## Holography, Gauge-gravity Connection and Black Hole Entropy Parthasarathi Majumdar,

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#### Theoretical Physics Department, TIFR, Mumbai; 18 May 2010

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Black Holes from Newton's law ? Dark stars Mitchell 1774; Laplace 1789



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c is very high; but did Newton have reason to believe that nothing could travel faster than c?





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Galileian relativity :  $c \rightarrow c \pm v \Rightarrow$  No dark stars!

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$$\omega_D = \omega_S \left( 1 + \frac{\Delta \phi_{SD}}{c^2} \right)$$

 $c(D) = c(S) \left( 1 + \frac{\Delta \phi_{SD}}{c^2} \right)$ 







### **Spacetime is curved!**

Toy example of curved space: geography globe



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Non-Euclidean in the large, but locally Euclidean

Einstein's GR model of spacetime : Curved but locally Minkowskian  $\Rightarrow$  have local light cones



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Tilting of local light cones  $\rightarrow$  measure of local spacetime curvature GRAVITATIONAL FORCE replaced by CURVED SPACETIME GE-OMETRY (Gauss, Riemann)

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#### Black hole spacetime Eddington-Finkelstein



#### **Black hole spacetime : another view**



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- What degrees of freedom contribute to  $S_{bh}$  ?

Vac EM in Minkowski sptm:  $\nabla \cdot \vec{E} = 0$  everywhere in  $V \Rightarrow Q(V) = 0$ Can define total charge globally

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 $\Rightarrow$  no analogue of  $\mathbf{E}^2 + \mathbf{B}^2$  in vac GR! Excitations 'polymeric'

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As  $|h| \nearrow$ ,  $bkreactn \nearrow$ , approx. invalid

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Hamiltonian constraint (bulk)

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$$Z = Tr_v Tr_b \exp -\beta \left[ \hat{H}_v + \hat{H}_b \right]$$
$$= Tr_b \exp -\beta \hat{H}_b \equiv Z_b$$

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... Given any closed surface, we can represent all that happens (gravitationally) inside it by degrees of freedom on this surface itself. This ... suggests that quantum gravity should be described by a **topological** quantum field theory in which all (gravitational) degrees of freedom are projected onto the boundary.

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Work with Isolated Horizons (IH) as local, non-stationary generalization of EHs (Ashtekar et. al. 1997-2001)





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- $\bullet$  Hawking radiation requires IH  $\rightarrow$  Dynamical Hor

## **Black hole radiance**



- **Canonical Ensemble of IHs in rad bath** : compute  $Z_b \rightarrow S_{can}$ 
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Generalizable to more general black holes with charge and angular momentum, within Grand canonical ensemble Chatterjee, PM 2005; PM in prog

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 $\frac{\mathcal{S}_{GR}}{k} + \frac{\mathcal{S}_{IH}}{(\mathcal{A}_{IH}/4\pi l_P^2)_{nearest int}} \rightarrow \text{variational principle OK, provided}$   $k \equiv (\mathcal{A}_{IH}/4\pi l_P^2)_{nearest int} >> 1$ 

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Quantize CS + sources  $\rightarrow S_{IH} \equiv \log \dim \mathcal{H}_{CS+sources}$ 

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For  $\mathcal{A}, E$  canonical quantization  $\Rightarrow$ 

$$\left[\hat{\mathcal{A}}_{I}^{a}, \hat{E}_{b,J}\right] = i \,\delta_{b}^{a} \,\eta_{IJ} \,\delta^{(3)}(...)$$

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LQG : promote these to operators  $\hat{h}_l(\hat{\mathcal{A}})$  ,  $\hat{E}_{f,S}$ 

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Holonomies completely specified by spin  $j_l$  associated with link l

# Spin network : Quantum Space



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Equispaced  $\forall j_{p} = 1/2$ 

#### **'Quantum' Isolated Horizon** → effective description (Ashtekar, Baez, Corichi, Krasnov 1997)



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 $\Rightarrow$  (Kaul, PM 1998)

dim 
$$\mathcal{H}_{CS+(j_1,...,j_n)} = \prod_{p=1}^{n} \sum_{m_p=-j_p}^{j_p} [\delta_{m_1+\dots+m_n,0} - \frac{1}{2} \delta_{m_1+\dots+m_n,-1} - \frac{1}{2} \delta_{m_1+\dots+m_n,1}]$$

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**Infinite series of corrections to semicl BHAL : characteristic signature of LQG** 

# **IT from BIT**



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$$qu.sptm.corr.$$



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