

# Penguin pollution in $\beta$ and $\beta_s$

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- 1  $B$  decays to charmonium
- 2 Summary

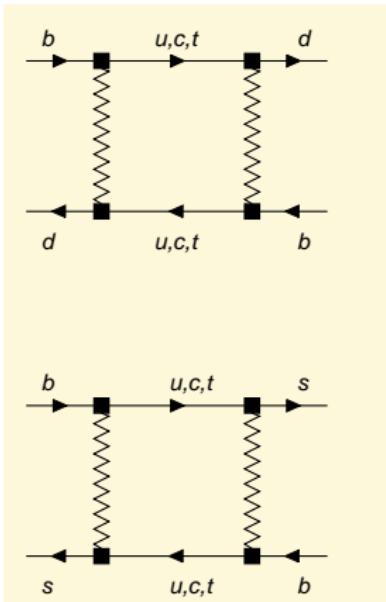
## $B$ decays to charmonium

Time-dependent CP asymmetries  
(for  $q=d$  or  $s$ ):

$$A_{\text{CP}}^{B_q \rightarrow f}(t) = \frac{S_f \sin(\Delta m_q t) - C_f \cos(\Delta m_q t)}{\cosh(\Delta \Gamma_q t/2) + A_{\Delta \Gamma_q}^f \sinh(\Delta \Gamma_q t/2)}$$

$\Delta m_q$ : mass difference

$\Delta \Gamma_q$ : width difference



The coefficients  $S_f$ ,  $C_f$ , and  $A_{\Delta \Gamma_q}^f$  encode the information on the decay amplitudes  $A_f \equiv A(B_q \rightarrow f)$  and  $\bar{A}_f \equiv A(\bar{B}_q \rightarrow \bar{f})$ .

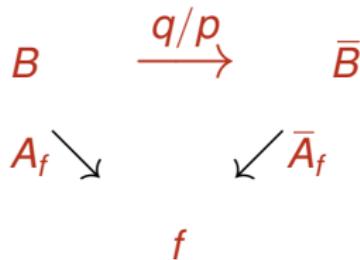
Golden mode:  $B$  decay into a CP eigenstate  $f = f_{\text{CP}}$  which only involves a single CKM factor ( $\Rightarrow |A_{f_{\text{CP}}}| = |\bar{A}_{f_{\text{CP}}}|$  and  $|\lambda_f| = 1$ ).

$$CP|f_{\text{CP}}\rangle = \eta_{f_{\text{CP}}} |f_{\text{CP}}\rangle \quad \text{with } \eta_{f_{\text{CP}}} = \pm 1.$$

Time-dependent CP asymmetry:

$$a_{f_{\text{CP}}}(t) = -\frac{\text{Im } \lambda_f \sin(\Delta m_q t)}{\cosh(\Delta \Gamma_q t/2) - \text{Re } \lambda_f \sinh(\Delta \Gamma_q t/2)},$$

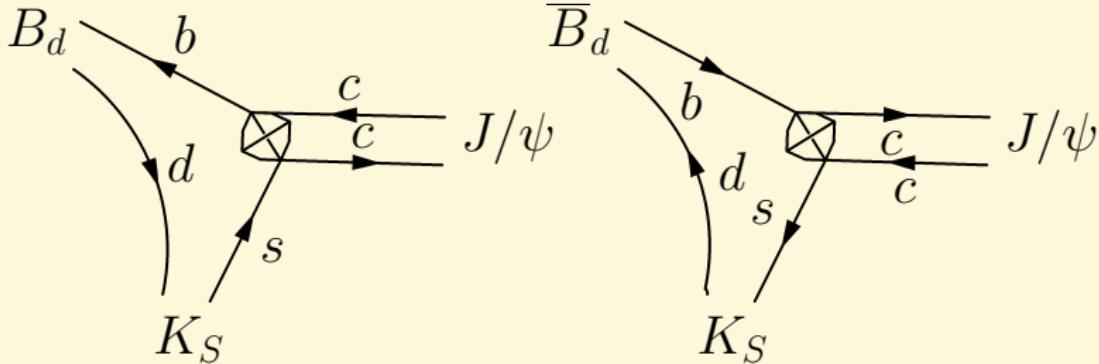
$\text{Im } \lambda_f$  quantifies the CP violation in the interference between mixing and decay:



$$\text{Recall: } \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

## Example 1:

$$B_d \rightarrow J/\psi K_S \quad \Rightarrow \quad |\bar{f}\rangle = -|f\rangle \text{ (CP-odd eigenstate)}$$



$$a_{J/\psi K_S}(t) \simeq -\sin(2\beta) \sin(\Delta m_d t),$$

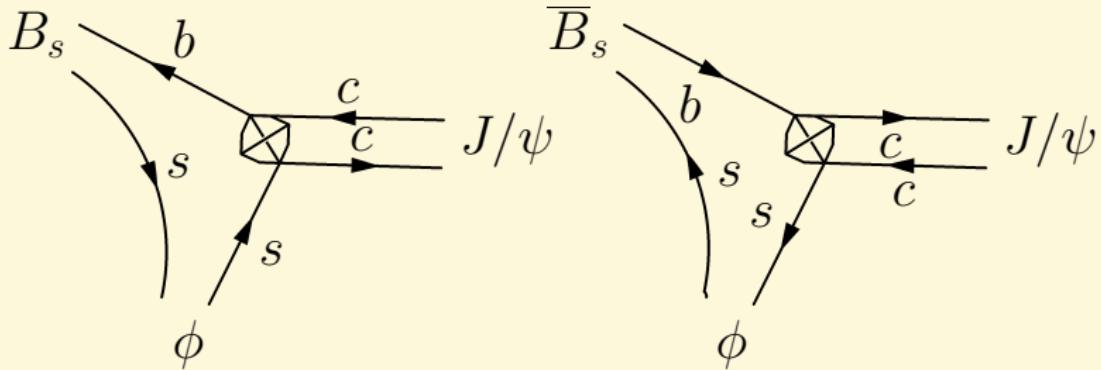
where

$$\beta = \arg \left[ -\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right]$$

golden mode to measure the angle  $\beta$  of the unitarity triangle

## Example 2:

$$B_s \rightarrow (J/\psi \phi)_{L=0} \quad \Rightarrow \quad |\bar{f}\rangle = |f\rangle \text{ (CP-even eigenstate)}$$



$$a_{(J/\psi \phi)_{L=0}}(t) = -\frac{\sin(2\beta_s) \sin(\Delta m_s t)}{\cosh(\Delta \Gamma_s t/2) - \cos(2\beta_s) \sinh(\Delta \Gamma_s t/2)},$$

where

$$\beta_s = \arg \left[ -\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right] \simeq \lambda^2 \bar{\eta}$$

## Penguin pollution in $b \rightarrow c\bar{c}s$ decays

The decay amplitudes  $A(B_{d,s} \rightarrow J/\psi X)$  are dominated by the CKM structure  $V_{cb} V_{cs}^*$ , but have a small contribution with  $V_{ub} V_{us}^*$ , called penguin pollution.

How golden are these modes?

Experimental world average:

$$S_{J/\psi K_S} = 0.665 \pm 0.024$$

Averaging all charmonia and including final states with  $K_L$  gives

$$\sin(2\beta) = 0.679 \pm 0.020, \quad \text{HFAG winter 2015}$$

... if the penguin pollution is set to zero.

## Penguin pollution in $b \rightarrow c\bar{c}s$ decays

$$S(B_q \rightarrow f) = \sin(\phi_q + \Delta\phi_q)$$

If one neglects  $\lambda_u = V_{ub}V_{us}^*$  in the decay amplitude,  $S(B_q \rightarrow f)$  measures  $\phi_q$  with

$$\begin{aligned} B_d \rightarrow J/\psi K^0: & \quad \phi_d = 2\beta \\ B_s \rightarrow J/\psi \phi: & \quad \phi_s = -2\beta_s \end{aligned}$$

The penguin pollution  $\Delta\phi_q$  is parametrically suppressed by

$$\epsilon \equiv \left| \frac{V_{us} V_{ub}}{V_{cs} V_{cb}} \right| = 0.02.$$

New method to constrain  $\Delta\phi_q$ :

Ph. Frings, UN, M. Wiebusch, Phys.Rev.Lett. 115 (2015) 061802, 1503.00859

# Overview: Experimental and Theoretical Precision

$$\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin \phi_d \quad S_{J/\psi K^0} = \sin(\phi_d + \Delta\phi_d)$$

HFAG 2014:

$$\sigma_{S_{J/\psi K^0}} = 0.02 \quad \sigma_{\phi_d} = 1.5^\circ$$

| Author                      | $\Delta S_{J/\psi K^0}$    | $\Delta\phi_d$                      | Method                      |
|-----------------------------|----------------------------|-------------------------------------|-----------------------------|
| De Bruyn,<br>Fleischer 2014 | $-0.01 \pm 0.01$           | $- (1.1^\circ)^{+0.70}_{-0.85}$     | SU(3) flavour               |
| Jung 2012                   | $ \Delta S  \lesssim 0.01$ | $ \Delta\phi_d  \lesssim 0.8^\circ$ | SU(3) flavour               |
| Ciuchini <i>et al.</i> 2011 | $0.00 \pm 0.02$            | $0.0^\circ \pm 1.6^\circ$           | U-spin                      |
| Faller <i>et al.</i> 2009   | $[-0.05, -0.01]$           | $[-3.9, -0.8]^\circ$                | U-spin                      |
| Boos <i>et al.</i> 2004     | $-(2 \pm 2) \cdot 10^{-4}$ | $0.0^\circ \pm 0.0^\circ$           | perturbative<br>calculation |

Extract penguin contribution from  $b \rightarrow c\bar{c}d$  control channels such as  $B_d \rightarrow J/\psi \pi^0$  or  $B_s \rightarrow J/\psi K_S$ , in which the penguin contribution is Cabibbo-unsuppressed.

Drawbacks:

- statistics in control channels smaller by factor of 20
- size of  $SU(3)$  breaking in penguin contributions to  $B_{d,s} \rightarrow J/\psi X$  decays unclear

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- $SU(3)$  does not help in  $B_s \rightarrow J/\psi \phi$ , because  $\phi$  is an equal mixture of octet and singlet.

Define  $\lambda_q = V_{qb} V_{qs}^*$  and use  $\lambda_t = -\lambda_u - \lambda_c$ .

Generic  $B$  decay amplitude:

$$A(B \rightarrow f) = \lambda_c t_f + \lambda_u p_f$$

Terms  $\propto \lambda_u = V_{ub} V_{us}^*$  lead to the penguin pollution.

Remark: One can include first-order SU(3) breaking in the extraction of  $t_f$  from control channels (Jung 2012).

This is not possible for  $p_f$ .

# What contributes to the penguin pollution $p_f$ ?

Penguin operators:

$$\langle f | \sum_{i=3}^6 C_i Q_i | B \rangle \approx C_8^t \langle f | Q_{8V} | B \rangle$$

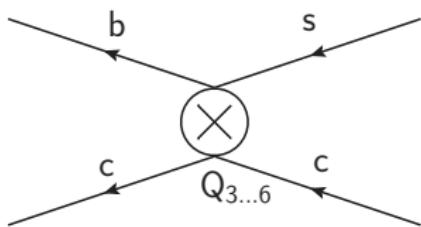
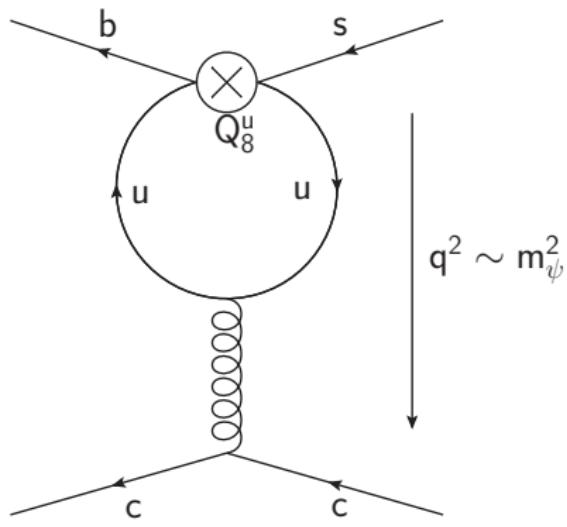
with

$$C_8^t \equiv 2(C_4 + C_6)$$

$$Q_{8V} \equiv (\bar{s} T^a b)_{V-A} (\bar{c} T^a c)_V$$

Tree-level operator insertion:

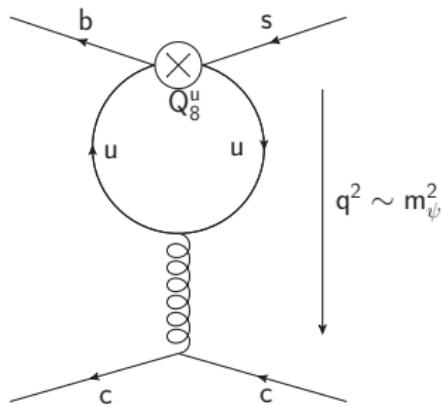
$$\langle f | C_0 Q_0^u + C_8 Q_8^u | B \rangle$$



# Feared and respected: the up-quark loop

Idea: employ an **operator product expansion**,

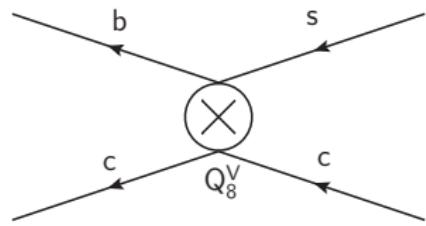
to factorise the *u*-quark loop into a perturbative coefficient and matrix elements of local operators:



$$q^2 \sim m_\psi^2$$

$$q^2 \gg \Lambda_{QCD}^2$$

→



$$Q_8 V = (\bar{s} T^a b)_{V-A} (\bar{c} T^a c)_V$$

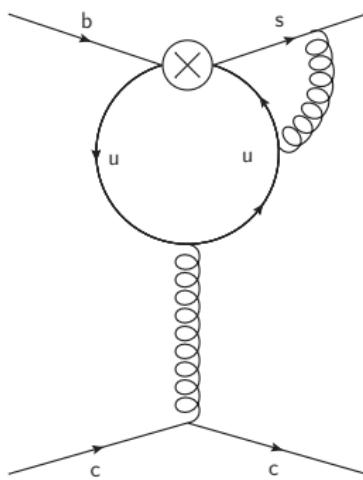
## Is this Bander Soni Silverman?

Perturbative approach is due to Bander Soni Silverman (1979) (BSS).  
Boos, Mannel and Reuter (2004) applied this method to  $B_d \rightarrow J/\psi K_S$ .  
Our study:

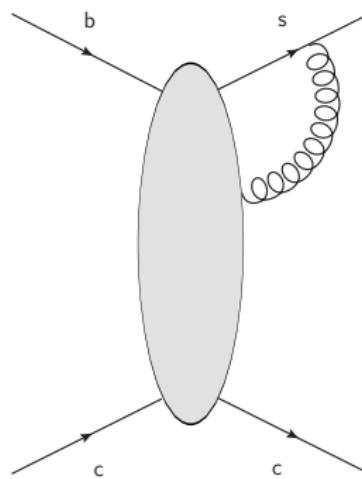
- Investigate soft and collinear infrared divergences to prove factorization.
- Analyse spectator scattering.
- Organise matrix elements by  $1/N_c$  counting, no further assumptions on magnitudes and strong phases.

# Infrared Structure - Collinear Divergences

Collinear divergent diagrams



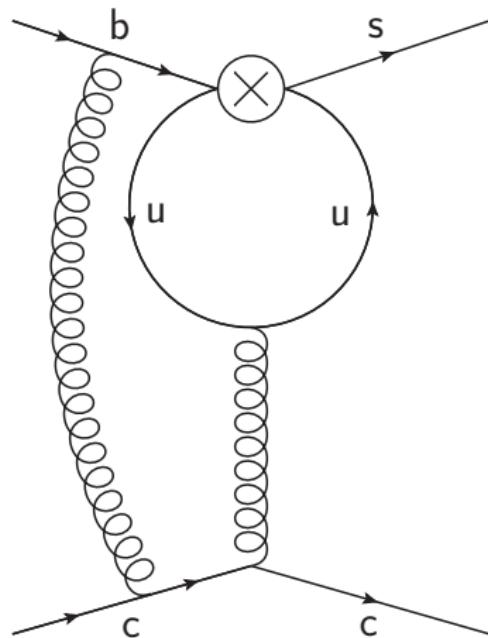
are infrared-safe if summed over



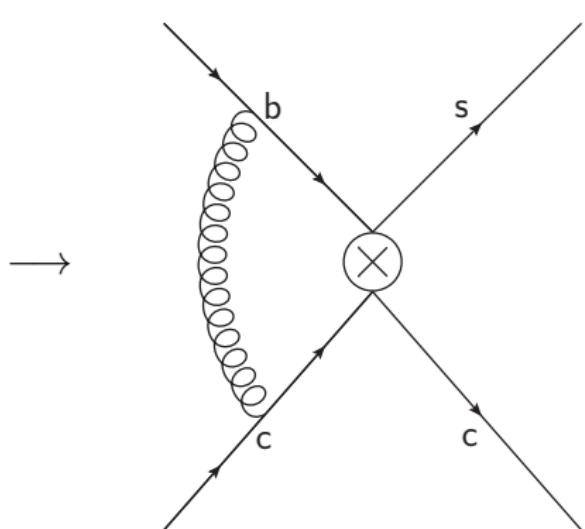
or are individually infrared-safe if considered in a physical gauge.

# Infrared Structure - Soft Divergences

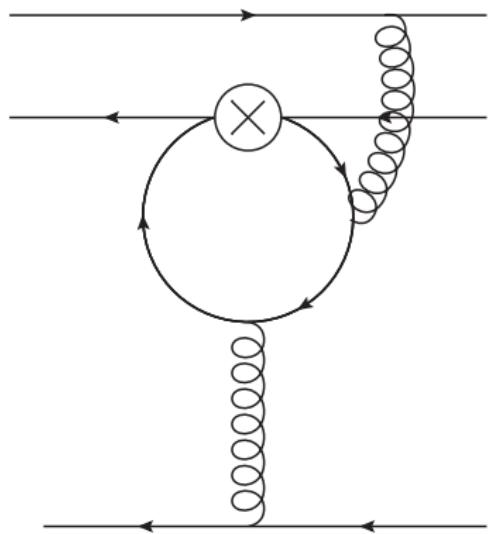
Soft divergent diagrams ...



... factorise.



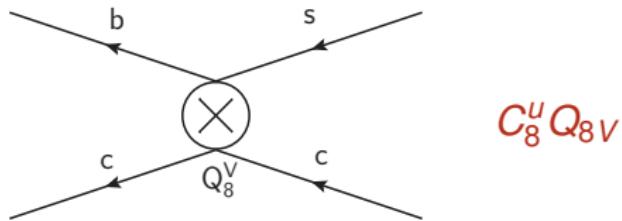
Spectator scattering  
diagrams...



... factorise up to power-suppressed contributions.

# Operator product expansion works!

- Soft divergences factorise.
- Collinear divergences cancel or factorise.
- Non-factorisable spectator scattering is power-suppressed.  
⇒ Up-quark penguin can be absorbed into a Wilson coefficient  $C_8^u$ !



Local operators:

$$\begin{aligned} Q_{0V} &\equiv (\bar{s}b)_{V-A}(\bar{c}c)_V \\ Q_{8V} &\equiv (\bar{s}T^a b)_{V-A}(\bar{c}T^a c)_V \end{aligned}$$

$$\begin{aligned} Q_{0A} &\equiv (\bar{s}b)_{V-A}(\bar{c}c)_A \\ Q_{8A} &\equiv (\bar{s}T^a b)_{V-A}(\bar{c}T^a c)_A \end{aligned}$$

## $1/N_c$ counting

For example:  $B_d \rightarrow J/\psi K^0$

$$V_0 = \langle J/\psi K^0 | Q_{0V} | B_d \rangle = 2f_\psi m_B p_{cm} F_1^{BK} \left[ 1 + \mathcal{O}\left(\frac{1}{N_c^2}\right) \right]$$

$1/N_c$  counting for  $V_8, A_8 \equiv \langle J/\psi K^0 | Q_{8V,8A} | B_d \rangle$ :

- Octet matrix elements are suppressed by  $1/N_c$  w.r.t. singlet  $V_0$
- Motivated by  $1/N_c$  counting set the limits:  $|V_8|, |A_8| \leq V_0/3$

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Does the  $1/N_c$  expansion work?

$$\frac{BR(B_d \rightarrow J/\psi K^0)|_{\text{th}}}{BR(B_d \rightarrow J/\psi K^0)|_{\text{exp}}} = 1 \Rightarrow 0.06|V_0| \leq |V_8 - A_8| \leq 0.19|V_0|$$

## Results

$$A_{\text{CP}}^{B_q \rightarrow f}(t) = \frac{S_f \sin(\Delta m_q t) - C_f \cos(\Delta m_q t)}{\cosh(\Delta \Gamma_q t/2) + A_{\Delta \Gamma_q}^f \sinh(\Delta \Gamma_q t/2)}$$

$B_d$  decays:

| Final State:                       | $J/\psi K_S$ | $\psi(2S)K_S$ | $(J/\psi K^*)^0$ | $(J/\psi K^*)^{\parallel}$ | $(J/\psi K^*)^{\perp}$ |
|------------------------------------|--------------|---------------|------------------|----------------------------|------------------------|
| $\max( \Delta\phi_d )$ [°]         | 0.68         | 0.74          | 0.85             | 1.13                       | 0.93                   |
| $\max( \Delta S_f )$ [ $10^{-2}$ ] | 0.86         | 0.94          | 1.09             | 1.45                       | 1.19                   |
| $\max( C_f )$ [ $10^{-2}$ ]        | 1.33         | 1.33          | 1.65             | 2.19                       | 1.80                   |

... and more.

$B_s$  decays:

| Final State                        | $(J/\psi \phi)^0$ | $(J/\psi \phi)^{\parallel}$ | $(J/\psi \phi)^{\perp}$ |
|------------------------------------|-------------------|-----------------------------|-------------------------|
| $\max( \Delta\phi_s )$ [°]         | 0.97              | 1.22                        | 0.99                    |
| $\max( \Delta S_f )$ [ $10^{-2}$ ] | 1.70              | 2.13                        | 1.73                    |
| $\max( C_f )$ [ $10^{-2}$ ]        | 1.89              | 2.35                        | 1.92                    |

## Cabibbo-unsuppressed $p_f/t_f$

We can also constrain  $p_f/t_f$  in  $b \rightarrow c\bar{c}d$  decays:

$B_d$  decays:

| Final State                    | $J/\psi\pi^0$ | $(J/\psi\rho)^0$ | $(J/\psi\rho)^{\parallel}$ | $(J/\psi\rho)^{\perp}$ |
|--------------------------------|---------------|------------------|----------------------------|------------------------|
| $\max( \Delta S_f ) [10^{-2}]$ | 18            | 22               | 27                         | 22                     |
| $\max( C_f ) [10^{-2}]$        | 29            | 35               | 41                         | 36                     |

$B_s$  decays:

| Final State                    | $J/\psi K_S$ |
|--------------------------------|--------------|
| $\max( \Delta S_f ) [10^{-2}]$ | 26           |
| $\max( C_f ) [10^{-2}]$        | 27           |

## $B_d \rightarrow J/\psi \pi^0$ : Belle or BaBar?

|                     | $S_{J/\psi \pi^0}$ | $C_{J/\psi \pi^0}$ |
|---------------------|--------------------|--------------------|
| BaBar (Aubert 2008) | $-1.23 \pm 0.21$   | $-0.20 \pm 0.19$   |
| Belle (Lee 2007)    | $-0.65 \pm 0.22$   | $-0.08 \pm 0.17$   |

Our results:

$$-0.86 \leq S_{J/\psi \pi^0} \leq -0.50$$

$$-0.29 \leq C_{J/\psi \pi^0} \leq 0.29$$

→ Belle favoured

- OPE works for the penguin pollution in  $B_{d,s}$  decays to charmonium, defining the “**BSS mechanism**” for the up-quark loop.
- No mysterious long-distance enhancement of up-quark penguins.
- Matrix elements are the dominant source of uncertainty. The charm-quark loop is contained in the matrix elements, no justification for the “**BSS mechanism**” for charm loop.
- Belle measurement of  $S_{J/\psi\pi^0}$  is theoretically favoured over BaBar measurement.

# Backup slides

# Numerics

Analytic result for the penguin pollution:

$$\frac{p_f}{t_f} = \frac{(C_8^u + C_8^t) V_8}{C_0 V_0 + C_8 (V_8 - A_8)}$$

$$\tan(\Delta\phi) \approx 2\epsilon \sin(\gamma) \operatorname{Re} \left( \frac{p_f}{t_f} \right) \quad \epsilon \equiv \left| \frac{V_{us} V_{ub}}{V_{cs} V_{cb}} \right|$$

Scan for largest value of  $\Delta\phi$  using

$$V_0 = 2f_\psi m_B p_{cm} F_1^{BK}$$

$$\begin{aligned} 0 &\leq |V_8| \leq V_0/3 \\ 0 &\leq \arg(V_8) < 2\pi \\ 0 &\leq |A_8| \leq V_0/3 \\ 0 &\leq \arg(A_8) < 2\pi \end{aligned}$$

and varying all input quantities within their experimental and theoretical uncertainties.