

# Flow and its fluctuations at ATLAS --in large systems

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India+ lectures on Heavy Ion Collision experiments

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## Outline

- Introduction and flow observables
- ATLAS detector and trigger
- Selected results with analysis details
  - v<sub>n</sub> from event plane and two-particle correlation methods
  - Event plane correlations
  - p(v<sub>n</sub>) distributions
  - v<sub>n</sub>-v<sub>m</sub> correlation via event-shape engineering
  - Longitudinal flow decorrelations
- Outlook

### High-energy heavy ion collision

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- Collision takes a snapshot of the nuclear and nucleon wavefunction.
- Large particle production enable description of QGP in terms of hydrodynamics.
- Big unknown: What is the nature of initial condition and pre-equilibrium phase?
- How to probe the dynamics and properties via flow and its fluctuations?

Not covered: small systems, high p<sub>T</sub>, heavy flavor, Jet tagged

https://twiki.cern.ch/twiki/bin/view/AtlasPublic/HeavylonsPublicResults

### Connecting the initial and final state



### Perturbing the system with different initial state fluctuations

### **Richness of flow fluctuations**



$$\frac{dN}{d\phi} \propto 1 + 2\sum_{n} \mathbf{v}_{n}(p_{T}, \eta, ...) \cos n \left( \phi - \Phi_{n}(p_{T}, \eta, ...) \right) + \text{noise}$$

$$\overset{\sim}{\underset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}_{\overset{\sim}{\sim}}$$
How do we analyze this object?

### Flow observables arXiv: 1407.6057<sup>6</sup>



$$\left\langle \frac{dN_1}{d\phi d\eta dp_T} \frac{dN_2}{d\phi d\eta dp_T} \right\rangle \implies \left\langle V_n(p_{T1},\eta_1) V_n^*(p_{T2},\eta_2) \right\rangle \implies v_n \{2\text{PC}\} \equiv \sqrt{V_n V_n^*}$$

Multi-particle correlation function

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Multi-particle correlation function

### **Example cumulants**

Single-flow cumulants

$$c_{n} \{2\} = \langle v_{n}^{2} \rangle \qquad n=1-7$$

$$c_{n} \{4\} = \langle v_{n}^{4} \rangle - 2 \langle v_{n}^{2} \rangle^{2}$$

$$c_{n} \{6\} = \langle v_{n}^{6} \rangle - 9 \langle v_{n}^{4} \rangle \langle v_{n}^{2} \rangle + 12 \langle v_{n}^{2} \rangle^{3}$$

- Symmetric cumulants  $\operatorname{sc}_{n,m}\{4\} = \langle v_n^2 v_m^2 \rangle \langle v_n^2 \rangle \langle v_m^2 \rangle$  (n,m)=(2,3), (2,4)...
- Asymmetric cumulants (Event plane correlator)

$$\left\langle v_2^2 v_4 \cos 4(\Psi_2 - \Psi_4) \right\rangle \\ \left\langle v_2^3 v_3^2 \cos 6(\Psi_2 - \Psi_3) \right\rangle \\ \left\langle v_2 v_3 v_5 \cos (2\Psi_2 + 3\Psi_3 - 5\Psi_5) \right\rangle$$

See Y. Zhou's talk last week

•  $\mathbf{v}_{n}$ - $\mathbf{v}_{0}$  correlators  $\langle v_{n}^{2} N \rangle$ ,  $\langle v_{n}^{2} \delta p_{T} \rangle$ ...  $\langle \delta p_{T} \delta p_{T} \rangle$ ,  $\langle \delta p_{T} \delta p_{T} \delta p_{T} \rangle$ ...

## **ATLAS Detector**



Heavy flavor and quarkonium flow

## **ATLAS** Triggers

Selection of interesting events up to 1/30,000 with high efficiency

 $\rightarrow$  Achieved by combination of L1 and HLT trigger, critical especially in pp and pPb



 $N_{\rm ch}^{\rm rec} (p_{_{\rm T}} > 0.5 {\rm ~GeV})$ 

**Pileup** rejection



Jet trigger efficiency

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 $N_{\rm ch}^{\rm rec}$ 

HLT\_noalg\_mb\_L1TE20 HLT\_noalg\_mb\_L1TE10

10<sup>-1</sup>



<sup>10</sup> Events [Millions]

### ATLAS capability for flow measurements

$$v_n = rac{\langle \cos(n(\phi-\Psi_n)
angle))}{{
m Res}\{\Psi_{
m n}\}} 
onumber \ {
m Res}\{\Psi_{
m n}\} = \langle \cos(n(\Psi_n-\Psi_{n,{
m true}})
angle)$$



### Large and flexible set of choices of detectors for correlations



Detector	Name	Description	$ \eta $ coverage	Calorimeter-Layers
1	EMB0	EMcal Barrel	0-0.5	presamp+layer1,2
2	EMB1	EMcal Barrel	0.5-1.5	presamp+layer1,2
3	EMB2	EM Barrel	0-1.5	sum of Detectors 1 and 2
4	EME0	EMcal End Cap	1.5-2.1	presamp+layer1,2
5	EME1	EMcal End Cap	1.5-2.7	Detector 4 +
				presamp+layer1,2,3 for $2.1 < \eta < 2.7$
6	EME2	EMcal End Cap	1.5-3.2	Detector 4+
				presamp+layer1,2 for $2.7 < \eta < 3.2$
7	EMB1EME0	EM Barrel + End Cap	0.5-2.1	sum of Detectors 2 and 4
8	ID0	Inner Detector	0.5-2.0	charged particles $p_T > 0.5 \text{ GeV}$
9	ID1	Inner Detector	0-2.5	charged particles $p_T > 0.5 \text{ GeV}$

Table 2: Detectors used in the three sub-event method to determine Full-FCal and Sub-Fcal resolution. If only one side of the detector is used, we use a substript "N" or "P" to indicate the either negative or the positive  $\eta$ .



### **Detector nonuniformity**



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## $v_n(cent, p_T, \eta)$ via the Event plane method



- Features of Fourier coefficients
  - v<sub>n</sub> coefficients rise and fall with centrality.
  - $v_n$  coefficients rise and fall with  $p_T$ .
  - v<sub>n</sub> coefficients are ~boost invariant.

Flow correlations are geometric and long range!

### **Two-particle correlation method**



 $\Delta \phi$ 

### Effects of residual detector effects

- For each event, make the foreground **ab** pairs. Mixed event: **a** with **b** from a random event with similar centrality (5%) and z-vertex (0.5cm).
- Three checks were done for the pair acceptance
  - Time dependence  $\rightarrow$  vary the event gap and check the result
  - Centrality matching  $\rightarrow$  vary the width of the centrality bin for mixing
  - Z-vertex matching  $\rightarrow$  vary the width of zbin for mixing.



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results with different z vertex binning: 25, 20, 15, 10, 5, 2.5 and 1mm match with the mixed event. See some convergence (already pretty good with 5mm), the error band is around  $2x10^{-6}$ .



### v<sub>n</sub> via two-particle correlations



• Long range structures ("ridge") described by harmonics  $v_{1,1}$ - $v_{6,6}$ 

$$\frac{dN}{d\Delta\phi} \propto 1 + \sum_{n} 2\mathbf{v}_{n,n} \left( \mathbf{p}_{T}^{a}, \mathbf{p}_{T}^{b} \right) \cos\left(n\Delta\phi\right) \qquad v_{n,n} \left( \mathbf{p}_{T}^{a}, \mathbf{p}_{T}^{b} \right) = \mathbf{v}_{n} \left( \mathbf{p}_{T}^{a} \right) \mathbf{v}_{n} \left( \mathbf{p}_{T}^{b} \right)$$

### Flow fluctuations and their power



Disentangle the initial and final state effects

## How to measure event plane correlation?<sup>19</sup>

### • We use scalar product method, which approximately gives

 $\approx$ 

$$\begin{aligned} \cos(c_1\Phi_1 + \dots + lc_l\Phi_l)\rangle &= \frac{\langle \cos(c_1\Psi_1 + \dots + lc_l\Psi_l)\rangle}{\operatorname{Res}\{c_1\Psi_1\}\dots\operatorname{Res}\{c_ll\Psi_l\}} \ c_1 + 2c_2\dots + lc_l = 0\\ \operatorname{Res}\{c_nn\Psi_n\} &= \langle \cos c_nn(\Psi_n - \Phi_n)\rangle \end{aligned}$$

Ľ

$$rac{\left\langle v_1^{c_1}v_2^{c_2}\ldots v_l^{c_l}\cos(c_1\Psi_1+2c_2\Psi_2+\ldots+lc_l\Phi_l)
ight
angle}{\sqrt{\left\langle v_1^{2c_1}
ight
angle \left\langle v_2^{2c_2}
ight
angle \ldots \left\langle v_l^{2c_l}
ight
angle }}$$

Taken from different subevents

Sensitivity limit is set by the resolution Res{}

$$\operatorname{Res}\{jn\Psi_n\} = \langle \cos jn(\Psi_n - \Phi_n) \rangle \qquad \begin{array}{l} \text{Jean-Yves Ollitrault} \\ \operatorname{Phys. Rev. D 46, 229} \\ = \frac{\chi_n \sqrt{\pi}}{2} e^{-\frac{\chi_n^2}{2}} \left[ I_{(j-1)/2}(\frac{\chi_n^2}{2}) + I_{(j+1)/2}(\frac{\chi_n^2}{2}) \right] \\ \approx \begin{cases} 1 - \frac{j^2}{8z} + \frac{j^2(j^2 - 4)}{128z^2}, z = \chi_n^2/2 & \text{for large } \chi_n \\ \\ \frac{\sqrt{\pi}}{2^j \Gamma(\frac{j+1}{2})} \chi_n^j & \text{for small } \chi_n \end{cases}$$

- $\chi_n$ , thus Res{}, decreases fast with n
- Decrease slower with j, especially if  $\chi_n$  is large



### **EP** correlation for alignment



A rotation between two subevents will show up in correlations

 $rac{\left\langle \sin k ig( \Psi_n^{
m N} - \Psi_n^{
m P} + \delta ig) 
ight
angle}{\left\langle \cos k ig( \Psi_n^{
m N} - \Psi_n^{
m P} + \delta ig) 
ight
angle} pprox an k\delta pprox k\delta$ 

Detector response phase-shift between + and - side, revealed by flow

 $rac{dN}{d\Delta\Psi} \propto 1+2v_n f(\Delta\Psi+\delta)$ 

see the rotation  $\delta$  only if signal is non-zero. Can not correct via mixed-event, since v<sub>n</sub>=0 in mixed-event.



### **Results and interpretation**



Glauber model fails , while hydrodynamics (AMPT) model works

Indicating importance of non-linear responses:

Teany & Yan arXiv:1312.3689

### Two plane correlations



## Extraction of $p(v_n)$



## Obtaining p(v<sub>n</sub>) via unfolding

• Flow vector in each event has flow and smearing contribution

$$\boldsymbol{q}_n = \boldsymbol{v}_n + \boldsymbol{s}_n$$
  $p(\boldsymbol{q}_n) = p(\boldsymbol{v}_n) \otimes p(\boldsymbol{s}_n)$ 

Estimating statistical smearing from sub-events

1304.1417,1305.2942



"Unsmear"  $p(q_n)$  by  $p(s_n)$  to get  $p(v_n)$ 

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### **Bayesian unfolding**

### • unfolding algorithm as implemented in the RooUnfold

• True ("cause" c or  $v_n$ ) vs measured distribution ("effect" e or  $v_n^{obs}$ )

Denote response function  $A_{ji} = p(e_j|c_i)$ 

G. D'Agostini, A multidimensional unfolding method based on Bayes' theorem, Nucl. Instrum. Meth. A 362 (1995) 487 [.SPIRE].

Unfolding matrix M is determined via iterative procedure

$$\hat{c}^{\text{iter}+1} = \hat{M}^{\text{iter}}e, \quad \hat{M}_{ij}^{\text{iter}} = \frac{A_{ji}\hat{c}_i^{\text{iter}}}{\sum_{m,k}A_{mi}A_{jk}\hat{c}_k^{\text{iter}}}$$

Prior, c<sup>0</sup>, can be chosen as input v<sub>n</sub><sup>obs</sup> distribution or it can be chosen to be closer to the truth by a simple rescaling according to the EP v<sub>n</sub>

$$\langle v_n \rangle \leq v_n^{\mathrm{EP}} \leq \sqrt{\langle v_n^2 \rangle} = \sqrt{\langle v_n \rangle^2 + \sigma_{v_n}^2}$$

Number of iterations N<sub>iter</sub> adjusted according to sample statistics and binning.

### Unfolding performance: v<sub>2</sub>, 20-25%



- Use the standard Bayesian unfolding technique
- Converges within a few % for  $N_{iter}=8$ , small improvements for larger  $N_{iter}$ .
- Many cross checks show good consistency
  - Unfolding with different prior distributions
  - Unfolding using tracks in a smaller detector
  - Unfolding directly on the EbE two-particle correlation.

Details in arXiv:1305.2942

### Flow probability distributions



 $v_2$  distributions has significant reaction plane component:

$$p(v_2) = rac{v_2}{\sigma^2} e^{-rac{(v_2)^2 + \left(v_2^{ ext{RP}}
ight)^2}{2\sigma^2}} I_0\!\left(rac{v_2^{ ext{RP}}v_2}{\sigma^2}
ight)$$

•  $v_2$  in central, and  $v_3 v_4$  in all centrality are described by a radial Gaussian function:  $P(v_n) = \frac{v_n}{\sigma^2} e^{-\frac{v_n^2}{2\sigma^2}} \qquad \frac{\sigma_{v_n}}{\langle v_n \rangle} = \sqrt{\frac{4}{\pi} - 1} = 0.523$ 

### Cumulants from correlation method and from $p(v_2)$



- Measuring  $p(v_2)$  is equivalent to cumulants, more intuitive
- Non-Bessel Gaussian is reflected by a 2% change beyond 4<sup>th</sup> order cumulants

### More info by selecting on event-shape



Jurgen, Anthony, Sergei arXiv:1208.4563

Peng, Jiangyong, Soumya arxiv:1311.7091

• Select events with certain v<sub>2</sub><sup>obs</sup> in Forward Rapidity:

### More info by selecting on event-shape





Jurgen, Anthony, Sergei arXiv:1208.4563

Peng, Jiangyong, Soumya arxiv:1311.7091

• Fix centrality, then select events with certain  $v_2^{obs}$  in Forward rapidity:

→ATLAS: measure  $v_n$  via two-particle correlations in  $|\eta| < 2.5$ Fix system size and change ellipticity!!

### More info by selecting on event-shape



## $p(v_n, v_m)$ via event-shape engineering tech.<sup>32</sup>

• Directly observe the functional form (more info than symmetric cumulant)



Expected quadratic corr. for  $v_2 - v_4$ , linear corr. for  $v_2 - v_5 \rightarrow$  final state mode-mixing  $v_4 e^{i4\Psi_4} = c_0 e^{i4\Phi_4} + c_1 (v_2 e^{i2\Phi_2})^2 \Rightarrow$  Fit by  $v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$ 

 $v_5 e^{i5\Psi_5} = c_0 e^{i5\Phi_5} + c_1 v_2 e^{i2\Phi_2} v_3 e^{i3\Phi_3} \Rightarrow ext{ Fit by } v_5 = \sqrt{c_0^2 + c_1^2 v_2^2 v_3^2}$ 

■ anti-correlation  $v_2$ - $v_3$  → anti-correlation of  $\varepsilon_2$ - $\varepsilon_3$  from initial state





Curtsey of L.Pang and X.N Wang, EbyE 3D hydro+AMPT condition

### Origin of flow decorrelation

Shape of overlap driven by eccentricity of F-going and B-going participants





Centrality dependence of F<sub>n</sub> reflects geometry effects



Centrality dependence of  $F_n$  reflects geometry effects Decorrelation of  $v_2, v_3 \& v_4$  is 10-20% stronger in 2.76 TeV



Decorrelation of  $v_2, v_3 \& v_4$  is 10-20% stronger in 2.76 TeV

Scale by beam rapidity removes most difference

 $F_n \propto 1/y_{
m beam} \ y_{
m beam} = \ln(\sqrt{s_{_{
m NN}}}/2) \ igsquar > \ rac{F_n(2760{
m GeV})}{F_n(5020{
m GeV})} = rac{y_{
m beam}(5020{
m GeV})}{y_{
m beam}(2760{
m GeV})} = 1.08$ 



Extensive set of new observables also measured

- Higher-moments of longitudinal decorrelation
- Separating v<sub>n</sub> asymmetry and event-plane twist
- Longitudinal decorrelation between v<sub>n</sub> and v<sub>m</sub>

### System dependence: Xe+Xe vs PbPb

- Consider Glauber model with parameterized longitudinal structure
  - Describe  $v_n$ -ratio vs  $N_{part} \rightarrow$  viscous effects controls by overall size
  - Describe  $F_n$ -ratio vs  $N_{part}/2A \rightarrow$  control by overall shape not the size
- Better agreement than hydro $\rightarrow$  due to wrong longitudinal initial state?



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### Outlook

Strategy: systematically peering into earlier time from large to smaller systems



### Intersection to nuclear structure: a new research frontier

#### https://indico.bnl.gov/event/13769/ RIKEN BNL Research Center Physics Opportunities from the RHIC Isobar Run This workshop will be held virtually.

#### Workshop Organizers

- Jiangyong Jia (Stony Brook)
- Chun Shen (RBRC/Wayne State)
- Derek Teaney (Stony Brook)
- Zhangbu Xu (BNL)

### https://indico.gsi.de/event/14430/

#### **Organizers:**

EMMI Rapid Reaction Task Force

Nuclear Physics Confronts Relativistic Collisions of Isobars Heidelberg University, Germany, May 30 – June 3 & October 12-14 2022 Giuliano Giacalone Jiangyong Jia Vittorio Somà You Zhou



https://esnt.cea.fr/Phocea/Page/index.php?id=107

### https://www.int.washington.edu/programs-and-workshops/23-1a

#### Intersection of nuclear structure and high-energy nuclear collisions

#### Organizers:

January 25-28, 2022

Jiangyong Jia (Stony Brook & BNL) Giuliano Giacalone (ITP Heidelberg) Jacquelyn Noronha-Hostler (Urbana-Champaign) Dean Lee (Michigan State & FRIB) Matt Luzum (São Paulo) Fuqiang Wang (Purdue)

#### Jan 23rd - Feb 24th 2023





- Partonic structure of protons and nuclei
- Physics at low-x and gluon saturation
- The initial stages and nuclear structure in heavy-ion collisions
- Collective dynamics from small to large systems
- New theoretical techniques at large and small coupling
- New facilities: DIS and hadronic experiments

### Do not let your imagination being limited by your detector!