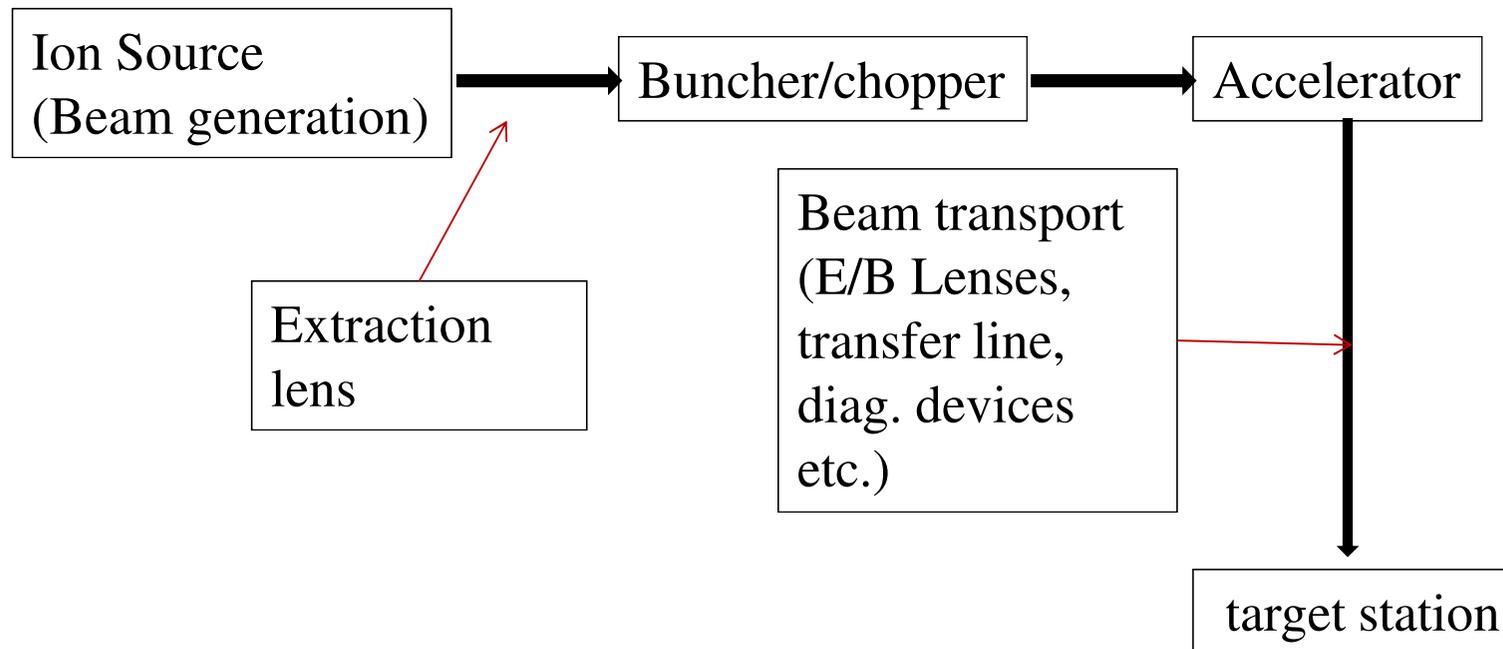


# ACCELERATOR

Interaction of “q” with static/dynamic E/B & Technical realization

Controlled Manipulation of an ensemble of charged particles



# Brief history of accelerators

- 1919 Rutherford gets the first nuclear reactions using natural alpha rays (radio activity) of some MeV.  
« He notes already that he will need many MeV to study the atomic nucleus »
- 1932 Cockcroft & Walton build a 700 KV electrostatic generator and break Lithium nucleus with 400 KeV protons.  
(Nobel Price in 1951)
- 1924 Ising proposes the acceleration using a variable electric field between drift tubes ( the father of the Linac).
- 1928 Wideroe uses Ising principle with an RF generator, 1MHz, 25 kV and accelerate potassium ions up to 50 keV.
- 1929 Lawrence driven by Wideroe & Ising ideas invents the cyclotron.
- 1931 Livingston demonstrates the cyclotron principle by accelerating hydrogen ions up to 80 KeV.

## Brief history of accelerators

- 1932 The cyclotron of **Lawrence** produces protons at 1.25 MeV and « breaks atoms » a few weeks after **Cockcroft & Walton**  
*(Nobel Prize in 1939)*
- 1923 **Wideroe** invents the concept of betatron
- 1927 **Wideroe** builds a model of betatron but fails
- 1940 **Kerst** re-invents the betatron which produces 2.2 MeV electrons
- 1950 **Kerst** builds a 300 MeV betatron

Electrons , Protons, Heavy Ions: non-relativistic, relativistic

Antiparticles : p/e on heavy Z target  $\rightarrow \bar{p}, e^+$

$\rightarrow$  cooling/damping ring, accumulator ring

Beam +Fixed target

Collider

Non-relativistic : E increases  $\rightarrow$  v increases

Relativistic : v  $\sim$  constant, differences in beam dynamics vanish

Beam intensity /luminosity = e Z  $\dot{N}$

Pulsed beam : instantaneous current, average current

# Types of accelerators

	Kinetic energy W	
	Electrons	Protons/ions
Electrostatic Van de Graaf & Tandems		20-35 MeV (Vivitron)
Betatron	10-300 MeV	
Microtron	25-150 MeV	
Cyclotron		10-100 MeV
Synchro-cyclotron		100-750 MeV
Synchrotron	1-10 GeV	1-1000 GeV
Storage ring	1-7 GeV (ESRF)	
Collider ring	10-100 GeV (LEP)	1-7 TeV (LHC)
Linacs	20 MeV-50 GeV (SLC)	50-800 MeV (LAMPF)
Linear collider	50-1000 GeV (TESLA)	

Total energy = Rest energy + Kinetic energy

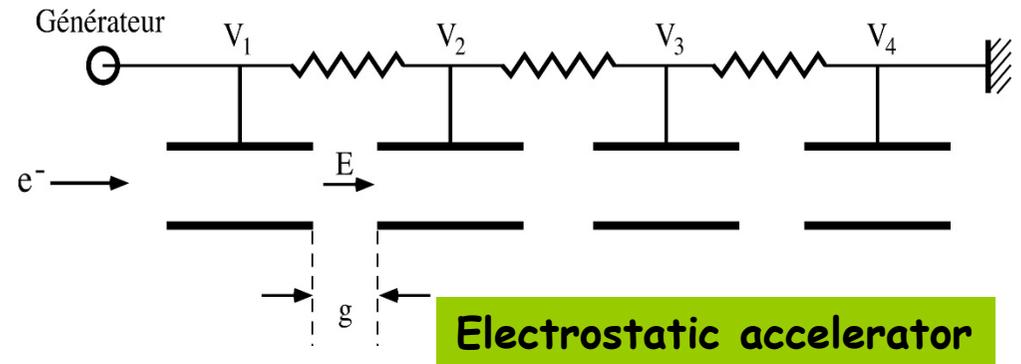
$$\begin{array}{l} \uparrow \\ \uparrow \end{array} = E_0 + W \quad \begin{array}{l} \uparrow \\ \uparrow \end{array} E_0 = m_0 c^2 \Rightarrow \begin{array}{l} \text{electron } E_0 = 0,511 \text{ MeV} \\ \text{protons } E_0 = 938 \text{ MeV} \end{array}$$

# Methods of Acceleration

## 1\_ Electrostatic Field

Energy gain :  $W = n \cdot e \cdot (V_2 - V_1)$

limitation :  $V_{\text{generator}} = \sum V_i$



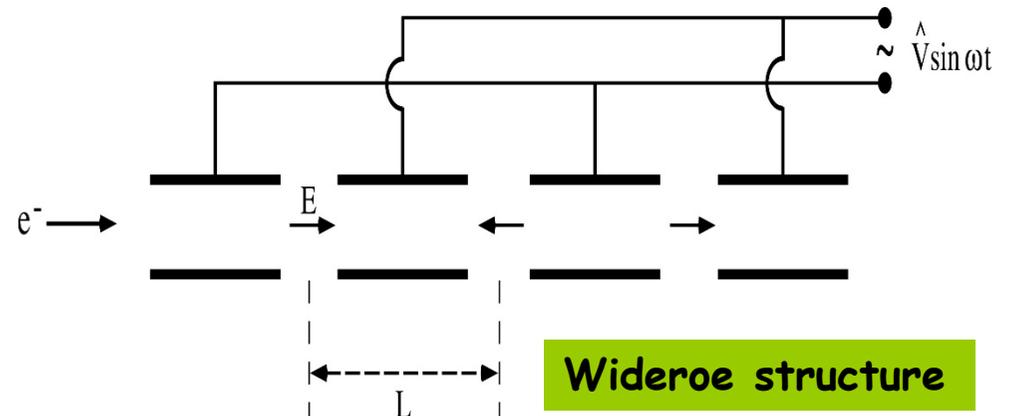
## 2\_ Radio-frequency Field

Synchronism :  $L = vT/2$

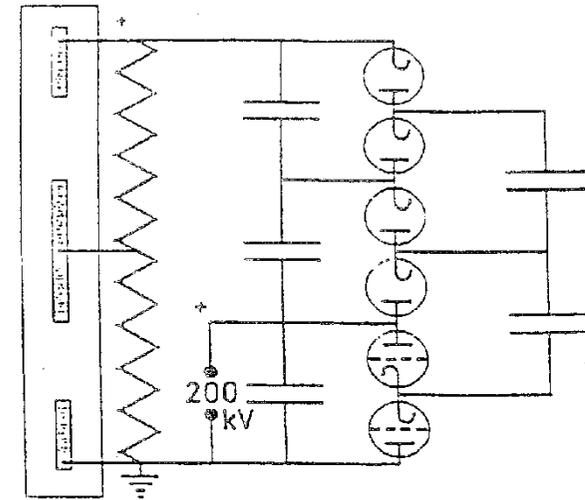
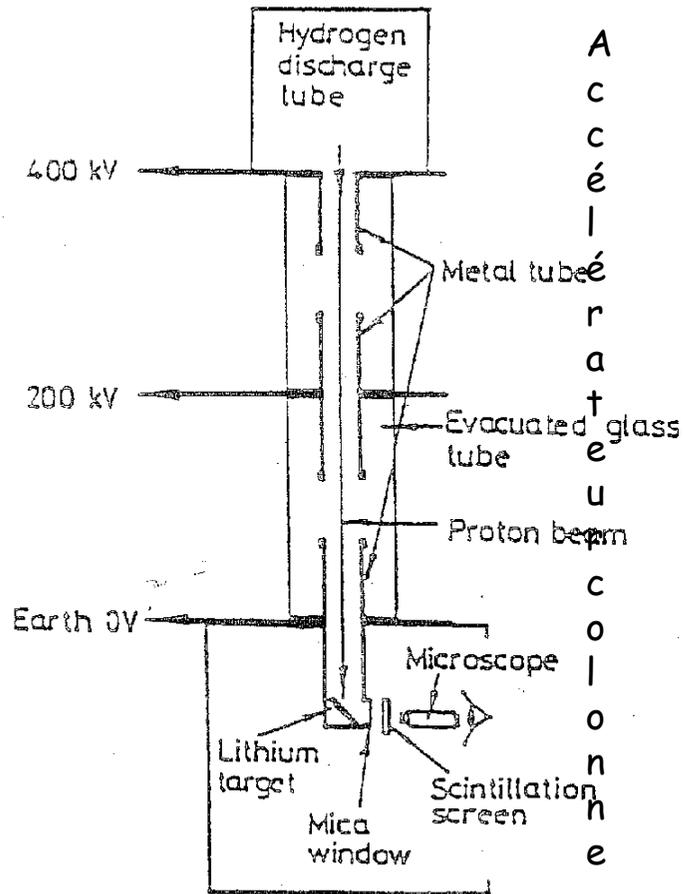
$v$  = particle velocity

$T$  = RF period

also : 
$$L = v \frac{T}{2} = \beta \frac{\lambda_0}{2}$$



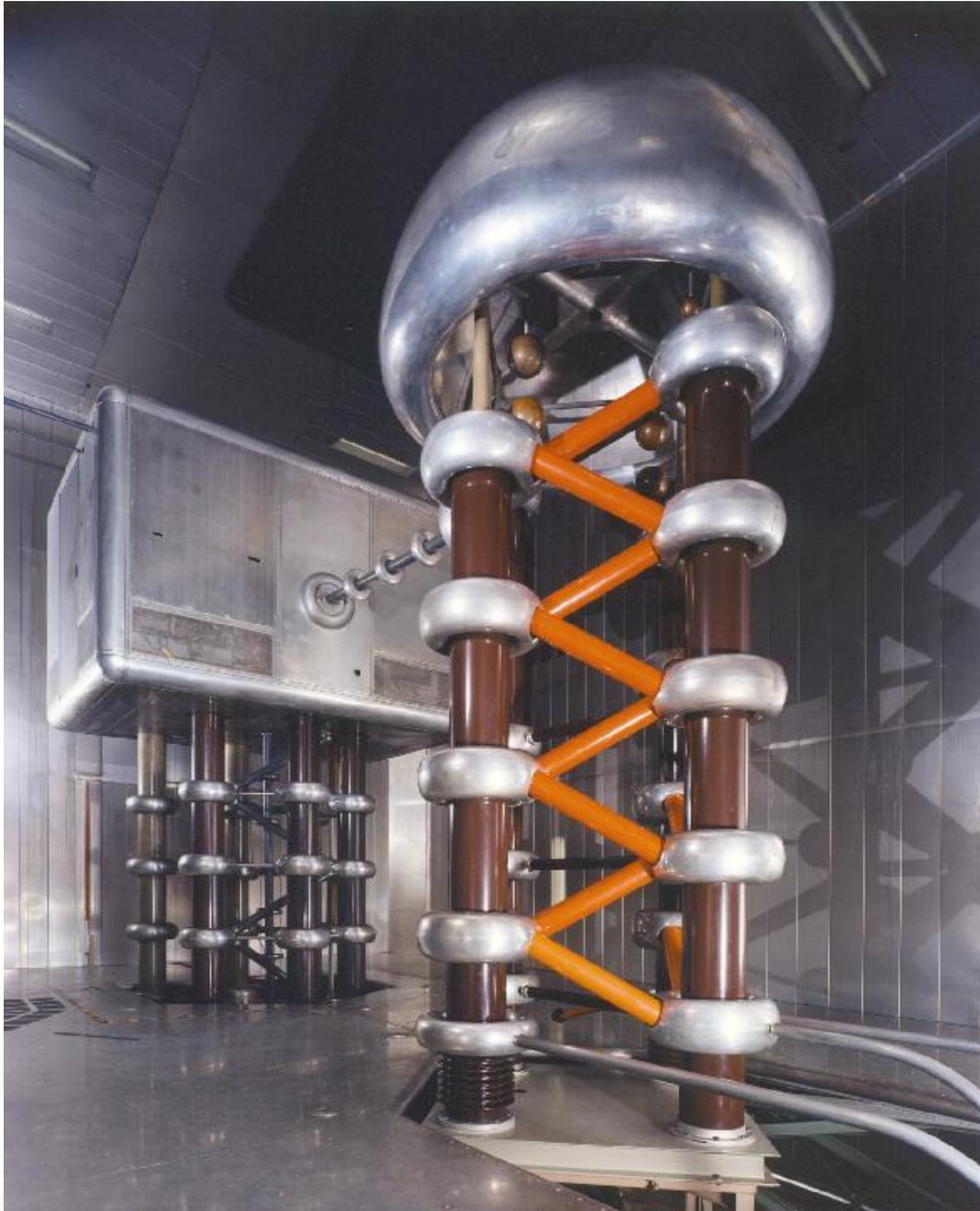
# Electrostatic accelerator



d.c. high voltage generator

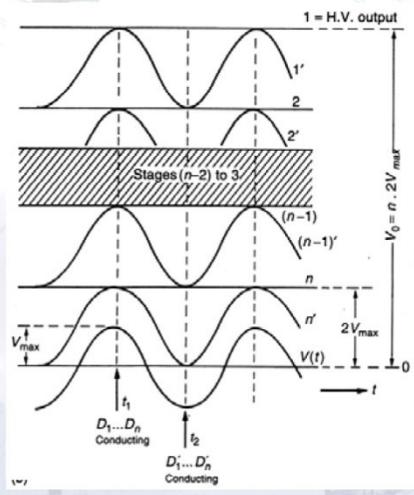
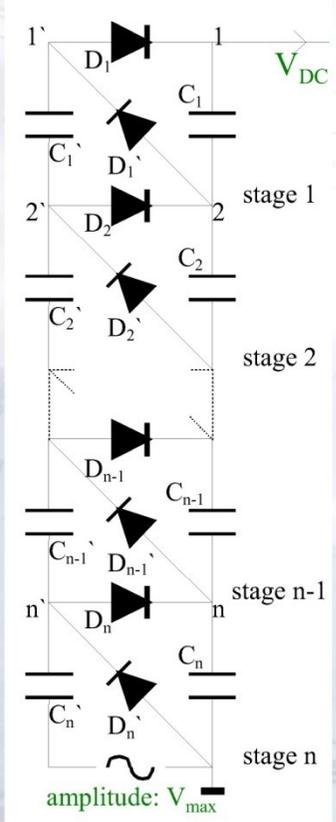
Accelerating column

HV system used by Cockcroft & Walton to break the lithium nucleus



Because of its simplicity of design, the Cockcroft and Walton accelerator is in use today to provide sources of neutrons ( ${}^2\text{H} + {}^2\text{H} \rightarrow \text{n} + {}^3\text{He}$  can be done successfully at a few hundred keV) and also as an injector of particles, especially protons, for high energy accelerators.

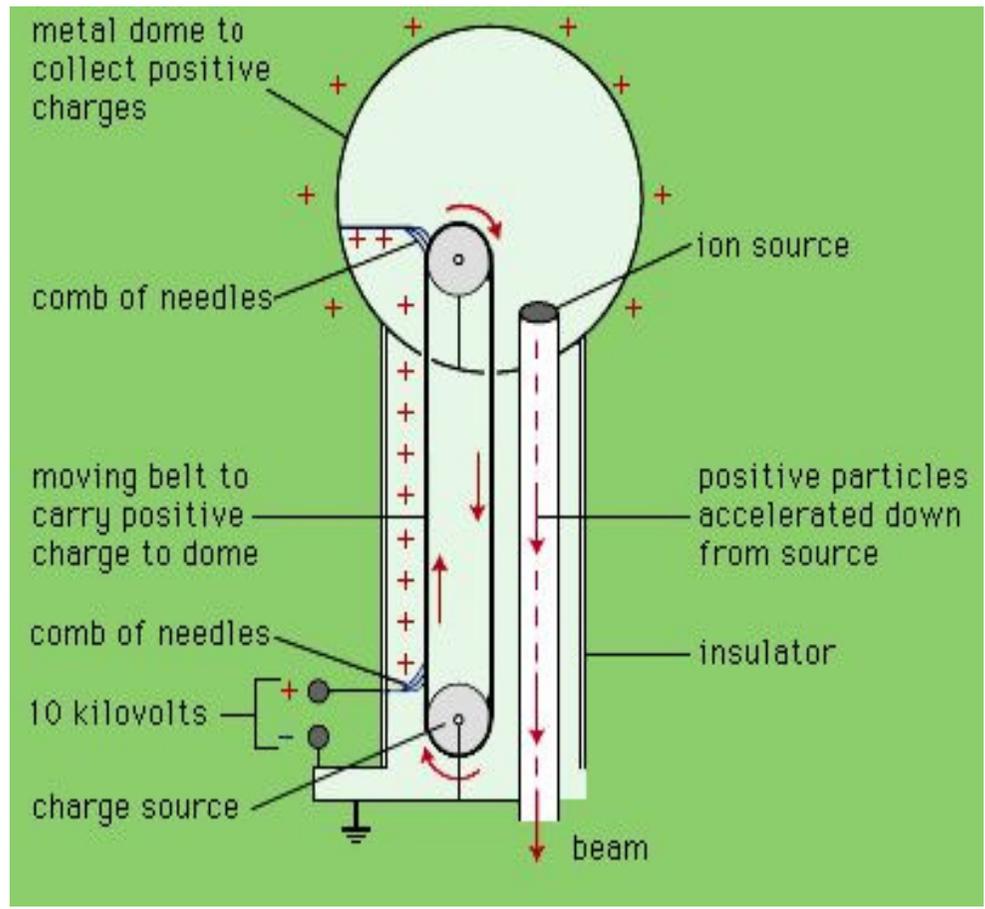
# Cascaded Rectifier (Greinacher; Cockcroft - Walton)

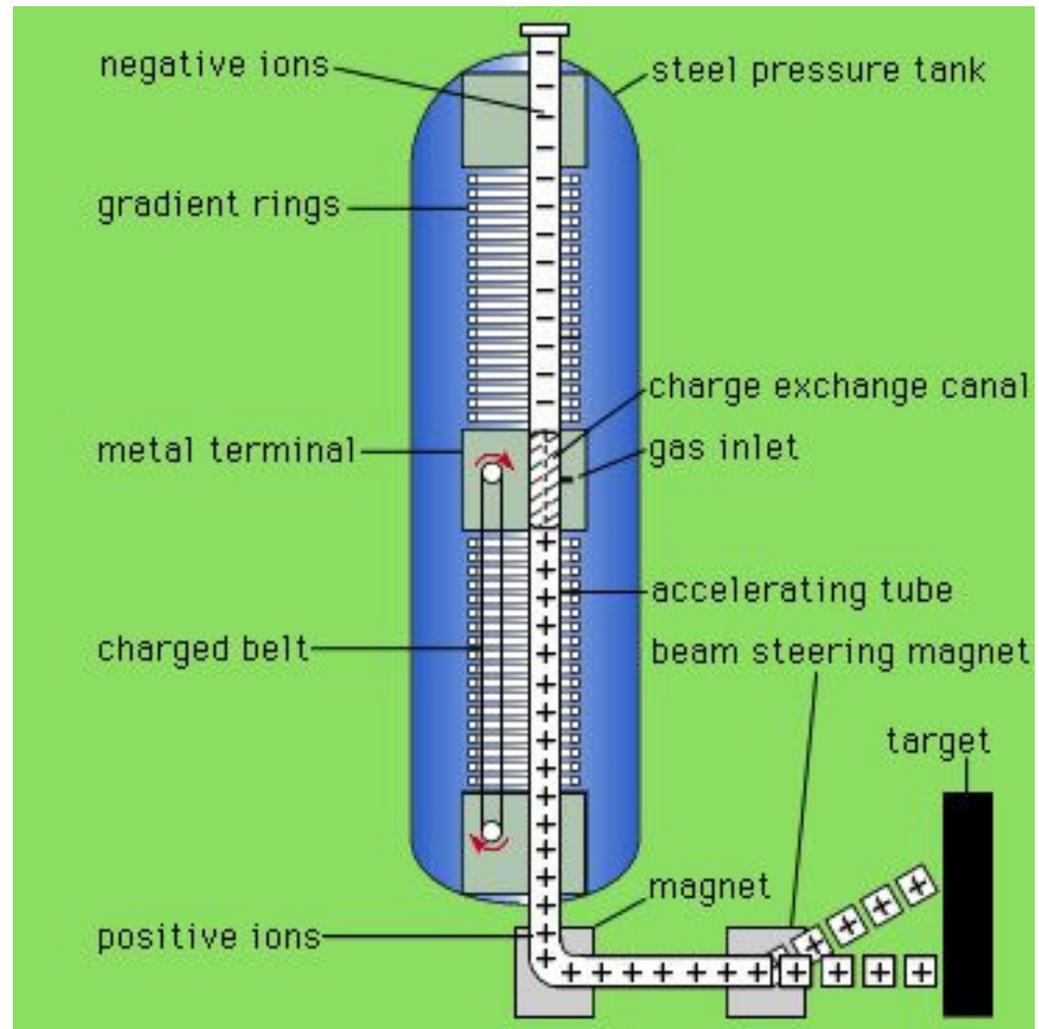


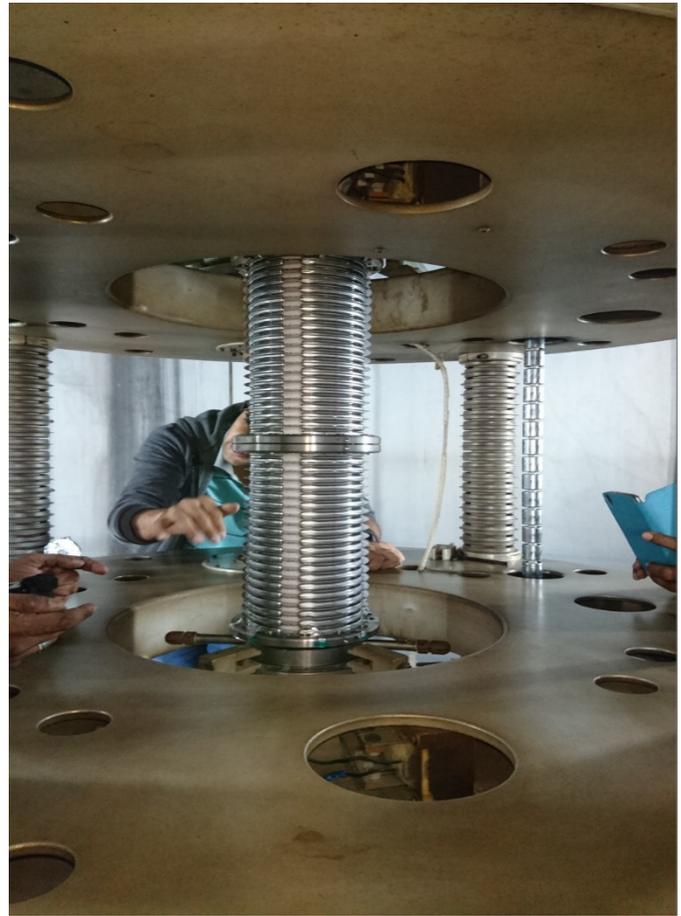
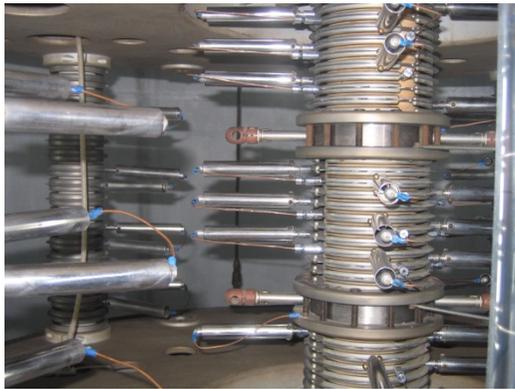
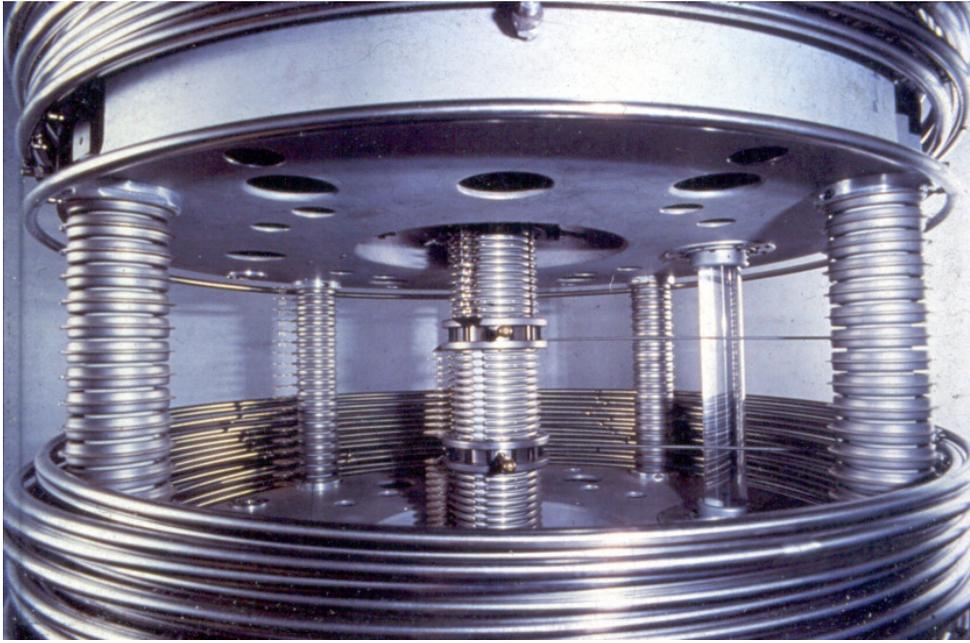
$$V_{DC} = 2nV_{max}$$

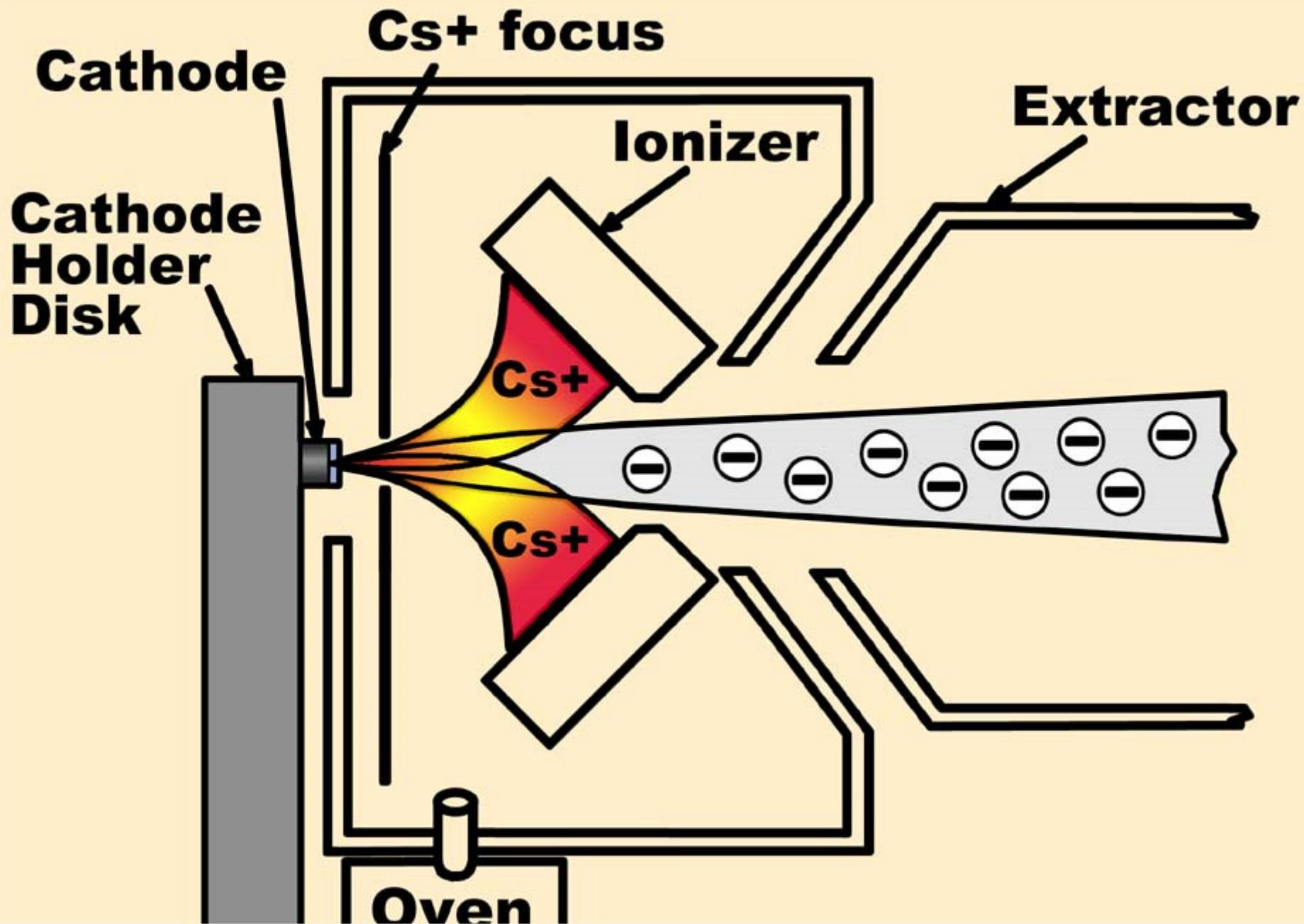
Voltage: 2 MV

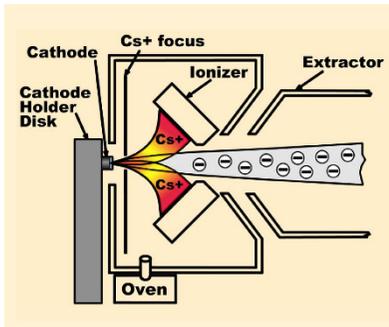
Reduce  $\delta V$  ( $\sim n^2$ ) and  $\Delta V$  ( $\sim n^3$ ) by:  
 larger C's (more energy in cascade)  
 higher f (up to tens of kilohertz)



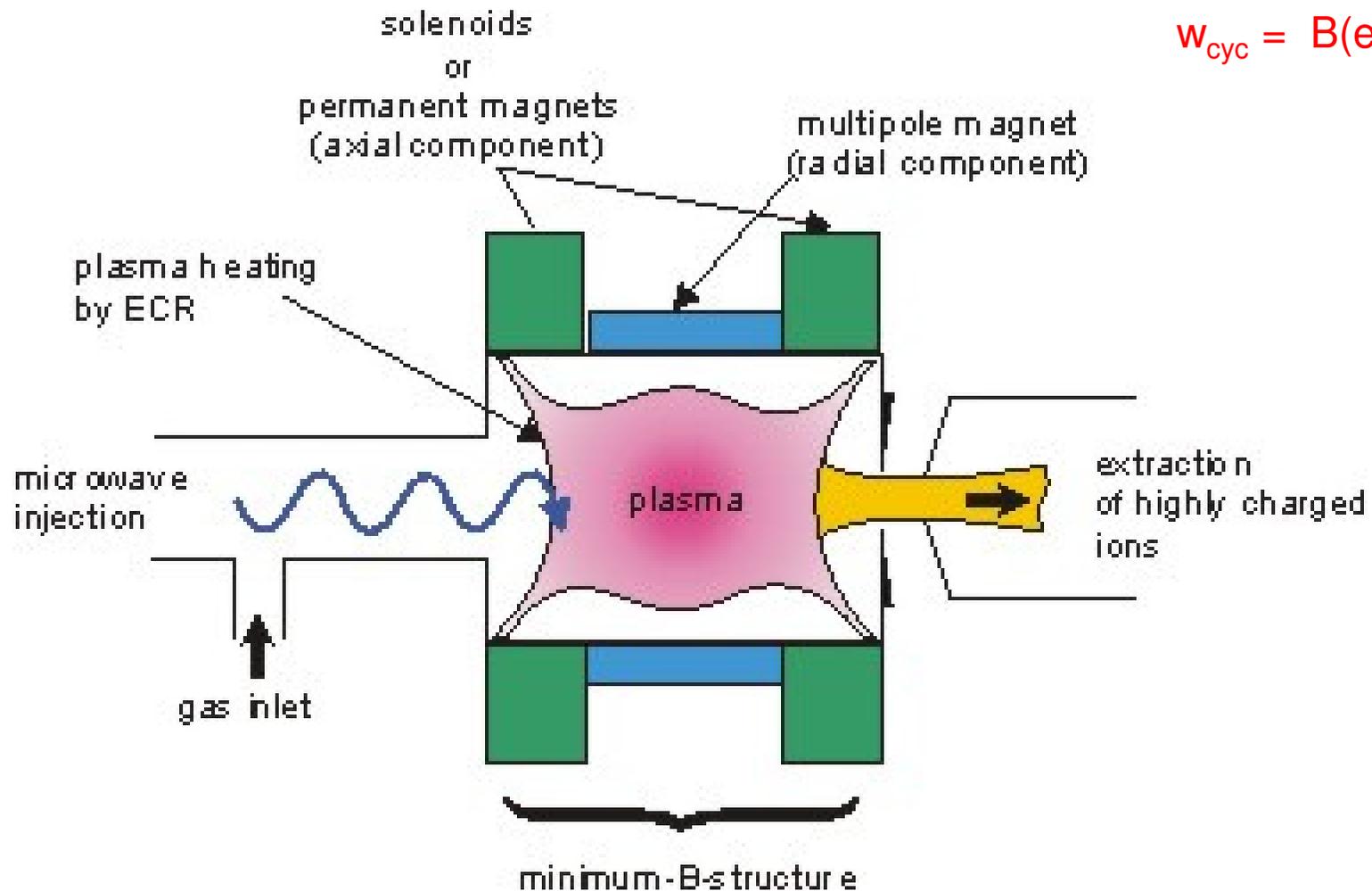






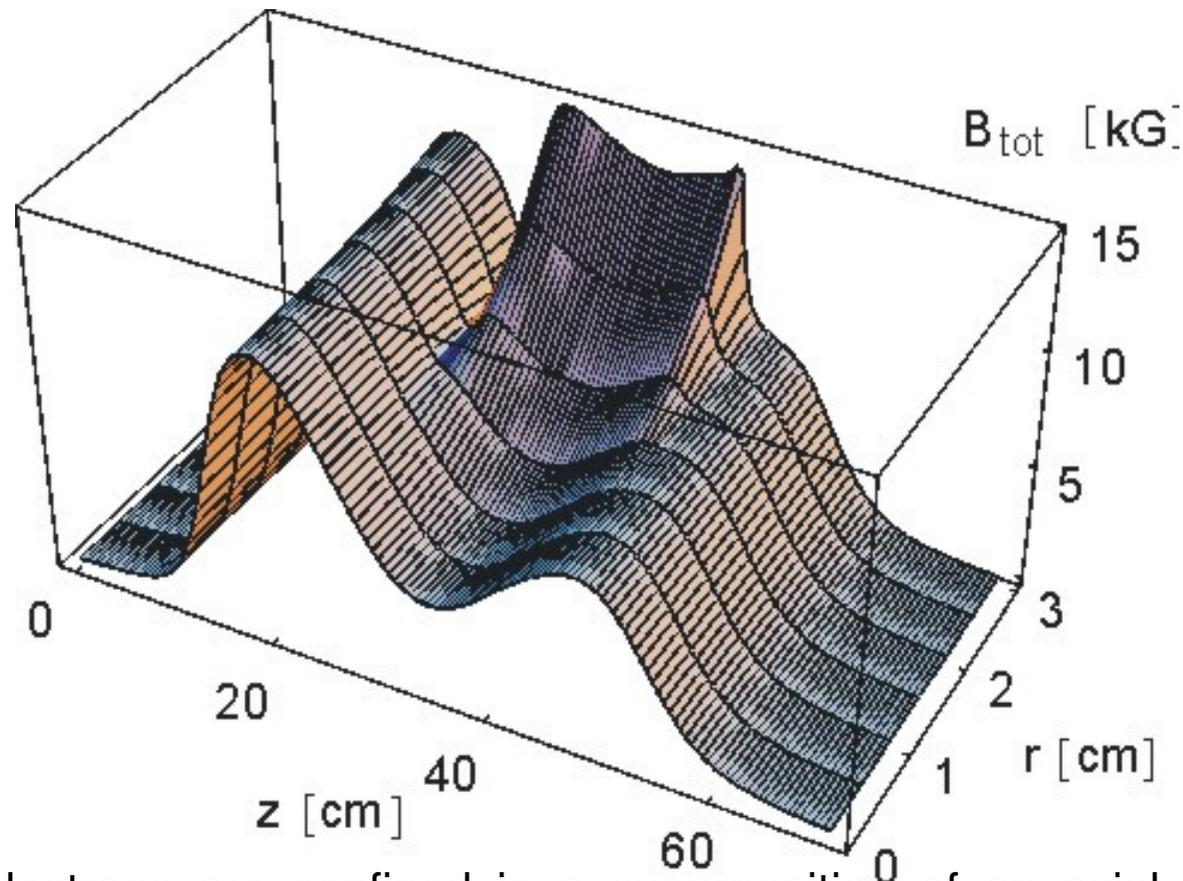


- Cesium vapour comes from the cesium oven into area between the cooled cathode and the heated ionizing surface.
- Some of the cesium condenses on the front of the cathode and some of the cesium is ionized by the hot surface.
- The ionized cesium accelerates towards the cathode, sputtering particles from the cathode through the condensed cesium layer.
- Some materials will preferentially sputter negative ions. Other materials will preferentially sputter neutral or positive particles which pick up electrons as they pass through the condensed cesium layer, producing negative ions



only electron beam ion sources (EBIS) and electron cyclotron resonance (ECR) ion sources are capable of producing highly charged ions of all natural elements with  $Q$  (charge state)/ $Z$  (atomic number)  $> 0.5$ .

$$\omega_{\text{cyc}} = B(e/m)$$

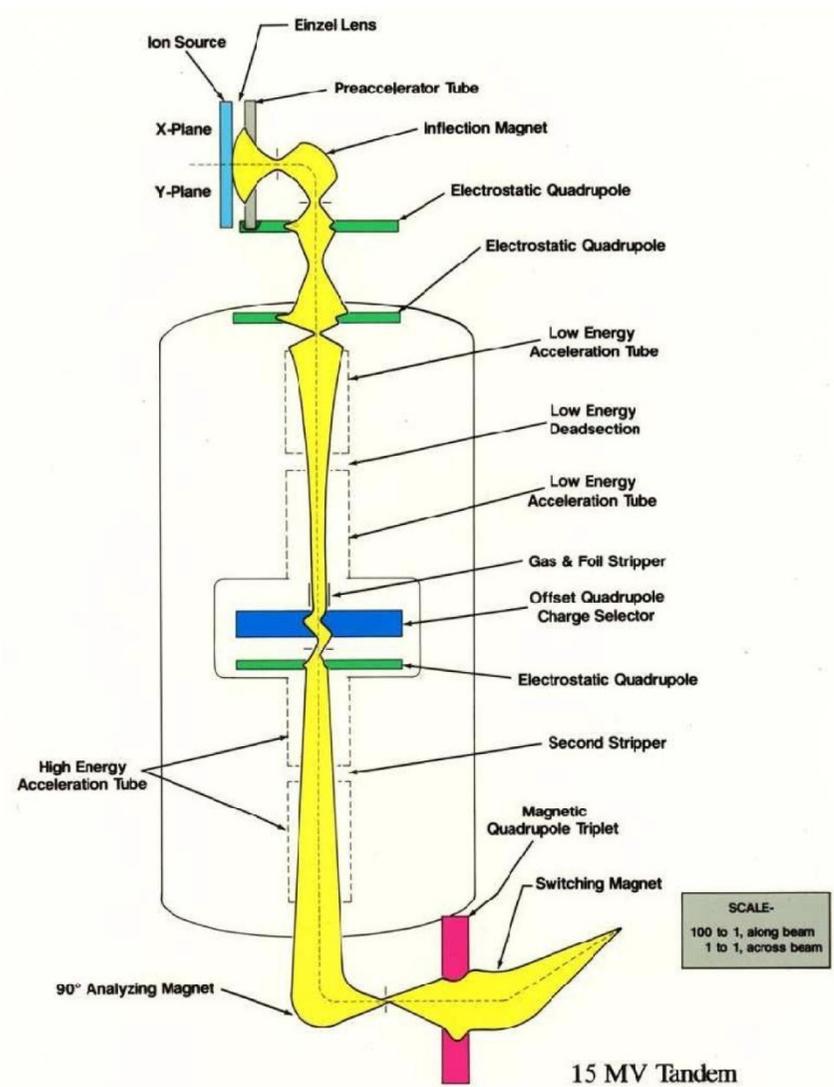


- The plasma electrons are confined in a superposition of an axial magnetic field component (produced by solenoids / permanent magnets) and the radial magnetic field of a multipole magnet. This results in a so-called *minimum-B-structure*- minimum in the middle of the structure and increases in all directions.
- A closed surface is created where the electron cyclotron resonance condition is fulfilled. Electrons passing through that surface can be accelerated resonantly.
- Furthermore, a high mirror ratio of the magnetic field leads to long confinement times for the plasma electrons.
- multiple passes, gain high energies and yield high charge states via successive single ionization.

High Voltage measurement  
Secondary electrons  
Corona discharges  
SF6 for high dielectric constant

Stable operation  
Excellent beam emittance  
Precise energy  
Ease of energy variation

Nuclear Physics, Material science, Industry,  
AMS



**Fig. 8:** Beam envelopes in a 15 MV Tandem accelerator from NEC (courtesy of G. A. Norton, NEC)

# LINAC

## Advantages

- Can handle high beam currents
- High duty cycle
- Low radiation losses

## Draw backs

- space and cavity consuming
- The synchrotron radiation damping of e-/e+ used to reduce native beam emittance

## Main Usage

- Low energy injectors (high duty cycle, dominated by space-charge force)
- High intensity/power beams
- ILC at very high energy (no radiation losses)

# Methods of Acceleration

## Radio-frequency Field

Synchronism :

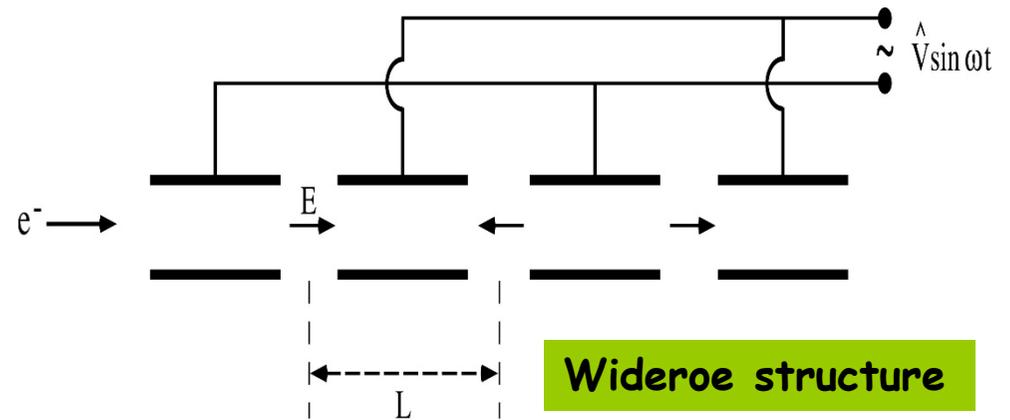
$$L = vT/2$$

$v$  = particle velocity

$T$  = RF period

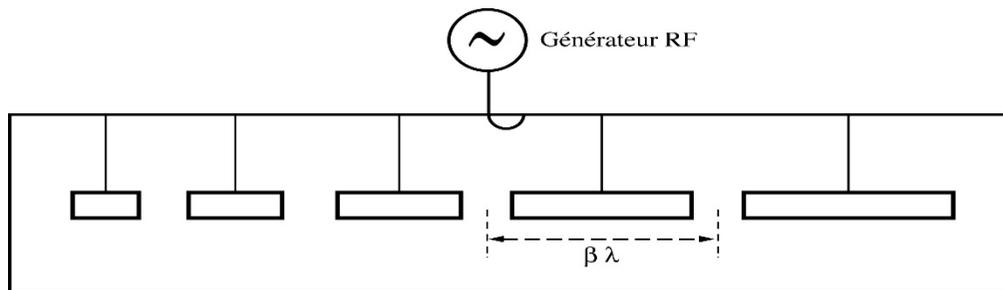
also :

$$L = v \frac{T}{2} = \beta \frac{\lambda_0}{2}$$



**Wideroe structure**

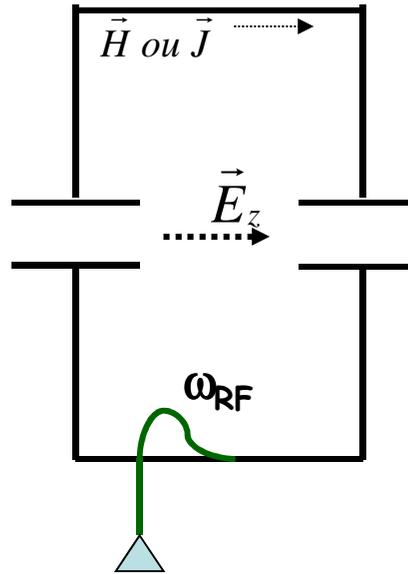
radiated power  $\propto \omega CV$



*In order to reduce the radiated power, the gap is enclosed in a resonant volume at the operating frequency.*

**ALVAREZ structure**

# The advantage of Resonant Cavities



- Each such cavity can be independently powered from the RF generator.

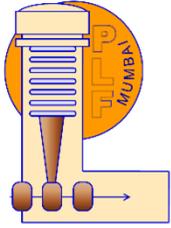
- The electromagnetic power is now constrained in the resonant volume.

- Note however that joule losses will occur in the cavity walls (unless made of superconducting materials)

- Considering RF acceleration, it is obvious that when particles get high velocities the drift spaces get longer and one loses on the efficiency. The solution consists of using a higher operating frequency.

- The power lost by radiation, due to circulating currents on the electrodes, is proportional to the RF frequency. The solution consists of enclosing the system in a cavity which resonant frequency matches the RF generator frequency.

- The RF resonator with suitably designed drift tubes constitutes the basic accelerating structure in LINACs
- Particles in synchronisation with the phase of the RF voltage.
- A finite electrical resistance of the internal surfaces of the cavity results in loss of RF power and the quality factor  $Q$  of the cavity is a measure of this loss.
- The power dissipation can be reduced drastically by using superconducting surfaces, whereby  $Q$  values in the range  $10^8$ - $10^9$  can be obtained.
- Accelerating fields for heavy ions  $\sim 3$  MV/m can be easily achieved for RF power dissipation of  $\sim 5$ – $10$  watts.



## Why superconducting?

$Q=f/\Delta f=\omega U/P$  ; Quality factor

QWR:  $f=150\text{MHz}$ ,  $\omega\sim 10^9$

$E\sim 3\text{ MV/m}$

U (stored energy)  $\sim 0.5\text{ Joules}$

$Q(\text{Cu}, 300\text{K})\sim 10^4$ ;  $P\sim 50\text{ kWatts}$

$Q(\text{Pb}, 4.2\text{K})\sim 10^8$ ;  $P\sim 5\text{ Watts}$

$\epsilon(4.2\text{K}:300\text{K})\sim 1:750$

**Superconducting LINAC smaller & efficient**

Use of superconducting technology leads to  
considerable saving of electrical power  
a compact accelerator design

simplifies the RF control electronics since the power levels are  
low.

**Remember:** even in the superconducting state, the AC surface  
resistance  $R_s$  is not zero but has a finite though small value;  $R_s$  is a  
function of  $f$ ,  $T_C$  and temperature

At higher power levels, the surface magnetic and electric fields in  
the resonator become very large and the power dissipation is  
dominated by losses at high magnetic fields due to flux penetration  
and at high electric fields due to field emission.

In addition, thermal breakdown of superconductivity can occur due  
to the presence of small defect regions on the superconducting  
surface. *careful design and fabrication of resonators is essential  
to maintain high  $Q$  values at very high accelerating field values.*

Purity of the material RRR

Transit Time factor  $T(\beta) < 1$  → velocity acceptance of linac

Average electric field  $E = \frac{V}{l}$

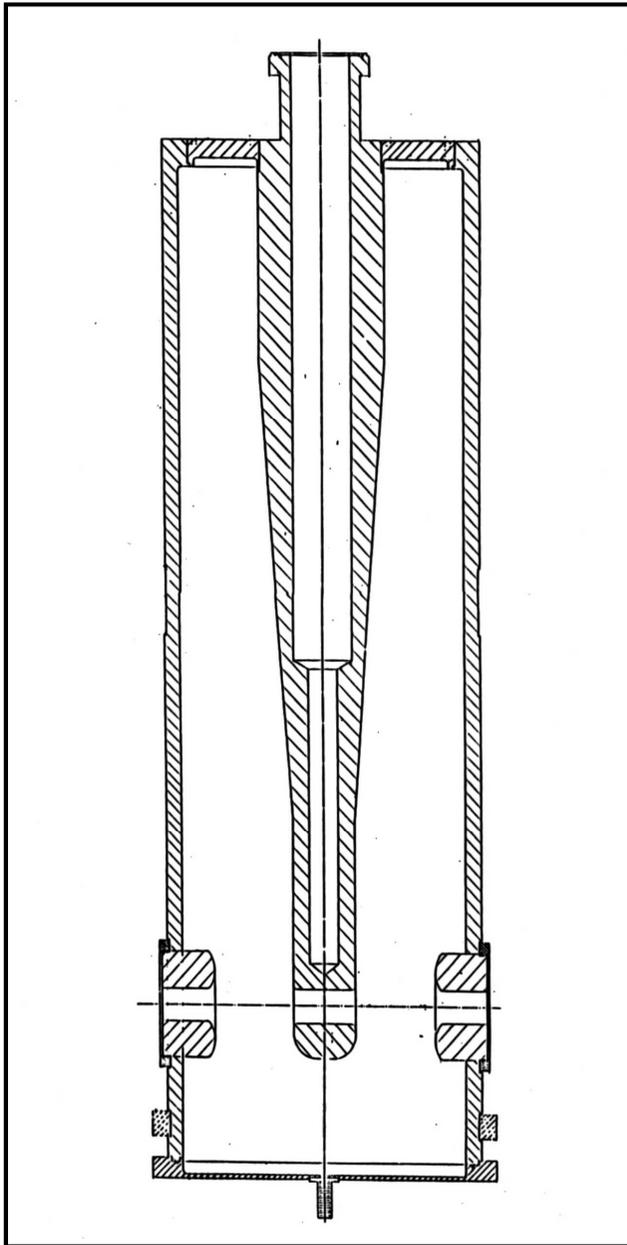
Effective shunt Impedance of the cavity – geometry dependence

$$ZT^2 = \frac{(\Delta U'_{max})^2}{2P'_d}$$

$\Delta U'_{max}$  : *max energy gain per unit length*

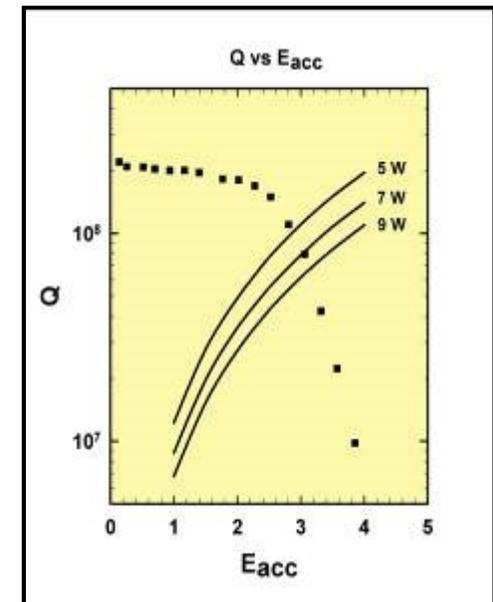
$P'_d$  : *power lost per unit time*

*higher aperture, smaller shunt impedance*



## Quarter Wave Resonators

<b>Material</b>	OFHC Cu
<b>Superconducting surface</b>	2 $\mu\text{m}$ thick. Pb
<b>Frequency</b>	150 MHz
<b>Cavity Length</b>	64 cm
<b>Cavity Diameter</b>	20 cm
<b>Optimum velocity</b>	$\beta=0.1$
<b>Design goal</b>	2.5 to 3 MV/m @ 6 to 9 Watts



$$\vec{E} = -\vec{\nabla}\phi - \frac{\partial \vec{A}}{\partial t}$$

$$\vec{B} = \mu\vec{H} = \vec{\nabla} \times \vec{A}$$

**Induction law**

$$2\pi R E_{\theta} = -\frac{d\Phi}{dt} = -\pi R^2 \frac{d\overline{B}_z}{dt}$$

**Newton-Lorentz force**

$$\frac{dp}{dt} = eE_{\theta} = -\frac{1}{2}eR \frac{d\overline{B}_z}{dt}$$

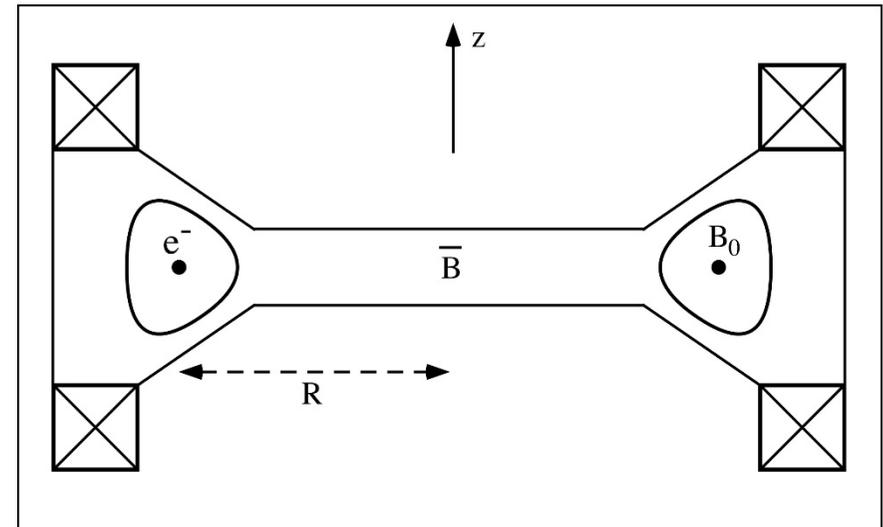
A constant trajectory also requires :

$$p = -eR B_0$$

$$\frac{dp}{dt} = -eR \frac{dB_0}{dt}$$

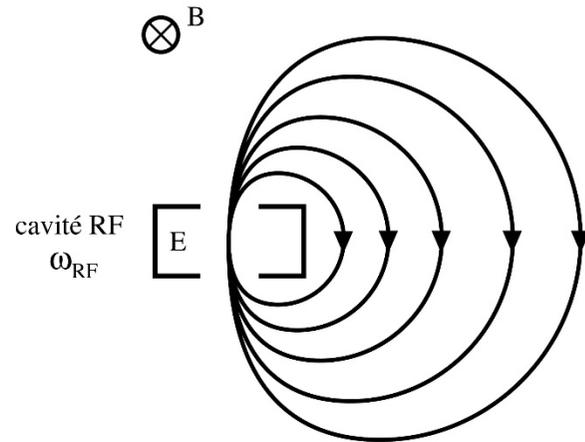
$$B_0 = \frac{1}{2}\overline{B}_z$$

## Betatron



*The betatron uses a variable magnetic field with time. The pole shaping gives a magnetic field  $B_0$  at the location of the trajectory, smaller than the average magnetic field.*

# Microtron



If the first turn is synchronous :  $\frac{\Delta T_r}{T_{RF}} = \text{integer} \Rightarrow \Delta \gamma_{turn} = \text{integer} (\gamma_0 = 1)$

Energy gain per turn

electrons	→ 0.511 MeV
protons	→ 0.938 GeV !!!

*Since required energy gains are large the concept is essentially valid for electrons.*

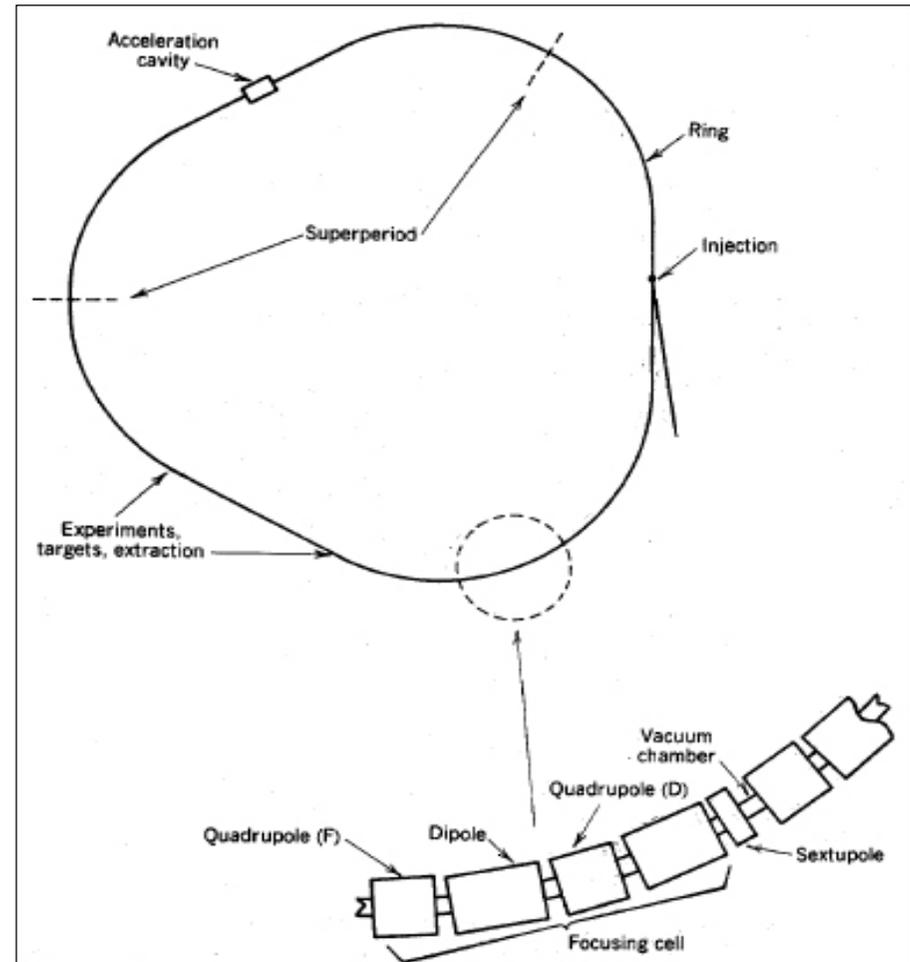
# Synchrotrons

*Synchrotrons* are the present standard accelerators for particle physics research.

Both the magnitude of the magnetic field and *rf* frequency are varied to maintain a synchronous particle at a constant orbit radius.

The constant-radius feature is very important; bending and focusing fields need extend over only a small volume.

This minimizes the cost of the magnets, allowing construction of large-diameter machines.



**Table 3.1.** Parameter disposition for different acceleration principles

principle	energy	velocity	orbit	field	frequency	flux
	$\gamma$	$v$	$r$	$B$	$f_{\text{rf}}$	
Cyclotron:	1	var.	$\sim v$	const.	const.	cont. <sup>a</sup>
Synchro cyclotron:	var.	var.	$\sim p$	$B(r)$	$\sim \frac{B(r)}{\gamma(t)}$	pulsed
Isochron cyclotron:	var.	var.	$r = f(p)$	$B(r, \varphi)$	const.	cont. <sup>a</sup>
Proton/Ion- synchrotron:	var.	var.	$R$	$\sim p(t)$	$\sim v(t)$	pulsed
Electron- synchrotron:	var.	const.	$R$	$\sim p(t)$	const.	pulsed

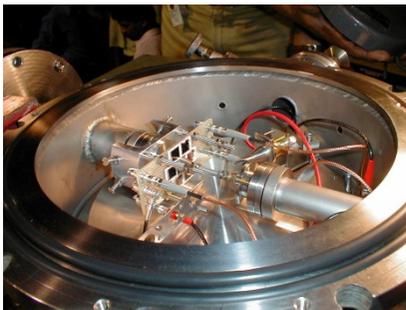
<sup>a</sup> continuous beam, but rf modulated



## Stable vs. Unstable ?

### Stable beams – controlled experiments

- unique beam selection (specific N,Z)
- well defined energy
- well collimated beam (small spatial and angular spread)  
defines interaction point on target, angles of scattered particles etc.
- large intensities ( $>10^{10}$  pps)  
Easier tracking and measurement of beam particles
- no decay products from the beam itself  
Cleaner environments for experiment,  
lesser background issues

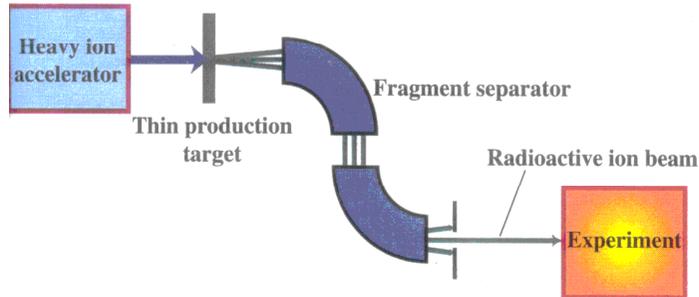


snp06, expt.al techniques for RIB

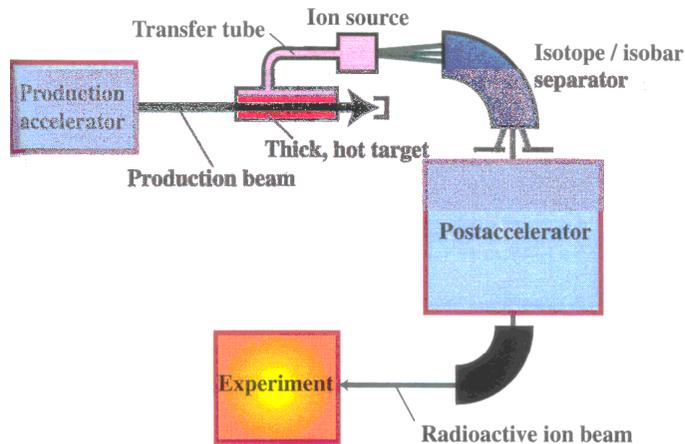


# Why experiments with RIB pose more challenges?

## Projectile Fragmentation



## ISOL



## *Study of very short lived nuclei*

RIKEN (JAPAN), MSU, GSI

## reaction products

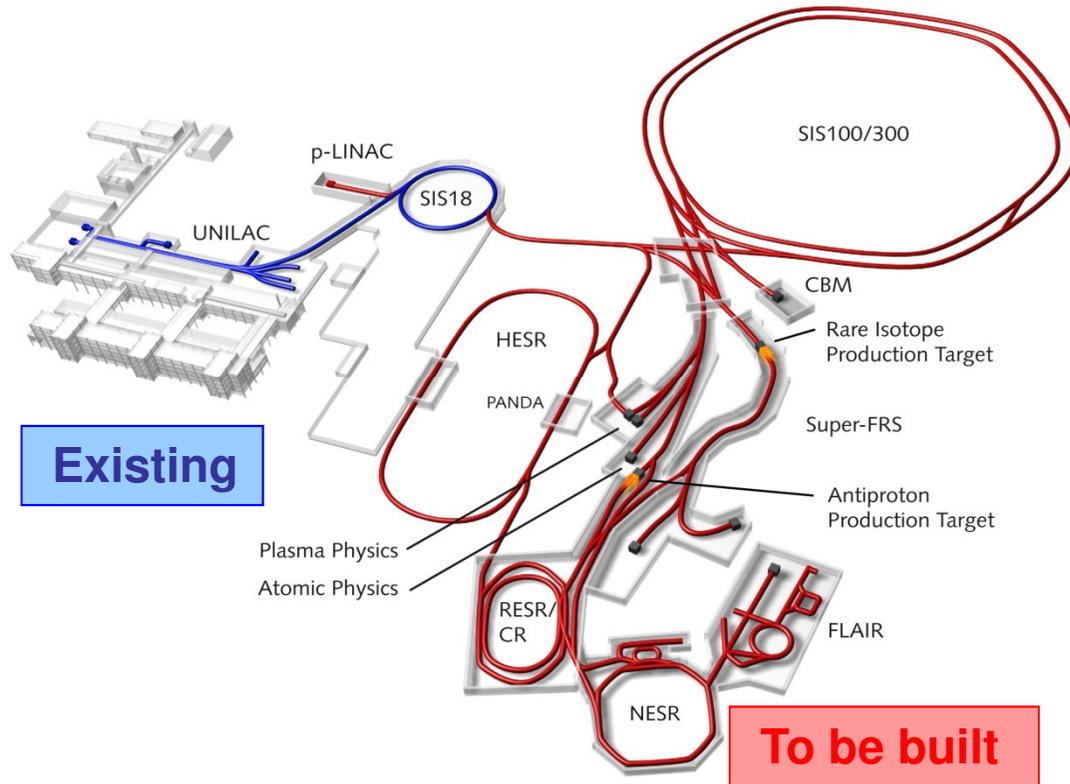
- angular spread, energy (momentum spread)
- isotopic/isobaric mixture
- background
  - scattered primary beam, in flight decays

## *Specific beams – controlled experiments*

Univ. of Louvain, GANIL, ORNL, TRIUMF

- good energy definition
- large spot size
- background
  - in flight decays

# FAIR – The Facility



Existing

To be built

## Primary Beams

- $10^{12}/s$ ; 1.5-2 GeV/u;  $^{238}\text{U}^{28+}$
- Factor 100-1000 over present in intensity
- $2(4) \times 10^{13}/s$  30 GeV protons
- $10^{10}/s$   $^{238}\text{U}^{73+}$  up to 25 (- 35) GeV/u

## Secondary Beams

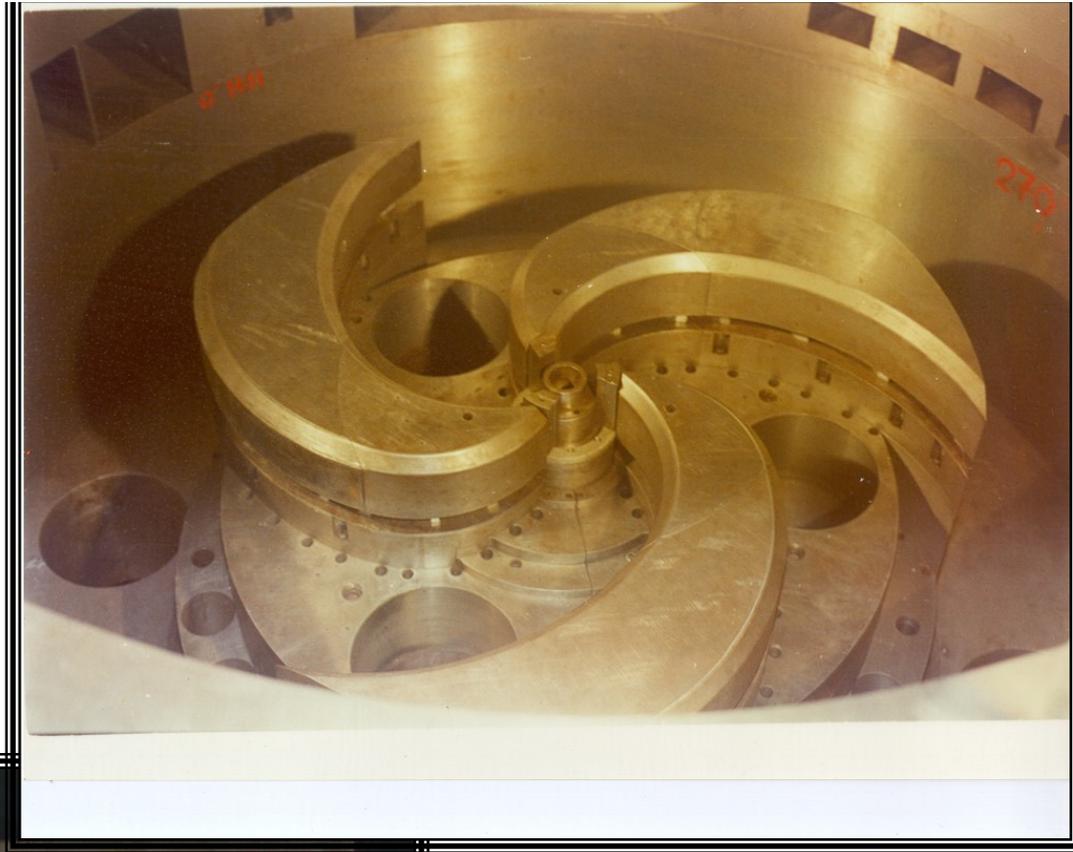
- Broad range of radioactive beams up to 1.5 - 2 GeV/u; up to factor 10 000 in intensity over present
- Antiprotons 3 - 30 GeV

## Storage and Cooler Rings

- Radioactive beams
- e – A collider
- $10^{11}$  stored and cooled 0.8 - 14.5 GeV antiprotons

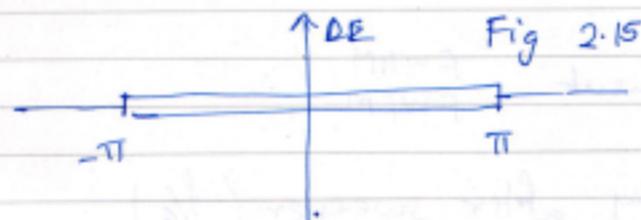
## Key Technical Features

- Cooled beams
- Rapidly cycling superconducting magnets



# Buncher.

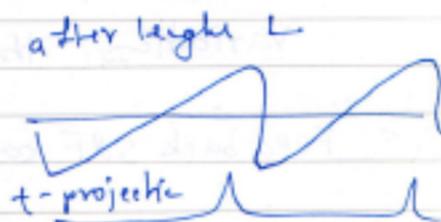
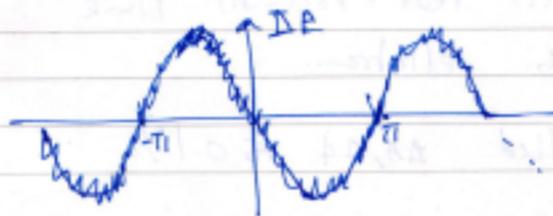
RF cavity TM<sub>010</sub>.



$$AF \sim 0.$$

$$\Delta T \in \{-\pi, \pi\}$$

some are accelerated / decelerated.



prebuncher  $V = V_0 \sin \phi$

$$\Delta E = eV_0 \sin \phi$$

$$= mc^2 \beta \gamma^3 \Delta \beta$$

$$\Delta v \Delta t = \frac{\phi}{2\pi} \lambda_{rf}$$

$$\Delta t = \frac{\lambda_{rf}}{2\pi} \cdot \frac{m v}{e V_0}$$

$$L = v \Delta t = \frac{2 E_{kin}}{K_{rf} e V_0}$$

$$K_{rf} = \frac{2\pi}{\lambda_{rf}}$$

$$\delta L = \frac{\delta E_{kin}}{K_{rf} e V_0}$$

bunch length

Double Harmonic bunches  $f/16, f/8$

- sweeper:  $f/32$   $\approx 26.6\%$   
 $\tau \approx 106.7 \text{ ns}$

- chopper: ( $> 1 \mu\text{s}$ )

- Time measurement FWHM  
FWTM.

phase pickup cavity after sweeper ( $f/4$ )

↓  
- feedback to correct for transit time variations through pellets.

- Feedback SRF controlled  $\Delta A, \Delta \phi \approx 0.1\%$

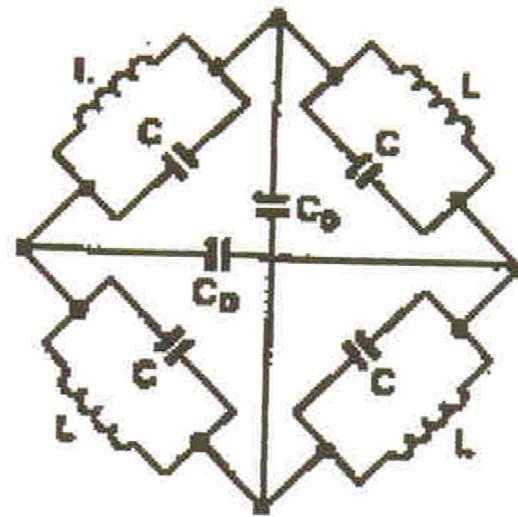
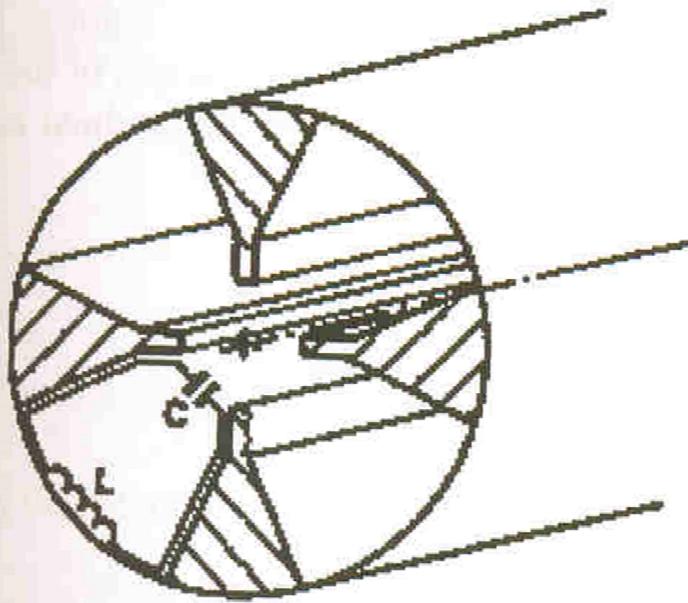
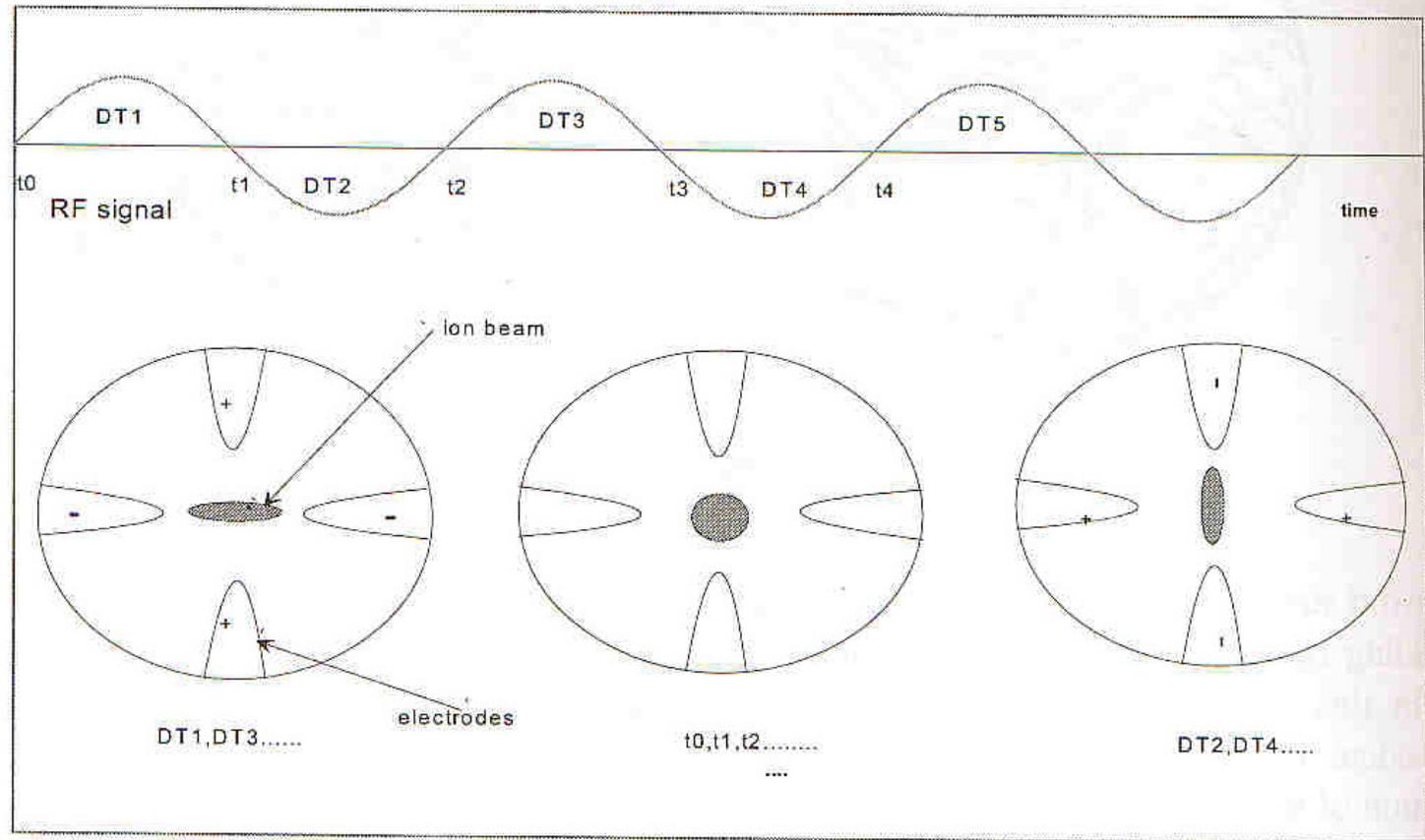
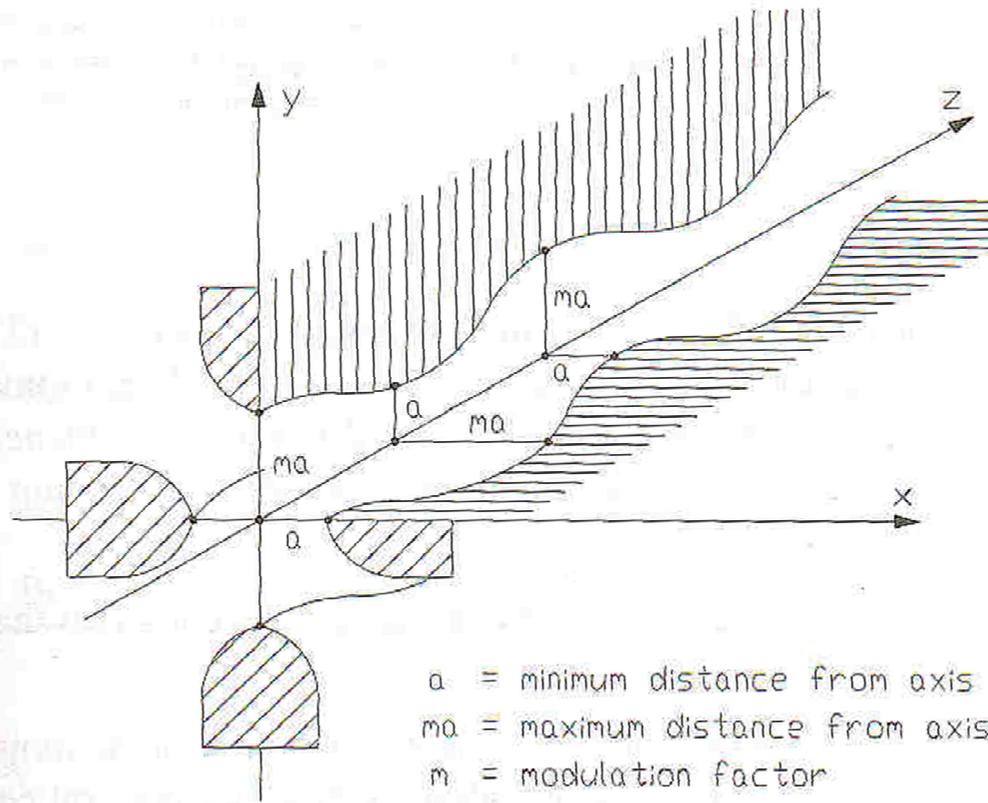


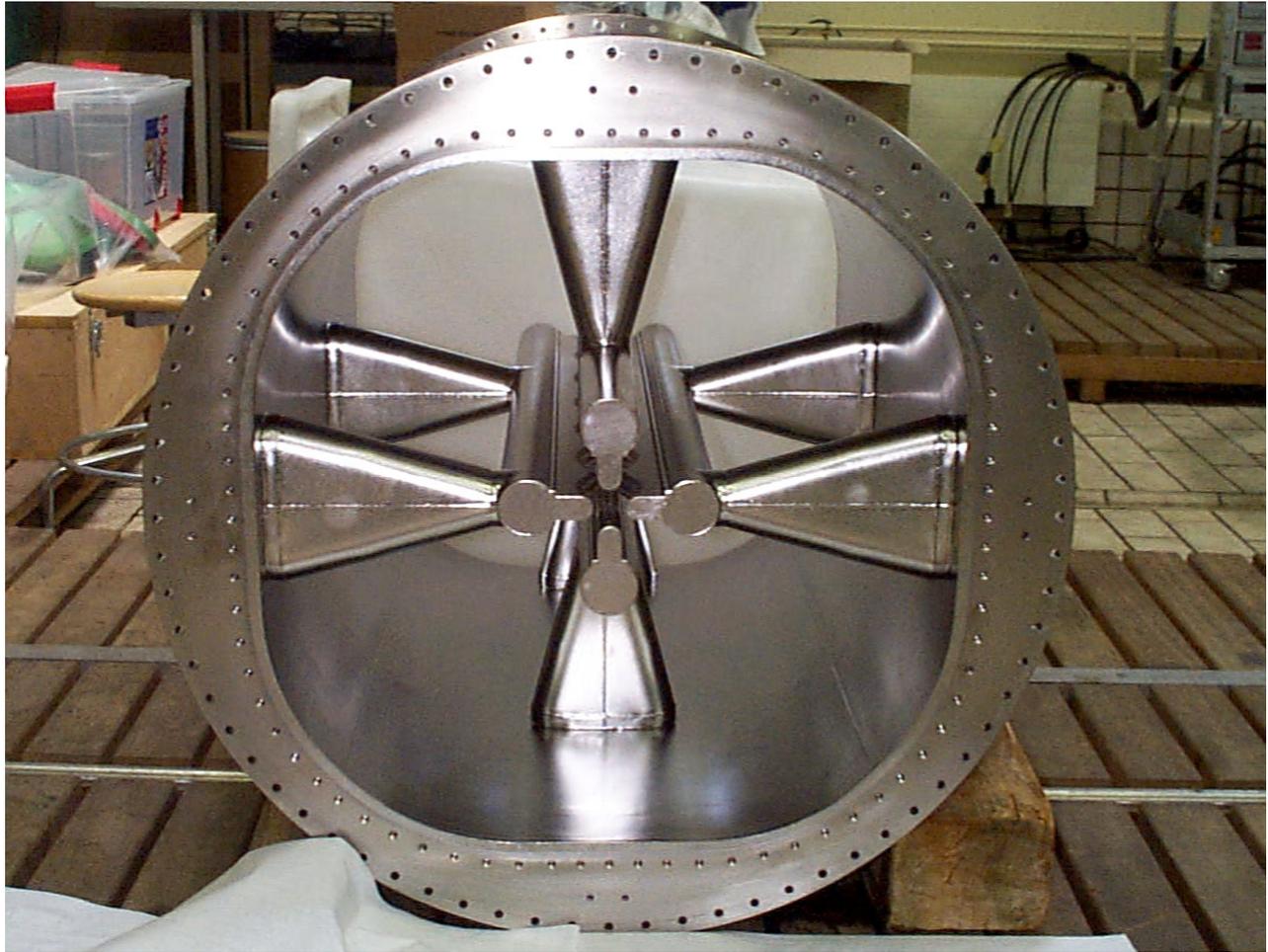
Fig. 4: Electrostatic ...



**Fig. 6:** Time-varying transverse focusing field in a RFQ

TE210  
mode





6D phase space : motion of particles

$$\bar{x} = (x, p_x, y, p_y, z, p_z)$$

$$\chi_p = \tan^{-1} \beta \gamma \frac{p_x}{p_z} \approx \beta \gamma \frac{p_x}{p_z} \quad \text{paraxial approximation}$$

$$\chi' = \frac{v_x}{v_z} \quad y' = \frac{v_y}{v_z}$$

Longitudinal phase space  $z, p_z \in z, \frac{\Delta p}{p} \in E, H$

Transverse phase space  $(x, \chi', y, y')$

Phase space matching important.

Electrostatic lenses

Magnetic lenses (RD, solenoids)

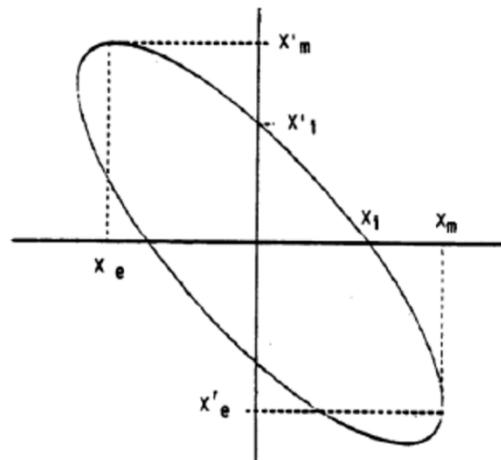
Steerers

## Courant Snyder definition

Under the influence of linear forces, trajectory of particles in phase space  $(x, x')$  follows an elliptical path

$$\gamma \cdot x^2 + 2 \cdot \alpha \cdot x \cdot x_p + \beta \cdot x_p^2 = \frac{E}{\pi} = \varepsilon$$

$$\beta\gamma - \alpha^2 = 1$$



$\varepsilon$  : Beam Emittance

$\alpha, \beta, \gamma$  : Twiss parameters

$\alpha > 0$  converging beam

$\alpha < 0$  diverging beam

Louville's theorem : under the influence of conservative forces, density of phase space stays constant

*phase space current must satisfy the continuity equation*

Evolution of boundary of ellipse (beam envelope), without having to calculate individual particles

## Geometrical beam emittance

rms definition

$$E_{\text{rms}} = \pi \sqrt{\langle x^2 \rangle \cdot \langle x_p^2 \rangle - \langle x \cdot x_p \rangle^2} \text{ metres}$$

brilliance ( ~63%)

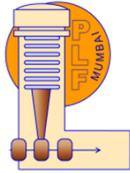
Admittance : maximum single particle emittance that can be transmitted

### Growth of emittance (mm-mrad)

- Steering effects
- Momentum spread
- Focussing errors
- Non-linear effects
- Space-charge effects
- Scattering from foil, gas
- Bends and tune fluctuations
- Power supply ripples
- Intra beam scattering

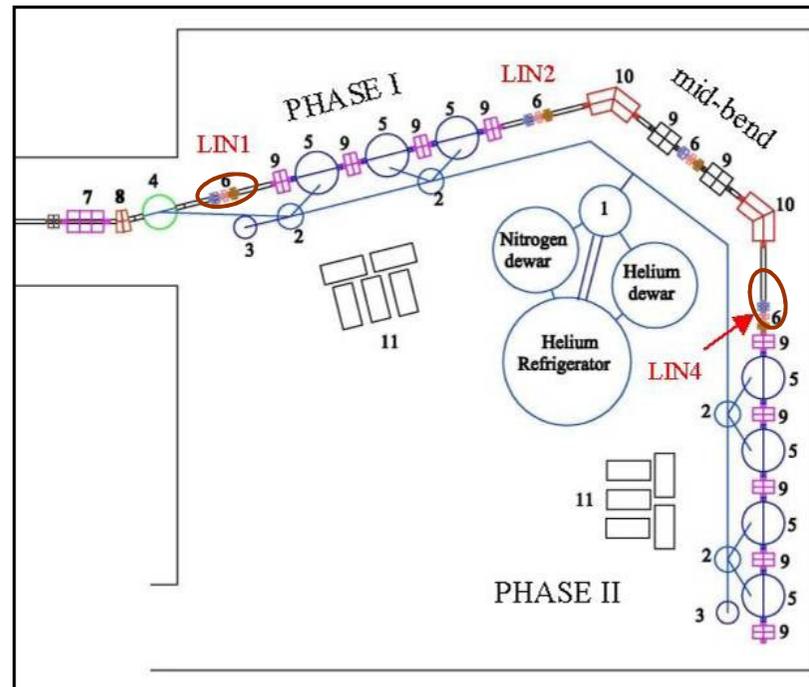
**BEAM : size and divergence**

**Beam waist : point of minimum beam size**



## Evolution of longitudinal phase space

Final configuration corresponding to an optimal phase space at target determined by measurement of the transmission and the time structure.



Timing Detector (1" BaF<sub>2</sub>)

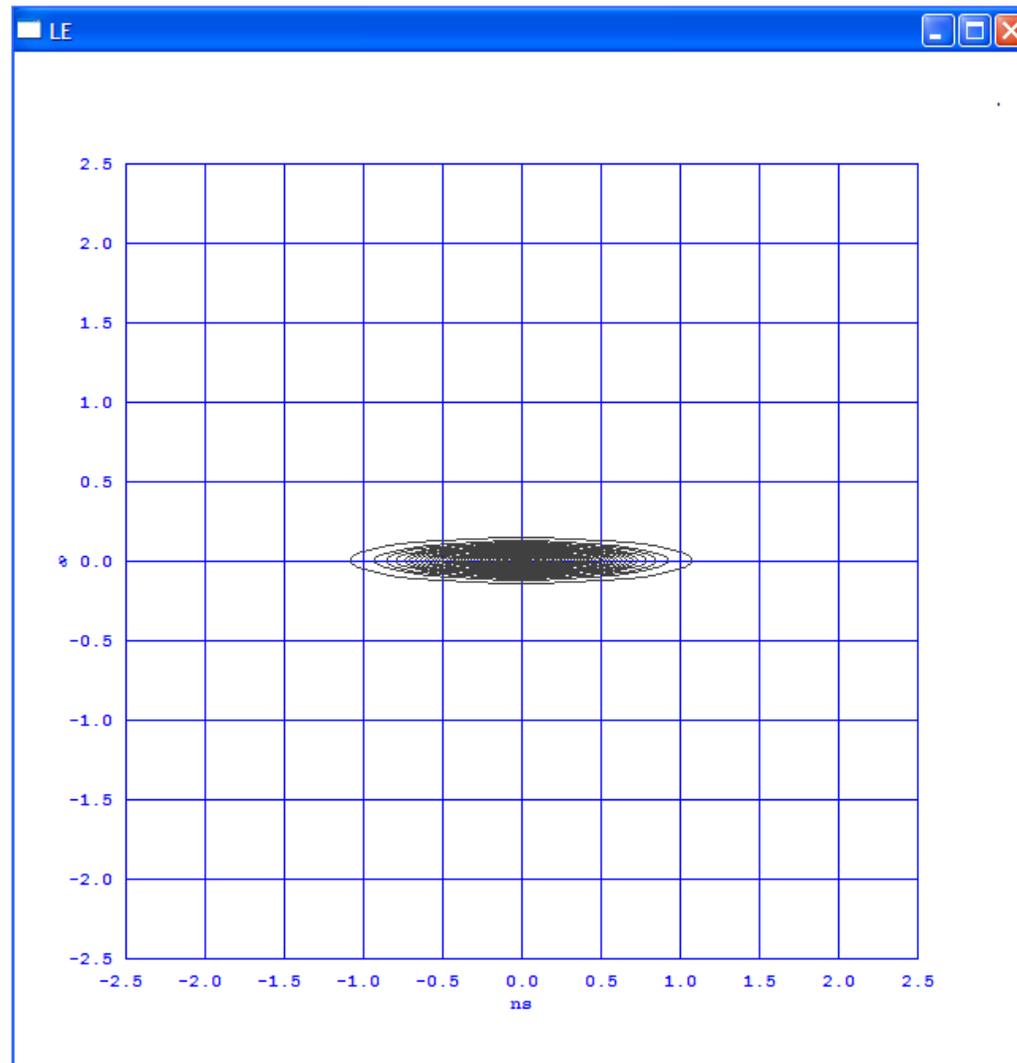
@LIN1 : entrance of Phase I

@LIN4 : entrance of Phase II

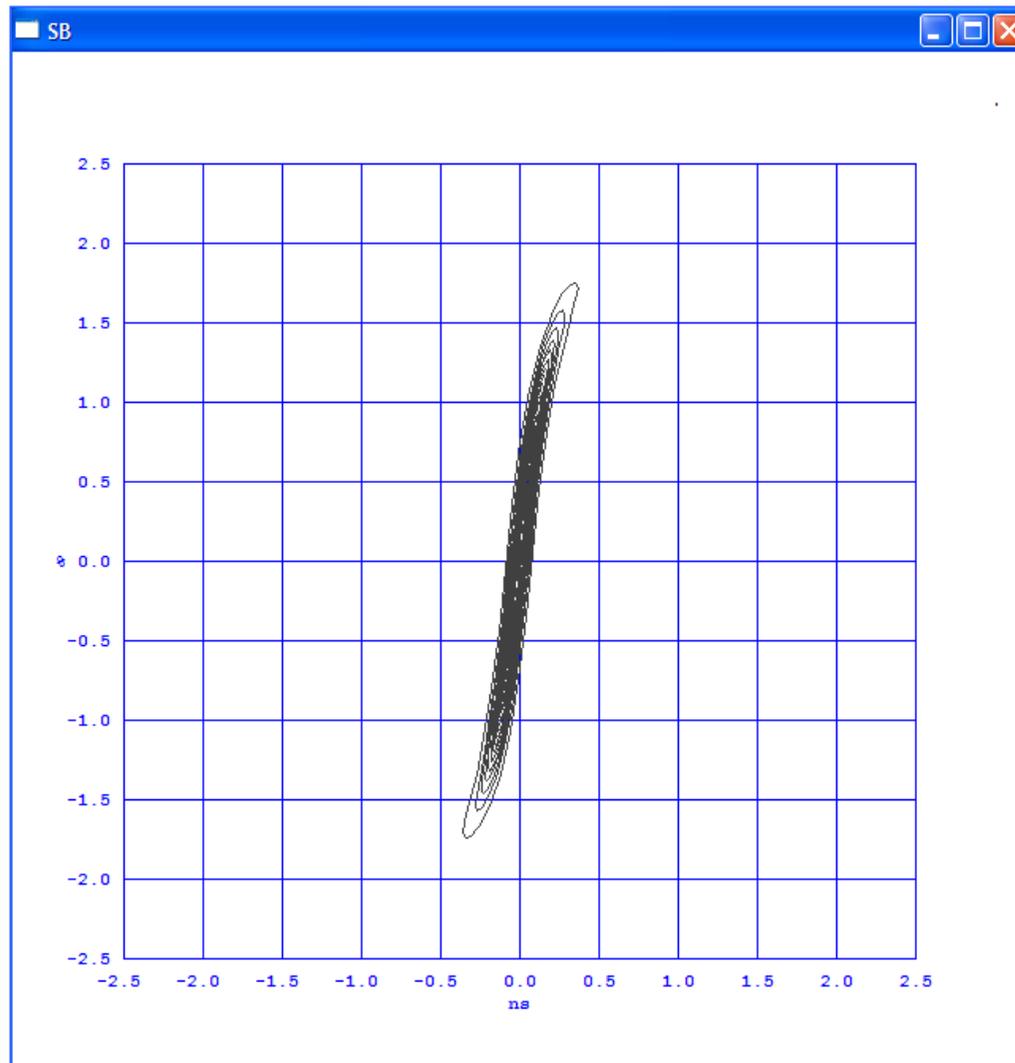
@LIN7 : after switching magnet

@target position

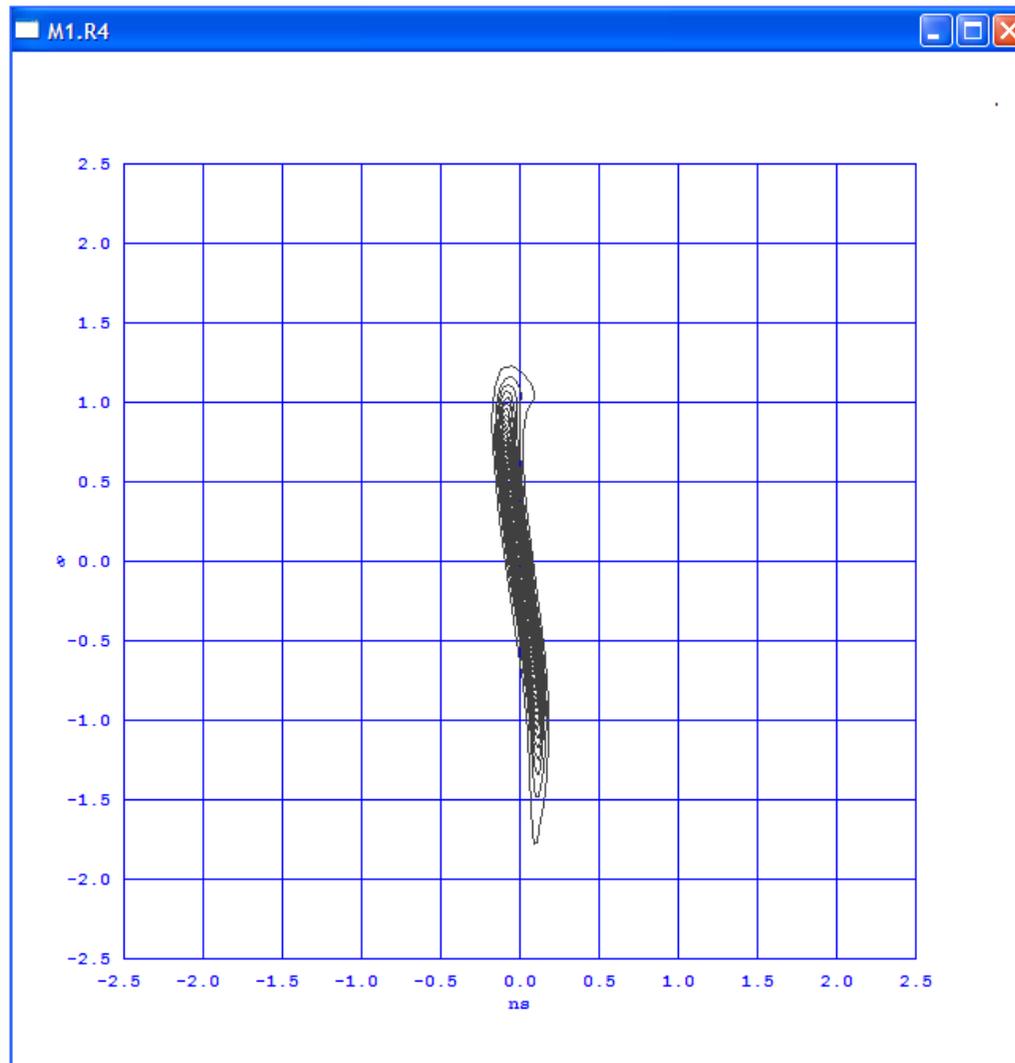
# Longitudinal phase space



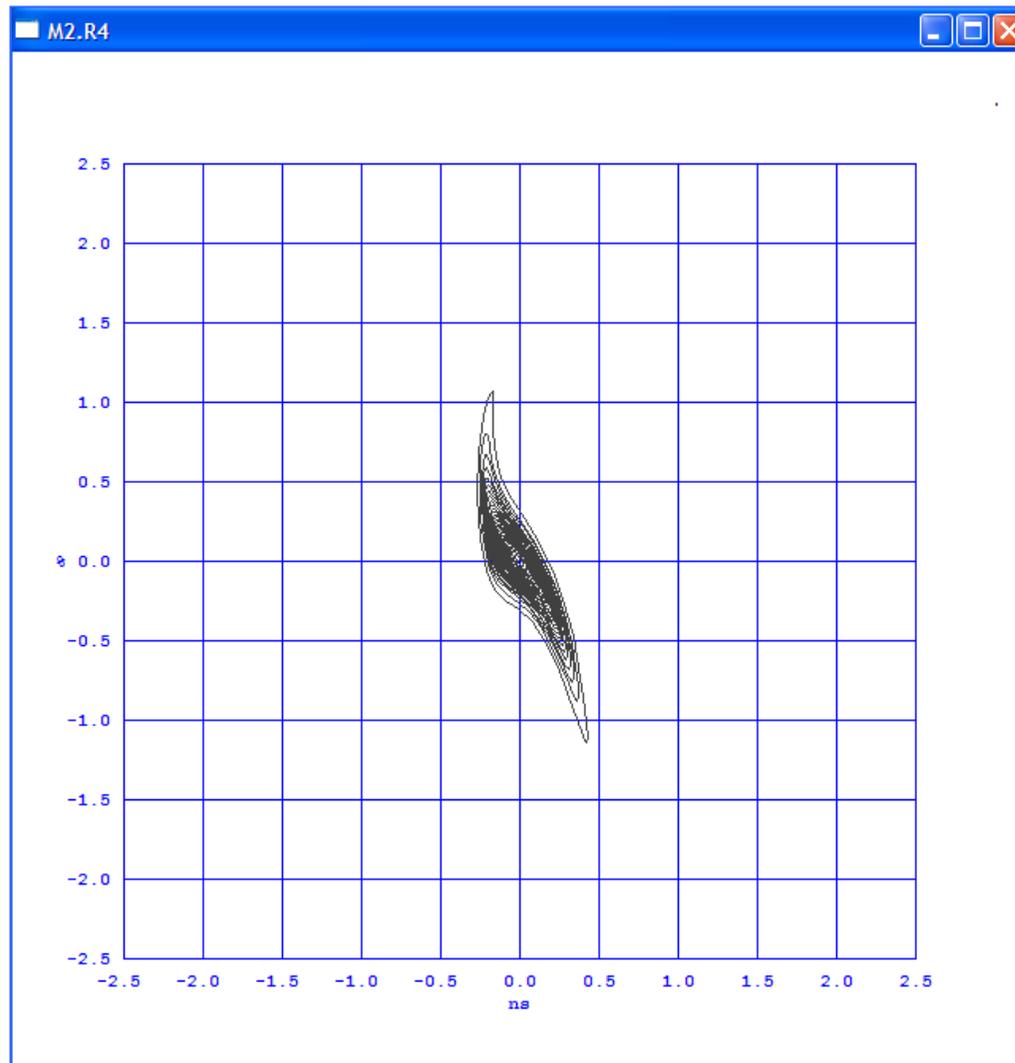
At LINAC Injection



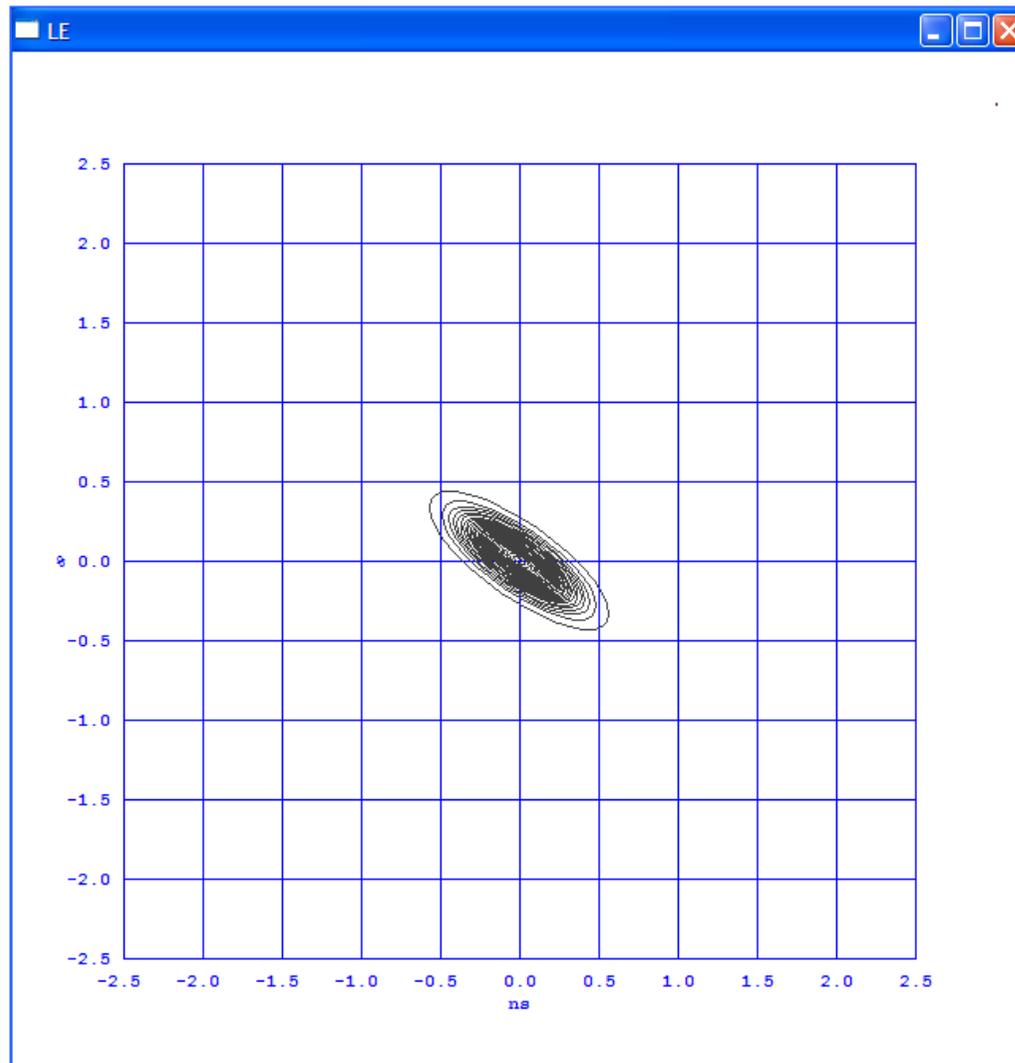
After Superbuncher at the entry of M1



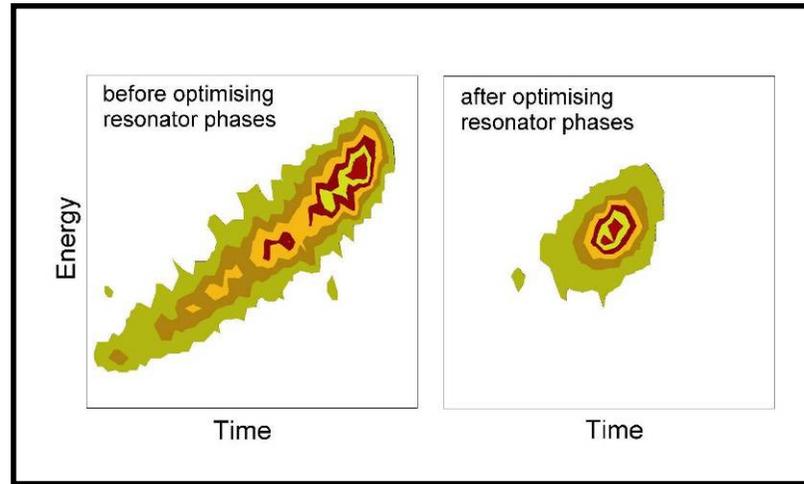
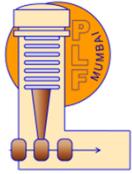
After M1, at the entry of M2



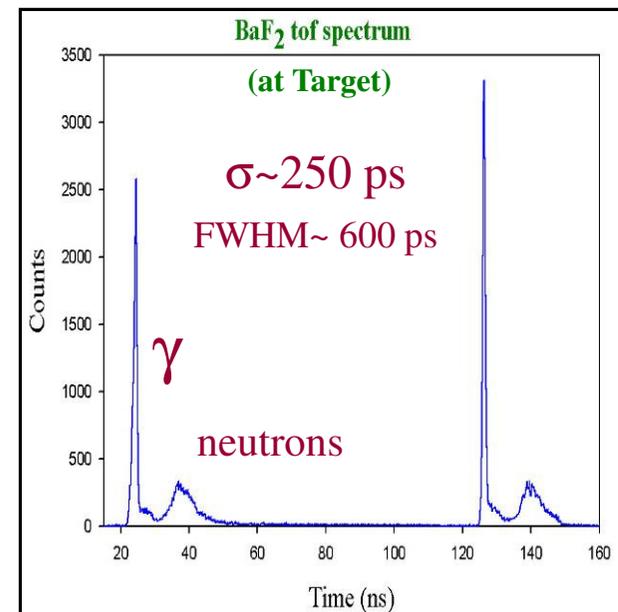
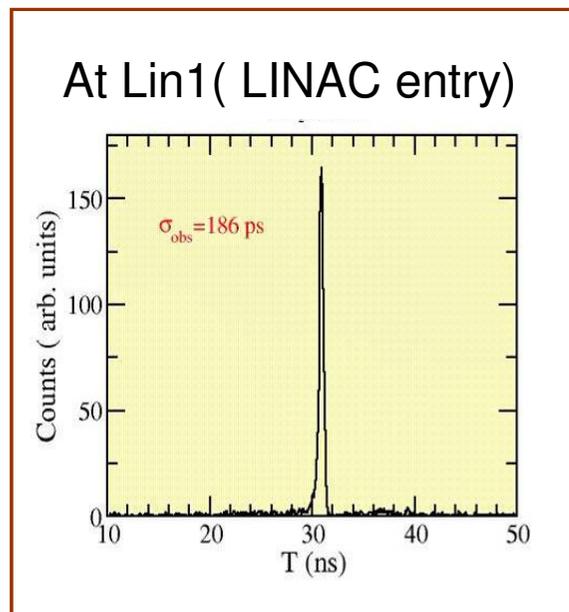
After M2, at the entry of M3

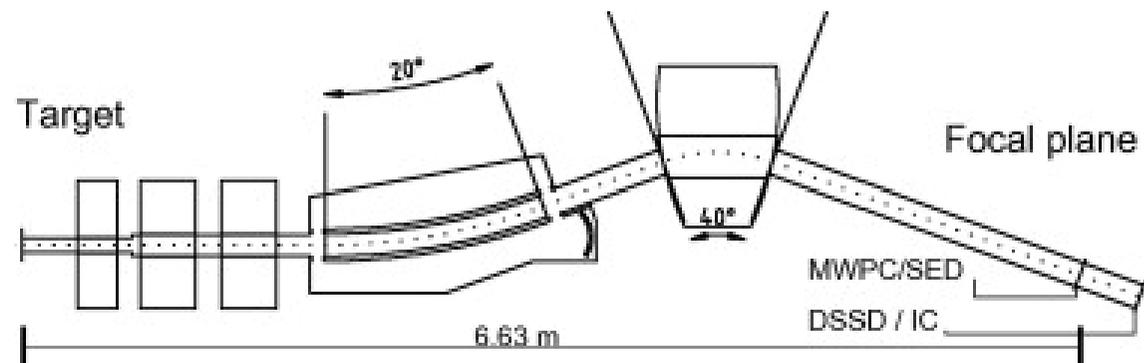
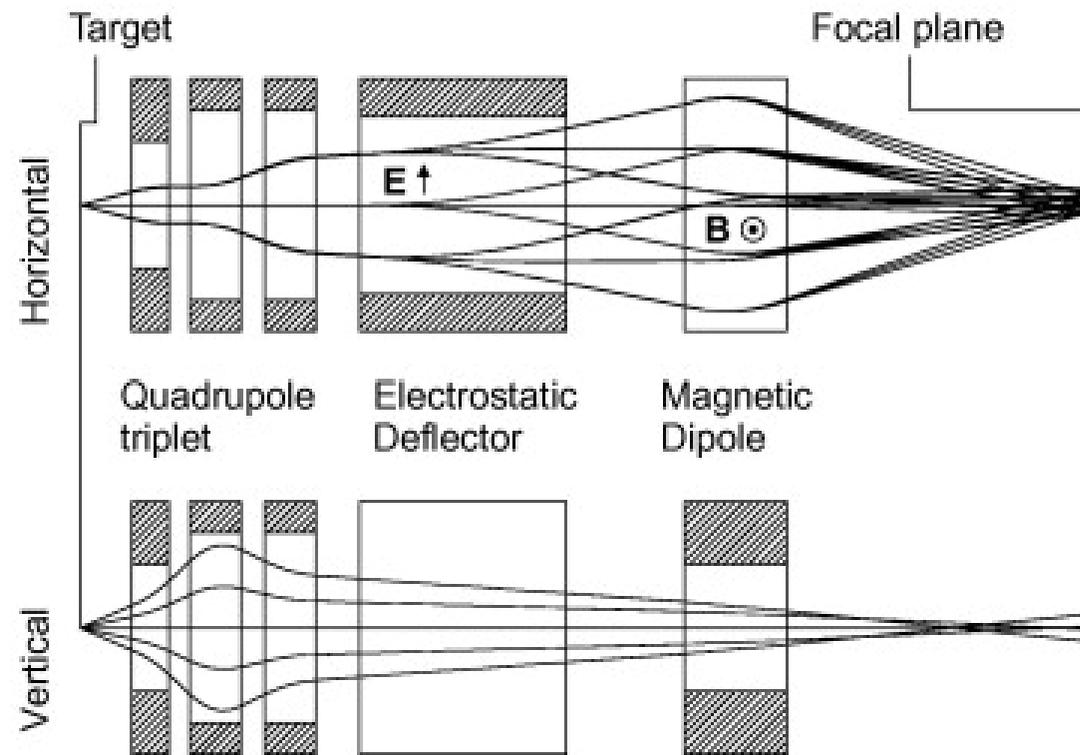


Equivalent distribution for the Phase II



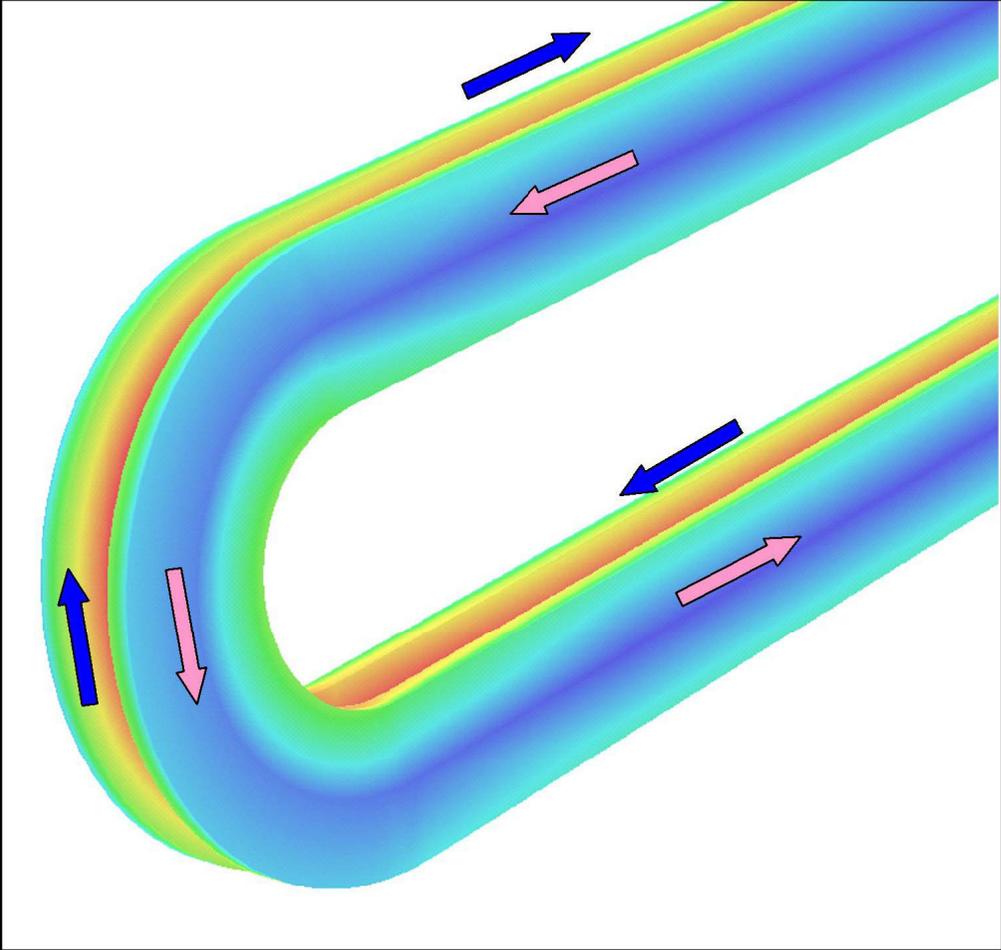
*Longitudinal phase space after mid-bend (E-T measurement)*





## *Magnets*

- *Sector*
- *Wedge*
- *Edge focusing*
- *Higher order component measurement*
- *Wiggler magnet*
- *Fast kicker*
- *Measurement of harmonics*
- *Measurement of magnetic field- hall probe & NMR*



**Table 1:** Instruments, measured quantities and physical effects used

<b>Instrument</b>	<b>Physical effect</b>	<b>Measured quantity</b>	<b>Effect on the beam</b>
Faraday cup	Charge collection	Intensity	Destructive
Current transformer	Magnetic field	Intensity	Non-destructive
Wall current monitor	Image current	Intensity, longitudinal density distribution	Non-destructive
Pick-up, beam-position monitor (BPM)	Electric/magnetic field	Position, trajectory, orbit	Non-destructive
Secondary emission monitor	Secondary electron emission	Transverse profile, intensity, emittance	Disturbing, at low energy: destructive
Wire scanner	Secondary emission, creation of secondary particles	Transverse profile, emittance	Slightly disturbing
Scintillator screen	Atomic excitation with light emission	Transverse profile, position	Destructive
Residual gas monitor	Ionization	Transverse profile	Non-destructive

magnetization curve will be perfectly symmetric, only odd harmonics of the modulation frequency will be present in the modulation spectrum. It is clear that the pair of coils must be carefully matched such that the induced signal after subtraction is minimized.

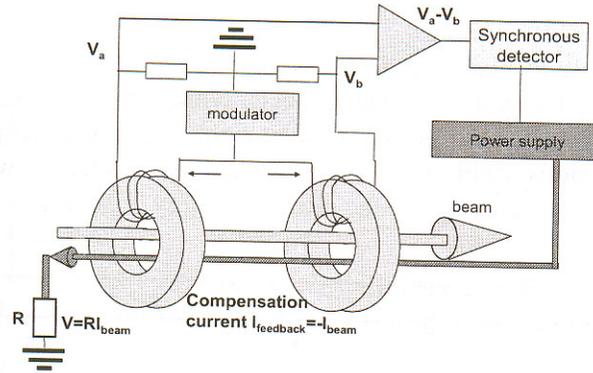


Fig. 13: The zero flux magnetometer

A DC current passing through the coils introduces a bias in the excitation, the sum signal becomes non-zero and even harmonics, in particular the second harmonic, will appear in the spectrum.

A synchronous detector extracts the information about the signal amplitude and phase of the component at the second harmonic of the modulation frequency. This signal is used to create a feedback current cancelling the flux induced by the beam. This feedback current is finally measured.

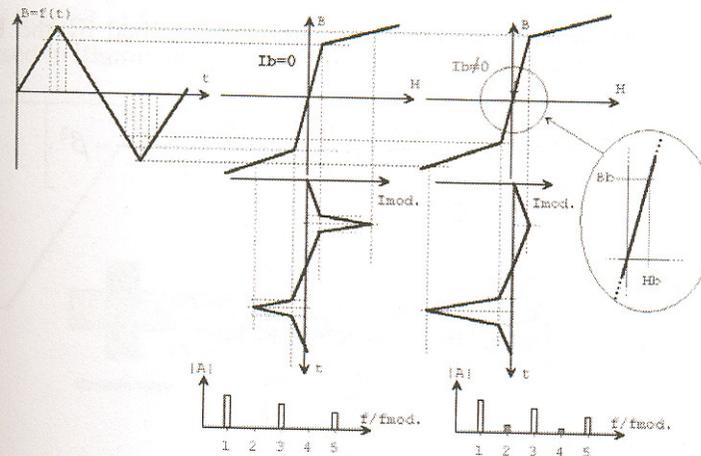
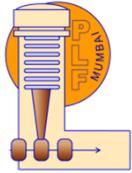


Fig. 14: Modulation of a DCCT left: without beam, right: with beam

Beam profile monitor

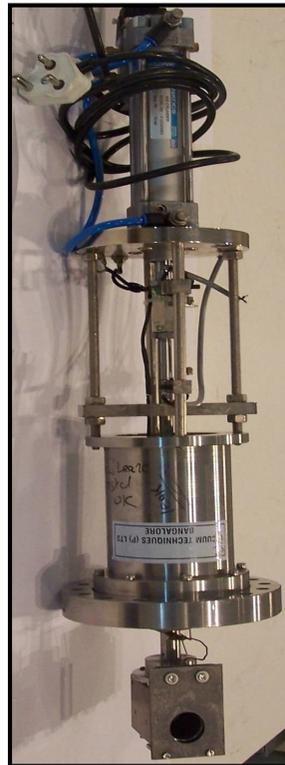




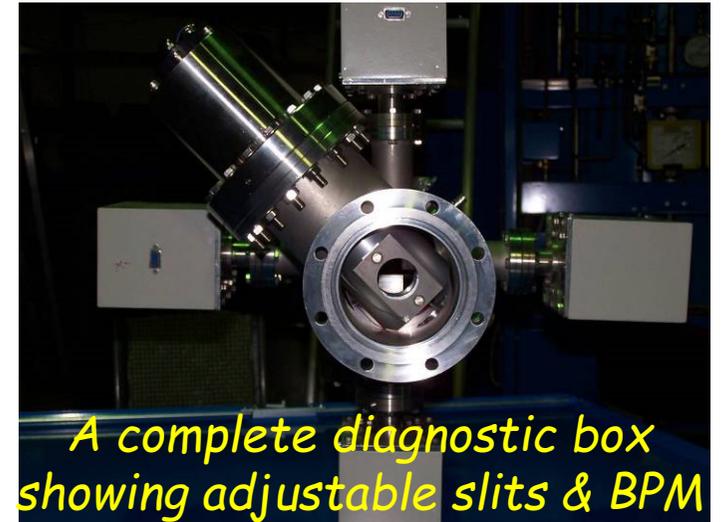
# Beam Diagnostic devices



BPM developed at TIFR



Faraday cup



*A complete diagnostic box showing adjustable slits & BPM*



Magnetic Steerer

## *Other accelerators*

- *Storage rings*
- *Free Electron lasers*
- *Synchrotron radiation sources*
- *Laser based accelerators*

## *Cryogenics & vacuum*

- *Cryogenics production and transport*
- *Thermal anchoring*
- *Minimization of heat load*
- *Quench protections*

## *Applications*

- *Nuclear physics*
- *Particle physics*
- *Atomic physics*
- *Material science*
- *AMS*
- *Medical treatment, isotope production*
- *Industry*
- *Agriculture – foodgrain irradiation*
- *Waste treatment*
- *Energy production*