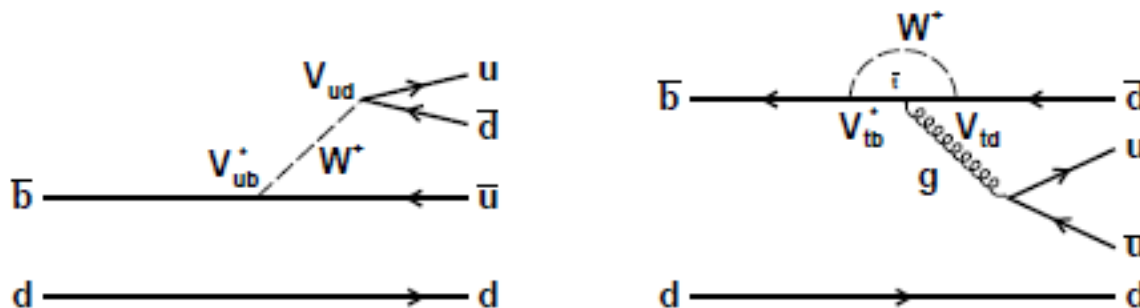
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Our result definitely disfavored the second solutions obtained from the golden mode



# $B^0 \rightarrow \rho^+ \rho^-$

- Mixing-induced CPV in this decay is sensitive to the parameter  $\phi_2 = \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ub}V_{ud}^*}\right)$



- If tree only, then  $S_f$  is directly connected to  $\sin(2\phi_2)$  and  $A_f=0$
- Penguin contribution shift the measured angle to  $\phi_2^{\text{eff}} = \phi_2 + \Delta\phi_2$ ;  $\Delta\phi_2$  can be extracted from an isospin analysis or SU(3) flavor symmetry.

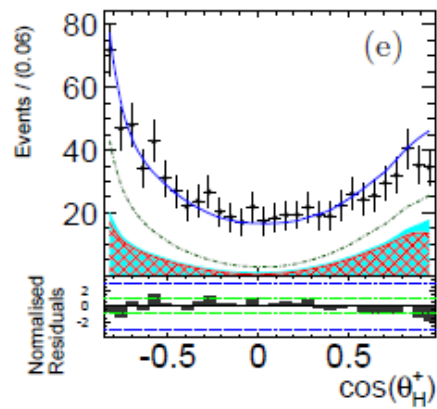
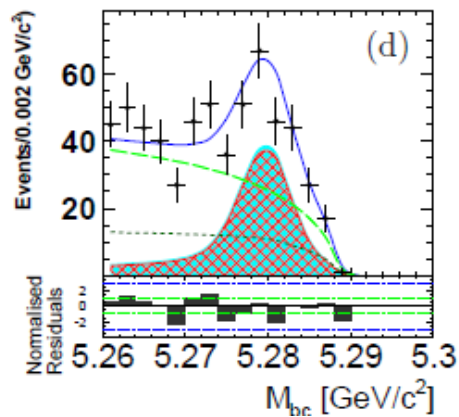
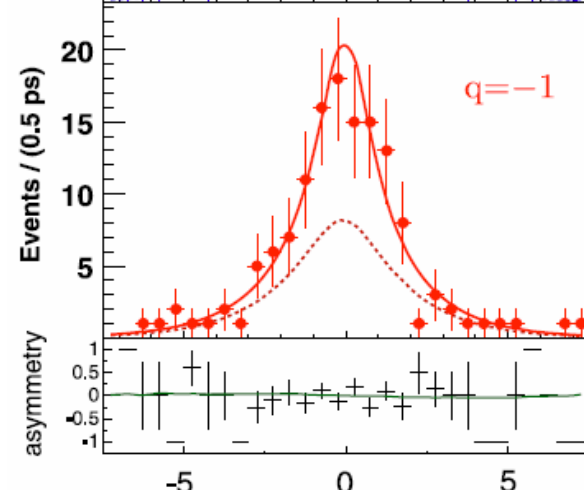
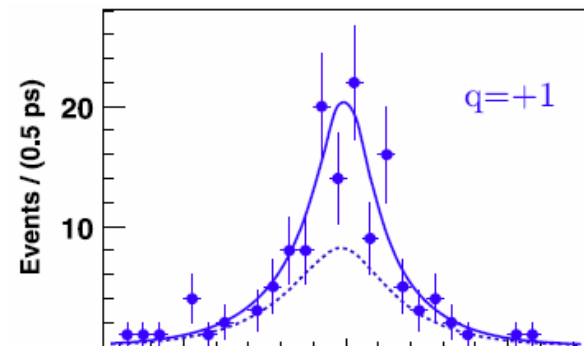
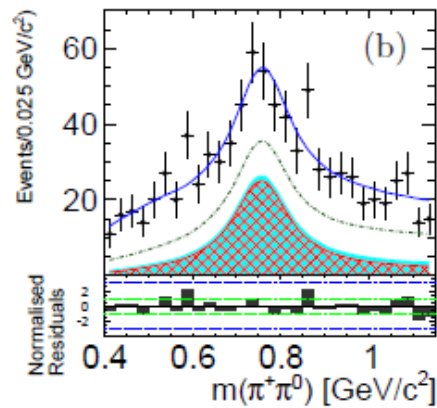
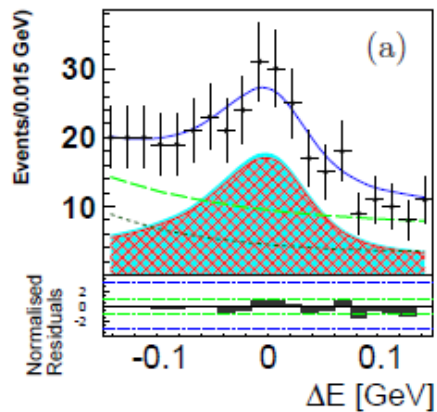
- Previous Belle publication with  $535 \times 10^6$  BB  
[PRD 76, 011104 (2007)]
- This analysis uses full set of Belle Data
- Fisher discriminant is used to reduce the continuum background

P. Vanhoefer *et. al.*,  
PRD 93, 032010 (2016)



# $B^0 \rightarrow \rho^+ \rho^-$

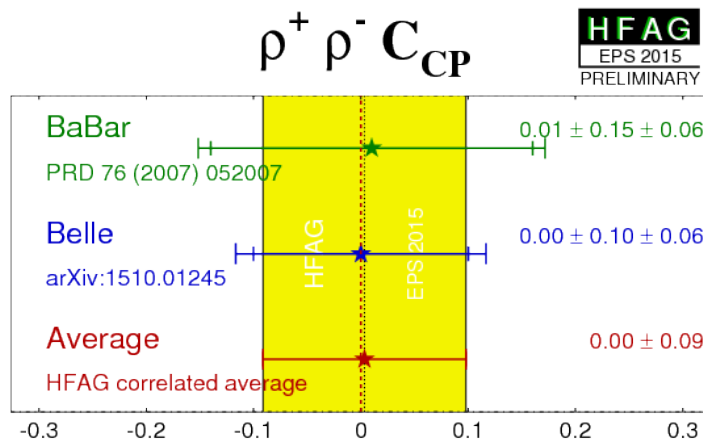
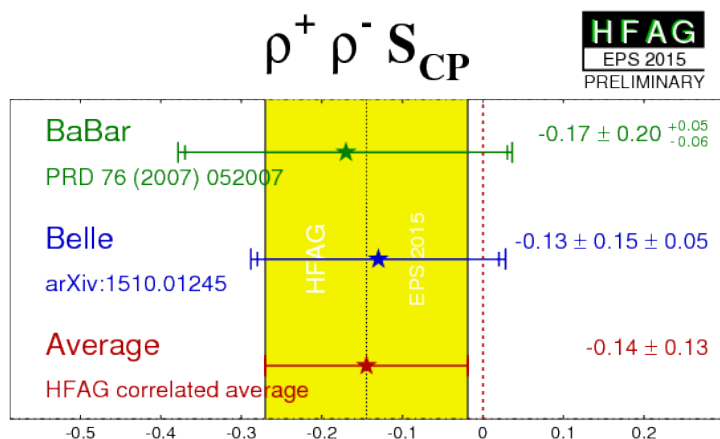
9D MLH fit to  $\Delta E$ ,  $M_{bc}$ ,  $\mathcal{F}_{S/B}$ ,  $m_1(\pi^+ \pi^0)$ ,  $m_2(\pi^- \pi^0)$ ,  $\cos \theta_H^+$ ,  $\cos \theta_H^-$ ,  $\Delta t$ ,  $q$





# $B^0 \rightarrow \rho^+ \rho^-$

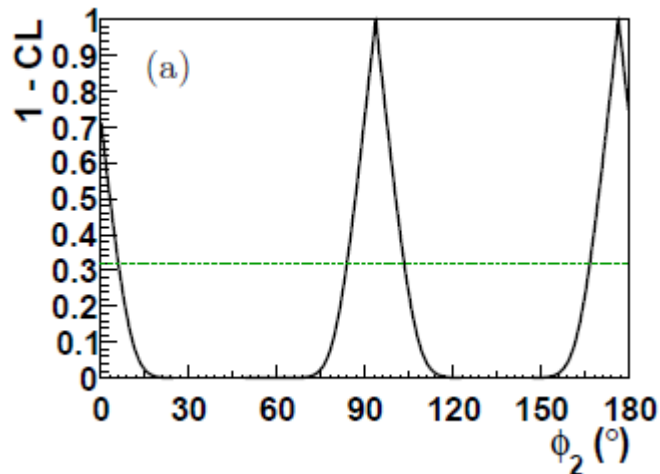
$$\begin{aligned} \mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) &= (28.3 \pm 1.5 \text{ (stat)} \pm 1.5 \text{ (syst)}) \times 10^{-6}, \\ f_L &= 0.988 \pm 0.012 \text{ (stat)} \pm 0.023 \text{ (syst)}, \\ \mathcal{A}_{CP} &= 0.00 \pm 0.10 \text{ (stat)} \pm 0.06 \text{ (syst)}, \\ \mathcal{S}_{CP} &= -0.13 \pm 0.15 \text{ (stat)} \pm 0.05 \text{ (syst)}. \end{aligned}$$



These are the most precise measurements to date for this decay mode. An improvement of a factor of 2 is achieved compared to previous Belle analysis.

# $B^0 \rightarrow \rho^+ \rho^-$

Isospin analysis is performed with inputs also from Belle's  $\rho^0 \rho^+$  and  $\rho^0 \rho^0$  measurements. [PRD 89,072008 (2014); PRL 91, 221801(2003)]



- Two solutions are found, one consistent with SM is  $(93.7 \pm 10.6)$  deg.
- Also the size of penguin contribution is consistent with zero,  $(0.0 \pm 9.6)$  deg

• BaBar:  $\alpha = (92.4^{+6.0}_{-6.5})^\circ$



# Summary

- First observation of the decay  $B^0 \rightarrow \psi(2S)\pi^0$  is presented, this decay mode can be used in future to measure  $\phi_1$
- First observation of CPV in  $B \rightarrow D_{CP}h^0$  is presented using BaBar + Belle joint analysis, which was not possible without combining.
- Result of model-independent time-dependent binned Dalitz plot for  $B \rightarrow D^{(*)0}h^0$  is presented.
- $\phi_2$  from  $B \rightarrow \rho\rho$  decays is presented
  - But that's not all – Belle still has number of analyses in preparation for  $\phi_1$  and  $\phi_2$  measurements
  - Many years after it's shutdown Belle still producing interesting results and expecting many more from the upcoming Belle II
  - Specially, modes with  $h^0$  are more interesting with Belle II statistics which may not be so easy by LHCb