# Probing the relaxed relation across frontiers 

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## (e)tifr

Free Meson Seminar

## Outline

- Intro, 21st century log crisis/opportunity
- Case study, relaxed-relaxion, a few lessons
- Relaxion searches \w energy, luminosity on Earth, the sun (XENON1T)
- Precision (isotope shift spectroscopy)
- Conclusions


## Intro, (potential) hints from theory

- Our current 21st century puzzle:
knowledge that new physics (NP) exists vs our safest bets (LHC, WIMP,...) that came empty
- Motivates us to look for new paradigms
- Motivates us to look for new search strategies


## Intro, (potential) hints from theory

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## Conventional wisdom

For $>40$ yrs Higgs served us as anchor to determine the new phys. (NP) scale.
Sym'based solution to Naturalness $<=>\operatorname{TeV} N P$ (still the most compelling)

Conventional NP searches @ E-frontier, polynomial time-progress, linear scale 2019:


## Higgs @ 21st century => crisis \& opportunity

- New ideas \& null LHC results cast tiny doubt on this paradigm
eg: "Cosmic attractors","dynamical relaxation","N-naturalness", "relating the weak-scale to the CC" \& "inflating the Weak scale".

Are they all anthropic solutions? Is it satisfying for the weak scale?

## Higgs @ 21st century => crisis \& opportunity

- New ideas \& null LHC results cast tiny doubt on this paradigm.
eg: "Cosmic attractors","dynamical relaxation","N-naturalness", "relating the weak-scale to the CC" \& "inflating the Weak scale".
- New scalar common to several of above: concretely let us consider the relaxion:

Graham, Kaplan \& Rajendran (15) under some assumption allows for a concrete QFT realisation.

- Bottomline here: relaxion is axion-like-particle (ALP)-DM that (due to CP violation) can be described as scalar mixes $\backslash \mathrm{w}$ the Higgs but with weird (shallow) potential.

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Flacke, Frugiuele, Fuchs, Gupta & GP; Choi & Im (16); Banerjee, Kim & GP (18)
```

- Searching the relaxion => log crisis as follows:


## The relaxion (Higgs portal) parameter space \& the log crisis

Overview plot: the relaxion 30-decade-open parameter space


## The log crisis, toy example, lessons

- Lesson 1 - finding NP requires diverse approach, searches across frontier
- Lesson 2 - experimentally, worth checking where many decades are covered:



## Relaxion mechanism (inflation based)

(i) Add an ALP (relaxion) Higgs dependent mass:

(ii) $\phi$ roles till $\mu^{2}$ changes sign $\Rightarrow\langle H\rangle \neq 0 \Rightarrow$ stops rolling.



## A comment about the hierarchy problem

(i) Add an ALP (relaxion) Higgs dependent mass:


The hierarchy problem: we need to understand why today $\mu^{2}\left(\phi_{\text {today }}\right) \ll \Lambda^{2}$

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## The relaxion parameter space

- As effective relaxion models can be described as a Higgs portal:

$$
L_{S} \in m_{S}^{2} S S+\mu S H^{\dagger} H+\lambda S^{2} H^{\dagger} H, \text { with } S=\text { light scalar \& } H=\text { SM Higgs } .
$$

Naive naturalness implies: $\sin \theta \simeq \mu /\langle H\rangle \lesssim \frac{m_{S}}{\langle H\rangle} \quad\left(\& \lambda \lesssim \frac{m_{S}^{2}}{\langle H\rangle^{2}}\right)$.

- However, the ("relaxed") relaxion parameter space, goes well above the natural mixing region $=>$ interesting $\&$ encouraging for pheno.


## 3 differences from generic Higgs portal

(i) Lower + upper bound on mixing angle, apparent unnaturalness
(ii) Tiny "distance" between 1st minimum \& maximum
(iii) [Relaxion has also parity-odd-ALP (axion-like-particle) couplings]

## Point i: Relaxion's naive parameters (similar to aLP, backreaction domination)

$$
\begin{aligned}
& m_{\phi}^{2} \sim \partial_{\phi}^{2} V_{b r}(\phi, h) \sim \frac{\mu_{b}^{2} v_{\mathrm{EW}}^{2}}{f^{2}} \cos \frac{\phi_{0}}{f} \sim 1 \\
& \sin \theta_{h \phi} \sim \partial_{\phi} \partial_{h} V_{b r}(\phi, h) / v_{\mathrm{EW}}^{2} \sim \frac{\mu_{b}^{2}}{f v_{\mathrm{ELV}}} \sin \frac{\phi_{0}}{f}
\end{aligned}
$$

Naively: mixing angle in terms of mass $\sin \theta_{h \phi} \sim \frac{m_{\phi}}{v_{\mathrm{EW}}} \frac{\mu_{b}}{v_{\mathrm{EW}}}$

Maximum mixing angle $\quad\left(\sin \theta_{h \phi}\right)_{\max } \sim \frac{m_{\phi}}{v_{\mathrm{EW}}} \quad \begin{gathered}\text { Naturalness } \\ \text { bound }\end{gathered}$

Minimum mixing angle

$$
\left(\sin \theta_{h \phi}\right)_{\min } \sim \frac{m_{\phi}^{2} \Lambda_{\min }}{v_{\mathrm{EW}}^{3}}
$$

## The relaxion's naive parameter space



## (Less naive treatment)

$V(\phi, h)=\left(\Lambda^{2}-\Lambda^{2} \frac{\phi}{f_{\text {eff }}}\right)|h|^{2}-\frac{\Lambda^{4}}{f_{\text {eff }}} \phi-\mu_{\mathrm{b}}^{2}|H|^{2} \cos \frac{\phi}{f} \quad v^{2}(\phi)=\left\{\begin{array}{l}0 \text { when } \phi<\mathrm{f}_{\text {eff }} \\ >0 \text { when } \phi>\mathrm{f}_{\mathrm{eff}}\end{array}\right.$

Relaxion stopping point determines the EW scale $\quad \frac{\Lambda^{4}}{f_{\text {eff }}} \sim \frac{\mu_{\mathrm{b}}^{2} v_{\mathrm{EW}}^{2}}{f}$

Resolution parameter
Higgs mass change for $\Delta \phi=2 \pi f \quad \frac{\Delta v^{2}}{v^{2}} \sim \frac{\Lambda^{2}}{f_{\text {eff }}} \frac{f}{v^{2}} \sim \frac{\mu_{b}^{2}}{\Lambda^{2}} \equiv \delta^{2} \ll 1$

$$
V_{\mathrm{br}}=-\mu_{\mathrm{b}}^{2}|H|^{2} \cos \frac{\phi}{f} \quad \square \quad \begin{gathered}
\text { Potential height grows } \\
\text { incrementally }
\end{gathered}
$$

Stopping condition, fine resolution $=>$ tuned (relaxed) mass

$$
\begin{array}{r}
V_{\phi}^{\prime}=0 \Rightarrow \sin \theta=\frac{v_{\mathrm{EW}}^{2}}{v^{2}(\phi)}+\frac{v_{\mathrm{EW}}^{2}}{\Lambda^{2}}, \frac{\phi_{0}}{f} \sim \frac{\pi}{2} \text { upto resolution factors } \\
m_{\phi}^{2} \approx \delta \times\left(m_{\phi}^{2}\right)_{\text {naive }} \ll\left(m_{\phi}^{2}\right)_{\text {naive }}
\end{array}
$$



Relaxion: barriers increase incrementally:
relaxion stops at shallow region $=>$ small mass

Credit: A. Banerjee \& H. Kim


## Relaxed mass => natural violation of naturalness bound

Max. Mixing angle: $\sin \theta_{h \phi}^{\max }=\left(\frac{m_{\phi}}{v_{E W}}\right)^{\frac{2}{3}} \gg\left(\frac{m_{\phi}}{v_{E W}}\right)_{\text {naturalness }}$

$m_{\phi}[\mathrm{eV}]$

## Point ii: Distance between 1st min. \& max. \& relaxion as chameleon

1st min. \& maximum are very close, environmental effects may destabilised:

$$
\Delta \phi_{\mathrm{mima}} / f \sim \delta \Rightarrow \Delta \phi_{\mathrm{mima}} \sim \sin \theta_{h \phi} v^{5 / 3} / m_{\phi}^{2 / 3} \ll f
$$



Credit: A. Banerjee \& H. Kim

## Intro, new search strategies

- Our current 21st century puzzle:
knowledge that new physics (NP) exists vs our safest bets (LHC, WIMP,...) that came empty
- Motivates us to look for new paradigms
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## Overview: collider probes of relaxion

Preliminary, zooming in on relation region


Preliminary, scalar portal, \w timing $\&$ displacement


Fuchs, Matsedonski, GP, Savoray, Schlaffer;

## Luminosity \& precision: the era of Kaon factories



## The solar relaxion

The relaxion is copiously produced in the solar core. (via Bremsstrahlung \& resonant processes)

This flux can be absorbed by liquid xenon dark matter (DM) detectors.
Redondo (13)

Used XENON (19) \& LUX (17) to constrain the relaxion-electron couplings ( $g_{\varphi e e}$ ):


The coupling to electrons is chosen to be $g_{\phi e e}=10^{-14}$, and scalar taken to be massless. Green dashed line is Bremsstrahlung flux from electrons interacting with hydrogen and helium ions, red dashed line is the flux due to recombination and transitions of bounded electrons in heavier elements, blue dashed line is the flux from Compton-like scattering, black line is the total scalar flux.

## Can search for it with S1 (high threshold) \& \w S2 (low threshold)

Hardy and R. Lasenby (17)
unpublished: resonant spectrum


The dashed line ignores the mixing between scalar and longitudinal photon excitation, while solid line includes it.


XENON1T data $=$ black dots, blue histogram $=$ partial background model, signal $=$ orange histogram (massless scalar, $g_{\phi e e}=2 \times 10^{-15}$ - the peak around 400 PE corresponds scalar $E \sim 0.2 \mathrm{keV}$.

Massless case

$$
\begin{aligned}
& g_{\text {qee }}<2 \times 10^{-15} \\
& \sin \theta<7 \times 10^{-10}
\end{aligned}
$$

## XENON1T result on S1 (not looking at scalars)

E. Aprile et al., "Observation of Excess Electronic Recoil Events in XENONIT," arXiv:2006.09721 [hep-ex].


FIG. 4. A zoomed-in and re-binned version of Fig. 3 (top), where the data display an excess over the background model $B_{0}$. In the following sections, this excess is interpreted under solar axion, neutrino magnetic moment, and tritium hypotheses.

Fitting to scalar preliminary, S1



Left: showing the 1-2-3sigma CL with and without the BG. The three benchmark points with $\mathrm{m}_{\phi}=(0,1.3,1.9) \mathrm{keV}$ and $\mathrm{g}_{\phi \mathrm{e}}=(0.8,1.5,2.4) \times 10^{-14}$, are marked in green, orange and purple, respectively. The purple $\left(\mathrm{BM}_{3}\right)$ is the best fit point. Right: The signal+background is shown for the three benchmark point. The black points and gray line are data and background (without tritium) from XENON1T.

Fitting to scalar preliminary, S2; notice the background is not completely known!


Strong tension with red-giant ( RG ) observation if the mass is keV.

## S2: Tension is lower for < 300eV

Budnik, Davidi, Kim, GP \& Priel, 1909.02568


## S2: Tension is lower for mass of 200 eV => relaxion = Chameleon



$$
\frac{\Delta \phi_{\mathrm{RG}}}{\Delta \phi_{\operatorname{mima}}} \sim \frac{g_{\phi p p}}{10^{-6}} \times\left(\frac{200 \mathrm{eV}}{m_{\phi}}\right)_{\theta_{\text {min }}}^{\frac{8}{3}}
$$

For max. allowed natural coupling to protons inside the red giant the relation is destabilised for mass of order 200 eV .

## Precision Front

(i) virtual processes searching for atomic-range "Yukawa" force
(ii) time-depend. background if relaxion/scalar = ultra-light dark matter (DM)

## Recent progress:

Hunting "heavy" relaxion with isotope shift spectroscopy

## Basic concept: precision isotope shift spectroscopy

- New forces acts on electron \& quarks leads to change of energy levels.

- We cannot switch on and off these light Higgs-like couplings.
- Use different isotopes to effectively compare force mass dependence.
- Suppress nuclear effects via 2 transition comparison => King Linearity.

$$
\left[\left(\nu_{i j}^{\alpha}\right)_{\mathrm{SM}} \simeq K^{\alpha} \mu_{i j}+F^{\alpha} \delta\left\langle r^{2}\right\rangle_{i j} \Longrightarrow \bar{\nu}_{i j}^{\alpha} \propto \bar{\nu}_{i j}^{\alpha}\right] \quad \text { King (1963) }
$$

## Bounds \& sensitivity



## Recent ex. improving bounds by $10^{3}$

Search for King-linearity-violation (KLV), from $O(100) \mathrm{kHz}$ to $O(100)$.

## 2015: Isotope shift @ 1:104

Gebert et al. (PTB)


$$
\begin{aligned}
& \mathrm{Ca}^{+}(\mathrm{A}=40,42,44,48) \\
& \mathrm{D}_{3 / 2}-\mathrm{P}_{1 / 2} \\
& \mathrm{~S}_{1 / 2}-\mathrm{D}_{5 / 2}
\end{aligned}
$$

2020: Isotope shift @ 1:107

## Counts et al. (MIT), 3sigmas


$\mathrm{Yb}^{+}(\mathrm{A}=168,70,72,74,76)$

$$
\mathrm{S}_{1 / 2}-\mathrm{D}_{3 / 2}
$$

$$
\mathrm{S}_{1 / 2}-\mathrm{D}_{5 / 2}
$$

$\mathrm{Ca}^{+}(\mathrm{A}=40,42,44,46,48)$

$$
\mathrm{D}_{3 / 2}-\mathrm{D}_{5 / 2}
$$

$$
\mathrm{S}_{1 / 2}-\mathrm{D}_{5 / 2}
$$




Recent ex. improving bounds by $10^{3}$
Search for King-linearity-violation (KLV), from $O(100) \mathrm{kHz}$ to $O(100)$.


## How robust is the $(g-2)_{e}$ bound? Can we reduce SM contamination?

- The $(g-2)_{e}$ bound is model dep. \& can be naturally suppressed (mirror sym.).

Looking at (2-3) isotope shifts in "heavy" Rydberg transitions => reduce nuclear-impact.

See also: Jones, Potvliege \& Spannowsky (19); Capolupo et al. (20)


Duque-Mesa, Geller, Firstenberg, Fuchs, Ozeri, GP \& Shpilman, in prep.

## Projections, complementarity between precision \& accelerators



2D KLV (2DK) analysis w (blue) \wo (green) $\mathrm{NL}_{S M}$; generalized King analysis (GK) adding the $\mathrm{S} \rightarrow \mathrm{P}$ transition (black). NP bounds in $\mathrm{Yb}^{+}\left(95 \%\right.$ CL NP interval) $+\mathrm{Ca}^{+}$(upper bound) in yellow and cyan. 5th force searches, e-n scattering, neutron-nucleus scattering, lw (g-2)e, hydrogen-deuterium (HD) IS \& globular cluster. Dotted lines describes the relaxed-relaxion 42 \& the KOTO result.

Best case scenario: largest possible (non-SM) Yukawas \& no non-linearity


## Conclusions

- Null-results + new theories $=>$ log crisis/opportunity (ex.: relaxion)
- Several Lessons: calls for experimental diversity \w coordinated efforts
- Briefly: i. Kaon factories; ii. Solar vs. XENON; iii. isotope shifts ...
- Future look at S2 (XENON) could be very interesting.
- (Dark searches $\backslash \mathrm{w}$ quantum sensors $=>$ emerging frontier).


## Hunting for ultra light scalar/relaxion DM

- Scalar effects:
[(i) 5th force/equivalence principles;]
(ii) DM , slow oscillations - clock-clock comparison;
(iii) DM, rapid oscillation - clock-clock \& clock-cavity \& cavity-cavity comparisons;
[(iv) DM properties (local density vs halo).]
- Pseudo scalar, axial effect:
(i)long range axion coupling;
(ii) correlated axion DM signals;
(iii) DM property (local density vs halo)


## Scalar DM \& oscillating of constants

Generically, time-varying scalar => variations of fundamental constants.

- Scalar (dilaton) DM could induce an oscillation of fundamental constants.
- Can use quantum field theory (QFT) description to avoid confusions <=> scalar background is the only object that oscillates => can go beyond LO.
- Here we only focus on leading order, linear, with respects to scalar DM, as the scalar has quantum number can be "glued" to any SM operator:

$$
\mathscr{L}_{\phi} \in \frac{\phi}{v}\left[-\bar{m}_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right]+\ldots
$$

# Relaxion/scalar light dark matter 

Arvanitaki, Huang \& Van Tilburg (15) Banerjee, Kim \& GP (18)

## Concrete ex.: relaxion dark matter (DM)

- Basic idea is similar to axion DM (but avoiding missalignment problem):



## Concrete ex.: relaxion dark matter (DM)

- Basic idea is similar to axion DM (but avoiding missalignment problem): After reheating the wiggles disappear (sym' restoration):



## Concrete ex.: relaxion dark matter (DM)

- Basic idea is similar to axion DM (but avoiding missalignment problem): After reheating the wiggles disappear: and the relaxion roles a bit.



## Concrete ex.: relaxion dark matter (DM)

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Now the relaxion not at the min' and start to oscillates $=\mathrm{DM}$.


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## Relaxion/Higgs-portal \& benchmarking

- Relaxion DM: a concrete realisation of the idea, via its Higgs mixing. Interesting that preferred region has oscillating frequency in the (blind-spot) $\mathrm{kHz}-\mathrm{MHz}$ :

$\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right] ; \quad$ for instance: $\frac{\delta m_{e}}{m_{e}} \sim y_{e} \sin \theta_{\phi h} \frac{\sqrt{\rho_{\mathrm{DM}}}}{m_{e} m_{\phi}} \sin \left(m_{\phi} t\right)$


## Hunting oscillating DM, strategy \& scales

- How to search for the time variation?
- General: find 2 systems \w different dependence of scalar background.
- Classical ex.: clock comparisons: $\delta E_{1,2} \equiv \nu_{1,2}=f_{1,2}\left(\alpha^{\xi \alpha^{\xi, 2}}, \alpha_{s}^{\xi \alpha_{s}}, m_{e}^{\xi m_{e}, 2}, m_{q}^{\xi m_{q}, 2}\right)$



$$
R_{\infty} \propto \alpha^{2}\left(m_{e}+O\left(m_{e} / m_{A}\right)\right), R_{\text {Bohr }}^{-1} \propto \alpha\left(m_{e}+\ldots\right), \ldots
$$

## Relaxion oscillating DM, scales

- Relaxion-Higgs mixing => Higgs VEV oscillation:

$$
\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right]
$$



- Problem with several scales: (for instance we use below)

DM oscillating time: $\tau_{\mathrm{DM}} \sim 1 \mathrm{~s} \times \frac{10^{-15} \mathrm{eV}}{m_{\mathrm{DM}}}$
DM coherent time: $\tau_{\mathrm{DM}}^{\mathrm{co}} \sim 10^{6} \mathrm{~s} \times \frac{10^{-15} \mathrm{eV}}{m_{\mathrm{DM}}} \times \frac{10^{6}}{\beta^{2}}$
Exp. ave stability time: $\tau_{\text {sta }} \sim 1 \mathrm{~s} ; T \sim 10^{6} \mathrm{~s}$ - total integration time

Exp. cycle time: $\tau_{\text {cyc }} \sim 10^{-3}$ s

## Slow oscillation, long DM coherence, clock comparisons

Let us assume for simplicity that $\tau_{\mathrm{DM}}^{\mathrm{co}}$ is the longer scale in problem.

The sensitivity will be give by:

$$
\mathrm{SNR}=\frac{\Delta\left(f_{A} / f_{B}\right) /\left(f_{A} / f_{B}\right)}{\sigma_{y}\left(\tau_{\text {sta }}\right)} \times \sqrt{T} \quad\left(\sigma_{y}(\tau)=10^{-15} / \sqrt{\tau \mathrm{Hz}}\right)
$$

As the signal goes like $\phi \sim 1 / m_{\phi}$, we find that $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}$.

## Rapid oscillation vs. cycle time

If $\tau_{\text {cyc }}<\tau_{\mathrm{DM}}<\tau_{\text {ave }}$ we can't average over full ave. time, instead we optimise result by averaging of "DM-cycle" time.

The sensitivity will be give by $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}^{3 / 2}$.

If $\tau_{\mathrm{DM}}<\tau_{\mathrm{cyc}}<\tau_{\text {ave }}$ we only get residual contribution from last oscillation.
The sensitivity will be give by $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}^{2} \cdot{ }_{\text {Derviainko (16) },}$

## Ideal system

- The largest coupling of the relaxion is to the gluons.

The strongest sensitivity would be via a clock where the energy levels are prop to the QCD scale $=>$ (229Th) nuclear clock (there's big uncer.!):

$$
\Delta\left(\frac{f_{A} / f_{B}}{f_{A} / f_{B}}\right) \simeq 10^{5-6} \frac{\Delta\left(m_{q} / \Lambda_{\mathrm{QCD}}\right)}{\left(m_{q} / \Lambda_{\mathrm{QCD}}\right)} \propto 10^{5-6} \sin \theta_{h \phi}
$$

where $m_{q}$ is the light quark mass, and $\Lambda_{\mathrm{QCD}}$ is the QCD scale

## What about the size of the scalar DM amplitude itself?

The effects are linear with the scalar amplitude:

$$
\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right]
$$

This is astro stuff, there are considerable uncertainties.
We consider 2 options:

$$
\begin{array}{rlrl}
\text { Conventional - } & \phi & \sim \sqrt{\rho}_{\mathrm{DM}} / m_{\phi} \\
& \text { Extreme - } & \phi & \sim \sqrt{\rho}_{\text {halo }} / m_{\phi}
\end{array}
$$

## Searching for a relaxion DM planet around us

- Massive object may trap the (rel)axion => stable solution of EOM, "gravitational hydrogen":

$$
\begin{aligned}
& \text { Assume small DM density \& large } \\
& \text { radius => mass-radii relation: }
\end{aligned} \quad R_{\text {star }} \approx \frac{M_{\mathrm{Pl}}^{2}}{m_{\phi}^{2}} \frac{1}{M_{\text {Earth }}} \quad\left(M_{*} \ll M_{\text {Earth }}\right) .
$$

Eby, Leembruggen, Street, Suranyi \& Wijewardhana (18); Banerjee, Budker, Eby, Kim \& GP (19)

Can obtain large density enhancement:

$$
\begin{aligned}
r & \equiv \frac{\rho_{\text {star }}}{\rho_{\text {loc-DM }}} \sim \xi \frac{M_{\text {Earth }}^{4} m_{\phi}^{6}}{M_{\mathrm{Pl}}^{6} \rho_{\text {loc-DM }}} \sim \xi \times 10^{28} \times\left(\frac{m_{\phi}}{10^{-10}}\right)^{6} \\
& \xi \equiv M_{\text {star }} / M_{\text {Earth }}
\end{aligned}
$$



Enhancements in the axion halo scenario compared to the background DM case, in the field value for the Earth halo (blue) and solar halo (red) compared to the usual ALP DM case. Solid lines correspond to maximal halo mass M. by gravitational constraints.

## Ideal system, nuclear clock, current \& near future bounds

Banerjee, Kim, Matsedonski, GP \& Safranova (20)


Best case "crazy" scenario: largest possible DM density as allowed by indirect bounds.


## Further in to the future

- Recent large scale Earth-based \& space-based atom-interferometer were proposed/initiated ELGAR, 1911.03701; MIGA, Sci. Rep. (18); MAGIS, 1711.02225; ZAIGA 1903.09288.

Can potentially probe very large region, for intermediate DM masses (albeit slowly oscillating), for ex.:
Relevant th.: Graham, Hogan, Kasevich \& Rajendran (13); Arvanitaki, Graham, Hogan, Rajendran, \& Van Tilburg (18); Grote \& Stadnik (19)



## THE STOPPING POINT

Relaxion stops when

$$
V_{\phi}^{\prime}=0 \Rightarrow \sin \theta=\frac{v_{\mathrm{EW}}^{2}}{v^{2}(\phi)}+\frac{v_{\mathrm{EW}}^{2}}{\Lambda^{2}} \quad \square \quad \frac{\phi_{0}}{f} \sim \frac{\pi}{2} \text { upto resolution factors }
$$



## Overview: accelerator probes of relaxion

Prelim: Banerjee, Kim, Matsedonski, GP, Safranova


## Hunting for ultra light relaxion DM - roadmap

- Scalar effects:
[(i) 5th force/equivalence principles;]
(ii) DM, slow oscillations - clock-clock comparison;
(iii) DM, rapid oscillation - clock-clock \& clock-cavity \& cavity-cavity (?!) comparisons;
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## Relaxion/Higgs-portal \& benchmarking

- The relaxion DM provides us with a concrete \& simple realisation of the idea (via dynaminal misalignment, see yesterday's talk), via it is Higgs mixing:

$\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right] ; \quad$ for instance: $\quad \frac{m_{\phi}[\mathrm{eV}]}{m_{e}} \lesssim y_{e} \sin _{\phi h} \frac{\sqrt{\rho_{\mathrm{DM}}}}{m_{e} m_{\phi}} \sin \left(m_{\phi} t\right)$


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- Relaxion-Higgs mixing => Higgs VEV oscillation:

$$
\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right]
$$

Problem with several scales: (for instance we use below)


Blog, Nat. Ast., Eby (20)
Banerjee, Budker, Eby, Kim \& GP (19)

DM oscillating time: $\tau_{\mathrm{DM}} \sim 1 \mathrm{~s} \times \frac{10^{-15} \mathrm{eV}}{m_{\mathrm{DM}}}$
DM coherent time: $\tau_{\mathrm{DM}}^{\mathrm{co}} \sim 10^{6} \mathrm{~s} \times \frac{10^{-15} \mathrm{eV}}{m_{\mathrm{DM}}} \times \frac{10^{6}}{\beta^{2}}$
Exp. ave stability time: $\tau_{\text {sta }} \sim 1 \mathrm{~s} ; T \sim 10^{6} \mathrm{~s}$ - total integration time

Exp. cycle time: $\tau_{\text {cyc }} \sim 10^{-3} \mathrm{~s}$

## Slow oscillation, long DM coherence, clock comparisons

Let us assume for simplicity that $\tau_{\mathrm{DM}}^{\mathrm{co}}$ is the longer scale in problem.

The sensitivity will be give by:

$$
\mathrm{SNR}=\frac{\Delta\left(f_{A} / f_{B}\right) /\left(f_{A} / f_{B}\right)}{\sigma_{y}\left(\tau_{\text {sta }}\right)} \times \sqrt{T} \quad\left(\sigma_{y}(\tau)=10^{-15} / \sqrt{\tau \mathrm{Hz}}\right)
$$

As the signal goes like $\phi \sim 1 / m_{\phi}$, we find that $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}$.

## Rapid oscillation vs. cycle time

If $\tau_{\text {cyc }}<\tau_{\mathrm{DM}}<\tau_{\text {ave }}$ we can't average over full ave. time, instead we optimise result by averaging of "DM-cycle" time.

The sensitivity will be give by $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}^{3 / 2}$.

If $\tau_{\mathrm{DM}}<\tau_{\mathrm{cyc}}<\tau_{\mathrm{ave}}$ we only get residual contribution from last oscillation.
The sensitivity will be give by $\sin \theta_{h \phi}^{\text {bound }} \propto 1 / m_{\phi}^{2} \cdot{ }_{\text {Derviainko (16) },}$

## Ideal system

- The largest coupling of the relaxion is to the gluons.

The strongest sensitivity would be via a clock where the energy levels are prop to the QCD scale $=>$ (229Th) nuclear clock (there's big uncer.!):

$$
\Delta\left(\frac{f_{A} / f_{B}}{f_{A} / f_{B}}\right) \simeq 10^{5-6} \frac{\Delta\left(m_{q} / \Lambda_{\mathrm{QCD}}\right)}{\left(m_{q} / \Lambda_{\mathrm{QCD}}\right)} \propto 10^{5-6} \sin \theta_{h \phi}
$$

where $m_{q}$ is the light quark mass, and $\Lambda_{\mathrm{QCD}}$ is the QCD scale

## What about the size of the scalar DM amplitude itself?

The effects are linear with the scalar amplitude:

$$
\mathcal{L} \supset \sin \theta_{h \phi} \frac{\phi}{v}\left[-m_{f} \bar{f} f+\frac{c_{\gamma}}{4 \pi} F F+\frac{c_{g}}{4 \pi} G G\right]
$$

This is astro stuff, there are considerable uncertainties.
We consider 2 options:

$$
\begin{array}{rlrl}
\text { Conventional - } & \phi & \sim \sqrt{\rho}_{\mathrm{DM}} / m_{\phi} \\
& \text { Extreme - } & \phi & \sim \sqrt{\rho}_{\text {halo }} / m_{\phi}
\end{array}
$$

## Searching for a relaxion DM planet around us

- Massive object may trap the (rel)axion => stable solution of EOM, "gravitational hydrogen":

$$
\begin{aligned}
& \text { Assume small DM density \& large } \\
& \text { radius => mass-radii relation: }
\end{aligned} \quad R_{\text {star }} \approx \frac{M_{\mathrm{Pl}}^{2}}{m_{\phi}^{2}} \frac{1}{M_{\text {Earth }}} \quad\left(M_{*} \ll M_{\text {Earth }}\right) .
$$

Eby, Leembruggen, Street, Suranyi \& Wijewardhana (18); Banerjee, Budker, Eby, Kim \& GP (19)

Can obtain large density enhancement:

$$
\begin{aligned}
r & \equiv \frac{\rho_{\text {star }}}{\rho_{\text {loc-DM }}} \sim \xi \frac{M_{\text {Earth }}^{4} m_{\phi}^{6}}{M_{\mathrm{Pl}}^{6} \rho_{\text {loc-DM }}} \sim \xi \times 10^{28} \times\left(\frac{m_{\phi}}{10^{-10}}\right)^{6} \\
& \xi \equiv M_{\text {star }} / M_{\text {Earth }}
\end{aligned}
$$



Enhancements in the axion halo scenario compared to the background DM case, in the field value for the Earth halo (blue) and solar halo (red) compared to the usual ALP DM case. Solid lines correspond to maximal halo mass M. by gravitational constraints.

## Ideal system, nuclear clock

Prelim: Banerjee, Kim, Matsedonski, GP, Safranova


## Beyond IHz DM mass Iw dynamical decoupling



## Beyond IHz DM mass Iw polarization spectroscopy

Antypas, Tretiak, Garcon, Ozeri, GP \& Budker, (19)
Cs $6 \mathrm{~S}_{1 / 2} \rightarrow 6 \mathrm{P}_{3 / 2}$ transition frequency ( 10 GHz )


3rd laser harmonics.

## Cavity-cavity comparisons - stay tune for Fri.

Stadnik \& Flambaum (14); Grote \& Stadnik (19) ...

The (rel)axion frontier

## Axial coupling searches of relaxion DM

- The relaxion being an axion-like-particle (ALP) obtain pseudo-scalar coupling to matter, that are model dependent.

```
See e.g.: Graham, Kaplan & Rajendran; Gupta, Komargodski, GP & Ubaldi (15);
```

Davidi, Gupta, GP, Redigolo \& Shalit (17,18)

Generically, one loop below backreaction scale we expect axial coupling to be induced.

$$
\downarrow
$$

Motivate us to search for an associated signal via "magnetometers"

## Axial coupling searches of relaxion DM

- One can look at signals at variety of experiments (we consider 2):

ABRACADABRA

$$
\nabla \times \vec{B}=\frac{\partial \vec{E}}{\partial t}-g_{\phi \gamma \gamma}\left(\vec{E} \times \nabla \phi-\vec{B} \frac{\partial \phi}{\partial t}\right) \cdot \text { Kahn, Safdi \& Thaler (16); Ouellet et al (18) }
$$

$\left(\mathcal{L} \supset-\frac{1}{4} g_{\phi \gamma \gamma} \phi F_{\mu \nu} \widetilde{F}^{\mu \nu}\right)$

CASPEr(Wind)

$$
\begin{aligned}
H \simeq-\left[\left(d_{a} / I\right) \vec{I} \cdot \vec{E}+\left(\mu_{n} / I\right) \vec{I} \cdot \vec{B}_{\phi}\right] \cos \left(m_{\phi} t\right) . & \vec{d}_{a}
\end{aligned}=g_{a d} \phi \vec{I}, ~=\vec{B}_{\phi}=g_{\phi N N} \gamma_{n}^{-1} \nabla \phi .
$$

$$
\left(\mathcal{L} \supset g_{\phi N N} \partial_{\mu} \phi \bar{N} \gamma^{\mu} \gamma_{5} N-\frac{\imath}{2} g_{d} \phi \bar{N} \sigma_{\mu \nu} \gamma_{5} N F^{\mu \nu}+\ldots,\right)
$$

Budker, Graham, Ledbetter, Rajendran \& Sushkov (13); Jackson Kimball et al (2017)

- In the case of axion-halo the "wind" is replaced by density gradient which is orientation-dependent => new type of signature.


## Axial coupling searches of relaxion DM



Sensitivity to $g_{\phi \gamma \gamma}$ in the ABRACADABRA experiment. Black lines: projected sen- sitivity for background axion dark matter; blue lines: sensitivity for Earth axion halo; red: sensitivity for solar axion halo. The shaded regions represent the QCD axion band (purple), the current CAST constraint (green), and the current ABRACADABRA constraint (black/blue).

Banerjee, Budker, Eby, Flambaum, Kim, Matsedonskyi \& GP (19)


Sensitivity to $g_{d}$ in presence of an axion halo for CASPERElectric; the blue (red) curves represent the Earth-based (Sunbased) halo, the black lines represent the standard back- ground DM density, and the shaded regions are current constraints from astrophysics (green) and static EDM searches (gray).

## Conclusions

- Higgs physics has been always our beacon for new physics.
- Null-results + new theories (ex.: relaxion) => log crisis/opportunity, calls for experimental diversity.
- Accelerators provided a unique opportunity to search for (relaxed) relaxion.
- Ultra-light relaxion DM => Higgs VEV oscillating => exciting signals ...
- Signals are correlated with axion-searches which is a unique property.

