

# Coherence of $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$ and consequences for the determination of $\phi_3$

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## CKM 2016

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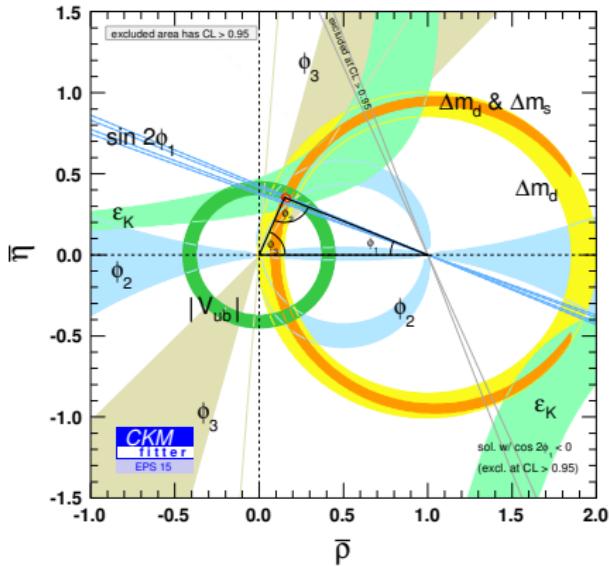


Acknowledgement: CLEO-c colleagues.

- Introduction
- CLEO-c and quantum correlation
- Calculation of CP content  $F_+$
- Extraction of  $c_i$  and  $s_i$
- CPV sensitivity
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# Introduction

## CKM angles - current status



## Current best results for CKM angles

- $\phi_1 = 21.5^{+0.8}_{-0.7}$  deg.
  - $\phi_2 = 85.4^{+4.0}_{-3.8}$  deg.
  - $\phi_3 = 73.2^{+6.3}_{-7.0}$  deg.

Recent results from LHCb

- $\phi_3 = 72.2^{+6.8}_{-7.3}$  deg. [2]

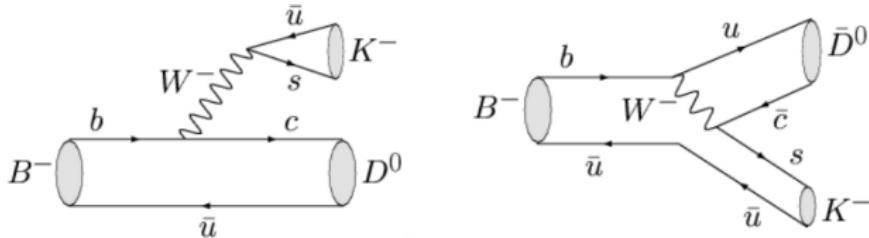
**Figure :** Constraints on CKM parameters as of 2015 [1].

<sup>1</sup> <http://ckmfitter.in2p3.fr>

<sup>2</sup>arXiv:1611.03076v1 [hep-ex]

# $\phi_3$ measurements

- Determine  $\phi_3$  via interference between  $B^- \rightarrow D^0 K^-$  and  $B^- \rightarrow \bar{D}^0 K^-$



colour allowed

$$B^- \rightarrow D^0 K^- \approx V_{cb} V_{us}^*$$

colour suppressed

$$B^- \rightarrow \bar{D}^0 K^- \approx V_{ub} V_{cs}^*$$

- The above two amplitudes are related by

$$\frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B - \phi_3)}$$

- $r_B = \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|$ ,  $\delta_B = \delta(B^- \rightarrow \bar{D}^0 K^-) - \delta(B^- \rightarrow D^0 K^-)$ .
- No loop contribution  $\Rightarrow$  clean way to measure  $\phi_3$ .

# $\phi_3$ measurements - different methods

- Gronau - London - Wyler (GLW) method [3]
  - Modes with known CP content ( $F_+$ ) [4] can be used along with CP eigenstates.
- Giri - Grossman - Soffer - Zupan (GGSZ) method [5]
  - Binned Dalitz plot analysis of multibody  $D$  final states like  $K_S^0\pi^+\pi^-$ ,  $K_S^0K^+K^-$ ,  $K_S^0\pi^+\pi^-\pi^0$ .

- For the decay  $B^- \rightarrow D(K_S^0 h^+ h^-) K^-$

$$\Gamma_i^- = K_i + r_B^2 \bar{K}_i + 2\sqrt{K_i \bar{K}_i} (c_i x_- + s_i y_-),$$

and for  $B^+ \rightarrow D(K_S^0 h^+ h^-) K^+$ ,

$$\Gamma_i^+ = \bar{K}_i + r_B^2 K_i + 2\sqrt{K_i \bar{K}_i} (c_i x_+ - s_i y_+).$$

- $x_{\pm} = r_B \cos(\delta_B \pm \phi_3)$ ;  $y_{\pm} = r_B \sin(\delta_B \pm \phi_3)$ .

- $c_i, s_i$  - cos and sin of the strong phase difference between  $D^0$  and  $\bar{D}^0$  averaged over the region of phase space.

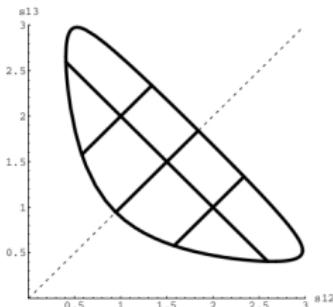


Figure : A typical Dalitz plot binning for a three body  $D$  decay.

<sup>3</sup> M. Gronau and D. London, Phys. Lett. B **253**, 483 (1991); M. Gronau and D. Wyler, Phys. Lett. B **265**, 172 (1991).

<sup>4</sup> M. Nayak *et al.* (CLEO collaboration), Phys. Lett. B **740**, 1 (2015).

<sup>5</sup> A. Giri, Yu. Grossman, A. Soffer and J. Zupan, Phys. Rev. D **68**, 054018 (2003).

# Motivation

- Information on the  $D$  decay is required to determine  $x, y$ .
- Quantum correlated  $D\bar{D}$  mesons produced in  $e^+e^-$  collisions at an energy corresponding to  $\Psi(3770)$  at CLEO-c can be used.
- A  $D$  decay mode not yet used is  $K_S^0\pi^+\pi^-\pi^0$ .
- The decay  $D^0 \rightarrow K_S^0\pi^+\pi^-\pi^0$  has a relatively large branching fraction of 5.2% which is almost twice that of  $K_S^0\pi^+\pi^-$  [6].
- Interesting resonance substructure.
  - $K_S^0\omega$  - CP eigenstate - GLW like.
  - $K^-\pi^+\pi^0$  - Cabibbo-favored state (CF) - ADS like.
- As powerful as  $K_S^0\pi^+\pi^-$  in the determination of  $\phi_3$ ?

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<sup>6</sup>C. Patrignani *et al.* (Particle Data Group), Chin. Phys. C **40**, 100001 (2016).

# CLEO-c and quantum correlation

# Quantum correlated $D$ mesons at CLEO-c

- $\Psi \rightarrow D\bar{D}$  are produced coherently in the  $C = -1$  state.

$$\frac{(|D\rangle|\bar{D}\rangle - |\bar{D}\rangle|D\rangle)}{\sqrt{2}}$$

- If  $\Psi(3770)$  decays into two states  $F$  and  $G$ , then decay rate ( $\Gamma$ ) depends on their CP eigenvalue.

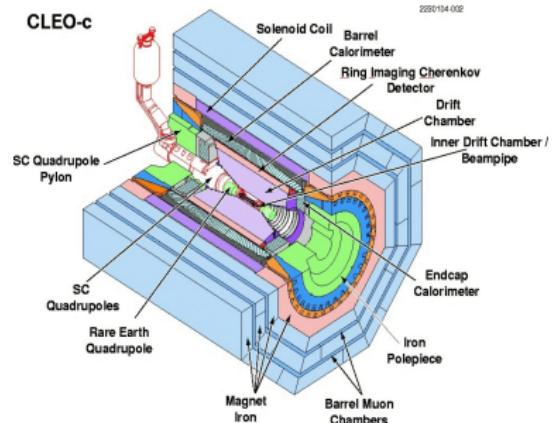


Figure : CLEO-c detector.

- $F = \text{CP even (odd)}, G = \text{CP odd (even)} \Rightarrow \text{two-fold enhancement.}$
- $F = \text{CP even (odd)}, G = \text{CP even (odd)} \Rightarrow \text{zero.}$
- $\Gamma$  changes with  $F$  or  $G$  being quasi CP states ( $\pi^+\pi^-\pi^0$ ) or self conjugate states ( $K_S^0\pi^+\pi^-$ ).

# CLEO-c data sample and signal selection

- A total of  $818 \text{ pb}^{-1}$  data collected at the CLEO-c -  $D\bar{D}$  pairs from the  $\Psi(3770)$ .
- One of the  $D$  mesons reconstructed to  $K_S^0\pi^+\pi^-\pi^0$  (signal) and the other one to any other channel (tag).
- Fully reconstructed modes -  $M_{bc}$  and  $\Delta E$ .
- Partially reconstructed modes - missing mass technique.

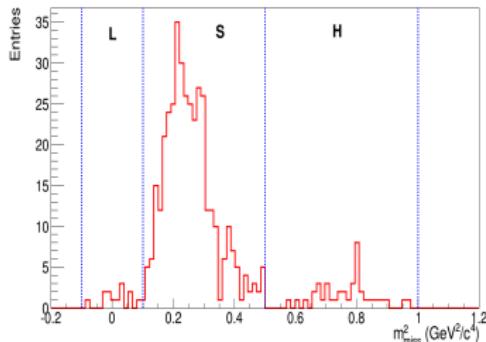


Figure :  $M_{\text{miss}}^2$  plot for  $K_L^0\pi^0$  tag for the data sample.

Type	mode	yield
CP even tags	$K^+K^-$	$200.7 \pm 14.2$
	$\pi^+\pi^-$	$91.45 \pm 9.59$
	$K_S^0\pi^0\pi^0$	$106.3 \pm 10.9$
	$K_L^0\pi^0$	$357.3 \pm 20.2$
	$K_L^0\omega$	$162.1 \pm 13.7$
CP odd tags	$K_S^0\pi^0$	$93.97 \pm 9.84$
	$K_S^0\eta$	$11.64 \pm 3.68$
	$K_S^0\eta'$	$7 \pm 3$
Quasi CP tags	$\pi^+\pi^-\pi^0$	$428.8 \pm 21.7$
Self conjugate tags	$K_S^0\pi^+\pi^-$	$504.8 \pm 23.3$
	$K_L^0\pi^+\pi^-$	$864.1 \pm 46.1$
	$K_S^0\pi^+\pi^-\pi^0$	$176.4 \pm 14.8$
Flavour tag	$K^\pm e^\mp\nu$	$1010 \pm 32$

# Calculation of $F_+$

## CP content ( $F_+$ )

- The double tagged yield for the signal and tag

$$M(S|T) = 2N_{D\bar{D}} \times BF(S) \times BF(T) \times \epsilon(S|T) \times [1 - \lambda_{CP}(2F_+ - 1)].$$

- The single tag yield

$$S(T) = 2N_{D\bar{D}} \times BF(T) \times \epsilon(T).$$

- If we assume  $\epsilon(S|T) = \epsilon(S)\epsilon(T)$ , then we get  $N^+$  for CP odd tag and  $N^-$  for CP even tag as follows:

$$N^\pm = \frac{M(S|T)}{S(T)} = BF(S) \times \epsilon(S) \times [1 - \lambda_{CP}(2F_+ - 1)].$$

- From these, we can calculate  $F_+$  as

$$F_+ = \frac{N^+}{N^+ + N^-}; \quad F_+ = 1 \Rightarrow \text{CP even}, F_+ = 0 \Rightarrow \text{CP odd}.$$

# Calculation of $F_+$ - CP tags

- The CP odd and CP even tags are used to evaluate  $N^+$  and  $N^-$  respectively.

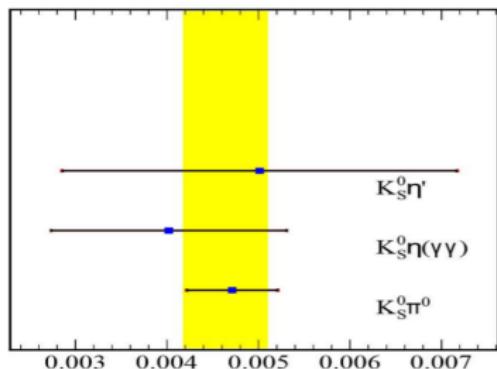


Figure :  $N^+$  values for the CP odd tags. The yellow region shows the average value

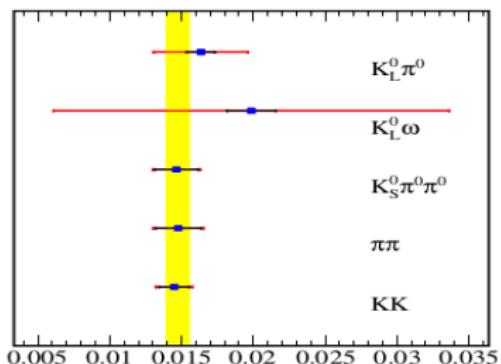


Figure :  $N^-$  values for the CP even tags. The yellow region shows the average value

Note: The x-axis scale for  $N^+$  is much smaller than that of  $N^-$ .

- The value of  $F_+$  is obtained to be  **$0.240 \pm 0.021$** , i.e  $K_S^0\pi^+\pi^-\pi^0$  is significantly **CP odd**.

## Calculation of $F_+$ - $\pi^+\pi^-\pi^0$ tag

- $F_+$  for  $\pi^+\pi^-\pi^0 = 0.973 \pm 0.017$  [7].
- Define  $N^{\pi^+\pi^-\pi^0}$  as the ratio of double tagged events and  $\pi^+\pi^-\pi^0$  single tag events

$$N^{\pi^+\pi^-\pi^0} = \frac{M(K_S^0\pi^+\pi^-\pi^0|\pi^+\pi^-\pi^0)}{S(\pi^+\pi^-\pi^0)}.$$

- Then with  $N^+$  from CP tags, we can get

$$F_+^{K_S^0\pi^+\pi^-\pi^0} = \frac{N^+ F_+^{\pi^+\pi^-\pi^0}}{N^{\pi^+\pi^-\pi^0} - N^+ + 2N^+ F_+^{\pi^+\pi^-\pi^0}}.$$

- With CP and  $\pi^+\pi^-\pi^0$  tags,  $F_+$  is **0.244±0.021**.

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<sup>7</sup>S. Malde et.al, Phys. Lett. B **747**, 9 (2015).

# Calculation of $F_+$ - $K_S^0\pi^+\pi^-$ and $K_L^0\pi^+\pi^-$ tags

- The  $K_S^0\pi^+\pi^-$  and  $K_L^0\pi^+\pi^-$  Dalitz plots are binned according to Equal  $\delta_D$  BABAR 2008 scheme [8].

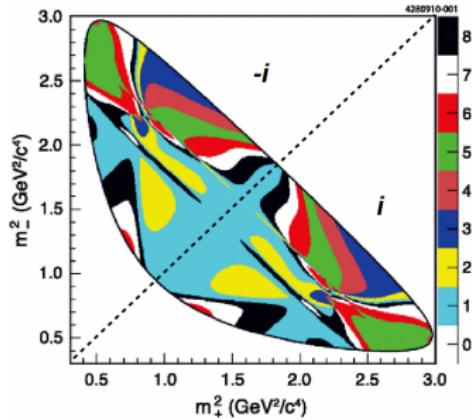


Figure :  $D^0 \rightarrow K_S^0\pi^+\pi^-$  Dalitz plot.

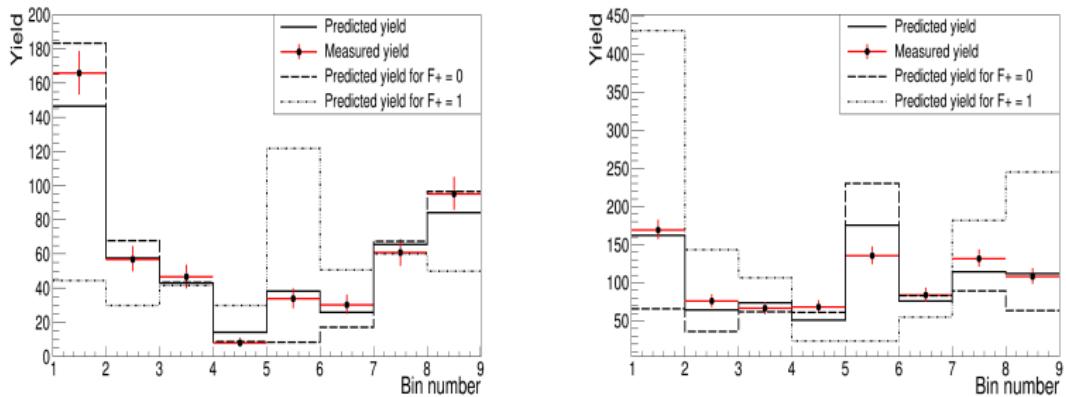
$$Y_i^{K_S^0\pi^+\pi^-} = h_{K_S^0\pi^+\pi^-}(K_i^{K_S^0\pi^+\pi^-} + K_{-i}^{K_S^0\pi^+\pi^-} - 2c_i \sqrt{K_i^{K_S^0\pi^+\pi^-} K_{-i}^{K_S^0\pi^+\pi^-} (2F_+^{K_S^0\pi^+\pi^-\pi^0} - 1)}).$$

$$Y_i^{K_L^0\pi^+\pi^-} = h_{K_L^0\pi^+\pi^-}(K_i^{K_L^0\pi^+\pi^-} + K_{-i}^{K_L^0\pi^+\pi^-} + 2c_i \sqrt{K_i^{K_L^0\pi^+\pi^-} K_{-i}^{K_L^0\pi^+\pi^-} (2F_+^{K_L^0\pi^+\pi^-\pi^0} - 1)}).$$

<sup>8</sup>B. Aubert et al. (BaBar collaboration), Phys. Rev. D **78**, 034023 (2008).

# Calculation of $F_+$ - $K_S^0\pi^+\pi^-$ and $K_L^0\pi^+\pi^-$ tags

- Fit with 64 observables;  $\frac{\chi^2}{\text{DoF}} = 1.3$ .



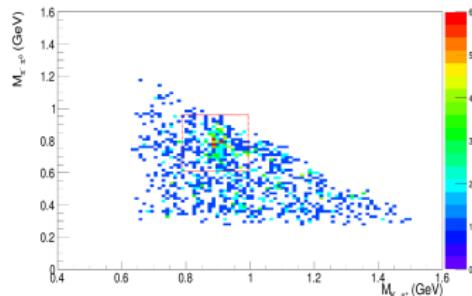
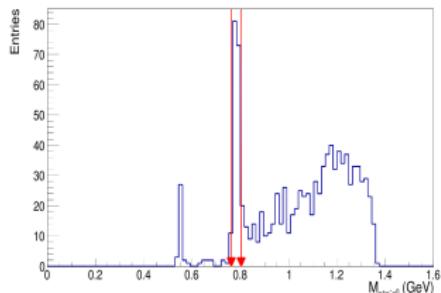
**Figure :** The predicted and measured yields for  $K_S^0\pi^+\pi^-$  (left) and  $K_L^0\pi^+\pi^-$  (right).

- $F_+$  is found to be  **$0.265 \pm 0.029$** .
- With all the three methods, the average  $F_+$  is  **$0.246 \pm 0.018$** .

# Extraction of $c_i$ and $s_i$

# Binning $K_S^0\pi^+\pi^-\pi^0$ phase space

- $N_{\text{bins}} > 4 \Rightarrow \phi_3$  extraction in  $B^\pm \rightarrow DK^\pm$  data in GGSZ framework - requires  $c_i$ ,  $s_i$ ,  $K_i$  and  $\bar{K}_i$ .
- Dividing the 5-D phase space of  $K_S^0\pi^+\pi^-\pi^0$  - not as trivial as the 2-D phase space of  $K_S^0\pi^+\pi^- \Rightarrow i$  and  $-i$  symmetry non-trivial.
- Amplitude model not available  $\Rightarrow$  a proper optimisation difficult.
- Split the phase-space into a series of bins around the resonances and work out partial rates in each.
- Exclusive binning.



**Figure :** Invariant mass distribution for  $\pi^+\pi^-\pi^0$  (left) and 2-D distribution between the invariant masses of  $K_S^0\pi^-$  and  $\pi^+\pi^0$  (right).

# Extraction of $c_i$ and $s_i$

- For a CP tag, the double tagged yield is given by

$$M_i^\pm = h_{CP} \left[ K_i + \bar{K}_i \pm 2\sqrt{K_i \bar{K}_i} c_i \right].$$

For  $\pi^+\pi^-\pi^0$  tag, the  $c_i$  sensitive term is scaled by  $(2F_+ - 1)$  rather than 1.

- For  $K_S^0\pi^+\pi^-\pi^0$  double tagged events, the yield is given by

$$M_{ij} = h_{corr} \left[ K_i \bar{K}_j + \bar{K}_i K_j - 2\sqrt{K_i \bar{K}_j \bar{K}_i K_j} (c_i c_j + s_i s_j) \right].$$

- For  $K_S^0\pi^+\pi^-$  tag

$$M_{i\pm j}^{K_S\pi\pi} = h_{K_S\pi\pi} \left[ K_i K_{\mp j}^{K_S\pi\pi} + \bar{K}_i \bar{K}_{\pm j}^{K_S\pi\pi} - 2\sqrt{K_i K_{\pm j}^{K_S\pi\pi} \bar{K}_i \bar{K}_{\mp j}^{K_S\pi\pi}} (c_i c_j^{K_S\pi\pi} \pm s_i s_j^{K_S\pi\pi}) \right].$$

- Similarly for  $K_L^0\pi^+\pi^-$  tag,

$$M_{i\pm j}^{K_L\pi\pi} = h_{K_L\pi\pi} \left[ K_i K_{\mp j}^{K_L\pi\pi} + \bar{K}_i \bar{K}_{\pm j}^{K_L\pi\pi} + 2\sqrt{K_i K_{\pm j}^{K_L\pi\pi} \bar{K}_i \bar{K}_{\mp j}^{K_L\pi\pi}} (c_i c_j^{K_L\pi\pi} \pm s_i s_j^{K_L\pi\pi}) \right].$$

# Extraction of $c_i$ and $s_i$

Bin number	Specification	$K_i$	$\bar{K}_i$
1	$m(\pi^+\pi^-\pi^0) \approx m(\omega)$	$0.222 \pm 0.019$	$0.176 \pm 0.017$
2	$m(K_S^0\pi^-) \approx m(K^{*-})$ & $m(\pi^+\pi^0) \approx m(\rho^+)$	$0.394 \pm 0.022$	$0.190 \pm 0.017$
3	$m(K_S^0\pi^+) \approx m(K^{*+})$ & $m(\pi^-\pi^0) \approx m(\rho^-)$	$0.087 \pm 0.013$	$0.316 \pm 0.021$
4	$m(K_S^0\pi^-) \approx m(K^{*-})$	$0.076 \pm 0.012$	$0.046 \pm 0.009$
5	$m(K_S^0\pi^+) \approx m(K^{*+})$	$0.057 \pm 0.010$	$0.065 \pm 0.011$
6	$m(K_S^0\pi^0) \approx m(K^{*0})$	$0.059 \pm 0.011$	$0.092 \pm 0.013$
7	$m(\pi^+\pi^0) \approx m(\rho^+)$	$0.045 \pm 0.009$	$0.045 \pm 0.009$
8	Remainder	$0.061 \pm 0.011$	$0.070 \pm 0.011$

- The semileptonic tag  $K^\pm e^\mp \nu$  is used to calculate  $K_i$  and  $\bar{K}_i$ , the fraction of decays in each bin.
- The double tagged yields are given to the fitter along with the  $c_i$ ,  $s_i$ ,  $K_i$  and  $\bar{K}_i$  values for  $K_S^0\pi^+\pi^-$  and  $K_L^0\pi^+\pi^-$  [9] as input.
- Corrected for bin-to-bin migration.

<sup>9</sup>J. Libby et al. (CLEO collaboration), Phys. Rev. D **82**, 112006 (2010).

## $c_i$ and $s_i$ results - preliminary

- The combined fit: 472 observables including different tag yields in each bin;  $\frac{\chi^2}{\text{DoF}} = 1.04$ .

Bin	$c_i$	$s_i$
1	$-1.12 \pm 0.12$	$0.12 \pm 0.17$
2	$-0.29 \pm 0.07$	$0.11 \pm 0.13$
3	$-0.41 \pm 0.09$	$-0.08 \pm 0.18$
4	$-0.84 \pm 0.12$	$-0.73 \pm 0.34$
5	$-0.54 \pm 0.13$	$0.65 \pm 0.13$
6	$-0.22 \pm 0.12$	$1.37 \pm 0.22$
7	$-0.90 \pm 0.16$	$-0.12 \pm 0.40$
8	$-0.70 \pm 0.14$	$-0.03 \pm 0.44$

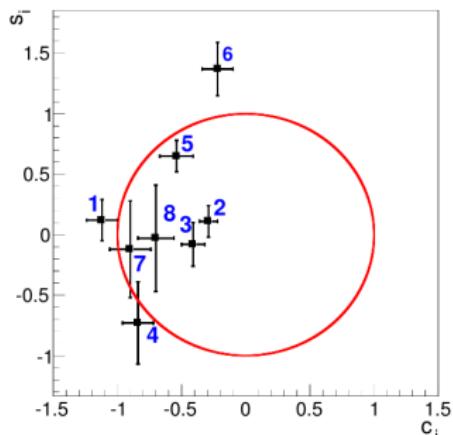


Figure :  $c_i$  and  $s_i$  values in each bin.

- The uncertainties shown are statistical only.
- $c_i < 0 \Rightarrow \text{CP oddness}$  of  $K_S^0 \pi^+ \pi^- \pi^0$ .

# CPV sensitivity and summary

# Estimates of $\phi_3$ sensitivity with $B^\pm \rightarrow D(K_S^0\pi^+\pi^-\pi^0)K^\pm$

- Assumed increase in BF compensated by loss of efficiency due to  $\pi^0$  in final state.
- With 1200 events (Belle sample of  $B^\pm \rightarrow D(K_S^0\pi^+\pi^-)K^\pm$ )  
 $\sigma_{\phi_3} = 25^\circ$  - 1000 pseudo experiments using  $c_i$ ,  $s_i$ ,  $K_i$  and  $\bar{K}_i$  measurements reported.
- Project to a  $50 \text{ ab}^{-1}$  sample  $\sigma_{\phi_3} = 3.5^\circ$ .
- Compare to  $B^\pm \rightarrow D(K_S^0\pi^+\pi^-)K^\pm$   $\sigma_{\phi_3} \sim 2^\circ$ .
- Improvements:
  - Optimized binning once a  $D^0 \rightarrow K_S^0\pi^+\pi^-\pi^0$  amplitude model developed.
  - Finer binning possible with  $10 \text{ fb}^{-1}$  of BESIII data.
- Caveat: background to be studied.

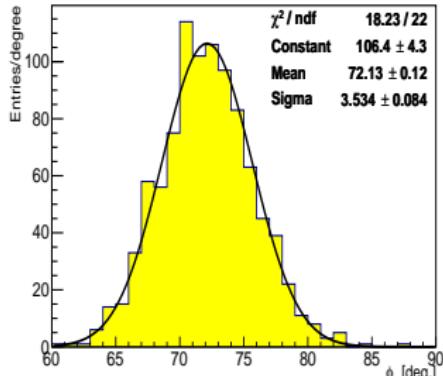


Figure :  $\phi_3$  sensitivity with  $50 \text{ ab}^{-1}$  Belle II sample.

- Calculated the CP content  $F_+$  for the decay  $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$  from CLEO-c data to be  **$0.246 \pm 0.018$** .
- Addition of this mode to quasi-GLW methods to determine  $\phi_3$ .
- Extracted the strong phase differences by introducing an eight bin scheme for the  $K_S^0 \pi^+ \pi^- \pi^0$  phase space.
- Addition to GGSZ formalism to determine  $\phi_3$ .
- Sensitivity to  $\phi_3$  from a  $50 \text{ ab}^{-1}$  sample,  $\sigma_{\phi_3} = 3.5^\circ$ .